

# Capybara dreaming

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# 1 Problemas

## 1.1 coloracao galaxy collision

```
#include <bits/stdc++.h>
using namespace std;

const int MAXN1 = 60000, MAXN2 = 60000, MAXM = 200000;
int n1, n2, edges, last[MAXN1], prevs[MAXM], head[MAXM], matching[MAXN2], dist[MAXN1], Q[MAXN1], used[MAXN1],
    vis[MAXN1];

typedef pair<int, int> ii;

void init(int _n1, int _n2)
{
    n1 = _n1;
    n2 = _n2;
    edges = 0;
    fill(last, last + n1, -1);
}

void addAresta(int u, int v)
{
    head[edges] = v;
    prevs[edges] = last[u];
    last[u] = edges++;
}

void bfs()
{
    fill(dist, dist + n1, -1);
    int sizeQ = 0;
    for (int u = 0; u < n1; ++u)
    {
        if (!used[u])
        {
            Q[sizeQ++] = u;
            dist[u] = 0;
        }
    }
    for (int i = 0; i < sizeQ; i++)
    {
        int u1 = Q[i];
        for (int e = last[u1]; e >= 0; e = prevs[e])
        {
            int u2 = matching[head[e]];
            if (u2 >= 0 && dist[u2] < 0)
            {
                dist[u2] = dist[u1] + 1;
                Q[sizeQ++] = u2;
            }
        }
    }
}

bool dfs(int u1)
{
    vis[u1] = true;
    for (int e = last[u1]; e >= 0; e = prevs[e])
    {
        int v = head[e];
        int u2 = matching[v];
        if (u2 < 0 || !vis[u2] && dist[u2] == dist[u1] + 1 && dfs(u2))
        {
            matching[v] = u1;
            used[u1] = true;
            return true;
        }
    }
    return false;
}

int maxMatching()
{
    fill(used, used + n1, false);
    fill(matching, matching + n2, -1);
    for (int res = 0;;)
    {
        bfs();
        fill(vis, vis + n1, false);
        int f = 0;
```

```

    for (int u = 0; u < n1; ++u)
        if (!used[u] && dfs(u))
            ++f;
    if (!f)
        return res;
    res += f;
}
}

int main() {
    int n, i, j, a, b;
    map<ii, int> pontos;
    vector<ii> validos;
    for(i = -5; i <= 5; i++)
        for(j = -5; j <= 5; j++)
            if(hypot(i, j) <= 5 && (i || j))
                validos.push_back(ii(i, j));

    while(scanf("%d", &n) > 0) {
        pontos.clear();

        for(i = 0; i < n; i++)
            scanf("%d %d", &a, &b), pontos[ii(a, b)] = i;

        init(n + 1, n + 1);

        for(auto &it : pontos)
            for(auto &dif : validos) {
                auto x = it.first.first + dif.first;
                auto y = it.first.second + dif.second;
                if(pontos.count(ii(x, y)))
                    addAresta(it.second, pontos[ii(x, y)]);
            }

        printf("%d\n", maxMatching() / 2);
    }
}

```

## 1.2 convex hull trick

```
#include <bits/stdc++.h>
using namespace std;
int pointer; //Keeps track of the best line from previous query
vector<long long> M; //Holds the slopes of the lines in the envelope
vector<long long> B; //Holds the y-intercepts of the lines in the envelope
//Returns true if either line l1 or line l3 is always better than line l2
bool bad(int l1, int l2, int l3)
{
    /*
     intersection(l1,l2) has x-coordinate (b1-b2)/(m2-m1)
     intersection(l1,l3) has x-coordinate (b1-b3)/(m3-m1)
     set the former greater than the latter, and cross-multiply to
     eliminate division
    */
    return (B[l3] - B[l1]) * (M[l1] - M[l2]) < (B[l2] - B[l1]) * (M[l1] - M[l3]);
}
//Adds a new line (with lowest slope) to the structure
void add(long long m, long long b)
{
    //First, let's add it to the end
    M.push_back(m);
    B.push_back(b);
    //If the penultimate is now made irrelevant between the antepenultimate
    //and the ultimate, remove it. Repeat as many times as necessary
    while (M.size() >= 3 && bad(M.size() - 3, M.size() - 2, M.size() - 1))
    {
        M.erase(M.end() - 2);
        B.erase(B.end() - 2);
    }
}
//Returns the minimum y-coordinate of any intersection between a given vertical
//line and the lower envelope
long long query(long long x)
{
    //If we removed what was the best line for the previous query, then the
    //newly inserted line is now the best for that query
    if (pointer >= M.size())
        pointer = M.size() - 1;
    //Any better line must be to the right, since query values are
    //non-decreasing
    while (pointer < M.size() - 1 &&
           M[pointer + 1] * x + B[pointer + 1] < M[pointer] * x + B[pointer])
        pointer++;
    return M[pointer] * x + B[pointer];
}
int main()
{
    int M, N, i;
    pair<int, int> a[50000];
    pair<int, int> rect[50000];
    freopen("acquire.in", "r", stdin);
    freopen("acquire.out", "w", stdout);
    scanf("%d", &M);
    for (i = 0; i < M; i++)
        scanf("%d %d", &a[i].first, &a[i].second);
    //Sort first by height and then by width (arbitrary labels)
    sort(a, a + M);
    for (i = 0, N = 0; i < M; i++)
    {
        /*
         When we add a higher rectangle, any rectangles that are also
         equally thin or thinner become irrelevant, as they are
         completely contained within the higher one; remove as many
         as necessary
        */
        while (N > 0 && rect[N - 1].second <= a[i].second)
            N--;
        rect[N++] = a[i]; //add the new rectangle
    }
    long long cost;
```

```

add(rect[0].second, 0);
//initially, the best line could be any of the lines in the envelope,
//that is, any line with index 0 or greater, so set pointer=0
pointer = 0;
for (i = 0; i < N; i++) //discussed in article
{
    cost = query(rect[i].first);
    if (i < N - 1)
        add(rect[i + 1].second, cost);
}
printf("%lld\n", cost);
return 0;
}

```

### 1.3 eliminacao gauss xor loteria

```
#include <bits/stdc++.h>
using namespace std;
typedef vector<int> vi;
typedef vector<vi> vvi;
int main()
{
    int n, k, matriz[10000][50], linha, coluna, rank, i, j, e;
    scanf("%d %d", &n, &k);
    for (i = 0; i < n; i++)
        for (j = 0; j < k; j++)
            scanf("%d", &e), matriz[i][j] = e & 1;
    linha = coluna = rank = 0;
    while (linha < n && coluna < k)
    {
        for (i = linha; i < n; i++)
            if (matriz[i][coluna] == 1)
                break;
        if (i == n || matriz[i][coluna] == 0)
        {
            puts("S");
            return 0;
        }
        for (j = 0; j < k; j++)
            swap(matriz[linha][j], matriz[i][j]);
        for (i = 0; i < n; i++)
        {
            if (i == linha || matriz[i][coluna] == 0)
                continue;
            for (j = 0; j < k; j++)
                matriz[i][j] ^= matriz[linha][j];
        }
        linha++, coluna++;
    }
    if(linha >= k && n > linha) {
        puts("N");
        return 0;
    }
    puts("S");
}
```

## 1.4 fft laboratorio biotecnologia

```
#include <bits/stdc++.h>
using namespace std;
const int MAX_DIST = 1 << 23;
typedef complex<double> cpx;
const double pi = acos(-1.0);
char txt[100000];
int maxDist;
// in:      vector de entrada
// type:    1 = Transformada, -1 = Transformada inversa
void fft (vector<cpx> &a, bool invert) {
    int n = (int) a.size();
    for (int i=1, j=0; i<n; ++i) {
        int bit = n >> 1;
        for (; j>=bit; bit>>=1)
            j -= bit;
        j += bit;
        if (i < j)
            swap (a[i], a[j]);
    }
    for (int len=2; len<=n; len<=1) {
        double ang = 2*pi/len * (invert ? -1 : 1);
        cpx wlen (cos(ang), sin(ang));
        for (int i=0; i<n; i+=len) {
            cpx w (1);
            for (int j=0; j<len/2; ++j) {
                cpx u = a[i+j], v = a[i+j+len/2] * w;
                a[i+j] = u + v;
                a[i+j+len/2] = u - v;
                w *= wlen;
            }
        }
    }
    if (invert)
        for (int i=0; i<n; ++i)
            a[i] /= n;
}

int main()
{
    int soma = 0, acc = 0, tam = 0, c;
    vector<cpx> fftEsq(MAX_DIST), fftDir(MAX_DIST);
    while((c = getchar()) >= 'a') {
        soma += txt[tam++] = c - 96;
        fftEsq[soma] = cpx(1, 0);
    }
    fftDir[soma] = cpx(1, 0);
    for(int i = 0; i < tam; i++) {
        acc += txt[i];
        fftDir[soma - acc] = cpx(1, 0);
    }
    int shiftAmount, lim = 2 * soma;
    for (shiftAmount = 0; (lim >> shiftAmount) != 0; shiftAmount++)
        ;
    maxDist = 1 << shiftAmount;
    fftEsq.resize(maxDist);
    fftDir.resize(maxDist);
    fft(fftEsq, false);
    fft(fftDir, false);
    for (int i = 0; i < maxDist; i++)
        fftEsq[i] = fftDir[i] * fftEsq[i];
    fft(fftEsq, 1);
    int total = 0;
    assert(lim < maxDist);
```

```
for (int i = soma + 1; i <= lim; i++)
{
    if (fftEsq[i].real() > 0.01)
        total++;
}
printf("%d\n", total);
}
```



## 1.5 geometria bloco preto branco

```
#include <bits/stdc++.h>
using namespace std;

struct Bloco {
    long long qt;
    char c;
};

Bloco bloco[200000];
long long totB, totW;
long long n;

long long getX(long long y) {
    return ceil((totB * y)*1.0/(totW));
}

long long getY(long long x) {
    return ceil((totW * x)*1.0/(totB));
}

int main() {
    long long t;
    cin >> t;

    while(t--) {
        cin >> n;
        totB = totW = 0;
        for(int i=0; i<n; i++) {
            scanf("%lld %c", &bloco[i].qt, &bloco[i].c);
            if(bloco[i].c == 'W')
                totW += bloco[i].qt;
            else
                totB += bloco[i].qt;
        }
        if(totW == 0 || totB == 0) {
            cout << totW + totB << endl;
            continue;
        }

        long long x = 0, y = 0;
        long long x_a = 0, y_a = 0;
        long long cont = 0;

        for(int i=0; i<n; i++) {
            if(i < n-1 && bloco[i].c == bloco[i+1].c) {
                if(bloco[i].c == 'B')
                    x_a += bloco[i].qt;
                else
                    y_a += bloco[i].qt;
            }
            else {
                if(bloco[i].c == 'B') {
                    x_a += bloco[i].qt;
                    double local = getX(y);
                    if(local >= x && local < x + x_a)
                        if((totB * y) % totW == 0)
                            cont++;

                    x += x_a;
                    x_a = 0;
                }
                else {
                    y_a += bloco[i].qt;
                    double local = getY(x);
                    if(local >= y && local < y + y_a)
                        if((totW * x) % totB == 0)
                            cont++;

                    y += y_a;
                    y_a = 0;
                }
            }
        }

        cout << cont << endl;
    }

    return 0;
}
```

## 1.6 geometria bolo do marcelo

```
#include <bits/stdc++.h>
using namespace std;
#define D(x) cout << #x << " = " << x << endl;
typedef pair<int, int> Ponto;
//O dobro da área definida pelo triangulo de pontos pontos a, b e c (com sinal).
long long area2(Ponto &a, Ponto &b, Ponto &c) {
    return (long long) (b.first - a.first) * (c.second - a.second) - (long long) (b.second - a.second) * (c.first - a.first);
}
//Retorna a área do polígono p definido pelos pontos p[i, f]
long long polygonArea2(vector<Ponto> &p, int i, int f) {
    long long s = 0.0;
    Ponto& primeiro = p[i];
    Ponto origem = Ponto(0, 0);
    for (; i != f; i = (i + 1) % p.size())
        s += area2(origem, p[i], p[(i + 1) % p.size()]);
    s += area2(origem, p[i], primeiro);
    return s;
}
long long corta(vector<Ponto> &p, long long &areaTot) {
    int atual = 0;
    int k = 0;
    int m = p.size();
    long long area = 0, areaVelha = 0;
    long long resp = 1ll<<62;
    for (atual = 0; atual < m; atual++) {
        while (true) {
            if (2 * area > areaTot) {
                areaVelha = area - area2(p[atual], p[(m + k - 1) % m], p[k]);
                resp = min(resp, max(areaTot - area, min(areaVelha, areaTot - areaVelha)));
                break;
            }
            k = (k + 1) % m;
            area += area2(p[atual], p[(m + k - 1) % m], p[k]);
        }
        area -= area2(p[atual], p[(atual + 1) % m], p[k]);
    }
    return resp;
}
int main() {
    int n;
    scanf("%d", &n);
    vector<Ponto> pontos(n);
    for (auto &it : pontos)
        scanf("%d %d", &it.first, &it.second);
    auto area = polygonArea2(pontos, 0, pontos.size() - 1);
    auto resp = corta(pontos, area);
    printf("%lld %lld\n", area - resp, resp);
    return 0;
}
```

## 1.7 geometria fila mineira

```
#include <bits/stdc++.h>
#define D(x) cout << #x << " = " << x << endl
using namespace std;
typedef pair<int, int> ii;
typedef vector<int> vi;
typedef vector<vi> vvi;
typedef vector<ii> vii;
typedef vector<vii> vvii;
#define pb push_back
vii pontos;
double f(double theta)
{
    double y_max = -1e100, y_min = 1e100, y;
    double sint = sin(theta), cost = cos(theta);
    for(auto &it : pontos) {
        y = -sint * it.first + cost * it.second;
        y_max = max(y, y_max);
        y_min = min(y, y_min);
    }
    return (y_max - y_min) / 2;
}
double gss(double a, double b)
{
    double r = (sqrt(5) - 1) / 2; //=.618...=golden ratio-1
    double x1 = b - r * (b - a), x2 = a + r * (b - a);
    double f1 = f(x1), f2 = f(x2);
    // while(fabs(f1 - f2) > e)
    for(int it = 0; it < 100; it++)
    {
        //change to > to find maximum
        if (f1 < f2)
        {
            b = x2;
            x2 = x1;
            f2 = f1;
            x1 = b - r * (b - a);
            f1 = f(x1);
        }
        else
        {
            a = x1;
            x1 = x2;
            f1 = f2;
            x2 = a + r * (b - a);
            f2 = f(x2);
        }
    }
    // return f1;
    return (f2 + f1) / 2;
}
int main()
{
    int n;
    cin >> n;
    pontos = vii(n);
    for(auto &it : pontos)
        cin >> it.first >> it.second;
    auto resp = gss(0, 90);
    resp = min(resp, gss(90, 180));
    resp = min(resp, gss(180, 270));
    resp = min(resp, gss(270, 360));
    printf("%.21f\n", resp);
}
```

## 1.8 grafo caminho unico entre 2 vertices

```
#include <bits/stdc++.h>
using namespace std;

typedef vector<int> vi;
typedef pair<int, int> ii;
typedef vector<ii> vii;
typedef vector<vii> vvii;

#define D(x) cout << #x " = " << x << endl;

vvii grafo;

vi dfs_num, dfs_low, dfs_parent, S, visited, pontes;
int dfsNC, root, rootChildren;

void tarjan(int u) {
    dfs_low[u] = dfs_num[u] = dfsNC++;
    S.push_back(u);
    visited[u] = 1;
    for(auto &it : grafo[u]) {
        if(dfs_num[it.first] == -1) {
            dfs_parent[it.first] = u;

            if(u == root)
                rootChildren++;

            tarjan(it.first);

            if(dfs_low[it.first] > dfs_num[u])
                pontes[it.second] = 1;

            dfs_low[u] = min(dfs_low[u], dfs_low[it.first]);
        }
        else if(it.first != dfs_parent[u])
            dfs_low[u] = min(dfs_low[u], dfs_low[it.first]);
    }
}

int dfs1(int atual, int destino) {
    if(atual == destino)
        return 1;

    if(visited[atual])
        return 0;

    visited[atual] = 1;
    int r = 0;
    for(auto &it : grafo[atual])
        if(pontes[it.second])
            r += dfs1(it.first, destino);

    return r;
}

int main()
{
    int r, c, q, a, b, i;
    while(scanf("%d %d %d", &r, &c, &q) && r) {
        grafo = vvii(r);
        pontes = vi(c + 1, 0);
        while(c--)
            scanf("%d %d", &a, &b),
            grafo[a-1].push_back({b-1, c}),
            grafo[b-1].push_back({a-1, c});

        dfs_num = vi(r, -1);
        dfs_parent = vi(r, -1);
        dfs_low = vi(r, 0);
        visited = vi(r, 0);
        dfsNC = 0;

        for(i = 0; i < r; i++)
            if(dfs_num[i] == -1)
                root = i, rootChildren = 0, tarjan(i);

        while(q--) {
            visited = vi(r, 0);
            scanf("%d %d", &a, &b);
```

```
        printf("%c\n", dfs1(a - 1, b - 1) ? 'Y' : 'N');  
    }  
    puts("-");  
}  
}
```

## 1.9 grafo centro arvore junte dois reinos

```
#include <bits/stdc++.h>
using namespace std;
#define pb push_back
typedef vector<int> vi;
typedef vector<vi> vvi;

vvi a_esq, a_dir;
vi grau_esq, grau_dir, tam_esq, tam_dir, dist_esq, dist_dir;
int centro_esq, centro_dir;

int dfs_esq(int atual, int pai) {
    int r = 0;
    for(auto &it : a_esq[atual])
        if(it != pai)
            r = max(r, dfs_esq(it, atual));
    return tam_esq[atual] = r + 1;
}

int dfs_dir(int atual, int pai) {
    int r = 0;
    for(auto &it : a_dir[atual])
        if(it != pai)
            r = max(r, dfs_dir(it, atual));
    return tam_dir[atual] = r + 1;
}

void calc_dist_esq(int atual, int maior) {
    dist_esq[atual] = maior;
    for(auto &it : a_esq[atual])
        if(dist_esq[it] == -1 && it != centro_esq)
            calc_dist_esq(it, maior + 1);
}

void calc_dist_dir(int atual, int maior) {
    dist_dir[atual] = maior;
    for(auto &it : a_dir[atual])
        if(dist_dir[it] == -1 && it != centro_dir)
            calc_dist_dir(it, maior + 1);
}

int main() {
    ios::sync_with_stdio(false);
    cin.tie(0);
    long long soma;
    int n, q, i, a, b, maxi, max_dir, max_esq;
    while(cin >> n >> q) {
        multiset<int> valores_esq, valores_dir;

        a_esq = vvi(n);
        a_dir = vvi(q);

        grau_esq = vi(n);
        grau_dir = vi(q);

        tam_esq = vi(n);
        tam_dir = vi(q);

        dist_esq = vi(n, -1);
        dist_dir = vi(q, -1);

        for(i = 1; i < n; i++)
            cin >> a >> b,
            a--,
            b--,
            a_esq[a].pb(b),
            grau_esq[a]++,
            a_esq[b].pb(a),
            grau_esq[b]++;

        for(i = 1; i < q; i++)
            cin >> a >> b,
            a--,
            b--,
            a_dir[a].pb(b),
```

```

        grau_dir[a]++,
        a_dir[b].pb(a),
        grau_dir[b]++;

    queue<int> fila;

    // Centro da arvore esquerda
    for(i = 0; i < n; i++)
        if(a_esq[i].size() <= 1) // <= por árvore vazia!
            fila.push(i);

    while(fila.size() > 1) {
        for(auto &it : a_esq[fila.front()]) {
            grau_esq[it]--;

            if(grau_esq[it] == 1)
                fila.push(it);
        }
        fila.pop();
    }

    centro_esq = fila.front();
    fila.pop();

    // Centro da arvore direita
    for(i = 0; i < q; i++)
        if(a_dir[i].size() <= 1) // <= por árvore vazia!
            fila.push(i);

    while(fila.size() > 1) {
        for(auto &it : a_dir[fila.front()]) {
            grau_dir[it]--;

            if(grau_dir[it] == 1)
                fila.push(it);
        }
        fila.pop();
    }

    centro_dir = fila.front();
    fila.pop();

    dfs_esq(centro_esq, -1);
    dfs_dir(centro_dir, -1);

    valores_esq.insert(0);
    for(auto &it : a_esq[centro_esq])
        valores_esq.insert(-tam_esq[it]);

    for(auto &it : a_esq[centro_esq]) {
        valores_esq.erase(valores_esq.find(-tam_esq[it]));
        calc_dist_esq(it, -(*valores_esq.begin()) + 1);
        valores_esq.insert(-tam_esq[it]);
    }

    dist_esq[centro_esq] = -(*valores_esq.begin());

    valores_dir.insert(0);
    for(auto &it : a_dir[centro_dir])
        valores_dir.insert(-tam_dir[it]);

    for(auto &it : a_dir[centro_dir]) {
        valores_dir.erase(valores_dir.find(-tam_dir[it]));
        calc_dist_dir(it, -(*valores_dir.begin()) + 1);
        valores_dir.insert(-tam_dir[it]);
    }

    dist_dir[centro_dir] = -(*valores_dir.begin());

    soma = maxi = max_esq = max_dir = 0;

    for(auto &it : dist_esq)
        max_esq = max(max_esq, it);

    for(auto &it : dist_dir)
        max_dir = max(max_dir, it);

    maxi = max(max_esq, max_dir);

    vi v_esq(max_esq + 1, 0), v_dir(max_dir + 1, 0);

    for(auto &i : dist_esq)

```

```

        v_esq[i]++;
for(auto &i : dist_dir)
    v_dir[i]++;
for(int i = 0; i <= max_esq; i++)
    for(int j = 0; j <= max_dir; j++)
        if(v_esq[i] && v_dir[j])
            soma += v_esq[i] * v_dir[j] * max(i + j + 1, maxi);
printf("%.3lf\n", 1.0 * soma / (q * n));
}
}

```



## 1.10 Grundy jogo da velha 1d

```
#include <iostream>
#include <cstring>
using namespace std;

#define MAX 10000

bool ganhou(char jogo[])
{
    char *p;
    if ((p=strstr(jogo,"XX"))!=NULL)
        return true;
    if ((p=strstr(jogo,"X.X"))!=NULL)
        return true;
    return false;
}

int main()
{
    int GrundyXX[MAX+1];
    int Grundy_X[MAX+1];
    int Grundy__[MAX+1];

    GrundyXX[2] = 0;
    GrundyXX[3] = 0;
    GrundyXX[4] = 0;

    for(int i=5; i<=MAX; i++) {
        bool s[MAX+1]={false};
        for(int j=2; j<=(i-1)/2; j++)
            s[GrundyXX[j] ^ GrundyXX[i-j-1]]=true;
        for(int j=0; j<i; j++)
            if (!s[j]) {
                GrundyXX[i] = j;
                break;
            }
    }

    Grundy_X[1] = 0;
    Grundy_X[2] = 0;
    Grundy_X[3] = 1;
    for(int i=4; i<=MAX; i++) {
        bool s[MAX+1]={false};
        s[GrundyXX[i-1]]=true;
        for(int j=2; j<=i-3; j++)
            s[GrundyXX[j] ^ Grundy_X[i-j-1]]=true;
        for(int j=0; j<i; j++)
            if (!s[j]) {
                Grundy_X[i] = j;
                break;
            }
    }

    Grundy__[3] = 1;
    for(int i=4; i<=MAX; i++) {
        if (Grundy_X[i-1]==0) //Jogar X-
            Grundy__[i] = 1;
        else {
            Grundy__[i] = 0;
            for(int j=1; j<=(i-1)/2; j++)
                if ((Grundy_X[j] ^ Grundy_X[i-j-1]) == 0) { //Jogar (-)X(-)
                    Grundy__[i] = 1;
                    break;
                }
        }
    }

    // cout << i << " " << j << "(" << Grundy_X[j] << " " << Grundy_X[i-j-1] << ")" << endl;

    cout << "Done!" << endl;

    int n, g = 0;
    char jogo[MAX+1];
    int i, j;

    cin >> n;
    while(n) {
        cin >> jogo;
        if (ganhou(jogo)) {
```

```

        cout << 'S' << endl;
        cin >> n;
        continue;
    }
    for(i=0; jogo[i]!='\0'; i++)
        if(jogo[i]=='X')
            break;
    if (jogo[i]!='\0') { //sem X
        g = grundy__[i];
        cout << "-- " << i << " g=" << grundy__[i] << endl;
    }
    else {
        if (i>0) { //nao comeca com X
            g = grundy_x[i];
            cout << "-x " << i << " g=" << grundy_x[i] << endl;
        }
        else
            g = 0;
        for(j=i+1; jogo[j]!='\0'; j++) {
            if (jogo[j]=='X') {
                g ^= grundyxx[j-i-1];
                cout << "x-x " << j-i-1 << " g=" << grundyxx[j-i-1] << endl;
                i = j;
            }
        }
        if (jogo[j-1]!='X') { //nao termina com X
            g ^= grundy_x[j-i-1];
            cout << "x- " << j-i-1 << " g=" << grundy_x[j-i-1] << endl;
        }
    }
    cout << (g?'S':'N') << endl;
    cin >> n;
}
return 0;
}

```

## 1.11 guloso azeitona do vovo pepe

```
#include <bits/stdc++.h>
using namespace std;
int main()
{
    int c, n, corte, atual, i, lim, azeitonas[20000];
    scanf("%d %d", &c, &n);
    lim = c / n;
    for(i = 0; i < n; i++)
        scanf("%d", &azeitonas[i]);
    for(corte = 0; corte <= lim; corte++) {
        atual = azeitonas[0] - corte;
        for(i = 0; i < n; i++) {
            if(!(azeitonas[i] >= atual && azeitonas[i] < atual + lim))
                goto a;
            atual += lim;
        }
        puts("S");
        return 0;
        a;;
    }
    puts("N");
}
```

## 1.12 line sweep k th fence fail

```
#include <bits/stdc++.h>
#include <ext/pb_ds/assoc_container.hpp>

using namespace std;
using namespace __gnu_pbds;

#define D(x) //cout << #x << " = " << x << endl

typedef pair<int, int> Ponto;
typedef pair<Ponto, int> Flor;

typedef tree<
    pair<int, int>,
    null_type,
    less<pair<int, int>>,
    rb_tree_tag,
    tree_order_statistics_node_update>
    ordered_set;

int main() {
    vector<Flor> flores;
    vector<Ponto> cercas;

    int p, v, aux;
    long long resp;

    scanf("%d %d", &p, &v);
    ordered_set eventos;
    flores = vector<Flor>(p);
    cercas = vector<Ponto>(v);

    for(int i = 0; i < p; i++)
        scanf("%d %d", &flores[i].first.first, &flores[i].first.second),
        flores[i].second = i + 1;

    for(auto &it : cercas)
        scanf("%d %d", &it.first, &it.second);

    sort(flores.begin(), flores.end());
    sort(cercas.begin(), cercas.end());

    auto flor = flores.begin();
    auto cerca = cercas.begin();

    resp = 0;
    aux = 1;

    while(flor != flores.end())
    {
        if(cerca == cercas.end())
        {
            resp += flor->second;
            ++flor;
        }
        else if(flor->first < *cerca)
        {
            auto lb = eventos.lower_bound({flor->first.second, 5000000});
            auto order = eventos.order_of_key(*lb);

            if(lb == eventos.end() || order % 2 == 0)
                resp += flor->second;

            ++flor;
        }
        else
        {
            auto lb = eventos.lower_bound({cerca->second, 0});
            if(lb != eventos.end() && lb->first == cerca->second)
                eventos.erase(lb);
            else
                eventos.insert({cerca->second, aux++});
            cerca++;
        }
    }

    printf("%lld\n", resp);
}
```

## 1.13 math integracao simpson

```
import java.util.function.DoubleFunction;

public class SimpsonIntegration {

    public static double integrate(DoubleFunction<Double> f, double a, double b) {
        double eps = 1e-10;
        double m = (a + b) / 2;
        double am = simpsonIntegration(f, a, m);
        double mb = simpsonIntegration(f, m, b);
        double ab = simpsonIntegration(f, a, b);
        if (Math.abs(am + mb - ab) < eps)
            return ab;
        return integrate(f, a, m) + integrate(f, m, b);
    }

    static double simpsonIntegration(DoubleFunction<Double> f, double a, double b) {
        return (f.apply(a) + 4 * f.apply((a + b) / 2) + f.apply(b)) * (b - a) / 6;
    }

    // Usage example
    public static void main(String[] args) {
        System.out.println(integrate(x -> Math.sin(x), 0, Math.PI / 2));
    }
}
```

## 1.14 math pascal

```
from sys import stdin
valores = []
fatorial = [1]
for i in range(1, 33):
    fatorial.append(fatorial[-1] * i)
def calc(n, x, produto, anterior):
    if(n == 0):
        valores.append(fatorial[h - 1] // produto)
        return
    if(x == 0):
        return
    for i in range(0, min(anterior + 1, n + 1)):
        calc(n - i, x - 1, produto * fatorial[i], i)
for line in stdin:
    d, h = map(int, line.split(' '))
    calc(h - 1, d, 1, h)
    valores = list(set(valores))
    valores.sort()
    for x in valores:
        print(x)
    valores = []
```

## 1.15 meet in the middle caxeiro indoring

```
#include <bits/stdc++.h>
using namespace std;
#define ultimo combi.size()-1
#define kultimo pos-1

long long dist_total, l;
int n;
bool visitado_combinacao[20];
long long mat_adj[20][20];
int para1, para2;

bool achei;
unordered_map<int, unordered_map<long long, int>[15]> puto;

int vet[20];
int preCP[20];

int elevado() {
    preCP[0] = 1;
    for(int i=1; i<20; i++)
        preCP[i] = preCP[i-1] * 2;
}

void combinacao(int val, int pos) {
    if(n-val + pos < para1)
        return;
    if(pos == para1) {
        int jaSei = 0;
        for(int i=0; i<pos; i++)
            jaSei = jaSei | preCP[vet[i]];

        do {
            dist_total = mat_adj[0][vet[0]];
            for(int i=1; i<pos; i++)
                dist_total += mat_adj[vet[i]][vet[i-1]];
            puto[jaSei][vet[pos-1]][dist_total] = 1;
        } while(next_permutation(vet, vet+pos));

        return;
    }
    for(int i=val; i<n; i++) {
        vet[pos] = i;
        combinacao(i + 1, pos+1);
    }
}

void combinacao2(int val, int pos) {
    if(n-val + pos < para2)
        return;
    if(pos == para2) {
        int jaSei = 0;
        for(int i=1; i<n; i++) {
            if(!visitado_combinacao[i])
                jaSei = jaSei | preCP[i];
        }
        do {
            dist_total = mat_adj[0][vet[0]];
            for(int i=1; i<pos; i++)
                dist_total += mat_adj[vet[i]][vet[i-1]];

            for(int it=1; it<n; it++) {
                if(!visitado_combinacao[it])
                    if (puto[jaSei][it].count(l-dist_total-mat_adj[it][vet[pos-1]]) != 0) {
                        puts("possible");
                        exit(0);
                    }
            }

        } while(next_permutation(vet, vet+pos));

        return;
    }
    for(int i=val; i<n; i++) {
        vet[pos] = i;
```

```

        visitado_combinacao[i] = true;
        combinacao2(i + 1, pos+1);
        visitado_combinacao[i] = false;
    }
}

int main() {
    elevado();
    cin >> n >> l;
    if(n%2 == 0) {
        para1 = n/2.0-1;
        para2 = n/2.0;
    }
    else {
        para1 = n/2.0;
        para2 = n/2.0;
    }

    achei = false;
    for(int i=0; i<n; i++)
        for(int j=0; j<n; j++)
            scanf("%lld", &mat_adj[i][j]);

    if(n == 2) {
        if(mat_adj[0][1]*2 == 1)
            puts("possible");
        else
            puts("impossible");
    }
    else {
        combinacao(1, 0);
        fill(visitado_combinacao, visitado_combinacao+n+1, false);
        visitado_combinacao[0] = true;
        vet[0] = 0;
        combinacao2(1, 0);

        if(!achei)
            puts("impossible");
    }

    return 0;
}

```



## 1.16 pd digitos digits counting

```
#include <bits/stdc++.h>
using namespace std;
struct SEQ {
    vector<int> qt;
    SEQ() {
        qt.assign(10,0);
    }
    SEQ operator - (const SEQ B) {
        SEQ novo;
        for(int i=0; i<=9; i++)
            novo.qt[i] = qt[i] - B.qt[i];
        return novo;
    }
    SEQ operator + (const SEQ B) {
        SEQ novo;
        for(int i=0; i<=9; i++)
            novo.qt[i] = qt[i] + B.qt[i];
        return novo;
    }
    void operator = (const SEQ B) {
        for(int i=0; i<=9; i++)
            qt[i] = B.qt[i];
    }
};

int exp(int a) {
    int cont = 1;
    for(int i=0; i<a; i++)
        cont *= 10;
    return cont;
}

SEQ andre(int n, int tam) {
    if(tam == 0) {
        SEQ novo;
        novo.qt[0]++;
        return novo;
    }
    int pot = exp(tam-1);
    int pri = n/pot;
    int rest = n%pot;
    SEQ cont;

    cont.qt[pri] = rest+1;
    for(int i=pri-1; i>=0; i--)
        cont.qt[i] += pot;

    for(int i=0; i<=9; i++)
        cont.qt[i] += pri*(tam-1)*(pot/10);

    cont.qt[0] -= pot;
    return cont + andre(rest, tam-1);
}

int main() {
    int a, b, aux_a, aux_b;
    int qt_a, qt_b;

    while((scanf("%d%d", &a, &b) && a+b)) {
        aux_a = a-1;
        aux_b = b;
        qt_a = qt_b = 0;

        while(aux_a) {
            qt_a++;
            aux_a /= 10;
        }

        while(aux_b) {
            qt_b++;
            aux_b /= 10;
        }

        SEQ novo = andre(b, qt_b) - andre(a-1, qt_a);
```

```
        cout << novo.qt[0];  
        for(int i=1; i<=9; i++)  
            cout << " " << novo.qt[i];  
        cout << endl;  
    }  
    return 0;  
}
```

## 1.17 pd garcom internet trouble

```
#include <bits/stdc++.h>
using namespace std;
long long custo[6010][6010], pd[6010][6010], valores[6100], acumulado[6100];
int k_opt[6010][6010] = {0}, b, n;

/*
    PD Original
    for (int i = 1; i <= n; i++)
        for (int j = 1; j <= n; j++)
            for (int k = 0; k < i; k++)
                if (b + pd[k][j - 1] + custo[k + 1][i] < pd[i][j])
                {
                    pd[i][j] = b + pd[k][j - 1] + custo[k + 1][i];
                    k_opt[i][j] = k;
                }
*/
void resolve(int i, int j, int opt_l, int opt_r)
{
    k_opt[i][j] = opt_l;
    for (int k = opt_l; k <= opt_r; k++)
        if (b + pd[k][j - 1] + custo[k + 1][i] < pd[i][j])
        {
            pd[i][j] = b + pd[k][j - 1] + custo[k + 1][i];
            k_opt[i][j] = k;
        }
}

void calcula(int i, int l, int r, int opt_l, int opt_r)
{
    if (l > r)
        return;
    int m = (l + r) / 2;
    resolve(i, m, opt_l, opt_r);
    calcula(i, l, m - 1, opt_l, k_opt[i][m]);
    calcula(i, m + 1, r, k_opt[i][m], opt_r);
}

int main()
{
    int c;
    while (scanf("%d %d %d", &n, &b, &c) > 0)
    {
        for (int i = 0; i <= n; i++)
        {
            fill(pd[i], pd[i] + n + 1, 0ll);
            fill(custo[i], custo[i] + n + 1, 0ll);
        }
        for (int i = 0; i < n; i++)
            scanf("%lld", &valores[i]);
        acumulado[0] = 0;
        for (int i = 0; i < n; i++)
            acumulado[i + 1] = valores[i] + acumulado[i];
        for (int i = 0; i < n; i++)
        {
            pd[i][0] = valores[0] * i;
            pd[i][n - 1] = valores[n - 1] * (n - 1 - i);
            for (int j = 1; j < i; j++)
                pd[i][j] = pd[i][j - 1] + valores[j] * (i - j);
            for (int j = n - 2; j > i; j--)
                pd[i][j] = pd[i][j + 1] + valores[j] * (j - i);
            if (i < n - 1)
                pd[i][i] += pd[i][i + 1];
            if (i)
                pd[i][i] += pd[i][i - 1];
        }
        for (int i = 0; i < n; i++)
        {
            custo[i][i] = 0;
```

```

for (int j = 0; j < i; j++)
{
    auto val_mediana = (acumulado[i + 1] - acumulado[j]) / 2 + acumulado[j];
    auto mediana = distance(acumulado, upper_bound(acumulado, acumulado + n, val_mediana)) - 1;
    auto val = pd[mediana][mediana];
    if (i < n - 1)
        val -= pd[mediana][i + 1];
    if (j)
        val -= pd[mediana][j - 1];
    custo[i + 1][j + 1] = c * val;
}
for (int j = i + 1; j < n; j++)
{
    auto val_mediana = (acumulado[j + 1] - acumulado[i]) / 2 + acumulado[i];
    auto mediana = distance(acumulado, upper_bound(acumulado, acumulado + n, val_mediana)) - 1;
    auto val = pd[mediana][mediana];
    if (j < n - 1)
        val -= pd[mediana][j + 1];
    if (i)
        val -= pd[mediana][i - 1];
    custo[i + 1][j + 1] = c * val;
}
}
for (int i = 0; i <= n; i++)
    fill(pd[i], pd[i] + n + 1, 111 << 60);
pd[0][0] = 0;
for (int i = 1; i <= n; i++)
    calcula(i, 1, i + 1, 0, i - 1);
for (int j = 1; j <= n; j++)
    cout << pd[n][j] << " \n"[j == n];
}
}

```

## 1.18 pd intervalos hiperatcive

```
#include <bits/stdc++.h>
using namespace std;
int m, n, s, f, a, b;
vector<pair<int, int> > intervalos;
map<pair<int, int>, int> pd;
int pdzona(int ii, int ini) {
    if(intervalos[ii].first == m)
        return 1;

    auto h = make_pair(ii, ini);
    if(pd.count(h) != 0)
        return pd[h];

    int cont = 0;
    for(int j=ii+1; j<n; j++) {
        if(intervalos[j].first > intervalos[ii].first && intervalos[j].second > ini && intervalos[j].
            second <= intervalos[ii].first) {
            cont = (cont+pdzona(j, intervalos[ii].first))%1000000000;
        }
    }
    return pd[h] = cont;
}
int main() {
    while(cin >> m >> n) {
        if(m+n == 0)
            return 0;
        intervalos.clear();
        pd.clear();

        for(int i=0; i<n; i++) {
            cin >> a >> b;
            intervalos.push_back(make_pair(b, a));
        }
        sort(intervalos.begin(), intervalos.end());

        int cont = 0;
        for(int i=0; i<n; i++) {
            if(intervalos[i].second == 0)
                cont = (cont+pdzona(i, 0))%1000000000;
        }
        cout << cont << endl;
    }
    return 0;
}
```

## 1.19 pd math prob war quarta mineira

```
#include <stdio.h>
#include <math.h>

long int probPerder[4][4][4] = {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 15, 21, 0, 0, 55,
    161, 0, 0, 55, 1241, 0, 0, 0, 0, 0, 0, 125, 91, 0, 0, 370, 290, 636, 0, 370, 1250, 6156, 0, 0, 0, 0, 0,
    1025, 271, 0, 0, 4030, 2090, 1656, 0, 3123, 11104, 10663, 21766};
double probs[4][4][4] = {0}, chances[10002][10002] = {0};

inline int max(int a, int b) {
    return a > b ? a : b;
}

inline int min(int a, int b) {
    return a < b ? a : b;
}

inline double dmax(double a, double b) {
    return a > b ? a : b;
}

inline double dmin(double a, double b) {
    return a < b ? a : b;
}

double chance(int atk, int def) {
    if(def <= 0)
        return 1;
    if(atk <= 0)
        return 0;
    return chances[atk][def];
}

double calc(int atk, int def, int da, int dd) {
    int i, j, qtd = min(da, dd);
    double prob = 0;
    for(i = 0; i <= qtd; i++)
        prob += probs[da][dd][i] * chance(atk-i, def-qtd+i);
    return prob;
}

double minimo(int atk, int def, int da) {
    int i, j, qtd = min(def, 3);
    double r = 2;
    for(i = 1; i <= qtd; i++)
        r = dmin(r, calc(atk, def, da, i));
    return r;
}

double maximo(int atk, int def) {
    int i, j, qtd = min(atk, 3);
    double r = 0;
    for(i = 1; i <= qtd; i++)
        r = dmax(r, minimo(atk, def, i));
    return r;
}

int main() {
    int i, j, k, a, b;
    for(i = 1; i <= 3; i++)
        for(j = 1; j <= 3; j++)
            for(k = 0; k < 4; k++)
                probs[i][j][k] = probPerder[i][j][k]/(pow(6, i+j));

    scanf("%d %d", &a, &b);
    a--;

    // min-max para atk <= 3 || def <= 3
    for(i = 1; i <= 50; i++)
        for(j = 1; j <= 3; j++) {
            chances[i][j] = maximo(i, j);
            chances[j][i] = maximo(j, i);
        }

    for(i = 51; i <= max(a, b); i++)
        chances[i][1] = chances[i][2] = chances[i][3] = 1;

    // guloso para atk > 3 && def > 3
    for(i = 4; i <= a; i++)
```

```

    for(j = (a+b)%3-(i%3); j <= b; j+=3) {
        if(j <= 3)
            continue;

        chances[i][j] = probs[3][3][0] * chances[i][j-3] + probs[3][3][1] * chances[i-1][j-2] +
            probs[3][3][2] * chances[i-2][j-1] + probs[3][3][3] * chances[i-3][j];

        if(chances[i][j] < 0.000001)
            break;
    }
    printf("%.04lf\n", chances[a][b]);
}

```

## 1.20 pd minmax bottomup cartoes

```
#include <bits/stdc++.h>
#define D(x) cout << #x << " = " << x << endl;
using namespace std;
int main() {
    int n;
    long long cartoes[12000];
    long long A[12000];
    long long W[12000];
    while(cin >> n) {
        for(int i=0; i<n; i++) {
            scanf("%lld", &cartoes[i]);
            A[i] = W[i] = 0;
        }
        for(int i=1; i<n; i++) {
            for(int j=0; j<n-i; j++) {
                if(i%2 == 0)
                    W[j] = min(A[j], A[j+1]);
                else
                    A[j] = max( (cartoes[j] + W[j+1]),
                               (cartoes[j+i] + W[j]));
            }
        }
        cout << A[0] << endl;
    }
    return 0;
}
```



## 1.21 pd segtree keep it energized

```
#include <bits/stdc++.h>
using namespace std;
#define MAX 1000000 // 0 valor aqui tem que ser >= 2 * tamanho do maior n
#define D(x) cout << #x << " = " << x << endl
int init[MAX], tree[MAX], lazy[MAX];
typedef vector<int> vi;
struct Loja {
    int l, s, c;
};
void build_tree(int node, int a, int b)
{
    if (a > b)
        return;

    // Se folha
    if (a == b)
    {
        tree[node] = 1 << 30;
        return;
    }

    build_tree(node * 2, a, (a + b) / 2);
    build_tree(node * 2 + 1, 1 + (a + b) / 2, b);
    tree[node] = min(tree[node * 2], tree[node * 2 + 1]);
}

void update_tree(int node, int a, int b, int i, int j, int value)
{
    // Se fora do intervalo - retorna
    if (a > b || a > j || b < i)
        return;

    if (a >= i && b <= j)
    {
        tree[node] = value;
        return;
    }

    // Atualiza os filhos.
    update_tree(node * 2, a, (a + b) / 2, i, j, value);
    update_tree(1 + node * 2, 1 + (a + b) / 2, b, i, j, value);

    // Atualiza o pai.
    tree[node] = min(tree[node * 2], tree[node * 2 + 1]);
}

int query_tree(int node, int a, int b, int i, int j)
{
    // Se fora do intervalo
    if (a > b || a > j || b < i)
    {
        return 1 << 30;
    }

    if (a >= i && b <= j)
        return tree[node];

    int q1 = query_tree(node * 2, a, (a + b) / 2, i, j);
    int q2 = query_tree(1 + node * 2, 1 + (a + b) / 2, b, i, j);
    return min(q1, q2);
}

int main() {
    int n, m;
    scanf("%d %d", &n, &m);
    build_tree(1, 0, n);
    auto custos = vi(n);
    auto acumulado = vi(n + 1);
    for(auto &it : custos)
        scanf("%d", &it);
    acumulado[n] = 0;
```

```

for(int i = n - 1; i >= 0; i--)
    acumulado[i] = acumulado[i + 1] + custos[i];
auto lojas = vector<Loja>(m);
auto pacotes = vector<vector<pair<int, int> > >(n);
auto alcance = vi(m);
auto count = 0;
for(auto &it : lojas) {
    scanf("%d %d %d", &it.l, &it.s, &it.c);
    pacotes[it.l - 1].push_back({count, it.c});
    auto eu = lower_bound(acumulado.rbegin(), acumulado.rend(), acumulado[it.l - 1] - it.s);
    alcance[count++] = distance(eu, acumulado.rend()) - 1;
}
auto pd = vi(n + 1, 1 << 30);
pd[n] = 0;
update_tree(1, 0, n, n, n, 0);
for(int i = n - 1; i >= 0; i--) {
    for(auto pacote : pacotes[i])
        pd[i] = min(pd[i], query_tree(1, 0, n, i, alcance[pacote.first]) + pacote.second);
    update_tree(1, 0, n, i, i, pd[i]);
}
if(pd[0] != 1 << 30)
    cout << pd[0] << endl;
else
    puts("-1");
}

```

## 1.22 pd string guardioes curiosos

```
#include <bits/stdc++.h>
using namespace std;
typedef vector<int> vl;
typedef vector<vl> vvl;
vvl pd;
int k, tam;
vvl pascal(101, vl(101, 0));
long long conta(int n, int m)
{
    if (n == 0)
        return 0;
    if (m == 1)
        return n;
    if (n == 1 && m < k || m == 0)
        return 1;
    if (pd[n][m] != -1)
        return pd[n][m];
    long long resp = 0;
    for (int i = 0; i < min(k, m + 1); i++)
        resp = (resp + (conta(n - 1, m - i) * pascal[m][i]) % 1000000007) % 1000000007;
    return pd[n][m] = resp;
}
int main()
{
    int i, j;
    pascal[0][0] = 1;
    for (i = 0; i < 101; i++)
        pascal[i][0] = 1;
    for (i = 1; i < 101; i++)
        for (j = 1; j < 101; j++)
            pascal[i][j] = (pascal[i - 1][j - 1] + pascal[i - 1][j]) % 1000000007;
    scanf("%d %d", &tam, &k);
    pd = vvl(tam + 1, vl(tam + 1, -1));
    printf("%d\n", conta(tam, tam - 2));
}
```

## 1.23 segtree acordes intergalaticos

```
#include <bits/stdc++.h>
using namespace std;
#define MAX 1000000 // 0 valor aqui tem que ser >= 4 * tamanho do maior n
#define ELEMENTO_NEUTRO 0
vector<int> freq(9);
struct No
{
    int F[9] = {0};
    No(int a)
    {
        F[a] = 1;
    }
    No() {}
    No operator+(const No &a) const
    {
        No novo;
        for (int i = 0; i < 9; i++)
            novo.F[i] = F[i] + a.F[i];
        return novo;
    }
    No operator=(const No &a)
    {
        for (int i = 0; i < 9; i++)
            this->F[i] = a.F[i];
        return *this;
    }
    void update(int max)
    {
        int temp[9];
        for (int i = 0; i < 9; i++)
            temp[i] = F[i];
        for (int i = 0; i < 9; i++)
            F[(i + max) % 9] = temp[i];
    }
    int val()
    {
        int max = 0;
        for (int i = 1; i < 9; i++)
            if (F[i] >= F[max])
                max = i;
        return max;
    }
};
int init[MAX], lazy[MAX];
No tree[MAX];
void build_tree(int node, int a, int b)
{
    if (a > b)
        return;
    if (a == b)
    {
        tree[node] = No(init[a]);
        lazy[node] = 0;
        return;
    }
    build_tree(node * 2, a, (a + b) / 2);
    build_tree(node * 2 + 1, 1 + (a + b) / 2, b);
    //Atualização do pai - verificar operação
    tree[node] = tree[node * 2] + tree[node * 2 + 1];
    lazy[node] = 0;
}
void update_tree(int node, int a, int b, int i, int j, int val)
{
    //Atualização atrasada - verificar operação
```

```

if (lazy[node] != 0)
{
    tree[node].update(lazy[node]);
    if (a != b)
    {
        lazy[node * 2] += lazy[node];
        lazy[node * 2 + 1] += lazy[node];
    }
    lazy[node] = 0;
    return;
}
if (a > b || a > j || b < i)
    return;
//Atualização do nó - verificar operação
if (a >= i && b <= j)
{
    tree[node].update(val);
    if (a != b)
    {
        lazy[node * 2] += val;
        lazy[node * 2 + 1] += val;
    }
    return;
}
update_tree(node * 2, a, (a + b) / 2, i, j, val);
update_tree(1 + node * 2, 1 + (a + b) / 2, b, i, j, val);
//Atualização do pai - verificar operação
tree[node] = tree[node * 2] + tree[node * 2 + 1];
}
int query_tree(int node, int a, int b, int i, int j)
{
    if (a > b || a > j || b < i)
    {
        return 0;
    }
    //Atualização atrasada - verificar operação
    if (lazy[node] != 0)
    {
        tree[node].update(lazy[node]);
        if (a != b)
        {
            lazy[node * 2] += lazy[node];
            lazy[node * 2 + 1] += lazy[node];
        }
        lazy[node] = 0;
    }
    if (a == i && b == j && a == b)
        return tree[node].val();
    int q1 = query_tree(node * 2, a, (a + b) / 2, i, j);
    int q2 = query_tree(1 + node * 2, 1 + (a + b) / 2, b, i, j);
    //Retorno da árvore - verificar operação
    return q1 + q2;
}
void most_freq(int node, int a, int b, int i, int j)
{
    if (a > b || a > j || b < i)
    {
        return;
    }
    //Atualização atrasada - verificar operação
    if (lazy[node] != 0)
    {
        tree[node].update(lazy[node]);
        if (a != b)
        {
            lazy[node * 2] += lazy[node];
            lazy[node * 2 + 1] += lazy[node];
        }
    }
}

```

```

        lazy[node] = 0;
    }
    if (a >= i && b <= j)
    {
        for (int i = 0; i < 9; i++)
            freq[i] += tree[node].F[i];
        return;
    }
    most_freq(node * 2, a, (a + b) / 2, i, j);
    most_freq(1 + node * 2, 1 + (a + b) / 2, b, i, j);
}

int main()
{
    int n, q, a, b;
    scanf("%d %d", &n, &q);
    fill(init, init + n, 1);
    build_tree(1, 0, n - 1);
    while (q--)
    {
        scanf("%d %d", &a, &b);
        int most = 0;
        for (auto &it : freq)
            it = 0;
        most_freq(1, 0, n - 1, a, b);
        for (int i = 1; i < 9; i++)
            if (freq[i] >= freq[most])
                most = i;
        update_tree(1, 0, n - 1, a, b, most);
    }
    for (int i = 0; i < n; i++)
        printf("%d\n", query_tree(1, 0, n - 1, i, i));
}

```

## 1.24 segtree homem elefante rato

```
#include <bits/stdc++.h>
using namespace std;
#define MAX 6000000
typedef struct tDado {
    int h, e, r;
    tDado operator++(int a) {
        int aux = e;
        e = h;
        h = r;
        r = aux;
    }
    tDado operator+(const tDado &a) {
        tDado b;
        b.h = h + a.h;
        b.e = e + a.e;
        b.r = r + a.r;
        return b;
    }
    tDado operator=(const tDado &a) {
        h = a.h;
        e = a.e;
        r = a.r;
        return *this;
    }
    tDado operator=(int a) {
        h = a == 0;
        e = a == 1;
        r = a == 2;
        return *this;
    }
} tDado;
tDado init[MAX], tree[MAX];
int lazy[MAX];
void build_tree(int node, int a, int b) {
    if(a > b)
        return;
    if(a == b) {
        tree[node] = init[a];
        lazy[node] = 0;
        return;
    }
    build_tree(node*2, a, (a+b)/2);
    build_tree(node*2+1, 1+(a+b)/2, b);
    tree[node] = tree[node*2] + tree[node*2+1];
    lazy[node] = 0;
}
void update_tree(int node, int a, int b, int i, int j, int value) {
    if(lazy[node] != 0) {
        for(int k = 0; k < lazy[node] % 3; k++)
            tree[node]++;
        if(a != b) {
            lazy[node*2] += lazy[node];
            lazy[node*2+1] += lazy[node];
        }
        lazy[node] = 0;
    }
    if(a > b || a > j || b < i)
        return;
    if(a >= i && b <= j) {
        tree[node]++;
        if(a != b) {
            lazy[node*2]++;
            lazy[node*2+1]++;
        }
        return;
    }
    if(a == b) {
        tree[node]++;
    }
}
```

```

    return;
}
update_tree(node*2, a, (a+b)/2, i, j, value);
update_tree(1+node*2, 1+(a+b)/2, b, i, j, value);
tree[node] = tree[node*2] + tree[node*2+1];
}

tDado query_tree(int node, int a, int b, int i, int j) {
    if(a > b || a > j || b < i) {
        tDado a;
        a = -1;
        return a;
    }

    if(lazy[node] != 0) {
        for(int k = 0; k < lazy[node] % 3; k++)
            tree[node]++;

        if(a != b) {
            lazy[node*2] += lazy[node];
            lazy[node*2+1] += lazy[node];
        }
        lazy[node] = 0;
    }

    if(a >= i && b <= j)
        return tree[node];

    tDado q1 = query_tree(node*2, a, (a+b)/2, i, j);
    tDado q2 = query_tree(1+node*2, 1+(a+b)/2, b, i, j);

    return q1 + q2;
}

int main () {
    char op;
    int n, m, i, a, b;
    tDado resp;

    while(scanf("%d %d", &n, &m) > 0) {
        for(i = 0; i < n; i++)
            init[i] = 0;

        build_tree(1, 0, n-1);

        for(i = 0; i < m; i++) {
            scanf(" %c %d %d", &op, &a, &b);

            if(op == 'M')
                update_tree(1, 0, n-1, a-1, b-1, 0);
            else {
                resp = query_tree(1, 0, n-1, a-1, b-1);
                printf("%d %d %d\n", resp.h, resp.e, resp.r);
            }
        }

        printf("\n");
    }

    return 0;
}

```



## 1.25 simulacao mochilas nwer

```
#include <bits/stdc++.h>
using namespace std;
long long mdc(long long a, long long b)
{
    long long remainder;
    while (b != 0)
    {
        remainder = a % b;
        a = b;
        b = remainder;
    }
    return a;
}
int main() {
    multiset<long long> original;
    long long n, s, t;
    long long aux;
    cin >> n >> s >> t;
    for(long long i=0; i<n; i++) {
        scanf("%lld", &aux);
        original.insert(aux);
    }
    long long melhor = 1LL<<60, pior = -1, media = 0;
    long long t_mod;
    for(auto it = original.begin(); it != original.end(); it++) {
        multiset<long long> esteira = original;
        long long tempo = *it;
        long long diferenca;
        auto quem = esteira.erase(esteira.lower_bound(tempo));
        auto fulano = esteira.begin();
        tempo += t;
        while(!esteira.empty()) {
            t_mod = tempo%s;
            quem = esteira.lower_bound(t_mod);
            if(quem == esteira.end())
                quem = esteira.begin();
            if(*quem < t_mod)
                tempo += s + *quem - t_mod;
            else
                tempo += *quem - t_mod;
            esteira.erase(quem);
            tempo += t;
        }
        tempo -= *it;
        melhor = min(melhor, tempo);
        if(it == original.begin()) {
            auto asd = original.end();
            asd--;
            diferenca = *it + s - *asd;
        }
        else {
            fulano = it;
            fulano--;
            diferenca = *it - *fulano;
        }
        pior = max(pior, tempo + diferenca - 1);
        media += diferenca*tempo + diferenca*(diferenca-1)/2;
    }
    if(original.count(*original.begin()) == original.size()) {
        pior = melhor+s-1;
        media = s*melhor + s*(s-1)/2;
    }
    cout << melhor << "\n" << pior << endl;
```

```
    long long mmm = mdc(media, s);  
    printf("%lld/%lld\n", media/mmm, s/mmm);  
    return 0;  
}
```

## 1.26 string aho crosahick

```
public class AhoCorasick {
    static final int ALPHABET_SIZE = 26;
    Node[] nodes;
    int nodeCount;
    public static class Node {
        int parent;
        char charFromParent;
        int suffLink = -1;
        int[] children = new int[ALPHABET_SIZE];
        int[] transitions = new int[ALPHABET_SIZE];
        boolean leaf;

        {
            Arrays.fill(children, -1);
            Arrays.fill(transitions, -1);
        }
    }

    public AhoCorasick(int maxNodes) {
        nodes = new Node[maxNodes];
        // create root
        nodes[0] = new Node();
        nodes[0].suffLink = 0;
        nodes[0].parent = -1;
        nodeCount = 1;
    }

    public void addString(String s) {
        int cur = 0;
        for (char ch : s.toCharArray()) {
            int c = ch - 'a';
            if (nodes[cur].children[c] == -1) {
                nodes[nodeCount] = new Node();
                nodes[nodeCount].parent = cur;
                nodes[nodeCount].charFromParent = ch;
                nodes[cur].children[c] = nodeCount++;
            }
            cur = nodes[cur].children[c];
        }
        nodes[cur].leaf = true;
    }

    public int suffLink(int nodeIndex) {
        Node node = nodes[nodeIndex];
        if (node.suffLink == -1)
            node.suffLink = node.parent == 0 ? 0 : transition(suffLink(node.parent), node.charFromParent);
        return node.suffLink;
    }

    public int transition(int nodeIndex, char ch) {
        int c = ch - 'a';
        Node node = nodes[nodeIndex];
        if (node.transitions[c] == -1)
            node.transitions[c] = node.children[c] != -1 ? node.children[c] : (nodeIndex == 0 ? 0 :
                transition(suffLink(nodeIndex), ch));
        return node.transitions[c];
    }

    // Usage example
    public static void main(String[] args) {
        AhoCorasick ahoCorasick = new AhoCorasick(1000);
        ahoCorasick.addString("bc");
        ahoCorasick.addString("abc");

        String s = "tabcbc";
        int node = 0;
        List<Integer> positions = new ArrayList<>();
        for (int i = 0; i < s.length(); i++) {
            node = ahoCorasick.transition(node, s.charAt(i));
            if (ahoCorasick.nodes[node].leaf)
                positions.add(i);
        }
        System.out.println(positions);
    }
}
```

## 1.27 string matching game of matchings

```
s=raw_input()
m=int(raw_input())
p=map(int,raw_input().split())
n=len(s)
#befp[i]=max {j: j<i and p[j]=p[i]}
last=[-1]*27
befp=[-1]*m
for i in range(m):
    ch=p[i]
    befp[i]=last[ch]
    last[ch]=i
#befp[i]=max {j: j<i and s[j]=s[i]}
last=[-1]*27
befp=[-1]*n
for i in range(n):
    ch=ord(s[i])-ord('a')
    befp[i]=last[ch]
    last[ch]=i
#f[i]=failure function
f=[0]*m
idx=0
for i in range(1,m):
    match=False
    while idx>0 and not match:
        match=True
        if befp[i]!=-1 and idx>=(i-befp[i]):
            at=idx-(i-befp[i])
            if p[idx]!=p[at]:
                idx=f[idx-1]
                match=False
            if match and befp[idx]!=-1:
                at=i-(idx-befp[idx])
                if p[at]!=p[i]:
                    idx=f[idx-1]
                    match=False
        idx+=1
    f[i]=idx
#kmp
idx=0
ans=0
for i in range(n):
    match=False
    while idx>0 and not match:
        match=True
        if befp[i]!=-1 and idx>=(i-befp[i]):
            at=idx-(i-befp[i])
            if p[idx]!=p[at]:
                idx=f[idx-1]
                match=False
            if match and befp[idx]!=-1:
                at=i-(idx-befp[idx])
                if s[at]!=s[i]:
                    idx=f[idx-1]
                    match=False
        idx+=1
    if idx==m:
        #match at i-m+1
        ans+=1
        idx=f[m-1]
print ans
```

## 1.28 string quebrar em palindromos russa

```
#include <bits/stdc++.h>
using namespace std;
typedef vector<int> vi;
#define D(x) cout << #x << " = " << x << endl
int main() {
    ios::sync_with_stdio(false);
    int n;
    string entrada;
    cin >> n;
    cin >> entrada;
    vi apareceu(255);
    for(auto &it : entrada)
        apareceu[it]++;
    int impares = 0, palindromos = 1, tamanho;
    vi usaveis;
    for(int i = 0; i < 255; i++)
        if(apareceu[i] % 2)
            usaveis.push_back(i), impares++, apareceu[i]--;
    palindromos = max(impares, palindromos);
    if(palindromos > 1)
        while(palindromos < entrada.size()) {
            if((entrada.size() % palindromos) == 0 && (entrada.size() / palindromos) % 2 == 1)
                break;
            else
                palindromos += 2;
        }
    if(entrada.size() % palindromos)
        palindromos = entrada.size();
    cout << palindromos << endl;
    tamanho = entrada.size() / palindromos;
    int j = 0;
    for(int i = 0; i < palindromos; i++) {
        string resposta;
        if(tamanho % 2) {
            if(usaveis.size())
                resposta = usaveis.back(), usaveis.pop_back();
            else {
                for(int k = 0; k < 255; k++)
                    if(apareceu[k]) {
                        usaveis.push_back(k);
                        resposta = k;
                        apareceu[k] -= 2;
                        break;
                    }
            }
        }
        for(; j < 255; j++) {
            while(apareceu[j]) {
                resposta += ((char) j);
                apareceu[j] -= 2;
                if(tamanho <= resposta.size() * 2)
                    break;
            }
            if(tamanho <= resposta.size() * 2)
                break;
        }
        reverse(resposta.begin(), resposta.end());
        cout << resposta;
        if(tamanho % 2)
```

```
        resposta.erase(resposta.end() - 1, resposta.end());
reverse(resposta.begin(), resposta.end());
cout << resposta;
cout << " \n"[i == palindromos-1];
    }
}
```

## 1.29 string trie dicionario portunhol

```
#include <bits/stdc++.h>
using namespace std;
long long sss1, sss2;
long long tot_pt[256];
long long tot_es[256];

struct No
{
    char c;
    vector<No> filhos;
};

void conta_pt(No &atual, long long qt) {
    if(atual.filhos.size() == 0) {
        sss1 += qt;
        return;
    }
    bool soma = true;
    for(auto &it : atual.filhos) {
        if(soma)
            conta_pt(it, qt+1);
        else
            conta_pt(it, 1);
        soma = false;
    }
}

void conta_es(No &atual, long long qt) {
    if(atual.filhos.size() == 0) {
        sss2 += qt;
        return;
    }
    bool soma = true;
    for(auto &it : atual.filhos) {
        if(soma)
            conta_es(it, qt+1);
        else
            conta_es(it, 1);
        soma = false;
    }
}

void total_pt(No &atual, bool faz) {
    if(faz)
        tot_pt[atual.c]++;
    for(auto &it : atual.filhos)
        total_pt(it, true);
}

void total_es(No &atual, bool faz) {
    if(faz)
        tot_es[atual.c]++;
    for(auto &it : atual.filhos)
        total_es(it, true);
}

int main()
{
    ios::sync_with_stdio(false);
    cin.tie(0);
    cout.tie(0);

    int n, i, m;
    string pal;

    No pt;
    No es;

    pt.c = es.c = '-';

    // Lê n palavras e monta a arvore de todas as palavras, adicionando $ a cada fim de palavra
    while(cin >> n >> m)
    {
        if(n+m == 0)
            return 0;
    }
}
```

```

sss1 = sss2 = 0;
fill(tot_es + 'a', tot_es + 'z' + 1, 0);
fill(tot_pt + 'a', tot_pt + 'z' + 1, 0);
pt.filhos.clear();
es.filhos.clear();
No *atual;
for(i = 0; i < n; i++)
{
    atual = &pt;
    cin >> pal;
    for(auto &it : pal)
    {
        for(auto &it2 : atual->filhos) {
            if(it2.c == it) {
                atual = &it2;
                goto prox1;
            }
        }
        atual->filhos.push_back(No());
        atual = &(atual->filhos.back());
        atual->c = it;
        prox1++;
    }
}
for(i = 0; i < m; i++)
{
    atual = &es;
    cin >> pal;
    for(int j=pal.size()-1; j >= 0; j--)
    {
        for(auto &it2 : atual->filhos) {
            if(it2.c == pal[j]) {
                atual = &it2;
                goto prox2;
            }
        }
        atual->filhos.push_back(No());
        atual = &(atual->filhos.back());
        atual->c = pal[j];
        prox2++;
    }
}
for(auto it : pt.filhos) {
    conta_pt(it, 1);
    total_pt(it, false);
}
for(auto it : es.filhos) {
    conta_es(it, 1);
    total_es(it, false);
}
long long soma_tot = 0;
for(int j = 'a'; j <= 'z'; j++)
    soma_tot -= tot_pt[j] * tot_es[j];
soma_tot += sss1 * sss2;
cout << soma_tot << '\n';
}
}

```



### 1.30 suffix array growing strings

```
#include <bits/stdc++.h>
using namespace std;
#define PB push_back
typedef vector<int> vi;
const int MAX = 1005000;
bool comp(string a, string b)
{
    return a.size() < b.size();
}
vi txt;
int iSA[MAX], SA[MAX]; //input //output
int cnt[MAX], prox[MAX]; //internal
bool bh[MAX], b2h[MAX];

// Compares two suffixes according to their first characters
bool smaller_first_char(int a, int b)
{
    return txt[a] < txt[b];
}

void suffixSort(int n)
{
    for (int i = 0; i < n; ++i)
        SA[i] = i;
    sort(SA, SA + n, smaller_first_char);
    for (int i = 0; i < n; ++i)
    {
        bh[i] = i == 0 || txt[SA[i]] != txt[SA[i - 1]];
        b2h[i] = false;
    }
    for (int h = 1; h < n; h <= 1)
    {
        int buckets = 0;
        for (int i = 0, j; i < n; i = j)
        {
            j = i + 1;
            while (j < n && !bh[j])
                j++;
            prox[i] = j;
            buckets++;
        }
        if (buckets == n)
            break;
        for (int i = 0; i < n; i = prox[i])
        {
            cnt[i] = 0;
            for (int j = i; j < prox[i]; ++j)
                iSA[SA[j]] = i;
        }
        cnt[iSA[n - h]]++;
        b2h[iSA[n - h]] = true;
        for (int i = 0; i < n; i = prox[i])
        {
            for (int j = i; j < prox[i]; ++j)
            {
                int s = SA[j] - h;
                if (s >= 0)
                {
                    int head = iSA[s];
                    iSA[s] = head + cnt[head]++;
                    b2h[iSA[s]] = true;
                }
            }
        }
        for (int j = i; j < prox[i]; ++j)
        {
            int s = SA[j] - h;
```

```

        if (s >= 0 && b2h[iSA[s]])
            for (int k = iSA[s] + 1; !bh[k] && b2h[k]; k++)
                b2h[k] = false;
    }
    for (int i = 0; i < n; ++i)
    {
        SA[iSA[i]] = i;
        bh[i] |= b2h[i];
    }
    for (int i = 0; i < n; ++i)
    {
        iSA[SA[i]] = i;
    }
}

int lcp[MAX];
void getlcp(int n)
{
    for (int i = 0; i < n; ++i)
        iSA[SA[i]] = i;

    lcp[0] = 0;
    for (int i = 0, h = 0; i < n; ++i)
    {
        if (iSA[i] > 0)
        {
            int j = SA[iSA[i] - 1];
            while (i + h < n && j + h < n && txt[i + h] == txt[j + h])
                h++;
            lcp[iSA[i]] = h;
            if (h > 0)
                h--;
        }
    }
}

int main()
{
    ios::sync_with_stdio(false);
    cin.tie(0);
    int n, resp;
    while (cin >> n && n)
    {
        txt.clear();
        map<int, int> posicoesIniciais, posicoesFinais, aVisitar;
        vi pd(n, 1);
        vector<string> palavras(n);
        resp = 0;

        for (auto &it : palavras)
            cin >> it;
        sort(palavras.begin(), palavras.end(), comp);

        for (int i = 0; i < n; i++)
        {
            posicoesIniciais[txt.size()] = i;
            for (auto &it : palavras[i])
                txt.PB(it + 20000);

            // Fim de palavra (menor que todas as letras e crescente)
            // pra ordenar certo;
            txt.PB(1 + i);
            posicoesFinais[txt.size()] = i;
        }
        suffixSort(txt.size());
        getlcp(txt.size());
        for (int i = 0; i < txt.size() - 1; i++)
        {
            auto inicial = posicoesIniciais.find(SA[i]);
            if (inicial != posicoesIniciais.end() && lcp[i + 1] == palavras[inicial->second].size())
                aVisitar[inicial->second] = i;
        }
    }
}

```

```

    }
    for (auto &it : aVisitar)
    {
        for (int j = it.second + 1; j < txt.size(); j++)
            if (lcp[j] < palavras[it.first].size())
                break;
            else
            {
                auto atual = posicoesFinais.upper_bound(SA[j])->second;
                pd[atual] = max(pd[atual], pd[it.first] + 1);
            }
    }
    for (auto &it : pd)
        resp = max(resp, it);
    cout << resp << "\n";
}
}

```

## 1.31 trie cellphone typing

```
#include <bits/stdc++.h>
using namespace std;
struct No {
    map<char, No> filhos;
};
int dfs(No &atual, int nivel, char v) {
    int resp = 0;
    for(auto &it : atual.filhos) {
        if(it.first == '$')
            resp += nivel;

        resp += dfs(it.second, nivel + (atual.filhos.size() > 1), it.first);
    }
    return resp;
}
int main() {
    ios::sync_with_stdio(false);
    cin.tie(0);
    int n, i;
    string pal;
    while(cin >> n) {
        No inicio, *atual;
        inicio.filhos['-'] = No();
        for(i = 0; i < n; i++)
        {
            atual = &inicio;
            cin >> pal;
            for(auto &it : pal) {
                if(atual->filhos.count(it))
                    atual = &(atual->filhos[it]);
                else {
                    atual->filhos[it] = No();
                    atual = &(atual->filhos[it]);
                }
            }
            atual->filhos['$'] = No();
        }
        printf("%.2lf\n", dfs(inicio, 0, '-') * 1.0 / n);
    }
}
```