## LIMITES NO INFINITO, LIMITES INFINITO E LIMITES FUNDAMENTAIS

## 1. Calcule os limites:

(a) 
$$\lim_{x \to +\infty} \frac{4x^3 - 5x^2 + x}{x^4 + 7x^2}$$

(b) 
$$\lim_{x\to-\infty} \frac{3x^5 - x^4 + 7x}{6x^5 + 8x^4 + 20}$$

(c) 
$$\lim_{x \to -\infty} \frac{x^5 + \sin(x)}{20x^4 + 3x^2 + x}$$

(d) 
$$\lim_{x\to+\infty} \frac{\sqrt{x^2-\sqrt{x}}}{\sqrt{x+1}}$$

(b) 
$$\lim_{x \to -\infty} \frac{3x^5 - x^4 + 7x}{6x^5 + 8x^4 + 20}$$
  
(c)  $\lim_{x \to -\infty} \frac{x^5 + \sin(x)}{20x^4 + 3x^2 + x}$   
(d)  $\lim_{x \to +\infty} \frac{\sqrt{x^2 - \sqrt{x}}}{\sqrt{x + 1}}$   
(e)  $\lim_{x \to -\infty} \frac{x}{\sqrt{x^2 + \sqrt{x^2 + 1}}}$   
(f)  $\lim_{x \to 0} \frac{x^4 + 7x^2}{6x^5 + 8x^4 + 20}$   
(i)  $\lim_{x \to 0} \frac{(7x^{-1} - \frac{1}{7})}{x}$   
(j)  $\lim_{x \to 0} \frac{((ab)^x - a^x)}{ax}$   $a, b \neq 0$   
(k)  $\lim_{x \to +\infty} \left(1 + \frac{2}{x + 1}\right)^x$   
(l)  $\lim_{x \to 0} x^2 \cot^2(x)$   
(l)  $\lim_{x \to 0} x^2 \cot^2(x)$ 

(f) 
$$\lim_{x\to 0} \frac{x}{\tan(x)}$$

(g) 
$$\lim_{x\to 0} \frac{1-\cos(x)^4}{x^2}$$

(a) 
$$\lim_{x \to +\infty} \frac{4x^3 - 5x^2 + x}{x^4 + 7x^2}$$
 (b)  $\lim_{x \to \infty} \left(1 + \frac{5}{x - 1}\right)^{x + 7}$ 

(i) 
$$\lim_{x\to 0} \frac{\left(7^{x-1} - \frac{1}{7}\right)}{x}$$

(j) 
$$\lim_{x\to 0} \frac{((ab)^x - a^x)}{ax}$$
  $a, b \neq 0$ 

(k) 
$$\lim_{x \to +\infty} \left( 1 + \frac{2}{x+1} \right)^x$$

(l) 
$$\lim_{x\to 0} x^2 \cot^2(x)$$

(m) 
$$\lim_{x\to 0} \frac{\tan(x)}{x \cdot \sec(x)}$$

(n) 
$$\lim_{x\to 0} x \cdot \sec(x) \cdot \csc(x)$$

2. Se 
$$f(x) = \frac{3x + |x|}{7x - 5|x|}$$
, calcule  $\lim_{x \to +\infty} f(x)$  e  $\lim_{x \to -\infty} f(x)$ .

## 3. Calcule:

(a) 
$$\lim_{x\to 0} \frac{\tan(x)}{x}$$

(b) 
$$\lim_{x\to 0} \frac{x}{\sin(x)}$$

(c) 
$$\lim_{x\to 0} \frac{\sin(3x)}{x}$$

(d) 
$$\lim_{x \to \pi} \frac{\sin(x)}{x - \pi}$$

(e) 
$$\lim_{x\to 0} \frac{x^2}{\sin(x)}$$

(f) 
$$\lim_{x\to 0} \frac{3x^2}{\tan(x)\sin(x)}$$

(g) 
$$\lim_{x\to 0} \frac{\tan(3x)}{\sin(4x)}$$

(h) 
$$\lim_{x\to 0} \frac{1-\cos(x)}{x}$$

(i) 
$$\lim_{x\to 0} \frac{x - \tan(x)}{x + \tan(x)}$$

(j) 
$$\lim_{x\to 1} \frac{\sin(\pi x)}{x-1}$$