

probability measure on $(\mathbb{R}, \mathcal{B})$,

$$P^X : \mathcal{B} \rightarrow [0, 1]$$

correspondence theorem

commulative distribution function,

$$F : \mathbb{R} \rightarrow [0, 1]$$

continuous:

$$P^X(A) = \int_A f \, d\lambda$$

discrete:

$$P^X(A) = \sum_{x \in A} f(x)$$

X continuous:

probability density function

$$f : \mathbb{R} \rightarrow [0, \infty)$$

X discrete:

probability mass function

$$f : \mathbb{R} \rightarrow [0, 1]$$

$P^X \ll \lambda$, σ -finite:

$f = \frac{dP^X}{d\lambda}$, Radon-Nikodym

P^X discrete (means?):

$$f(x) = P^X(\{x\})$$