

A Robust Approach for Discovering Functional Dependencies using Machine Learning Approaches

von

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ABSTRACT. Lorem ipsum dolor sit amet, consetetur sadipscing elitr, sed diam nonumy eirmod tempor invidunt ut labore et dolore magna aliquyam erat, sed diam voluptua. At vero eos et accusam et justo duo dolores et ea rebum. Stet clita kasd gubergren, no sea takimata sanctus est Lorem ipsum dolor sit amet.

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1 Introduction

IBM's Deep Blue chess-playing computer beat Garry Kasparov in 1997, becoming the first machine to defeat a reigning world chess-champion. IBM researchers implemented alpha-beta search algorithms in parallel, brute-force searching for optimal moves. This approach has been iteratively refined since then, leading to modern chess-engines like Stockfish.

When researchers published the performance of reinforced-learning algorithms in 2018, it became clear that learned algorithms offered superior performanced compared to conventional chess-playing algorithms.² This approach, based on empirical risk-minimization, has proven fruitful in domains other than artificial intelligence as well.

Data-driven methods change the way computer scientists approach algorithmic problems. Rather than designing and implementing complex algorithms themselves, recent advances in machine learning have allowed for learned algorithms. While these learned structures come with their own limitations and problems, e.g. lack of explainability, they have proven to solve classic algorithmic problems in a more performant fashion.

Kraska et al. showed in their 2018 publication "The case for Learned Index Structures" that different index structures can be replaced by learned ones, greatly improving performance.³

In the field of data cleaning and data enrichment, HoloClean lead the way for machinelearning approaches in the domain of data cleaning. HoloClean is agnostic of the way the database to be cleaned is structured, making it versitile.

One important concept in relational database theory is the idea of *functional dependencies*. Functional dependencies stem from the early days of relational databases. Historically, they were introduced to formalize schema normalization, where a normalized schema is one where no functional dependency between two non-key columns exists. In the past, functional dependencies found broader interest in data analysis and data cleaning.

A long history of academic research improved functional dependency search-algorithms. Most notably, TANE

¹https://en.wikipedia.org/wiki/Deep_Blue_(chess_computer)

²https://deepmind.com/research/alphago/alphazero-resources/

³https://arxiv.org/abs/1712.01208

2 Theory

Functional Dependencies (FDs) are a way of expressing "a priori knowledge of restrictions or constraints on permissible sets of data" [Mai83, p. 42] in relational database theory. Having been introduced in the 1970s for schema normalization of relational databases, FDs have proven to be useful in a multitude of domains. In this section, *functional dependencies* and the theoretical foundation necessary to put them into context are introduced.

2.1 Relational Database Theory

In order to give a definition of FDs, they need to be put in context to the domain they stem from: relational database theory. Some basic concepts will be introduced in this section.

2.1.1 Relation Scheme

A relation scheme⁴ R is a finite set of attribute names $\{A_1, A_2, \ldots, A_n\}$, where to each attribute name A_i corresponds a set D_i , called *domain* of A_i , $1 \le i \le n$. Let $D = D_1 \cup D_2 \cup \cdots \cup D_n$, then a relation r on relation scheme R is a finite set of mappings $\{t_1, t_2, \ldots, t_p\}$ from R to D:

$$t_i: \mathbf{R} \to \mathbf{D}$$
,

where we call those mappings tuples under the constraint that [Mai83, p.2]

$$t(A_i) \subseteq D_i$$
.

In application, attribute names are commonly called *column name* or *column attribute*. One can think of them as labels of data that is stored in the respective column.

2.1.2 Keys

A *key* on a relation r on a relation scheme R is a subset $K = \{B_1, B_2, ..., B_m\}$ with the property that for any tuple $t_i \in \{t_1, t_2, ..., t_3\}$ the relation

$$t_i(B_k) = t_i(B_k) \Rightarrow t_i \equiv t_i$$

holds for any single $B_k \in K$. In other words, any K-value of a tuple identifies that tuple uniquely. [Mai83, p. 4]

Having defined both *relation scheme* and *keys*, it is now possible to introduce the more complex concepts of relational databases and functional dependencies.

⁴also called *relational schema* in literature[Abe+19, p.21]

2.1.3 Definition of a Relational Database

When real-world data used by one or multiple application/s is stored on a machine according to the relational model, it is usually stored in a relational database. According to the definition of a relation scheme *R*, one can formally introduce databases and database schemes:

We assume that R is composed of two parts, S and K. We call S a set of attributes and K a set of designated keys and describe this composition by writing R = (S, K). A relational database scheme R over U can now be defined as a collection of relation schemes $\{R_1, R_1, \ldots, R_p\}$, where $R_i = (S_i, K_i)$, $1 \le i, j \le p$,

$$\bigcup_{i=1}^p S_i = \mathbf{U}.$$

We demand that $S_i \neq S_j$ if $i \neq j$.

A relational database d on a database scheme \mathbf{R} is a collection of relations $d = \{r_1, r_2, \dots, r_p\}$ such that for each relation scheme $R = (S, \mathbf{K})$ in \mathbf{R} there is a relation r in d such that r is a relation on S that satisfies every key in K. [Mai83, p. 94]

2.1.4 Definition of a Functional Dependency

Consider a relation r on scheme R with subset $X \subseteq R$ and a single attribute $A_i \in R$. A FD $X \to A$ is said to be *valid* in r, if and only if

$$t_i[X] = t_i[X] \Rightarrow t_i[A] = t_i[A] \tag{1}$$

holds for all all pairs of distinct tuples $t_i, t_j \in r$.[Abe+19, p. 21] We say that X functionally determines A[Mai83, p. 43] and name X the left hand side (lhs), whilst calling A the right hand side (rhs).

	le	right hand side		
ID	FIRST NAME	LAST NAME	TOWN	ZIP
1	Alice	Smith	Munich	19139
2	Peter	Meyer	Munich	19139
3	Ana	Parker	Munich	19139
4	John	Pick	Berlin	12055
5	John	Pick	Munich	19139

Table 1: Example for a FD.

Considering table 1, one can see that every tuple in the *left hand side* subset of the relation uniquely determines the *right hand side*. For the given example we say that ID, FIRST NAME, LAST NAME, TOWN functionally determines ZIP, or {ID, FIRST NAME, LAST NAME, TOWN} \rightarrow ZIP. [Mai83, p. 43]

inspected closely, discover **FDs** 1. one can even more **TOWN** ID example, **TOWN** and For ZIPand ID ZIP. Since subsets {ID, **FIRST** NAME, LAST NAME, TOWN}, {ID, FIRST NAME, LAST NAME, TOWN} non-minimal. A FD X \rightarrow A is minimal, if no subset of X functionally determines A. [Pap+15, p. 2] Thus, ID \rightarrow ZIP and TOWN \rightarrow ZIP are minimal FDs.

3 FDs in Application

FDs are primarily used in database normalization, [CDP16, p. 1] but also find application in the field of data profiling, where "any dependency can be turned into a rule to check for errors in the data". [Abe+19, p. 9]

3.1 Normalization

When introducing the relational database model in his 1970 article "A relational model of data for large shared data banks", Edgar F. Codd formalized database normalization alongside.[Cod70] Describing what will be know to academia as **First normal form** (1NF), Codd states that "problems treated [when normalizing databases] are those of *data independence*", aiming to protect future users of large databases "from having to know how the data is organized in the machine". [Cod70, p. 1]

Being designed for as efficient as possible query handling, databases at the time were structured hierarchically or navigationally. While this yielded good performance in times when computing time was very expensive, it came with a heavy cost of complexity: "Teams of programmers were needed to express queries to extract meaningful information. [...] Such databases [...] were absolutely inflexible[y]".[IBM03]

Update-, insertion- and deletion anomalies can be prevented when normalizing a relational database. [Kle11, p. 75]

3.1.1 First Normal Form

A relation scheme R is in *First Normal Form* (1NF), if values in dom(A) are atomic for every attribute A in R. [Mai83, p. 96] Consider table 2 which represents two relational database schemes. It serves as an example of what is called *atomic* and *compound* data in the Relational Database model. [Cod90, p. 6]

While the compound scheme's attributes can be decomposed into several other attributes, whereas an atomic attribute cannot be further split into any meaningful smaller components.

For a database it is said that the database in 1NF if every relation scheme in the database scheme is in 1NF. 1NF is the very foundation of the Relational Model, where the only type of compound data is the relation.[Cod90, p. 6]

	comp	ound scheme	atomic scheme			
	NAME	ADRESS	PRENAME	SURNAME	TOWN	STREET
1	Alice Smith	Munich, Alicestr.	Alice	Smith	Alicestr.	Munich
2	Peter Meyer	Munich, Peterstr.	Peter	Meyer	Munich	Peterstr.
3	Ana Parker	Munich, Anastr.	Ana	Parker	Munich	Anastr.
4	John Pick	Berlin, Johnstr.	John	Pick	Berlin	Johnstr.

Table 2: The compound attributes ADRESS and NAME can be split into their atomic components TOWN and STREET as well as PRENAME and SURNAME, respectively.

3.1.2 Second Normal Form (2NF)

A relation scheme *R* is said to be in *second normal form* (2NF) in respect to a set of FDs F, if it is in 1NF and every nonprime attribute is fully dependent on every key of of R.[Mai83, p. 99] This definition can be extended for databases: A database scheme **R** is in second normal form with respect to F if every relation scheme R in R is in 2NF with respect to F.

3.1.3 Third Normal Form (3NF)

3.2 Approximate Functional Dependencies

In the field of data profiling an extensive body of theory and algorithms for FD detection has been created in the past decades. [Pap+15] These mainly consider FDs as defined in formula 1. Howevever, the strict detection of FDs yields results that are solely applicable in a strictly controlled environment. Real-world datasets faced by data-scientists or database engineers are often noisy. Entries might be corrupted by missing data, wrongly entered entries or incomplete datasets. Inconsistencies are to be expected. Thus, functionally dependent column-combinations might not be detected as such. This may result in misleading insights when searching for FDs.

To illustrate this, table 3 shows an example of noisy data. The potential FD **Town** \rightarrow **ZIP** is not captured by the definition given in equation 1. Due to a type-error, the potential FD is invalidated. To still capture meta-information, a different dependency-measure than given in equation 1 is needed.

Approximate FDs (AFDs), sometimes called Relaxed FDs, improve the applicability of FDs, "in that they relax one or more constraints of the canonical FDs" [CDP16, p. 1]. While there are AFDs introducing general error measures, others are defined "aiming to solve specific problems" [CDP16, p. 1].

	Data					
ID	First name	Last name	Town	ZIP		
1	Alice	Smith	Munich	19139		
2	Peter	Meyer	Muinch	19139		
3	Ana	Parker	Munich	19139		
4	John	Pick	Berlin	12055		

Table 3: Even though column ZIP functionally determines column Town (and vice-versa), a FD is not capable of displaying this fact - a typing error invalidates the FD.

The error measure for this is not trivial at all. While F1-measures can be established for non-categorical cases, comparing results for different data-types tricky.

3.3 FD Imputer

The FD Imputer imputes the column of a table of a relational database. Empirical Risk Minimization strategies are used to do this. The table is first split in train-set and validation-set. Then, FDs are detected on the train-set using HyFD.[PN16] Having identified all FDs on the train-set, FD Imputer can impute values of any right-hand side of a particular FD: This is done by executing an SQL join clause. FD imputer performs an inner join on all left-hand side columns, joining train-set and validation-set. A second left join clause concatenates the original validation-set with the column of imputed tuples stemming from the first join.

Algorithm 1: FD Imputer

Result: Validation-subset of a relational database table with an additional column containing imputed tuples

Data: Relational database table

- 1 Split relational database table into train-set and validation-set
- 2 Detect FDs in train-set
- 3 ALTER TABLE train-set DROP COLUMN not in lhs
- 4 imputed-set = SELECT lhs FROM train-set INNER JOIN validation-set ON lhs
- 5 imputed-validation-set = SELECT imputed-column FROM imputed-set LEFT JOIN validation-set
- 6 return imputed-validation-set

3.4 Machine Learning Classifier Theory

Once a model has been trained and validated, it needs to be tested in order to determine whether or not overfitting occured during training. This is usually done by measuring the model's performance on a separate dataset not involved in training, the so called test set. Performance is measured according to the type of data and the kind of model involved. To visualize the performance of a classifier, a *confusion matrix* can be created.

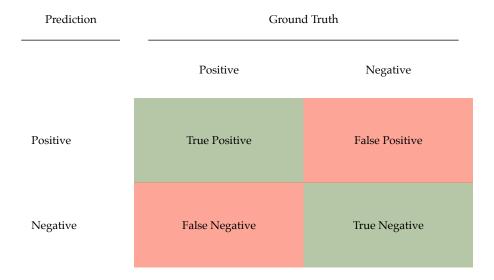


Figure 1: Illustration of a binary confusion matrix. "Prediction" refers to predicted labels $y_{pred}(x)$ while "Ground Truth" represents the actual labels y(x).

The simplest case of a confusion matrix can be created when measuring the performance of a binary classifier. Figure 1 shows such a binary confusion matrix. Here, "Ground Truth" describes the label y(x) of some data point $x \in X_{test}$, where $y \in \{0,1\}$. "Prediction" identifies the predicted labels $y_{pred}(x)$ that the model generates after is has been executed on the test-set X_{test} prior unknown.

Whenever $y_{pred}(x) = y(x)$, $x \in X_{test}$ holds, the predicted label can be assigned to be either a *True Positive* (TP) or a *True Negative* (TN). The opposite holds as well, such that a falsely predicted label will be either a *False Negative* (FN) or a *False Positive* (FP).

Using the classification introduced by the binary confusion matrix, all predicted labels y_{pred} are assigned to the four sets TP, TN, FN and FP. Using these four sets, we can introduce measures for classification performance.

Precision is a measure that depicts the proportion of correctly classified positive samples to the total amount of samples classified as positive.[Tha18, p.4] This can be algebraically expressed as

$$Precision = \frac{|TP|}{|TP| + |FP|} \tag{2}$$

where |A| is the cardinality of a set A. Precision measures how many elements classified as positive are True Positives.

Recall, also called *sensitivity*, represents the share of positive correctly classified samples to the total amount of positive samples.[Tha18, p.3] This can be formalized as

$$Recall = \frac{|TP|}{|TP| + |FN|} \tag{3}$$

Recall measures how many of the positive labelled elements were actually selected.

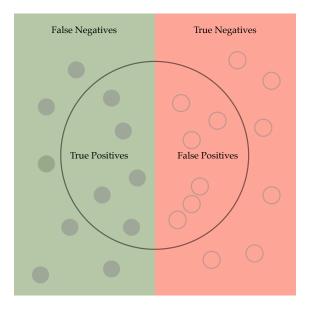


Figure 2: Each predicted label y_x is represented by a circle. Hollow circles stand for negative labels and full circles for positive lables.

The harmonic mean of precision and recall is called *F1-measure*:

$$F1 - measure = \left(\frac{Recall^{-1} + Precision^{-1}}{2}\right)^{-1} \tag{4}$$

4 Execution

A number of experiments have been conducted in order to evaluate the capabilities of empirical risk minimization (ERM) techniques for functional dependency discovery.

4.1 FD Imputer

The FD Imputer

4.2 ML Imputer

4.2.1 Overfitting the ML Imputer

4.3 Comparing ML Imputer with FD Imputer

When comparing the ML Imputer to the FD Imputer, it is necessary to explain the scope of such an comparison. Due to the definition of a FD, the FD Imputer cannot approximate numerical values. It allways assumes data to be classifiable. Meanwhile, the ML Imputer is able to perform regression, predicting a continuous label for a given input.

The measure chosen to compare imputation performance on columns containing numeric values is the *mean squared error* (MSE). To compare classification performance, the F1-measure was chosen.

4.4 Classification Performance

ML Imputer and FD Imputer were compared on two datasets, Adult⁵ and Nursery⁶.

Figure 3 compares the F1-scores of both ML Imputer and FD Imputer on the Adult dataset. One can observe that for most FDs, the ML Imputer performs better than the FD Imputer. FD Imputer performance and ML Imputer performance seem to be proportional. If the ML imputer's F1-score is lower than 0.7, the FD Imputer's F1-score for the same FD is 0. However, for FD's where the ML Imputer scores are larger than 0.7, the FD Imputer scores better than 0.0. Interestingly, there are two FDs for which the FD Imputer performs equally good or better than the ML Imputer.

The same comparison as

⁵https://archive.ics.uci.edu/ml/datasets/adult

⁶https://archive.ics.uci.edu/ml/datasets/nursery

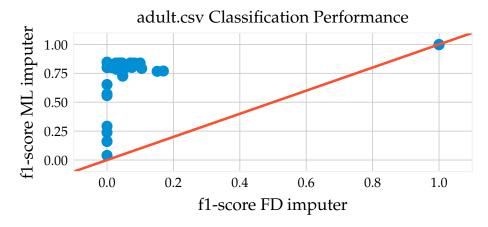


Figure 3: The figure compares the f1-score of the FD Imputer compared to the f1-score of the ML Imputer. Each point represents one FD.



Figure 4: Some ohter caption.

4.5 Begriffsdiskussion

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5 Discussion

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5.1 Begriffsdiskussion

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