

The Annotated Transformer

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from IPython.display import Image
Image(filename='images/aiayn.png')

Attention Is All You Need

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Abstract

The dominant sequence transduction models are based on complex recurrent or convolutional neural networks that include an encoder and a decoder. The best performing models also connect the encoder and decoder through an attention mechanism. We propose a new simple network architecture, the Transformer, based solely on attention mechanisms, dispensing with recurrence and convolutions entirely. Experiments on two machine translation tasks show these models to be superior in quality while being more parallelizable and requiring significantly less time to train. Our model achieves 28.4 BLEU on the WMT 2014 Englishto-German translation task, improving over the existing best results, including ensembles, by over 2 BLEU. On the WMT 2014 Englishto-French translation task, our model establishes a new single-model state-of-the-art BLEU score of 41.8 after training for 3.5 days on eight GPUs, a small fraction of the training costs of the best models from the literature. We show that the Transformer generalizes well to other tasks by applying it successfully to English constituency parsing both with large and limited training data.

The Transformer from "Attention is All You Need" has been on a lot of people's minds over the last year. Besides producing major improvements in translation quality, it provides a new architecture for many other NLP tasks. The paper itself is very clearly written, but the conventional wisdom has been that it is guite difficult to implement correctly.

In this post I present an "annotated" version of the paper in the form of a line-by-line implementation. I have reordered and deleted some sections from the original paper and added comments throughout. This document itself is a working notebook, and should be a completely usable implementation. In total there are 400 lines of library code which can process 27,000 tokens per second on 4 GPUs.

To follow along you will first need to install PyTorch. The complete notebook is also available on github or on Google Colab with free GPUs.

Note this is merely a starting point for researchers and interested developers. The code here is based heavily on our OpenNMT packages. (If helpful feel free to cite.) For other full-sevice implementations of the model check-out Tensor2Tensor (tensorflow) and Sockeye (mxnet).

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Prelims

 ${\rm \#~!pip~install~http://download.pytorch.org/whl/cu80/torch-0.3.0.post4-cp36-cp36m-linux_x86_64.whlnumpy~matplotlib~spacy~torchtext~seaborn}$

```
import numpy as np
import torch
import torch.nn as nn
import torch.nn.functional as F
import math, copy, time
from torch.autograd import Variable
import matplotlib.pyplot as plt
import seaborn
seaborn.set_context(context="talk")
%matplotlib inline
```

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My comments are blockquoted. The main text is all from the paper itself.

Background

The goal of reducing sequential computation also forms the foundation of the Extended Neural GPU, ByteNet and ConvS2S, all of which use convolutional neural networks as basic building block, computing hidden representations in parallel for all input and output positions. In these models, the number of operations required to relate signals from two arbitrary input or output positions grows in the distance between positions, linearly for ConvS2S and logarithmically for ByteNet. This makes it more difficult to learn dependencies between distant positions. In the Transformer this is reduced to a constant number of operations, albeit at the cost of reduced effective resolution due to averaging attention-weighted positions, an effect we counteract with Multi-Head Attention.

Self-attention, sometimes called intra-attention is an attention mechanism relating different positions of a single sequence in order to compute a representation of the sequence. Self-attention has been used successfully in a variety of tasks including reading comprehension, abstractive summarization, textual entailment and learning task-independent sentence representations. End- to-end memory networks are based on a recurrent attention mechanism instead of sequencealigned recurrence and have been shown to perform well on simple- language question answering and language modeling tasks.

To the best of our knowledge, however, the Transformer is the first transduction model relying entirely on self-attention to compute representations of its input and output without using sequence aligned RNNs or convolution.

Model Architecture

Most competitive neural sequence transduction models have an encoder-decoder structure (cite). Here, the encoder maps an input sequence of symbol representations $(x_1, ..., x_n)$ to a sequence of continuous representations $\mathbf{z} = (z_1, ..., z_n)$. Given \mathbf{z} , the

decoder then generates an output sequence $(y_1, ..., y_m)$ of symbols one element at a time. At each step the model is autoregressive (cite), consuming the previously generated symbols as additional input when generating the next.

```
class EncoderDecoder(nn.Module):
    .. .. ..
   A standard Encoder-Decoder architecture. Base for this and many
    other models.
    def init (self, encoder, decoder, src embed, tgt embed, generator):
       super(EncoderDecoder, self). init ()
       self.encoder = encoder
       self.decoder = decoder
       self.src embed = src embed
       self.tqt embed = tqt embed
       self.generator = generator
    def forward(self, src, tgt, src mask, tgt mask):
        "Take in and process masked src and target sequences."
       return self.decode(self.encode(src, src mask), src mask,
                            tgt, tgt mask)
    def encode(self, src, src mask):
        return self.encoder(self.src embed(src), src mask)
    def decode(self, memory, src mask, tgt, tgt mask):
       return self.decoder(self.tgt embed(tgt), memory, src mask, tgt mask)
```

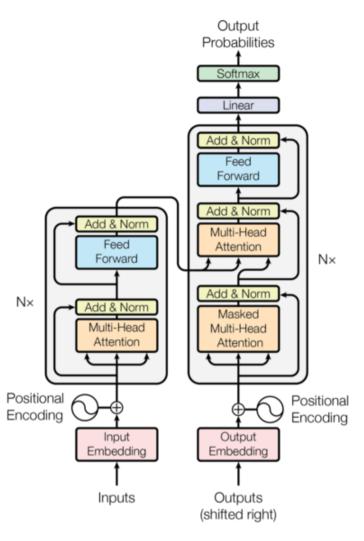
```
class Generator(nn.Module):
    "Define standard linear + softmax generation step."

def __init__(self, d_model, vocab):
    super(Generator, self).__init__()
    self.proj = nn.Linear(d_model, vocab)

def forward(self, x):
    return F.log_softmax(self.proj(x), dim=-1)
```

The Transformer follows this overall architecture using stacked self-attention and point-wise, fully connected layers for both the encoder and decoder, shown in the left and right halves of Figure 1, respectively.

```
Image(filename='images/ModalNet-21.png')
```



Encoder and Decoder Stacks

Encoder

The encoder is composed of a stack of ${\it N}=6$ identical layers.

```
def clones(module, N):
    "Produce N identical layers."
    return nn.ModuleList([copy.deepcopy(module) for _ in range(N)])
```

```
class Encoder(nn.Module):
    "Core encoder is a stack of N layers"

def __init__(self, layer, N):
    super(Encoder, self).__init__()
    self.layers = clones(layer, N)
    self.norm = LayerNorm(layer.size)

def forward(self, x, mask):
    "Pass the input (and mask) through each layer in turn."
    for layer in self.layers:
        x = layer(x, mask)
    return self.norm(x)
```

We employ a residual connection (cite) around each of the two sub-layers, followed by layer normalization (cite).

```
class LayerNorm(nn.Module):
    "Construct a layernorm module (See citation for details)."

def __init__ (self, features, eps=1e-6):
    super(LayerNorm, self).__init__()
    self.a_2 = nn.Parameter(torch.ones(features))
    self.b_2 = nn.Parameter(torch.zeros(features))
    self.eps = eps

def forward(self, x):
    mean = x.mean(-1, keepdim=True)
    std = x.std(-1, keepdim=True)
    return self.a_2 * (x - mean) / (std + self.eps) + self.b_2
```

That is, the output of each sub-layer is LayerNorm(x + Sublayer(x)), where Sublayer(x) is the function implemented by the sublayer itself. We apply dropout (cite) to the output of each sub-layer, before it is added to the sub-layer input and normalized.

To facilitate these residual connections, all sub-layers in the model, as well as the embedding layers, produce outputs of dimension $d_{\text{model}} = 512$.

```
class SublayerConnection(nn.Module):
    """
    A residual connection followed by a layer norm.
    Note for code simplicity the norm is first as opposed to last.
    """

def __init__(self, size, dropout):
    super(SublayerConnection, self).__init__()
    self.norm = LayerNorm(size)
    self.dropout = nn.Dropout(dropout)
```

```
def forward(self, x, sublayer):
    "Apply residual connection to any sublayer with the same size."
    return x + self.dropout(sublayer(self.norm(x)))
```

Each layer has two sub-layers. The first is a multi-head self-attention mechanism, and the second is a simple, position-wise fully connected feed- forward network.

```
class EncoderLayer(nn.Module):
    "Encoder is made up of self-attn and feed forward (defined below)"

def __init__ (self, size, self_attn, feed_forward, dropout):
    super(EncoderLayer, self).__init__()
    self.self_attn = self_attn
    self.feed_forward = feed_forward
    self.sublayer = clones(SublayerConnection(size, dropout), 2)
    self.size = size

def forward(self, x, mask):
    "Follow Figure 1 (left) for connections."
    x = self.sublayer[0](x, lambda x: self.self_attn(x, x, x, mask))
    return self.sublayer[1](x, self.feed_forward)
```

Decoder

The decoder is also composed of a stack of N=6 identical layers.

```
class Decoder(nn.Module):
    "Generic N layer decoder with masking."

def __init__(self, layer, N):
    super(Decoder, self).__init__()
    self.layers = clones(layer, N)
    self.norm = LayerNorm(layer.size)

def forward(self, x, memory, src_mask, tgt_mask):
    for layer in self.layers:
        x = layer(x, memory, src_mask, tgt_mask)
    return self.norm(x)
```

In addition to the two sub-layers in each encoder layer, the decoder inserts a third sub-layer, which performs multi-head attention over the output of the encoder stack. Similar to the encoder, we employ residual connections around each of the sub-layers, followed by layer normalization.

```
class DecoderLayer(nn.Module):
    "Decoder is made of self-attn, src-attn, and feed forward (defined below)"
```

```
def __init__ (self, size, self_attn, src_attn, feed_forward, dropout):
    super(DecoderLayer, self).__init__()
    self.size = size
    self.self_attn = self_attn
    self.src_attn = src_attn
    self.feed_forward = feed_forward
    self.sublayer = clones(SublayerConnection(size, dropout), 3)

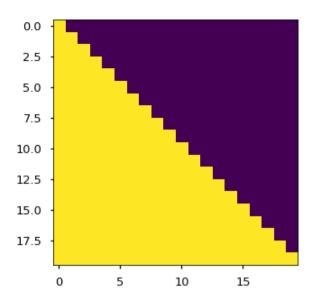
def forward(self, x, memory, src_mask, tgt_mask):
    "Follow Figure 1 (right) for connections."
    m = memory
    x = self.sublayer[0](x, lambda x: self.self_attn(x, x, x, tgt_mask))
    x = self.sublayer[1](x, lambda x: self.src_attn(x, m, m, src_mask))
    return self.sublayer[2](x, self.feed_forward)
```

We also modify the self-attention sub-layer in the decoder stack to prevent positions from attending to subsequent positions. This masking, combined with fact that the output embeddings are offset by one position, ensures that the predictions for position *i* can depend only on the known outputs at positions less than *i*.

```
def subsequent_mask(size):
    "Mask out subsequent positions."
    attn_shape = (1, size, size)
    subsequent_mask = np.triu(np.ones(attn_shape), k=1).astype('uint8')
    return torch.from_numpy(subsequent_mask) == 0
```

Below the attention mask shows the position each tgt word (row) is allowed to look at (column). Words are blocked for attending to future words during training.

```
plt.figure(figsize=(5,5))
plt.imshow(subsequent_mask(20)[0])
None
```

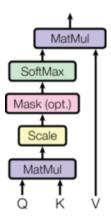


Attention

An attention function can be described as mapping a query and a set of key-value pairs to an output, where the query, keys, values, and output are all vectors. The output is computed as a weighted sum of the values, where the weight assigned to each value is computed by a compatibility function of the query with the corresponding key.

We call our particular attention "Scaled Dot-Product Attention". The input consists of queries and keys of dimension d_k , and values of dimension d_v . We compute the dot products of the query with all keys, divide each by $\sqrt{d_k}$, and apply a softmax function to obtain the weights on the values.

Image(filename='images/ModalNet-19.png')



In practice, we compute the attention function on a set of queries simultaneously, packed together into a matrix Q. The keys and values are also packed together into matrices K and V. We compute the matrix of outputs as:

Attention(Q, K, V) = softmax(
$$\frac{QK^T}{\sqrt{d_k}}$$
)V

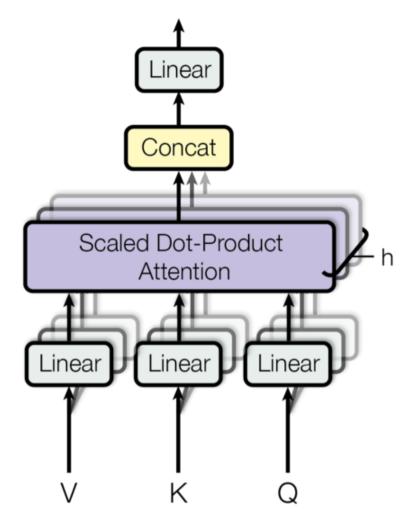
```
def attention(query, key, value, mask=None, dropout=None):
    "Compute 'Scaled Dot Product Attention'"
    d_k = query.size(-1)
    scores = torch.matmul(query, key.transpose(-2, -1)) \
        / math.sqrt(d_k)
    if mask is not None:
        scores = scores.masked_fill(mask == 0, -1e9)
    p_attn = F.softmax(scores, dim = -1)
    if dropout is not None:
        p_attn = dropout(p_attn)
    return torch.matmul(p_attn, value), p_attn
```

The two most commonly used attention functions are additive attention (cite), and dot-product (multiplicative) attention. Dot-product attention is identical to our algorithm, except for the scaling factor of $\frac{1}{\sqrt{d_k}}$. Additive attention computes the

compatibility function using a feed-forward network with a single hidden layer. While the two are similar in theoretical complexity, dot-product attention is much faster and more space-efficient in practice, since it can be implemented using highly optimized matrix multiplication code.

While for small values of d_k the two mechanisms perform similarly, additive attention outperforms dot product attention without scaling for larger values of d_k (cite). We suspect that for large values of d_k , the dot products grow large in magnitude, pushing the softmax function into regions where it has extremely small gradients (To illustrate why the dot products get large, assume that the components of q and k are independent random variables with mean 0 and variance 1. Then their dot product, $q \cdot k = \sum_{i=1}^{d_k} q_i k_i$, has mean 0 and variance d_k .). To counteract this effect, we scale the dot products by $\frac{1}{\sqrt{d_k}}$.

```
Image(filename='images/ModalNet-20.png')
```



Multi-head attention allows the model to jointly attend to information from different representation subspaces at different positions. With a single attention head, averaging inhibits this.

 $\text{MultiHead}(Q, K, V) = \text{Concat}(\text{head}_1, \dots, \text{head}_{\text{h}}) W^O \text{where head}_{\text{i}} = \text{Attention}(QW_i^Q, KW_i^K, VW_i^V)$

Where the projections are parameter matrices $W_i^Q \in \mathbf{R}^{d_{\mathrm{model}} \times d_k}$, $W_i^K \in \mathbf{R}^{d_{\mathrm{model}} \times d_k}$, $W_i^V \in \mathbf{R}^{d_{\mathrm{model}} \times d_v}$ and $W^O \in \mathbf{R}^{hd_v \times d_{\mathrm{model}}}$. In this work we employ h=8 parallel attention layers, or heads. For each of these we use $d_k=d_v=d_{\mathrm{model}}/h=64$. Due to the reduced dimension of each head, the total computational cost is similar to that of single-head attention with full dimensionality.

```
class MultiHeadedAttention(nn.Module):
    def init (self, h, d model, dropout=0.1):
       "Take in model size and number of heads."
       super(MultiHeadedAttention, self). init ()
       assert d model % h == 0
       # We assume d v always equals d k
       self.d k = d \mod 1 / h
       self.h = h
       self.linears = clones(nn.Linear(d model, d model), 4)
       self.attn = None
       self.dropout = nn.Dropout(p=dropout)
    def forward(self, query, key, value, mask=None):
        "Implements Figure 2"
       if mask is not None:
            # Same mask applied to all h heads.
           mask = mask.unsqueeze(1)
       nbatches = query.size(0)
       \# 1) Do all the linear projections in batch from d model => h x d k
       query, key, value = \
            [1(x).view(nbatches, -1, self.h, self.d k).transpose(1, 2)
            for 1, x in zip(self.linears, (query, key, value))]
        # 2) Apply attention on all the projected vectors in batch.
       x, self.attn = attention(query, key, value, mask=mask,
                                 dropout=self.dropout)
       # 3) "Concat" using a view and apply a final linear.
       x = x.transpose(1, 2).contiguous() \
            .view(nbatches, -1, self.h * self.d k)
       return self.linears[-1](x)
```

Applications of Attention in our Model

The Transformer uses multi-head attention in three different ways: 1) In "encoder-decoder attention" layers, the queries come from the previous decoder layer, and the memory keys and values come from the output of the encoder. This allows every position in the decoder to attend over all positions in the input sequence. This mimics the typical encoder-decoder attention mechanisms in sequence-to-sequence models such as (cite).

2) The encoder contains self-attention layers. In a self-attention layer all of the keys, values and queries come from the same place, in this case, the output of the previous layer in the encoder. Each position in the encoder can attend to all positions in the previous layer of the encoder.

3) Similarly, self-attention layers in the decoder allow each position in the decoder to attend to all positions in the decoder up to and including that position. We need to prevent leftward information flow in the decoder to preserve the auto-regressive property. We implement this inside of scaled dot- product attention by masking out (setting to $-\infty$) all values in the input of the softmax which correspond to illegal connections.

Position-wise Feed-Forward Networks

In addition to attention sub-layers, each of the layers in our encoder and decoder contains a fully connected feed-forward network, which is applied to each position separately and identically. This consists of two linear transformations with a ReLU activation in between.

$$FFN(x) = \max (0, xW_1 + b_1)W_2 + b_2$$

While the linear transformations are the same across different positions, they use different parameters from layer to layer. Another way of describing this is as two convolutions with kernel size 1. The dimensionality of input and output is $d_{\text{model}} = 512$, and the inner-layer has dimensionality $d_{\text{ff}} = 2048$.

```
class PositionwiseFeedForward(nn.Module):
    "Implements FFN equation."

def __init__(self, d_model, d_ff, dropout=0.1):
    super(PositionwiseFeedForward, self).__init__()
    self.w_1 = nn.Linear(d_model, d_ff)
    self.w_2 = nn.Linear(d_ff, d_model)
    self.dropout = nn.Dropout(dropout)

def forward(self, x):
    return self.w_2(self.dropout(F.relu(self.w_1(x))))
```

Embeddings and Softmax

Similarly to other sequence transduction models, we use learned embeddings to convert the input tokens and output tokens to vectors of dimension d_{model} . We also use the usual learned linear transformation and softmax function to convert the decoder output to predicted next-token probabilities. In our model, we share the same weight matrix between the two embedding layers and the pre-softmax linear transformation, similar to (cite). In the embedding layers, we multiply those weights by $\sqrt{d_{\text{model}}}$.

```
class Embeddings(nn.Module):
    def __init__(self, d_model, vocab):
        super(Embeddings, self).__init__()
        self.lut = nn.Embedding(vocab, d_model)
        self.d_model = d_model
```

```
def forward(self, x):
    return self.lut(x) * math.sqrt(self.d_model)
```

Positional Encoding

Since our model contains no recurrence and no convolution, in order for the model to make use of the order of the sequence, we must inject some information about the relative or absolute position of the tokens in the sequence. To this end, we add "positional encodings" to the input embeddings at the bottoms of the encoder and decoder stacks. The positional encodings have the same dimension $d_{\rm model}$ as the embeddings, so that the two can be summed. There are many choices of positional encodings, learned and fixed (cite).

In this work, we use sine and cosine functions of different frequencies: $PE_{(pos,2i)} = sin(pos/10000^{2i/d_{model}})$

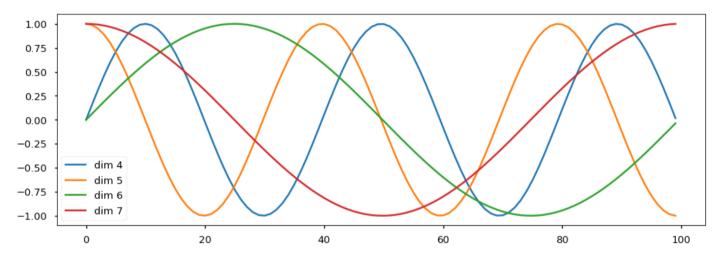
 $PE_{(pos,2i+1)} = cos(pos/10000^{2i/d_{model}})$ where pos is the position and i is the dimension. That is, each dimension of the positional encoding corresponds to a sinusoid. The wavelengths form a geometric progression from 2π to $10000 \cdot 2\pi$. We chose this function because we hypothesized it would allow the model to easily learn to attend by relative positions, since for any fixed offset k, PE_{pos+k} can be represented as a linear function of PE_{pos} .

In addition, we apply dropout to the sums of the embeddings and the positional encodings in both the encoder and decoder stacks. For the base model, we use a rate of $P_{drop} = 0.1$.

```
class PositionalEncoding(nn.Module):
    "Implement the PE function."
    def init (self, d model, dropout, max len=5000):
       super(PositionalEncoding, self). init ()
       self.dropout = nn.Dropout(p=dropout)
        # Compute the positional encodings once in log space.
       pe = torch.zeros(max len, d model)
       position = torch.arange(0, max len).unsqueeze(1)
       div term = torch.exp(torch.arange(0, d model, 2) *
                             -(math.log(10000.0) / d model))
       pe[:, 0::2] = torch.sin(position * div term)
       pe[:, 1::2] = torch.cos(position * div term)
       pe = pe.unsqueeze(0)
       self.register buffer('pe', pe)
   def forward(self, x):
       x = x + Variable(self.pe[:, :x.size(1)],
                         requires grad=False)
       return self.dropout(x)
```

Below the positional encoding will add in a sine wave based on position. The frequency and offset of the wave is different for each dimension.

```
plt.figure(figsize=(15, 5))
pe = PositionalEncoding(20, 0)
y = pe.forward(Variable(torch.zeros(1, 100, 20)))
plt.plot(np.arange(100), y[0, :, 4:8].data.numpy())
plt.legend(["dim %d"%p for p in [4,5,6,7]])
None
```



We also experimented with using learned positional embeddings (cite) instead, and found that the two versions produced nearly identical results. We chose the sinusoidal version because it may allow the model to extrapolate to sequence lengths longer than the ones encountered during training.

Full Model

Here we define a function that takes in hyperparameters and produces a full model.

```
# Small example model.
tmp_model = make_model(10, 10, 2)
None
```

Training

This section describes the training regime for our models.

We stop for a quick interlude to introduce some of the tools needed to train a standard encoder decoder model. First we define a batch object that holds the src and target sentences for training, as well as constructing the masks.

Batches and Masking

```
@staticmethod
def make_std_mask(tgt, pad):
    "Create a mask to hide padding and future words."
    tgt_mask = (tgt != pad).unsqueeze(-2)
    tgt_mask = tgt_mask & Variable(
        subsequent_mask(tgt.size(-1)).type_as(tgt_mask.data))
    return tgt_mask
```

Next we create a generic training and scoring function to keep track of loss. We pass in a generic loss compute function that also handles parameter updates.

Training Loop

```
def run_epoch(data iter, model, loss compute):
    "Standard Training and Logging Function"
   start = time.time()
   total tokens = 0
   total loss = 0
   tokens = 0
   for i, batch in enumerate(data iter):
       out = model.forward(batch.src, batch.trg,
                           batch.src mask, batch.trg mask)
       loss = loss compute(out, batch.trg y, batch.ntokens)
       total loss += loss
       total tokens += batch.ntokens
       tokens += batch.ntokens
       if i % 50 == 1:
            elapsed = time.time() - start
           print("Epoch Step: %d Loss: %f Tokens per Sec: %f" %
                    (i, loss / batch.ntokens, tokens / elapsed))
            start = time.time()
            tokens = 0
    return total loss / total tokens
```

Training Data and Batching

We trained on the standard WMT 2014 English-German dataset consisting of about 4.5 million sentence pairs. Sentences were encoded using byte-pair encoding, which has a shared source-target vocabulary of about 37000 tokens. For English-French, we used the significantly larger WMT 2014 English-French dataset consisting of 36M sentences and split tokens into a 32000 word-piece vocabulary.

Sentence pairs were batched together by approximate sequence length. Each training batch contained a set of sentence pairs containing approximately 25000 source tokens and 25000 target tokens.

We will use torch text for batching. This is discussed in more detail below. Here we create batches in a torchtext function that ensures our batch size padded to the maximum batchsize does not surpass a threshold (25000 if we have 8 gpus).

```
global max_src_in_batch, max_tgt_in_batch
def batch_size_fn(new, count, sofar):
    "Keep augmenting batch and calculate total number of tokens + padding."
    global max_src_in_batch, max_tgt_in_batch
    if count == 1:
        max_src_in_batch = 0
        max_tgt_in_batch = 0
        max_src_in_batch = max(max_src_in_batch, len(new.src))
    max_tgt_in_batch = max(max_tgt_in_batch, len(new.trg) + 2)
    src_elements = count * max_src_in_batch
    tgt_elements = count * max_tgt_in_batch
    return max(src_elements, tgt_elements)
```

Hardware and Schedule

We trained our models on one machine with 8 NVIDIA P100 GPUs. For our base models using the hyperparameters described throughout the paper, each training step took about 0.4 seconds. We trained the base models for a total of 100,000 steps or 12 hours. For our big models, step time was 1.0 seconds. The big models were trained for 300,000 steps (3.5 days).

Optimizer

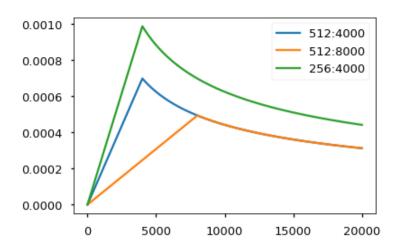
We used the Adam optimizer (cite) with $\beta_1 = 0.9$, $\beta_2 = 0.98$ and $\epsilon = 10^{-9}$. We varied the learning rate over the course of training, according to the formula: $lrate = d_{model}^{-0.5} \cdot \min(step_num^{-0.5}, step_num \cdot warmup_steps^{-1.5})$ This corresponds to increasing the learning rate linearly for the first $warmup_steps$ training steps, and decreasing it thereafter proportionally to the inverse square root of the step number. We used $warmup_steps = 4000$.

Note: This part is very important. Need to train with this setup of the model.

```
class NoamOpt:
   "Optim wrapper that implements rate."
   def __init__(self, model_size, factor, warmup, optimizer):
```

```
self.optimizer = optimizer
        self. step = 0
       self.warmup = warmup
       self.factor = factor
       self.model size = model size
       self. rate = 0
    def step(self):
        "Update parameters and rate"
       self. step += 1
       rate = self.rate()
       for p in self.optimizer.param groups:
           p['lr'] = rate
       self. rate = rate
       self.optimizer.step()
    def rate(self, step = None):
        "Implement `lrate` above"
       if step is None:
            step = self. step
       return self.factor * \
           (self.model size ** (-0.5) *
           min(step ** (-0.5), step * self.warmup ** (-1.5)))
def get std opt(model):
    return NoamOpt(model.src embed[0].d model, 2, 4000,
            torch.optim.Adam(model.parameters(), lr=0, betas=(0.9, 0.98), eps=1e-9))
```

Example of the curves of this model for different model sizes and for optimization hyperparameters.



Regularization

Label Smoothing

During training, we employed label smoothing of value $\epsilon_{ls} = 0.1$ (cite). This hurts perplexity, as the model learns to be more unsure, but improves accuracy and BLEU score.

We implement label smoothing using the KL div loss. Instead of using a one-hot target distribution, we create a distribution that has <code>confidence</code> of the correct word and the rest of the <code>smoothing</code> mass distributed throughout the vocabulary.

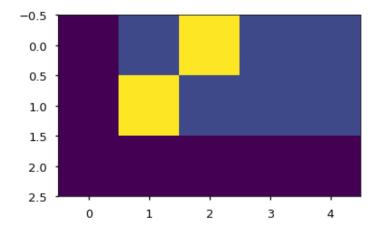
```
class LabelSmoothing(nn.Module):
    "Implement label smoothing."

def __init__(self, size, padding_idx, smoothing=0.0):
    super(LabelSmoothing, self).__init__()
    self.criterion = nn.KLDivLoss(size_average=False)
    self.padding_idx = padding_idx
    self.confidence = 1.0 - smoothing
    self.smoothing = smoothing
    self.size = size
    self.true_dist = None

def forward(self, x, target):
    assert x.size(1) == self.size
    true_dist = x.data.clone()
    true_dist.fill_(self.smoothing / (self.size - 2))
    true_dist.scatter_(1, target.data.unsqueeze(1), self.confidence)
```

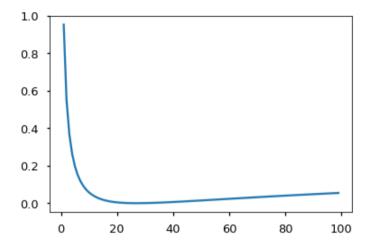
```
true_dist[:, self.padding_idx] = 0
mask = torch.nonzero(target.data == self.padding_idx)
if mask.dim() > 0:
    true_dist.index_fill_(0, mask.squeeze(), 0.0)
self.true_dist = true_dist
return self.criterion(x, Variable(true_dist, requires_grad=False))
```

Here we can see an example of how the mass is distributed to the words based on confidence.



Label smoothing actually starts to penalize the model if it gets very confident about a given choice.

```
crit = LabelSmoothing(5, 0, 0.1)
def loss(x):
    d = x + 3 * 1
    predict = torch.FloatTensor([[0, x / d, 1 / d, 1 / d], 1 / d],
```



A First Example

We can begin by trying out a simple copy-task. Given a random set of input symbols from a small vocabulary, the goal is to generate back those same symbols.

Synthetic Data

```
def data_gen(V, batch, nbatches):
    "Generate random data for a src-tgt copy task."
    for i in range(nbatches):
        data = torch.from_numpy(np.random.randint(1, V, size=(batch, 10)))
        data[:, 0] = 1
        src = Variable(data, requires_grad=False)
        tgt = Variable(data, requires_grad=False)
        yield Batch(src, tgt, 0)
```

Loss Computation

Greedy Decoding

```
Epoch Step: 1 Loss: 3.023465 Tokens per Sec: 403.074173

Epoch Step: 1 Loss: 1.920030 Tokens per Sec: 641.689380

1.9274832487106324

Epoch Step: 1 Loss: 1.940011 Tokens per Sec: 432.003378

Epoch Step: 1 Loss: 1.699767 Tokens per Sec: 641.979665

1.657595729827881

Epoch Step: 1 Loss: 1.860276 Tokens per Sec: 433.320240

Epoch Step: 1 Loss: 1.546011 Tokens per Sec: 640.537198

1.4888023376464843
```

```
Epoch Step: 1 Loss: 1.682198 Tokens per Sec: 432.092305
Epoch Step: 1 Loss: 1.313169 Tokens per Sec: 639.441857
1.3485562801361084
Epoch Step: 1 Loss: 1.278768 Tokens per Sec: 433.568756
Epoch Step: 1 Loss: 1.062384 Tokens per Sec: 642.542067
0.9853351473808288
Epoch Step: 1 Loss: 1.269471 Tokens per Sec: 433.388727
Epoch Step: 1 Loss: 0.590709 Tokens per Sec: 642.862135
0.5686767101287842
Epoch Step: 1 Loss: 0.997076 Tokens per Sec: 433.009746
Epoch Step: 1 Loss: 0.343118 Tokens per Sec: 642.288427
0.34273059368133546
Epoch Step: 1 Loss: 0.459483 Tokens per Sec: 434.594030
Epoch Step: 1 Loss: 0.290385 Tokens per Sec: 642.519464
0.2612409472465515
Epoch Step: 1 Loss: 1.031042 Tokens per Sec: 434.557008
Epoch Step: 1 Loss: 0.437069 Tokens per Sec: 643.630322
0.4323212027549744
Epoch Step: 1 Loss: 0.617165 Tokens per Sec: 436.652626
Epoch Step: 1 Loss: 0.258793 Tokens per Sec: 644.372296
0.27331129014492034
```

This code predicts a translation using greedy decoding for simplicity.

```
def greedy decode (model, src, src mask, max len, start symbol):
    memory = model.encode(src, src mask)
    ys = torch.ones(1, 1).fill (start symbol).type as(src.data)
    for i in range(max len-1):
        out = model.decode (memory, src mask,
                           Variable (ys),
                           Variable(subsequent mask(ys.size(1))
                                    .type as(src.data)))
        prob = model.generator(out[:, -1])
        , next word = torch.max(prob, dim = 1)
        next word = next word.data[0]
        ys = torch.cat([ys,
                        torch.ones(1, 1).type as(src.data).fill (next word)], dim=1)
    return ys
model.eval()
src = Variable(torch.LongTensor([[1,2,3,4,5,6,7,8,9,10]]))
src mask = Variable(torch.ones(1, 1, 10))
print(greedy decode(model, src, src mask, max len=10, start symbol=1))
```

```
1 2 3 4 5 6 7 8 9 10 [torch.LongTensor of size 1x10]
```

A Real World Example

Now we consider a real-world example using the IWSLT German-English Translation task. This task is much smaller than the WMT task considered in the paper, but it illustrates the whole system. We also show how to use multi-gpu processing to make it really fast.

```
#!pip install torchtext spacy
#!python -m spacy download en
#!python -m spacy download de
```

Data Loading

We will load the dataset using torchtext and spacy for tokenization.

```
# For data loading.
from torchtext import data, datasets
if True:
    import spacy
   spacy de = spacy.load('de')
    spacy en = spacy.load('en')
    def tokenize de(text):
        return [tok.text for tok in spacy de.tokenizer(text)]
    def tokenize en(text):
        return [tok.text for tok in spacy en.tokenizer(text)]
    BOS WORD = ' < s > '
    EOS WORD = '</s>'
    BLANK WORD = "<blank>"
    SRC = data.Field(tokenize=tokenize de, pad token=BLANK WORD)
    TGT = data.Field(tokenize=tokenize en, init token = BOS WORD,
                     eos token = EOS WORD, pad token=BLANK WORD)
```

```
MAX_LEN = 100
train, val, test = datasets.IWSLT.splits(
    exts=('.de', '.en'), fields=(SRC, TGT),
    filter_pred=lambda x: len(vars(x)['src']) <= MAX_LEN and
        len(vars(x)['trg']) <= MAX_LEN)
MIN_FREQ = 2
SRC.build_vocab(train.src, min_freq=MIN_FREQ)
TGT.build_vocab(train.trg, min_freq=MIN_FREQ)</pre>
```

Batching matters a ton for speed. We want to have very evenly divided batches, with absolutely minimal padding. To do this we have to hack a bit around the default torchtext batching. This code patches their default batching to make sure we search over enough sentences to find tight batches.

Iterators

```
class MyIterator(data.Iterator):
    def create batches(self):
        if self.train:
            def pool(d, random shuffler):
                for p in data.batch(d, self.batch size * 100):
                    p batch = data.batch(
                        sorted(p, key=self.sort key),
                        self.batch size, self.batch size fn)
                    for b in random shuffler(list(p_batch)):
                        yield b
            self.batches = pool(self.data(), self.random shuffler)
        else:
            self.batches = []
            for b in data.batch(self.data(), self.batch size,
                                          self.batch size fn):
                self.batches.append(sorted(b, key=self.sort key))
def rebatch(pad idx, batch):
    "Fix order in torchtext to match ours"
    src, trg = batch.src.transpose(0, 1), batch.trg.transpose(0, 1)
    return Batch(src, trg, pad idx)
```

Multi-GPU Training

Finally to really target fast training, we will use multi-gpu. This code implements multi-gpu word generation. It is not specific to transformer so I won't go into too much detail. The idea is to split up word generation at training time into chunks to be processed in parallel across many different gpus. We do this using pytorch parallel primitives:

- replicate split modules onto different gpus.
- · scatter split batches onto different gpus
- parallel_apply apply module to batches on different gpus
- gather pull scattered data back onto one gpu.
- nn.DataParallel a special module wrapper that calls these all before evaluating.

```
# Skip if not interested in multigpu.
class MultiGPULossCompute:
    "A multi-gpu loss compute and train function."
    def init (self, generator, criterion, devices, opt=None, chunk size=5):
       # Send out to different gpus.
       self.generator = generator
       self.criterion = nn.parallel.replicate(criterion,
                                              devices=devices)
       self.opt = opt
       self.devices = devices
       self.chunk size = chunk size
    def call (self, out, targets, normalize):
       total = 0.0
       generator = nn.parallel.replicate(self.generator,
                                                devices=self.devices)
       out scatter = nn.parallel.scatter(out,
                                          target gpus=self.devices)
       out grad = [[] for in out scatter]
       targets = nn.parallel.scatter(targets,
                                      target gpus=self.devices)
       # Divide generating into chunks.
       chunk size = self.chunk size
       for i in range(0, out scatter[0].size(1), chunk size):
           # Predict distributions
            out column = [[Variable(o[:, i:i+chunk size].data,
                                    requires grad=self.opt is not None) ]
                           for o in out scatter]
            gen = nn.parallel.parallel apply(generator, out column)
            # Compute loss.
```

```
y = [(g.contiguous().view(-1, g.size(-1)),
          t[:, i:i+chunk size].contiguous().view(-1))
         for g, t in zip(gen, targets)]
    loss = nn.parallel.parallel apply(self.criterion, y)
    # Sum and normalize loss
    1 = nn.parallel.gather(loss,
                           target device=self.devices[0])
    l = l.sum()[0] / normalize
    total += 1.data[0]
    # Backprop loss to output of transformer
    if self.opt is not None:
       1.backward()
       for j, l in enumerate(loss):
            out grad[j].append(out column[j][0].grad.data.clone())
# Backprop all loss through transformer.
if self.opt is not None:
    out grad = [Variable(torch.cat(og, dim=1)) for og in out grad]
    o1 = out
    o2 = nn.parallel.gather(out grad,
                            target device=self.devices[0])
    o1.backward(gradient=o2)
    self.opt.step()
    self.opt.optimizer.zero grad()
return total * normalize
```

Now we create our model, criterion, optimizer, data iterators, and paralelization

```
batch_size_fn=batch_size_fn, train=False)
model_par = nn.DataParallel(model, device_ids=devices)
None
```

Now we train the model. I will play with the warmup steps a bit, but everything else uses the default parameters. On an AWS p3.8xlarge with 4 Tesla V100s, this runs at ~27,000 tokens per second with a batch size of 12,000

Training the System

```
#!wget https://s3.amazonaws.com/opennmt-models/iwslt.pt
```

```
if False:
    model opt = NoamOpt(model.src embed[0].d model, 1, 2000,
            torch.optim.Adam(model.parameters(), lr=0, betas=(0.9, 0.98), eps=1e-9))
    for epoch in range(10):
        model par.train()
        run epoch ((rebatch (pad idx, b) for b in train iter),
                  model par,
                  MultiGPULossCompute (model.generator, criterion,
                                      devices=devices, opt=model opt))
        model par.eval()
        loss = run epoch((rebatch(pad idx, b) for b in valid iter),
                          model par,
                          MultiGPULossCompute (model.generator, criterion,
                          devices=devices, opt=None))
        print(loss)
else:
    model = torch.load("iwslt.pt")
```

Once trained we can decode the model to produce a set of translations. Here we simply translate the first sentence in the validation set. This dataset is pretty small so the translations with greedy search are reasonably accurate.

```
for i, batch in enumerate(valid_iter):
    src = batch.src.transpose(0, 1)[:1]
    src_mask = (src != SRC.vocab.stoi["<blank>"]).unsqueeze(-2)
    out = greedy_decode(model, src, src_mask,
```

```
max_len=60, start_symbol=TGT.vocab.stoi["<s>"])
print("Translation:", end="\t")
for i in range(1, out.size(1)):
    sym = TGT.vocab.itos[out[0, i]]
    if sym == "</s>": break
    print(sym, end =" ")
print()
print("Target:", end="\t")
for i in range(1, batch.trg.size(0)):
    sym = TGT.vocab.itos[batch.trg.data[i, 0]]
    if sym == "</s>": break
    print(sym, end =" ")
print()
break
```

```
Translation: <unk> <unk> . In my language , that means , thank you very much .

Gold: <unk> <unk> . It means in my language , thank you very much .
```

Additional Components: BPE, Search, Averaging

So this mostly covers the transformer model itself. There are four aspects that we didn't cover explicitly. We also have all these additional features implemented in OpenNMT-py.

1) BPE/Word-piece: We can use a library to first preprocess the data into subword units. See Rico Sennrich's subword- nmt implementation. These models will transform the training data to look like this:

```
__Die __Protokoll datei __kann __ heimlich __per __E - Mail __oder __FTP __an __einen __bestimmte n __Empfänger __gesendet __werden .
```

2) Shared Embeddings: When using BPE with shared vocabulary we can share the same weight vectors between the source / target / generator. See the (cite) for details. To add this to the model simply do this:

```
if False:
   model.src_embed[0].lut.weight = model.tgt_embeddings[0].lut.weight
   model.generator.lut.weight = model.tgt_embed[0].lut.weight
```

3) Beam Search: This is a bit too complicated to cover here. See the OpenNMT- py for a pytorch implementation.

4) Model Averaging: The paper averages the last k checkpoints to create an ensembling effect. We can do this after the fact if we have a bunch of models:

```
def average (model, models):
    "Average models into model"
    for ps in zip(*[m.params() for m in [model] + models]):
        p[0].copy_(torch.sum(*ps[1:]) / len(ps[1:]))
```

Results

On the WMT 2014 English-to-German translation task, the big transformer model (Transformer (big) in Table 2) outperforms the best previously reported models (including ensembles) by more than 2.0 BLEU, establishing a new state-of-the-art BLEU score of 28.4. The configuration of this model is listed in the bottom line of Table 3. Training took 3.5 days on 8 P100 GPUs. Even our base model surpasses all previously published models and ensembles, at a fraction of the training cost of any of the competitive models.

On the WMT 2014 English-to-French translation task, our big model achieves a BLEU score of 41.0, outperforming all of the previously published single models, at less than 1/4 the training cost of the previous state-of-the-art model. The Transformer (big) model trained for English-to-French used dropout rate Pdrop = 0.1, instead of 0.3.

```
Image(filename="images/results.png")
```

Table 2: The Transformer achieves better BLEU scores than previous state-of-the-art models on the English-to-German and English-to-French newstest2014 tests at a fraction of the training cost.

Model	BLEU		Training Cost (FLOPs)	
	EN-DE	EN-FR	EN-DE	EN-FR
ByteNet [18]	23.75			
Deep-Att + PosUnk [39]		39.2		$1.0 \cdot 10^{20}$
GNMT + RL [38]	24.6	39.92	$2.3 \cdot 10^{19}$	$1.4 \cdot 10^{20}$
ConvS2S [9]	25.16	40.46	$9.6 \cdot 10^{18}$	$1.5 \cdot 10^{20}$
MoE [32]	26.03	40.56	$2.0 \cdot 10^{19}$	$1.2 \cdot 10^{20}$
Deep-Att + PosUnk Ensemble [39]		40.4		$8.0 \cdot 10^{20}$
GNMT + RL Ensemble [38]	26.30	41.16	$1.8 \cdot 10^{20}$	$1.1 \cdot 10^{21}$
ConvS2S Ensemble [9]	26.36	41.29	$7.7 \cdot 10^{19}$	$1.2 \cdot 10^{21}$
Transformer (base model)	27.3	38.1	$3.3\cdot 10^{18}$	
Transformer (big)	28.4	41.8	$2.3 \cdot 10^{19}$	

The code we have written here is a version of the base model. There are fully trained version of this system available here (Example Models).

With the additional extensions in the last section, the OpenNMT-py replication gets to 26.9 on EN-DE WMT. Here I have loaded in those parameters to our reimplementation.

```
!wget https://s3.amazonaws.com/opennmt-models/en-de-model.pt
```

```
model, SRC, TGT = torch.load("en-de-model.pt")
```

```
Translation: <s> _Die _Protokoll datei _kann _ heimlich _per _E - Mail _oder _FTP _an _ einen _bestimmte n _Empfänger _gesendet _werden .
```

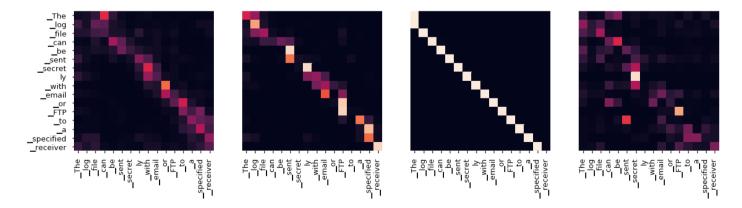
Attention Visualization

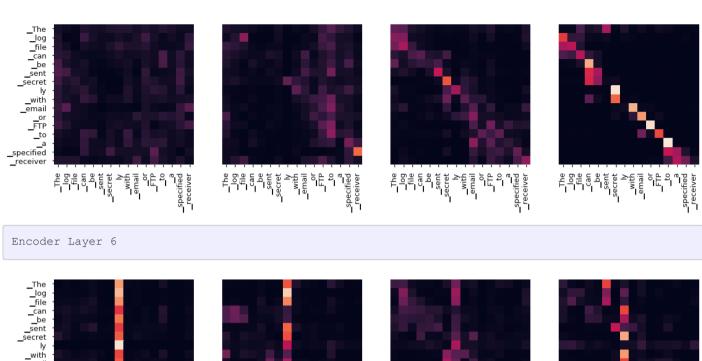
Even with a greedy decoder the translation looks pretty good. We can further visualize it to see what is happening at each layer of the attention

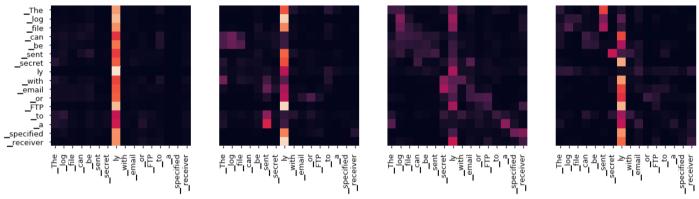
```
tgt_sent = trans.split()
def draw(data, x, y, ax):
```

```
seaborn.heatmap(data,
                    xticklabels=x, square=True, yticklabels=y, vmin=0.0, vmax=1.0,
                    cbar=False, ax=ax)
for layer in range (1, 6, 2):
    fig, axs = plt.subplots(1,4, figsize=(20, 10))
    print("Encoder Layer", layer+1)
    for h in range(4):
        draw(model.encoder.layers[layer].self attn.attn[0, h].data,
            sent, sent if h ==0 else [], ax=axs[h])
    plt.show()
for layer in range(1, 6, 2):
    fig, axs = plt.subplots(1,4, figsize=(20, 10))
    print("Decoder Self Layer", layer+1)
    for h in range(4):
        draw(model.decoder.layers[layer].self attn.attn[0, h].data[:len(tgt sent), :len(tgt sent)
)],
            tgt sent, tgt sent if h ==0 else [], ax=axs[h])
    plt.show()
    print("Decoder Src Layer", layer+1)
    fig, axs = plt.subplots(1,4, figsize=(20, 10))
    for h in range(4):
        draw(model.decoder.layers[layer].self attn.attn[0, h].data[:len(tgt sent), :len(sent)],
            sent, tgt sent if h ==0 else [], ax=axs[h])
    plt.show()
```

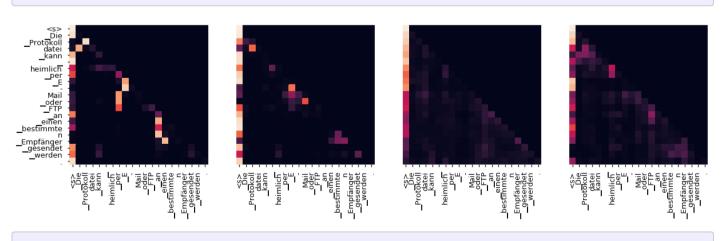
Encoder Layer 2

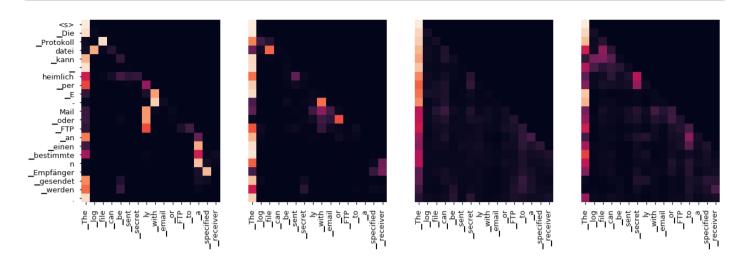




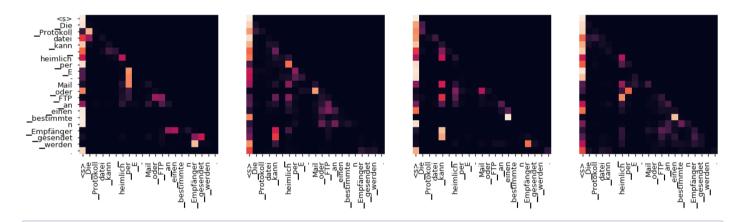


Decoder Self Layer 2

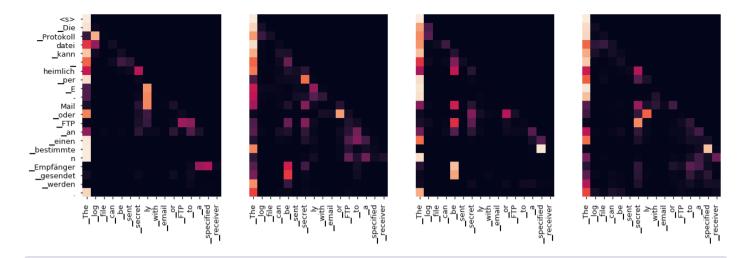




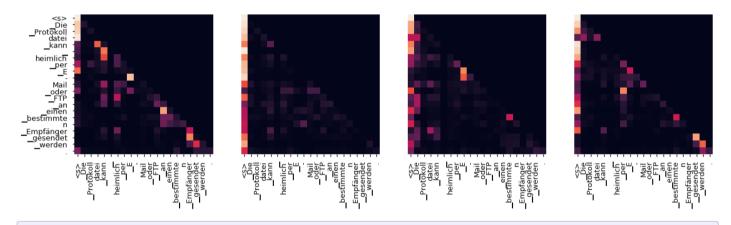
Decoder Self Layer 4



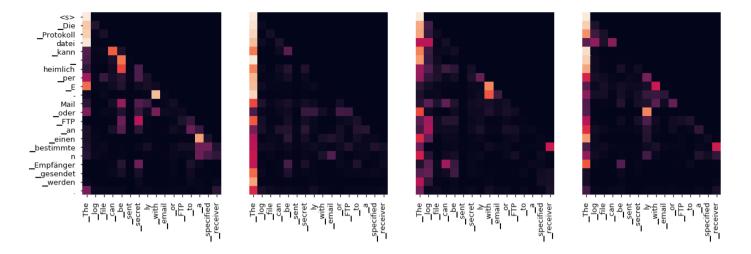
Decoder Src Layer 4



Decoder Self Layer 6



Decoder Src Layer 6



Conclusion

Hopefully this code is useful for future research. Please reach out if you have any issues. If you find this code helpful, also check out our other OpenNMT tools.

```
@inproceedings{opennmt,
            = {Guillaume Klein and
  author
               Yoon Kim and
               Yuntian Deng and
               Jean Senellart and
               Alexander M. Rush},
  title
            = {OpenNMT: Open-Source Toolkit for Neural Machine Translation},
  booktitle = {Proc. ACL},
            = \{2017\},
  year
            = {https://doi.org/10.18653/v1/P17-4012},
  url
  doi
            = \{10.18653/v1/P17-4012\}
```

Cheers, srush

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harvardnlp

Home of the Harvard SEAS natural-language processing group.