# Lambda Calculus with Lifetimes and Higher Kinded Types

Final Year Project Report

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## Introduction

## 1.1 Project Aims

This project aims to design and implement a language with a novel type system, with two main aspects. The first is the ability to abstract over type constructors as well as types, in effect allowing for a language at the level of types as well as expressions. The second is a memory management technique that guarantees memory safety at compile time. This technique is incorporated into the language as part of the type system. These two concepts will be implemented in the Lambda Calculus. A type checker and interpreter will be developed with Higher Kinded Types and a region-based memory management model similar to that of the Rust programming language.

The end purpose of this project is to investigate how Higher Kinded Types interact with the existing aspects of the Rust programming language, which already has a system of guaranteeing memory safety.

## 1.2 Types in Programming Languages

Type systems are designed to help programmers reason about behaviours in the programs that they write. Types restrict the kinds of statements that may be expressed, the most obvious reason for doing this is to detect certain types of errors before a program is executed. Small, obvious errors, found in expressions such as "this sentence" \* 69 are easily detected, because multiplication makes no sense when applied to a strings of characters and a number. However, modern type systems are capable of doing far more.

As programs become larger and more complex, separating parts of programs that do not need any knowledge of each other becomes more important. It is much easier to maintain a program composed of separate modules that have no knowledge of the inner workings of one another. Modules may interact through well defined interfaces to one another and in this way may be swapped out or replaced much more easily, as one may re-write code that conforms to an existing interface. A type system can be used to define this interface and to ensure that new code behaves as expected. Polymorphism, discussed in detail in Section 3.1.1 is one way of allowing more flexibility in these interfaces between parts of a program.

more about higher kinded polymorphsim? generic constructs?

Some programming language features may introduce whole new families of errors. Allowing a programmer to manually allocate and deallocate space for storing objects in memory is known to be a common source of bugs. Languages like C have a reputation for being difficult to write bug free programs in because of manual memory management. Memory leaks may occur if a programmer requests some storage in memory but does not deallocate it. This can lead to programs consuming unreasonably large amounts of memory. Referencing some location in memory after it has been deallocated (and possibly allocated with some new object) is another common pitfall associated with manual memory management. Garbage collection, or the automatic allocation and deallocation of objects in heap memory, may alleviate some of these issues. However, it can incur a sometimes unacceptable runtime overhead, especially in software systems where responsiveness is key.

A solution can be found in the type system. Restricting where a programmer can request or reference some location in memory allows a program to be statically analysed before it is run, and any errors related to memory usage can be highlighted. A type system can form the basis of this restriction, as shown in Section 3.3.2

### 1.3 Goals of This Project

design a type system for the lambda calculus that includes existing aspects from System F omega for the polymorphism bit and design a calculus that can reason about first class memory concerns

implement that lanagauge as a haskell program

The main objective of this project is to specify, implement, and investigate a language with a novel type system. There are two main aspects to this type system:

- Higher Kinded types, described in Section 3.1.1. Formalised in System F  $\omega$ , they allow for a neat implementation of very generic, high level programming concepts such as Monads and Functors.
- A system restricting the allocation and deallocation of memory, encoded into the type system. This aspect is
  based on the type system of the Rust programming language, which guarantees memory safety through the
  mechanisms of lifetime and the borrow checker.

Higher

#### 1.3.1 Base Objectives

The base objectives for the project are outlined below. These are objectives that should be reasonably achievable in the time given.

- Design a language which incorporates region based memory management techniques and Higher Kinded Types into the type system. Describe the language using a formal grammar.
- Implement the Lambda Calculus extended with references as a Haskell program, modelling dynamic memory allocation inside the interpreter for the language.
- Implement a system for ensuring all resources in the language have exactly one owner (are assigned to one variable), based on the model in Rust.
- Implement a type system that incorporates higher order polymorphism into the language (higher kinded types).
- Formalize the rules of the type checker and construct the appropriate typing derivations.

#### **1.3.2 Design**

### 1.3.3 Implementation

#### **1.3.4** Tests

#### **Extensions**

Some extensions to the project are outlined below, which should be completed depending on time and complexity constraints.

- Extend the base lambda calculus with constructs that more closely model the Rust programming language, including traits (or in the case of the language outlined in the project, type constructor classes), enums (discriminated union types), and local type inference.
- Investigate how concepts learned in this project can be incorporated into rusto, specifically adding Higher Kinded Types to the language.

## 1.4 Project Overview

The rest of this report is divided in several chapters. Chapter ?? describes concepts neccessary in order to understand the rest of the report. Chapter 2 gives an analysis of the ethical considerations of this project. Chapter 5 list the requirements of this project. This chapter is divided into the functional requirements, or what the project will do, and non-functional requirements which list how the project will be carried out. Finally the acceptance criteria are listed, which the final tests of the project will be based on. Chapter ?? breaks down the main phases of work to be completed in this project and gives an estimated time for each phase. Work done so far is also listed. Chapter ?? details what is discussed during meetings. Both meetings which have already happened and meetings which have yet to happen are listed. Appendix ?? gives the original project proposal which was already submitted. Appendix ?? describes the grammar of the extended Lambda Calculus that this project is based on.

## **Professional and Ethical Considerations**

No part of this project requires human participation and as such there are no ethical considerations.

This needs more detail, perhaps licensing issues?

## **Motivation**

This chapter attempts to give some background for the topics covered in this project. Aspects from existing type systems are introduced and explained.

## 3.1 Higher Kinded Types

This chapter introduces Higher Kinded Types, also known as higher order polymorphism, and show what kinds of problems a language that includes these features can solve.

### 3.1.1 Parametric Polymorphism

First order parametric polymorphism, known as Generics in Java, are types that are parametrized over some other type. This kind of polymorphism allows for the definition and use of functions that behave uniformly over all types. They can be used to write code that can be checked for safety at compile time. For example, without generics, a list could be used like:

```
List 1 = new ArrayList();
1.add("This_is_a_string");
Integer i = (Integer) 1.get(0); // Run time error here
```

Listing 3.1: Runtime error that could be avoided

This is problematic because a list in Java can contain any type of object, but methods that the List object provide must know about the type of object that the list contains. If those methods do not have a way of knowing what kind of object a list contains then calling the methods will not be type safe, as demonstrated in Listing 3.1. The same code written with Java's Generics will produce a compile time error:

```
List<String> l = new ArrayList<String>(); // Now the list has been parametrized with a type l.add("This\_is\_a\_string"); Integer i = l.get(0); // Compile time error here.
```

Listing 3.2: Compile time error

Compile time errors are much more desirable then runtime errors because they can be caught and fixed predictably, unlike runtime errors which may happen at unpredictable times. The code in Listing 3.2 parametrizes the List type with the String type, and hence the last line produces a compile time error as the list's get method returns a String.

Parametric polymorphism is an important addition to statically typed programming languages. However, Generics in Java and in lots of other programming languages have the limitation that types can only be parametrized with other types. This leads to some important limitations.

Talk about formalization,
System F

### 3.1.2 Higher Order Polymorphism

As mentioned in Section 3.1.1, first order parametric polymorphism can be very useful in expressing certain concepts succinctly in programming languages. However, there are limitations. This section will attempt to demonstrate one shortfall of first order polymorphism and then show how the problems can be solved with higher order polymorphism.

#### **Functors**

A Functor is important concept in modern programming languages. Most languages have constructs that can be thought of as Functors, such as lists, optional types, trees, and other constructs that can be mapped over. Anything that acts as a container for another type and provides a function for mapping a function over that contained type is a Functor. They are an important concept because they provide a common interface to working with any type that acts as a box for another type. This means that programs can be written more generically and is more open to changes and modifications.

Some languages seek to reify the general concept of functors so that aspects of a program can be checked for correctness at compile time. However, expressing Functors in a generic way requires a more expressive type system, specifically a type system that incorporates higher order polymorphism. Here is an example of an attempt to define a general Functor interface in Java:

```
interface Functor<A> {
    Functor<B> map(Function<A, B> f);
}
```

Listing 3.3: An attempt to define Functor in Java

The code in Listing 3.3 has one main issue. The map method defined here may return any type that implements Functor, not the necessarily the same class as the one that the method has been called from. This means that there is no type-safe way of calling any method on the result of calling the map function.

In order to define a generic Functor interface, a way of referencing the type constructor that is being used as a functor is needed. In other worlds, the programming language needs type constructors that can be parametrized with other type constructors. Generics in Java provide a way of making types like Integer, String, and even List<Integer> first class, but type constructors like List must be applied to some concrete type before they can be abstracted over.

Listing 3.4 shows how Functor can be defined in a Haskell, a language that does allow higher order polymorphism. Here, f is a variable that references a type constructor. This class in Haskell specifies that anything that instanciates it must provide a single function, fmap. fmap takes a function as a parameter that takes a value of type, a, and returns a value of type b. It then takes another argument of type f a, or a type that the type constructor f has been applied to. For example, it would take a value of type Maybe Int, Maybe being the type constructor f. It would then return a value of type b, wrapped in the same type constructor Maybe.

The ability to use type constructors as first class in a programming language allows programs to be written in a more succinct, patterned, and generic manner. Examples like Functor show how a generic interface to work with constructs commonly found in software engineering can be achieved with the use of Higher Order Polymorphism.

#### **Kinding**

Higher order polymorphism can be thought of as the polymorphic lambda calculus 'one level up', and as such the language at the level of types also needs to have a type system in order to prevent wrong expressions from being created.

A system that allows for abstracting over type constructors needs some way of enforcing type constructors are not applied to types in a way that does not make sense, e.g. Integer Integer does not make sense because the integer types does not take any type arguments in order to become a concrete type that can be inhabited by values. Alternately

just List cannot be instantiated with a value because it need one more type constructor, the type that will be contained within that list.

What is needed is essentially a type system for types. This is the notion of the kind of a type. Types can have the kind of \*, in which case they are concrete and can be inhabited by values, or they can have kind  $* \to *$ , or a function from types to other types. Types like Integer or List Integer have kind \* however type constructors like List have kind  $* \to *$  because they need to take one more concrete types before they can be used as a value. This system of kinding enforces that all types are well formed.

$$K ::= *$$
 Concrete types  $\mid K \to K$  Type functions from types to types

Figure 3.1: Syntax of types

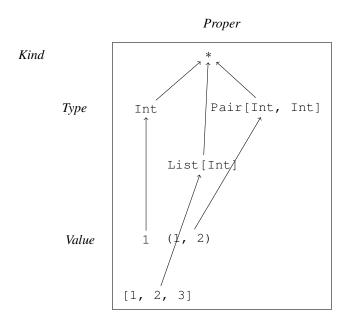


Figure 3.2: Some types and their associated kinds.

## 3.2 Problems with Existing Memory Management Techniques

Most programming languages allow for dynamic memory management where the program can request portions of memory at run time and free that memory when it is no longer required. This operation can be performed manually as in the case of languages such as C or automatically in languages with a garbage collector such as Java.

#### 3.2.1 Manual Memory Management: malloc and free

Some languages rely on manual instructions inserted by the programmer in order to allocate and deallocate regions of memory. Most implementations of the C programming language provide a group of library functions for this purpose, which include malloc and free. As mentioned, these constructs are insert manually by the programmer. This can lead to the issues described below.



#### **Dangling References**

Deallocating storage may lead to dangling references, where some reference exists that points to memory that has been deallocated. This is nearly always unintentional, however it is an easy for a programmer to make this mistake when writing a program. Using the value of deallocated storage can lead to nefarious bugs and most languages consider using deallocated storage to be undefined behaviour.

```
int *dangle()
{
    int i = 69;
    return &i; // Function return address of local variable!
}
int main()
{
    int *p;
    p = dangle();
}
```

Listing 3.5: A C program that leaves p pointing to deallocated memory.

In the Rust programming language, references to values must live longer than the resource that they refer to [**rust-borrowing**]. The same program as the C dangling pointer example (Listing 3.5) written in Rust does not compile as it does not meet this restriction.

```
fn dangle() -> &u32 {
    let i = 69;
    &i // This does not typecheck because this would be a dangling pointer
}
fn main() {
    let p = dangle();
}
```

Listing 3.6: A Rust program that does not type check.

#### **Memory Leaks**

Memory leaks occur when heap storage that is no longer usable is not deallocated. This can lead to software allocating more memory for itself and in the worst case can lead to a program consuming all available memory.

```
#include <stdlib.h>

void allocate()
{
    int* a = malloc(sizeof(int) * 100); // Allocate memory on the heap
    // Return and forget about the allocated memory!
}

int main()
{
    allocate();
    // ...
    // do more stuff, while heap space that allocate used is unreachable
}
```

Listing 3.7: A C program which leaks memory.

### 3.2.2 Automatic Memory Management: Garbage Collection

Techniques have been invented in order to mitigate errors related to manual memory management. Garbage collection is one such method. Garbage is a term for storage that has been allocated on the stack but is no longer reachable by the

program, e.g. the storage is pointed to by a variable that has gone out of scope. Automatic garbage collection alleviates the programmer of explicitly managing memory. However there are several downsides to garbage collection. For example, the garbage collector will be invoked to collect unusable memory outside of the control of the programmer. When it is running it affects the execution of the program for an indeterminate amount of time. This hang is not acceptable in real–time systems.

## 3.3 A Solution in the Type System

Rust, a systems programming language [**rust**] is designed to provide memory safety with no runtime overhead. Rather than relying on a garbage collector to provide run-time memory safety, Rust relies on strong compile time checks. This system of compile time checks is referred to as *ownership*, and is derived from affine type systems and unique pointers to memory locations[**rust-borrowing**] [**levy2015ownership**].

### 3.3.1 Affine types

Affine types are a development of Linear type systems. Linear type systems ensure that every variable is used exactly once. In an affine type system, a variable may be used at most once, i.e. zero or one times. This has applications for managing resources in a program that do not persist the whole time that the program is running, e.g. file handles or heap allocated memory [attapl] [tovAffine].

#### 3.3.2 Ownership

Values in Rust are bound to a single *owner*, which is the variable to which it is bound. When the owning variable goes out of scope, the value is freed. For example:

```
{
   let x = 69;
}
```

When  $\times$  goes out of scope the value associated with it will also be released from memory. Because there can only be a single owner associated with a value, aliasing a variable is not allowed. This prevents any two parts of a Rust program from accessing a section of heap memory at the same time.

```
{
    let x = Thing::new();
    let y = x;
    println("()", x);
}
```

The above code does not compile because x has been moved to y, there is an attempt to use x in the print statement. Using a variable as a function argument will also make it not available for use again. If a function uses some value that has been passing in as a parameter it must return that same value if the scope outside that function uses it.

```
// value is comes from outside the scope of this function
fn foo(value: Bar) -> Bar {
    // do stuff with value, returning it and hence handing back ownership
    value
}
```

This is not practical, and gets even less practical once there are more arguments that must be passed back to the caller of the function. To this end Rust allows references to a value to be created. Creating a reference to a value in Rust is called borrowing. A reference to a value may be created and passed in to a function that uses it in some way, and that function does not need to thread the ownership of that variable back to the caller.

```
// instead of passing value1 and value2 in by value, create references to values
fn foo(value1: &Bar, value2: &Bar) -> u32 {
    // do stuff with value1 and value2 and return the answer
    123
}
```

There are two kinds of borrows: immutable and mutable. There many be many immutable borrows of a resource at once or a single mutable borrow. This also prevents heap data from being accessed at the same time at different points in the program. The scope of borrow must always be shorter than that of the resource which it borrows.

This system where resources are freed after the single owner goes out of scope, as well as borrows always having shorter lifetimes than original resource mean that Rust can enforce the memory safety of programs. These concepts are built into the type system.

## **Formal Definitions**

This chapter attempts to formalize some of the concepts from Chapter ??. The lambda calculus is introduced as a model of computation and as a system for reasoning about features found in programming languages. Types are introduced to the lambda calculus as well as other more complex extensions relevant to this project. The higher order polymorphic lambda calculus, known as System F  $\omega$ , is included as well as a lifetime-calculus devised for this project.

### 4.1 Lambda Calculus

The lambda calculus is model of computation where the only behaviour is function definition and application. It is commonly used to specify programming language features and to formalize their behaviour. Specifically, it is used to reason about type systems. The lambda calculus can be viewed as a miniature programming language and a system where strict properties can be proved.



Figure 4.1: Grammer of the untyped lambda calculus.

### 4.1.1 Simple Types in the Lambda Calculus

The lambda calculus can be extended with the most simple of typing systems. In order to demonstrate how the lambda calculus can be used to reason about type systems, some additional constructs added. If Boolean literals some other concepts are added it becomes more clear how types are useful in programming languages.

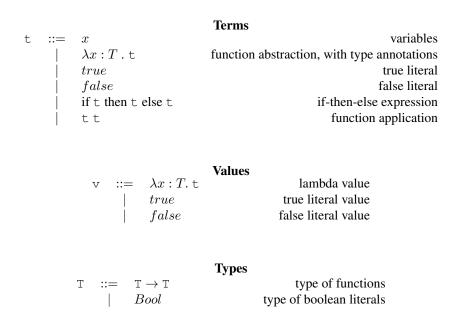


Figure 4.2: Lambda calculus extended with simple types and booleans.

Programs can be constructed using the language defined in Figure 4.1.1 that do not make any sense. For example:

baddef = if  $\lambda x : Bool.x$  then false else true

This program is constructed according to the grammar of terms. However, is not well type according to the typing rules in Figure ??. Specifically, the type of the term found in the guard of the if-expression,  $\lambda x : Bool.x$  has type  $Bool \rightarrow Bool$  but has to be Bool for the term to be considered well typed. It makes sense to restrict the kinds of values found in the guard of an if-then-else expression. Anything other than a boolean value in that place may indicate programmer error, which could be as simple as a typing mistake or a fundamental misunderstanding of what they are trying to express. Type systems help catch these kind of mistakes before program execution. Specifying these rules on top of the lambda calculus can be a very informative way of looking at programming language features. The rest of this chapter describes other extensions to the lambda calculus that model some of the programming concepts investigated in this report.

#### **4.1.2** System F

System F is an extension of the simply typed lambda calculus [**tapl**] that allows for quantification over types as well as terms. In doing this it formalizes the notion of polymorphism in programming languages, as described in Section 3.1.1. It is used to study implementations of polymorphism in programming languages.

As the simply typed lambda calculus allows for abstraction of terms outside of terms through function definitions, System F introduces abstractions at the level of types. The system also allows for application of type level expressions. This system can be used to reason about first order polymorphism, however more extensions to talk about higher order polymorphism. These extensions are introduced in Section 4.1.3.

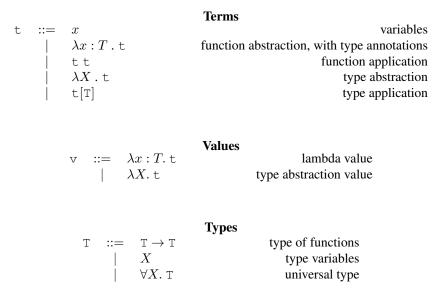


Figure 4.3: System F

### **Examples**

System F models first order polymorphism in programming languages, such as aspect of the generics found in Java. Some examples of how System F can be used are given below:

$$\text{id} = \lambda X.\lambda x : X.x \\ \text{boolId} = \text{id} \text{ [Bool]}$$

The example in Listing  $\ref{listing:property}$  shows type level lambdas, where X is a type variable that has been abstracted out of the function definition. The term level lambda abstracts x which has the type X. Applying id to a type maybe be written as id [Bool], which yields  $\lambda x : Bool.x$ , or the identify function over boolean values. Here X in the original definition of id has been instantiated with the type of Booleans.

#### 4.1.3 System F $\omega$

System F  $\omega$  is form

### **Type Operators**

## 4.2 Adding Lifetimes

showing how lifetimes are represented in this lanaguage

## 4.3 Final Typing Rules

## Requirements

The functional requirements of this project specify what this project shall do.

## **5.1** Functional Requirements

The functional requirements of this project are laid out in this section. Because the entire system is a Haskell program all of these requirements will be implemented in Haskell.

#### **5.1.1** Parser

**Description** A parser for the language specified in ?? shall be created using the

 $\verb|megaparsec[1]| parser combinator library.$ 

**Input** Source code from a file or interactive session.

**Output** A data type that represents the abstract syntax of the input provided, or

an error message pointing to the location of any syntax errors.

**Error** An error message with a line and column number and a message.

### **5.1.2** Simple Type Checker

**Description** A simple type checker that ensures that simple mistakes are not make,

e.g. using a function type where a numerical type is expected.

**Input** A syntactically valid (according to Figure ??) AST of a program as a

Haskell data type.

Output The same AST of the program that confirms the typing rules of the

language.

**Error** An error with a message that provides some indication of what went

wrong.

### 5.1.3 Ownership Checker

**Description** An ownership checker ensures there exactly one binding to a resource

all the time.

**Input** A syntactically valid (according to figure ??) AST of a program as a

Haskell data type.

**Output** The same AST of the program that confirms the ownership rules of the

language.

**Error** An error with a message that provides some indication of what went

wrong.

#### 5.1.4 Borrow and Lifetime Checker

**Description** A checker that ensures that references that borrow ownership from an-

other type last longer than the resource they borrow, and that there are only mutable references OR exactly one mutable reference at any one

point.

**Input** A syntactically valid (according to figure ??) AST of a program as a

Haskell data type.

**Output** The same AST of the program that confirms the borrowing rules of the

language.

Error An error with a message that provides some indication of what went

wrong.

#### 5.1.5 Kind Checker

**Description** Ensures that all type constructors using in a program have the correct

number and kind of arguments.

**Input** A syntactically valid (according to figure ??) AST of a program as a

Haskell data type.

**Output** The same AST of the program that confirms the kinding rules of the

language.

Error An error with a message that provides some indication of what went

wrong.

#### 5.1.6 Evaluator

**Description** A call-by-value evaluator of the language that will reduce a syntactically

valid expression.

**Input** A syntactically valid and type-checked AST of a program represented

as a Haskell data type.

**Output** The final resulting value of evaluating the AST.

**Error** A description of any runtime errors that occur within the program.

### **5.1.7** Interactive Interpreter

**Description** An interactive interpreter that type checks and then evaluates entered

expressions.

**Input** Source code as entered by the user.

**Output** The resulting value of evaluating the entered expression, some error.

**Error** An parsing, type, or runtime error message.

#### 5.1.8 Load a file

**Description** Provided with a path, the program loads a text file containing source

code.

**Input** A path provided by the user. **Output** The source code as a string.

**Error** An error reporting a file not found or any other errors.

## 5.2 Acceptance Criteria and Testing

The acceptance criteria of this program correspond to the functional requirements in Section 5.1. The finished project should pass the tests laid out in this section.

5.2.1 Parsing

**Functional Requirement** 5.1.1

**Passing Criteria** The program should be able to parse valid source code and correctly

report any errors that are encountered.

**Tests** Test numbers

5.2.2 Type checking

**Functional Requirement** 5.1.2, 5.1.3, 5.1.4, 5.1.5

**Passing Criteria** The type checker should detect any errors in the program.

**Tests** Test numbers

5.2.3 Evaluating

**Functional Requirement** 5.1.6, 5.1.7, 5.1.8

**Passing Criteria** Source code, provided by a file or through the interactive interpreter,

should be type checked and evaluated.

**Tests** Test numbers

Should this section be related to KEY TESTS? Maybe this section should exist but should reference that

chapter

## **Implementation**

This chapter describes how the ideas and type system described in Chapter 4 will be implemented. As stated in Chapter ??, one of the goals for this project is to build a program that will be able to parse, type check, and evaluate a language based on the lambda calculus. The most involved phase of implementation and the focus of this project involves the type checking phase, which includes lifetime checking of pointers and references, polymorphic type checking, and checking that the language of types themselves is well formed, or kind checking.

The requirements of this project influence the choice of the language of implementation. Haskell was chosen as it is well suited to the tasks of parsing, abstract syntax tree declaration, and is in general a practical language to work with

## **6.1** The Haskell Language

Haskell is a general purpose, statically typed, functional language [haskell]. It has several desirable features for a language implementation language. These include:

- Algebraic data types, which are very good at representing abstract syntax trees, used to describe programming languages.
- Pattern matching, which is useful for deconstruct abstract syntax trees.
- A wealth of effective parsing libraries, over several paradigms.
- Idiomatic monadic programming, which can be used to reduce error handling and state threading boilerplate out of the logic of the program.

It also has the benefit of having higher kinded types built into the language, making it ideal for testing potential features of the implemented language. The language described in Chapter 4 has been implemented as a Haskell program. The rest of this chapter describes how this was accomplished in more specific detail.

## 6.2 Parsing

A lexer generator Alex [alex], and parser generator, Happy [happy] were used in this project. Using these tools in combination made parsing the language into the Haskell representation of the abstract syntax simple. The grammars provided for the parser generator are a very close approximation of Haskell data type. Both Alex and Happy generate Haskell files when run which implement the specified grammars.

### 6.3 Terms

The Haskell representation of terms of the language are given in Listing 6.1. Type lambdas and Lifetime lambdas can be seen as first class citizens here.

Listing 6.1: Haskell representation of Terms.

### 6.4 Kind Checker

The kind checker makes sure that the type expressions in a supplied program are well–formed. The Haskell abstract data type that represents kind expression is show in Listing 6.2.

Listing 6.2: Haskell representation of Kinds.

## 6.5 Lifetime Checking

The syntax of lifetime is show in Listing 6.3.

```
data Lifetime
    = LiVar String
    | LiLit Int
    | LiStatic
    | LiDummy
    deriving (Eq, Show)
```

each of the lifetime consturctors mean

explain

what

Listing 6.3: Haskell representation of Lifetimes..

Lidummy is used here as a dummy place holder for occurrences of lifetime literals during parsing, as lifetimes are associated with the scope of terms. An initial walk of the tree replaces dummy values with the LiLit value that represents the depth of the scope that the lifetime value is found in.

#### **6.5.1** Ordering on Lifetimes

should probably write this, Ord instance for lifetimes.

## 6.6 Type Checking

Type checking is rather involved in this this language as the type system almost contains the lambda calculus itself.

Listing 6.4: Haskell representation of Types.

## 6.7 Error Reporting

Any part of the program that may result in some kind of error is wrapped in a partial application of Haskell's error monad, Except, to a custom error data type:

Listing 6.5: Partially applied error monad and language errors.

This has the advantage of being very compose able, and also of reducing error handling boilerplate in the program.

## **6.8** Context Management

The lifetime checker, kind checker, and type checker all rely on a variable typing context. These contexts are threaded thought the program using Haskell's environment monad, also known as the Reader monad. The record type holding these contexts is shown in Listing 6.6. Contexts are represented as a map from variable names are strings to some value, using Haskell's own built in strict map data structure.

Listing 6.6: Record data type showing contexts.

The monad stack where parsing, lifetime checking, kind checking, and type checking take place is therefore:

```
type Typing = ReaderT Env ThrowsError
```

Listing 6.7: Envirnment and error monad stack.

## 6.9 Testing

## **Key Tests**

## **Evaluation**

## Conclusion

## **Bibliography**

[1] megaparsec: Monadic parser combinators. https://hackage.haskell.org/package/megaparsec. Accessed: 2016-10-18.