



L3: Knowledge Base (example)

Chapter 4



Outline

- Hidden knowledge ($\text{brother}(X, Y)$)
- Represent negative knowledge
 - Example. Closed world assumption (new logical connectives)
- More problem modeling
 - Define orphan using $\text{father}/2$, $\text{mother}/2$, $\text{dead}/1$. Note closed world assumption.
 - Circuit problem
 - Hierarchical information



Hidden knowledge

- Define knowledge about brother.
 - For any person X and Y, X is a brother of Y if
 - X is a male,
 - X and Y have a same parent, and
 - $X \neq Y$.
 - Rule



Hidden knowledge

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 - For any person X and Y, X is a brother of Y if
 - X is a male,
 - X and Y have a same parent, and
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 - Rule

```
brother(X, Y) :- male(X),  
                 parent(Z, X), parent(Z, Y),  
                 X != Y.
```

Check which piece of condition you've missed when you defining the brother relation.



Represent negative knowledge

- Closed world assumption
 - Consider the family problem.
 - *Knowledge* : There is a family. John is the father and Joan is the mother. The children are Jim, Bill, and Sam.
 - *Questions*.
 - Is John the father of Bill? Who is Bill's mother?
 - Is John dad of Bill? Who is Bill's parent?
 - New question: is Jim the father of Bill?



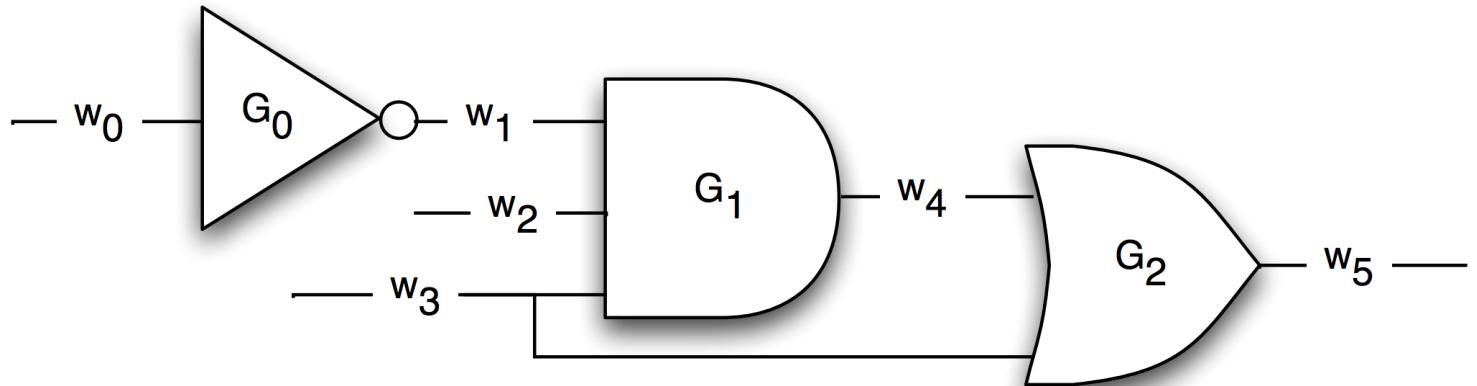
- We assume all information is given in the problem description about the father relation. So, we have the closed world assumption: “if we don’t know that X is the father of Y, X is not the father of Y.”
- rule
 - `father(X, Y) :- not father(X, Y).`



- New logical connectives
 - \neg : **classical negation**
 - `not`: **default negation**



Circuit Problem



- G_0 : not gate, G_1 : and gate, G_2 : or gate
- Questions?
 - What are the input wires of gate G_1 ? output wires of G_1 ?
 - Given the value of w_0 is 1, what is the value on wire w_1 ?



■ Identification

■ Objects:

- wires: $w_0, \dots,$
- gates: g_0, g_1, g_2, \dots
- signal (value): 0, 1
- type of gates: and, or, not

■ Relations:

- $\text{input_wire}(G, W)$: W is an input wire of G
- $\text{output_wire}(G, W)$: W is an output wire of G
- $\text{val}(W, V)$: the signal on wire W is V
- $\text{type}(G, T)$: type of gate G is T ((and, not, or)).

■ Knowledge

- All facts about wires and gates in the diagram. e.g., w_0 is an input wire of g_0 .
- not gate: the output of a not gate is the opposite of its input.



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- **not gate: the output of a not gate is the opposite of its input.**
- ```
val (Wo, V) :- type(G, not),
 output_wire(G, Wo),
 input_wire(G, Wi),
 val(Wi, Vi),
 opposite(V, Vi).

opposite(0, 1).
opposite(1, 0).
```



- value of output wire of and gate – method 1
  - %the output wire of an and gate is 0 if one of its
  - %input wire is 0. (note this define covers all cases when
  - %the output wire is 0, i.e., the knowledge is complete.)

```
val(W, 0) :- type(G, and),
 output_wire(G, W),
 input_wire(G, W1),
 val(W1, 0).
```

%the output wire of an and gate is 1 if we do not know (or cannot derive from the program) that its is 0.

```
val(W, 1) :- type(G, and),
 output_wire(G, W),
 not val(W, 0).
```



- value of output wire of and gate – method 2:  
% the value of the output wire of an and gate is 1  
% if that of all input wires is 1.

```
val(W, 1) :- type(G, and),
 output_wire(G, W),
 allInputWis1(G).
```

- **allInputWis1(G)**: all input wires of gate G is 1.  
◦ **someInputWis0(G)**: some input wire of G is 0.

```
allInputWis1(G) :- not someInputWis0(G).
someInputWis0(G) :- val(W, 0),
 input_wire(G, W).
```



## ■ Translation

### ■ Knowledge to Rules: (not gate)

- not gate: the output of a not gate is the opposite of its input.
  - refinements: (identify the objects/relations in the description above)
    - the signal on the output wire of a not gate is the opposite of the signal on the input wire of the gate.
    - For signal V, wire W, V is the signal on W if W is the output wire of a not gate, the input wire of the gate is W0 and V is the opposite of the signal V0 on wire W0. (you want also know the quantifier on "a gate". We also assume the input wire is unique here.)

```
val (W1, V) :-
 output_wire(G, W1),
 type(G, not),
 input_wire(G, W0),
 val(W0, V0),
 opposite(V, V0).
```

### ■ Knowledge to rules: (and gate)

- and gate: the output of an and gate is 0 if some of its input is 0.

# Hierarchical Information and Inheritance

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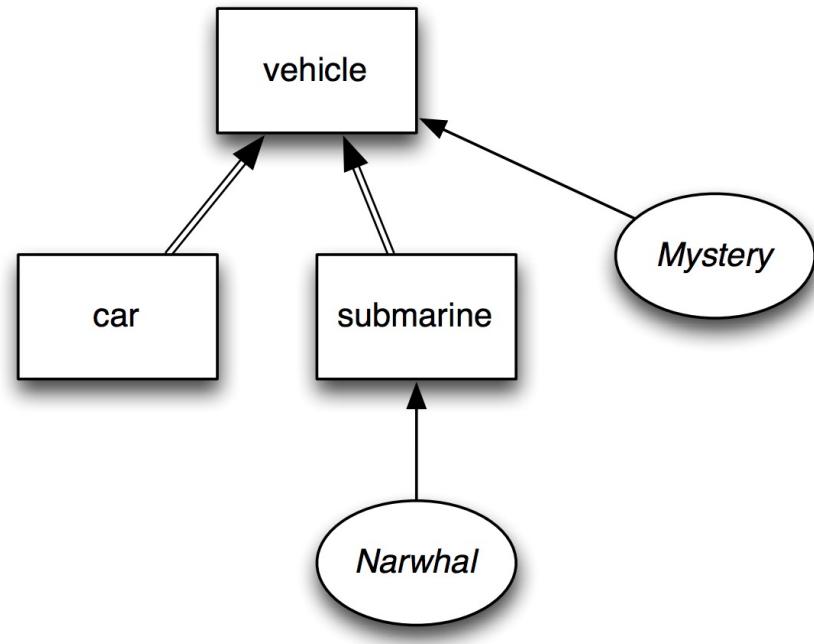


- Problem description
  - Knowledge:
    - The Narwhal is a submarine.
    - A submarine is a vehicle.
    - Submarines are black.
    - The Narwhal is a part of the U.S. Navy.
  - Questions:
    - What is the color of Narwhal?
    - Is Narwhale a vehicle?



## ■ Identification

- Objects:
  - classes: car, submarine, vehicle ...
  - objects: narwhal
- Relations:
  - directSubclass(X, Y): class X is a direct subclass of Y.
  - subclass(X, Y): class X is a subclass of Y.
  - member(X, Y): an object X is in class Y
  - is\_a(X, Y): X is a direct member of class Y
  - color(X, Y): object X of color Y.
- Knowledge ...





## ■ Translation

- subclass: X is subclass of Y if X is a direct subclass of Y or X is subclass X<sub>1</sub>, ..., X<sub>n</sub> subclass of Y

```
subclass(X, Y) :-
 directSubclass(X, Y).

subclass(X, Y) :-
 directSubclass(X, Z),
 subclass(Z, Y).
```

- member: X is a member of Y if X is a direct member of Y or X is a member of Z and Z is a subclass of Y.

```
member(X, Y) :-
```



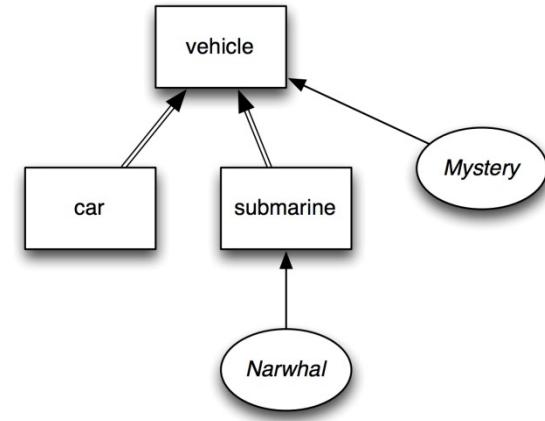
## ■ Translation

### ■ Narwhal is a submarine

is\_a(narwhal, submarine).

### ■ submarine is a direct subclass of vehicle

directSubclass (submarine, vehicle) .





## ■ Translation

- Submarines are black, i.e., every submarine is black.
  - `color(X, black) :- member(X, submarine).`
- An alternative knowledge: submarines are black unless they are not.
  - Refinements
    - A submarine is black unless its color is known (i.e., there is a color for it) and is not black.
    - We need two rules
      - The color of a submarine is known and is not black. We need a new relation: `knownNonBlack(X)`.

```
knownNonBlack(X) :-
 color(X, C), C != black.
```
      - A submarine X is black if we don't believe `knownNonBlack(X)`.

```
color(X, black) :-
 member(X, submarine),
 not knownNonBlack(X).
```
  - Compare this new approach with the one in the book.



# Summary

- Represent negative knowledge.
- More examples on problem description and how to model a problem.
- Discuss more about how to write a rule
  - object, relations, and
  - continuous refinement of English description (i.e., our understanding) of a piece of knowledge until it can be easily translated into rule(s). New relations may be introduced in this refinement process. We also see a top down/problem decomposition here in representing a piece of knowledge: considering the important info first and then go the details of the info.
  - and recursive definition again.