

Package ‘rddapp’

December 5, 2017

Title Regression Discontinuity Design Application

Version 0.1.0

Date 2017-12-05

Description Estimation of both single- and multiple-assignment RDDs (both sharp and fuzzy).
Provides both parametric (global) and non-parametric (local) estimation choices,
along with sensitivity and assumption checks.

Depends R (>= 3.2.3)

Imports AER (>= 1.2-5),
sandwich (>= 2.3-4),
lmtest (>= 0.9-35),
Formula (>= 1.2-1),
shiny (>= 0.14),
DT (>= 0.2)

Suggests rdd (>= 0.57),
rddtools (>= 0.4.0),
foreign (>= 0.8-67),
devtools (>= 1.12.0),
testthat (>= 1.0.2),
roxygen2 (>= 5.0.1),
knitr (>= 1.14),
rmarkdown (>= 1.1.9012)

VignetteBuilder knitr

License GPL (>= 2)

LazyData true

RoxygenNote 6.0.1

Collate 'attr_check.R'
'bw_ik09.R'
'bw_ik12.R'
'data.R'
'wt_kern.R'
'dc_test.R'
'treat_assign.R'
'mfrd_est.R'
'var_center.R'
'rd_est.R'
'mrd_est.R'
'mrd_impute.R'

```
'mrd_power.R'
'mrd_sens_bw.R'
'mrd_sens_cutoff.R'
'plot.mfrd.R'
'predict.rd.R'
'plot.rd.R'
'print.mfrd.R'
'print.rd.R'
'rd_impute.R'
'rd_power.R'
'rd_sens_bw.R'
'rd_sens_cutoff.R'
'rd_type.R'
'rddapp-package.R'
'sens_plot.R'
'summary.rd.R'
```

R topics documented:

rddapp-package	3
attr_check	3
bw_ik09	4
bw_ik12	5
CARE	5
dc_test	6
mfrd_est	7
mrd_est	8
mrd_impute	10
mrd_power	12
mrd_sens_bw	14
mrd_sens_cutoff	14
plot.mfrd	15
plot.rd	16
predict.rd	17
print.mfrd	17
print.rd	18
rd_est	18
rd_impute	20
rd_power	22
rd_sens_bw	23
rd_sens_cutoff	24
rd_type	24
sens_plot	25
summary.rd	26
treat_assign	26
var_center	27
wt_kern	28

rddapp-package

*Regression Discontinuity Design Package***Description**

rddapp: A package for regression discontinuity designs

Details

The rddapp package provides a set of functions for the analysis of the regression-discontinuity design (RDD). The three main parts are: estimation of effects of interest, power analysis, and assumption checks.

Estimation

A variety of designs can be estimated in various ways. The single-assignment RDD (both sharp and fuzzy) can be analyzed using both a parametric (global) or non-parametric (local) approach. The multiple-assignment RDD (both sharp and fuzzy) can be analyzed using both parametric and non-parametric estimation. The analysis choices are further to use estimate effects based on univariate scaling, the centering approach, or the frontier approach. The frontier approach can currently only be estimated using parametric regression with bootstrapped standard errors.

Power analysis

Statistical power can be estimated for both the single- and multiple-assignment RDD, (both sharp and fuzzy), including all parametric and non-parametric estimators mentioned in the estimation section. All power analyses are based on a simulation approach, which means that the user has to provide all necessary parameters for a data-generating model.

Assumption checks

An important part of any RDD are checks of underlying assumptions. The package provides users with the option to estimate McCrary's sorting test (to identify violations of assignment rules), checks of discontinuities of other baseline covariates, along with sensitivity checks of the chosen bandwidth parameter for non-parametric models, and so-called placebo tests, that examine the treatment effect at other cut-points along the assignment variable.

Author(s)

Ze Jin <zj58@cornell.edu>, Liao Wang <wl483@cornell.edu>, Felix Thoemmes, <fjt36@cornell.edu>

attr_check

*Attrition Checks***Description**

attr_check reports missing data on treatment variable, assignment variable, and outcome. Currently it only supports the design with one assignment variable.

Usage

```
attr_check(x1, y, t, x2 = NULL)
```

Arguments

x1	A numeric object, the assignment variable.
y	A numeric object, the outcome variable, with the same dimensionality as x.
t	A numeric object, the treatment variable, with the same dimensionality as x and y.
x2	A numeric object, the secondary assignment variable.

Value

A list with the missing data numbers and percentages for all variables and subgroups by treatment.

 bw_ik09

Imbens-Kalyanaraman 2009 Optimal Bandwidth Calculation

Description

bw_ik09 calculates the Imbens-Kalyanaraman (2009) optimal bandwidth for local linear regression in regression discontinuity designs. It is based on the `IKbandwidth` function in the `rdd` package.

Usage

```
bw_ik09(X, Y, cutpoint = NULL, verbose = FALSE, kernel = "triangular")
```

Arguments

X	A numerical vector which is the running variable.
Y	A numerical vector which is the outcome variable.
cutpoint	The cutpoint.
verbose	Logical flag indicating whether to print more information to the terminal. Default is FALSE.
kernel	String indicating which kernel to use. Options are "triangular" (default and recommended), "rectangular", "epanechnikov", "quartic", "triweight", "tricube", and "cosine".

Value

The optimal bandwidth.

References

Imbens, G., Kalyanaraman, K. (2009). Optimal bandwidth choice for the regression discontinuity estimator (Working Paper No. 14726). National Bureau of Economic Research. <http://www.nber.org/papers/w14726>.

bw_ik12

*Imbens-Kalyanaraman 2012 Optimal Bandwidth Calculation***Description**

bw_ik12 calculates the Imbens-Kalyanaraman (2012) optimal bandwidth for local linear regression in regression discontinuity designs. It is based on the `rdd_bw_ik` function in the **rddtools** package.

Usage

```
bw_ik12(X, Y, cutpoint = NULL, verbose = FALSE, kernel = "triangular")
```

Arguments

X	A numerical vector which is the running variable.
Y	A numerical vector which is the outcome variable.
cutpoint	The cutpoint.
verbose	Logical flag indicating whether to print more information to the terminal. Default is FALSE.
kernel	String indicating which kernel to use. Options are "triangular" (default and recommended), "rectangular", "epanechnikov", "quartic", "triweight", "tricube", and "cosine".

Value

The optimal bandwidth.

References

Imbens, G., Kalyanaraman, K. (2012). Optimal bandwidth choice for the regression discontinuity estimator. *The Review of Economic Studies*, 79(3), 933-959. <https://academic.oup.com/restud/article/79/3/933/1533189>.

CARE

*Carolina Abecedarian Project and the Carolina Approach to Responsive Education (CARE), 1972-1992***Description**

A subset of children of the randomized controlled CARE trial on early childhood intervention. The randomized controlled trial was subsetting to mimic a regression-discontinuity design in which treatment was assigned only to mothers whose IQ was smaller than 85.

Usage

CARE

Format

A data frame with 81 rows and 5 variables:

SUBJECT Unique ID variable

DC_TRT Day Care (Preschool) Treatment Group, 1=Treatment, 0=Control

APGAR5 APGAR score at 5 minutes after birth

MOMWAIS0 Biological mother's WAIS (Wechsler Adult Intelligence Scale) full-scale score at subject's birth

SBIQ48 Subject's Stanford Binet IQ score at 48 months

Source

<http://www.icpsr.umich.edu/icpsrweb/ICPSR/studies/4091>

<http://www.researchconnections.org/childcare/studies/4091/version/1>

dc_test	<i>McCrary Sorting Test</i>
---------	-----------------------------

Description

dc_test implements the McCrary (2008) sorting test. It is based on the `DCdensity` function in the `rdd` package.

Usage

```
dc_test(runvar, cutpoint, bin = NULL, bw = NULL, verbose = FALSE,
        plot = TRUE, ext.out = FALSE, htest = FALSE)
```

Arguments

runvar	Numerical vector of the running variable.
cutpoint	The cutpoint (defaults to 0).
bin	The binwidth (defaults to $2 * \text{sd}(\text{runvar}) * \text{length}(\text{runvar})^{(-.5)}$).
bw	The bandwidth to use (by default uses bandwidth selection calculation from McCrary (2008)).
verbose	Logical flag specifying whether to print diagnostic information to the terminal (defaults to FALSE).
plot	Logical flag indicating whether to plot the histogram and density estimations (defaults to TRUE). The user may wrap this function in additional graphical options to modify the plot.
ext.out	Logical flag indicating whether to return extended output. When FALSE (the default) <code>DCdensity</code> will return only the p-value of the test. When TRUE, <code>DCdensity</code> will return the additional information documented below.
htest	Logical flag indicating whether to return an "htest" object compatible with base R's hypothesis test output.
...	Additional arguments affecting the plot.

Value

If `ext.out` is `FALSE`, only the `p` value will be returned. Additional output is enabled when `ext.out` is `TRUE`. In this case, a list will be returned with the following elements:

<code>theta</code>	The estimated log difference in heights at the cutpoint.
<code>se</code>	The standard error of <code>theta</code> .
<code>z</code>	The <code>z</code> statistic of the test.
<code>p</code>	The <code>p</code> -value of the test. A <code>p</code> -value below the significance threshold indicates that the user can reject the null hypothesis of no sorting.
<code>binsize</code>	The calculated size of bins for the test.
<code>bw</code>	The calculated bandwidth for the test.
<code>cutpoint</code>	The cutpoint used.
<code>data</code>	A dataframe for the binning of the histogram. Columns are <code>cellmp</code> (the mid-points of each cell) and <code>cellval</code> (the normalized height of each cell).

References

McCrary, J. (2008). Manipulation of the running variable in the regression discontinuity design: A density test. *Journal of Econometrics*, 142(2), 698-714. <http://dx.doi.org/10.1016/j.jeconom.2007.05.005>.

Examples

```
# No discontinuity
x <- runif(1000, -1, 1)
dc_test(x, 0)

# Discontinuity
x <- runif(1000, -1, 1)
x <- x + 2 * (runif(1000, -1, 1) > 0 & x < 0)
dc_test(x, 0)
```

mfrd_est

Multivariate Frontier Regression Discontinuity Estimation

Description

`mfrd_est` implements the frontier approach in Wong, Steiner and Cook (2013). It is based on the MFRDD code in Stata.

Usage

```
mfrd_est(y, x1, x2, c1, c2, tr = NULL, t.design = c("1", "1"),
  local = 0.15, ngrid = 2500, margin = 0.03, boot = NULL,
  cluster = NULL)
```

Arguments

<code>y</code>	The outcome variable (continuous).
<code>x1</code>	The assignment variable 1.
<code>x2</code>	The assignment variable 2.
<code>c1</code>	The cutoff of assignment variable 1.
<code>c2</code>	The cutoff of assignment variable 2.
<code>tr</code>	The treatment variable used to compare with the derived treatment based on assignments and cutoffs.
<code>t.design</code>	The treatment option according to design. The 1st entry is for <code>x1</code> : "g" means treatment is assigned if <code>x1</code> is greater than its cutoff, "geq" means treatment is assigned if <code>x1</code> is greater than or equal to its cutoff, "l" means treatment is assigned if <code>x1</code> is less than its cutoff, "leq" means treatment is assigned if <code>x1</code> is less than or equal to its cutoff. The 2nd entry is for <code>x2</code> .
<code>local</code>	The range of neighboring points around the cutoff on the standardized The scale on each assignment variable, which is a positive number.
<code>ngrid</code>	The number of non-zero grid points on each assignment variable, which is also the number of zero grid points on each assignment variable.
<code>margin</code>	The range of grid points beyond the minimum and maximum of sample points on each assignment variable.
<code>boot</code>	The number of bootstrap samples to obtain standard deviation of estimates.
<code>cluster</code>	An optional vector specifying clusters within which the errors are assumed to be correlated. This will result in reporting cluster robust SEs. This option overrides anything specified in <code>se.type</code> . It is suggested that data with a discrete running variable be clustered by each unique value of the running variable (Lee and Card, 2008).

Value

`mfrd_est` returns an object of class "mfrd".

Examples

```
set.seed(12345)
x1 <- runif(1000, -1, 1)
x2 <- runif(1000, -1, 1)
cov <- rnorm(1000)
y <- 3 + 2 * x1 + 3 * cov + 10 * (x2 >= 0) + rnorm(1000)
mfrd_est(y = y, x1 = x1, x2 = x2, c1 = 0, c2 = 0)
```

Description

`mrd_est` estimates treatment effects in an MRDD with two assignment variables, including the frontier average treatment effect (`tau_MRD`) and frontier-specific effects (`tau_R` and `tau_M`) simultaneously.

Usage

```
mrd_est(formula, data, subset = NULL, cutpoint = NULL, bw = NULL,
        kernel = "triangular", se.type = "HC1", cluster = NULL,
        verbose = FALSE, less = FALSE, est.cov = FALSE, est.itd = FALSE,
        local = 0.15, ngrid = 2500, margin = 0.03, boot = NULL,
        method = c("center", "univ", "front"), t.design = c("1", "1"))
```

Arguments

formula	The formula of the MRDD. This is supplied in the format of $y \sim x_1 + x_2$ for a simple sharp MRDD, or $y \sim x_1 + x_2 \mid c_1 + c_2$ for a sharp MRDD with two covariates. Fuzzy MRDD may be specified as $y \sim x_1 + x_2 + z$ where x is the running variable, and z is the endogenous treatment variable. Covariates are then included in the same manner as in a sharp MRDD.
data	An optional data frame.
subset	An optional vector specifying a subset of observations to be used.
cutpoint	The cutpoint. If omitted, it is assumed to be $c(0, 0)$.
bw	A numeric vector specifying the bandwidths at which to estimate the RD. If omitted or it is "IK12", the bandwidth is calculated using the Imbens-Kalyanaraman 2012 method. If it is "IK09", the bandwidth is calculated using the Imbens-Kalyanaraman 2009 method. Then it is estimated with that bandwidth, half that bandwidth, and twice that bandwidth. If only a single value is passed into the function, the RD will similarly be estimated at that bandwidth, half that bandwidth, and twice that bandwidth.
kernel	A string specifying the kernel to be used in the local linear fitting. "triangular" kernel is the default and is the "correct" theoretical kernel to be used for edge estimation as in RDD (Lee and Lemieux, 2010). Other options are "rectangular", "epanechnikov", "quartic", "triweight", "tricube", "gaussian" and "cosine".
se.type	This specifies the robust SE calculation method to use. Options are, as in vcovHC , "HC3", "const", "HC", "HC0", "HC1", "HC2", "HC4", "HC4m", "HC5". This option is overridden by cluster.
cluster	An optional vector specifying clusters within which the errors are assumed to be correlated. This will result in reporting cluster robust SEs. This option overrides anything specified in se.type. It is suggested that data with a discrete running variable be clustered by each unique value of the running variable (Lee and Card, 2008).
verbose	Will provide some additional information printed to the terminal.
less	Logical. If TRUE, return the estimates of linear and optimal, instead of linear, quadratic, cubic, optimal, half and double.
est.cov	Logical. If TRUE, the estimates of covariates will be included.
est.itd	Logical. If TRUE, the estimates of ITT will be returned.
local	The range of neighboring points around the cutoff on the standardized scale on each assignment variable, which is a positive number.
ngrid	The number of non-zero grid points on each assignment variable, which is also the number of zero grid points on each assignment variable.
margin	The range of grid points beyond the minimum and maximum of sample points on each assignment variable.

boot	The number of bootstrap samples to obtain standard deviation of estimates.
method	The method to estimate rd effect. Options are "center", "univ", "front".
t.design	The treatment option according to design. The 1st entry is for X1: "g" means treatment is assigned if X1 is greater than its cutoff, "geq" means treatment is assigned if X1 is greater than or equal to its cutoff, "l" means treatment is assigned if X1 is less than its cutoff, "leq" means treatment is assigned if X1 is less than or equal to its cutoff. The 2nd entry is for X2.

Value

mrd_est returns an object of class "mrd".

References

Wong, V. C., Steiner, P. M., Cook, T. D. (2013). Analyzing regression-discontinuity designs with multiple assignment variables: A comparative study of four estimation methods. *Journal of Educational and Behavioral Statistics*, 38(2), 107-141. <http://journals.sagepub.com/doi/10.3102/1076998611432172>.

Examples

```
x1 <- runif(1000, -1, 1)
x2 <- runif(1000, -1, 1)
cov <- rnorm(1000)
y <- 3 + 2 * x1 + 3 * cov + 10 * (x2 >= 0) + rnorm(1000)
# centering
mrd_est(y ~ x1 + x2 | cov, method = "center")
# univariate
mrd_est(y ~ x1 + x2 | cov, method = "univ")
# frontier
mrd_est(y ~ x1 + x2 | cov, method = "front")
```

mrd_impute	<i>Multiple Imputation of Multivariate Regression Discontinuity Estimation</i>
------------	--

Description

mrd_impute estimates treatment effects in an MRDD with imputed missing values.

Usage

```
mrd_impute(formula, data, subset = NULL, cutpoint = NULL, bw = NULL,
  kernel = "triangular", se.type = "HC1", cluster = NULL, impute = NULL,
  verbose = FALSE, less = FALSE, est.cov = FALSE, est.itd = FALSE,
  local = 0.15, ngrid = 2500, margin = 0.03, boot = NULL,
  method = c("center", "univ", "front"), t.design = c("l", "l"))
```

Arguments

formula	The formula of the MRDD. This is supplied in the format of $y \sim x_1 + x_2$ for a simple sharp MRDD, or $y \sim x_1 + x_2 \mid c_1 + c_2$ for a sharp MRDD with two covariates. Fuzzy MRDD may be specified as $y \sim x_1 + x_2 + z$ where x is the running variable, and z is the endogenous treatment variable. Covariates are then included in the same manner as in a sharp MRDD.
data	An optional data frame.
subset	An optional vector specifying a subset of observations to be used.
cutpoint	The cutpoint. If omitted, it is assumed to be 0.
bw	A numeric vector specifying the bandwidths at which to estimate the RD. If omitted or it is "IK12", the bandwidth is calculated using the Imbens-Kalyanaraman 2012 method. If it is "IK09", the bandwidth is calculated using the Imbens-Kalyanaraman 2009 method. Then it is estimated with that bandwidth, half that bandwidth, and twice that bandwidth. If only a single value is passed into the function, the RD will similarly be estimated at that bandwidth, half that bandwidth, and twice that bandwidth.
kernel	A string specifying the kernel to be used in the local linear fitting. "triangular" kernel is the default and is the "correct" theoretical kernel to be used for edge estimation as in RDD (Lee and Lemieux, 2010). Other options are "rectangular", "epanechnikov", "quartic", "triweight", "tricube", "gaussian" and "cosine".
se.type	This specifies the robust SE calculation method to use. Options are, as in <code>vcovHC</code> , "HC3", "const", "HC", "HC0", "HC1", "HC2", "HC4", "HC4m", "HC5". This option is overridden by <code>cluster</code> .
cluster	An optional vector specifying clusters within which the errors are assumed to be correlated. This will result in reporting cluster robust SEs. This option overrides anything specified in <code>se.type</code> . It is suggested that data with a discrete running variable be clustered by each unique value of the running variable (Lee and Card, 2008).
impute	An optional vector specifying the imputed variables with missing values.
verbose	Will provide some additional information printed to the terminal.
less	Logical. If TRUE, return the estimates of linear and optimal, instead of linear, quadratic, cubic, optimal, half and double.
est.cov	Logical. If TRUE, the estimates of covariates will be included.
est.itd	Logical. If TRUE, the estimates of ITT will be returned.
local	The range of neighboring points around the cutoff on the standardized scale on each assignment variable, which is a positive number.
ngrid	The number of non-zero grid points on each assignment variable, which is also the number of zero grid points on each assignment variable.
margin	The range of grid points beyond the minimum and maximum of sample points on each assignment variable.
boot	The number of bootstrap samples to obtain standard deviation of estimates.
method	The method to estimate rd effect. Options are "center", "univ", "front".
t.design	The treatment option according to design. The 1st entry is for X1: "g" means treatment is assigned if X1 is greater than its cutoff, "geq" means treatment is assigned if X1 is greater than or equal to its cutoff, "l" means treatment is assigned if X1 is less than its cutoff, "leq" means treatment is assigned if X1 is less than or equal to its cutoff. The 2nd entry is for X2.

Value

rd_impute returns an object of class "mrd".

References

Stata: 64 mi estimate - Estimation using multiple imputations

Examples

```
x1 <- runif(1000, -1, 1)
x2 <- runif(1000, -1, 1)
cov <- rnorm(1000)
y <- 3 + 2 * x1 + 3 * cov + 10 * (x2 >= 0) + rnorm(1000)
group <- rep(1:10, each = 100)
# centering
mrd_impute(y ~ x1 + x2 | cov, impute = group, method = "center")
# univariate
mrd_impute(y ~ x1 + x2 | cov, impute = group, method = "univ")
# frontier
mrd_impute(y ~ x1 + x2 | cov, impute = group, method = "front")
```

mrd_power

Power Analysis of Multivariate Regression Discontinuity

Description

mrd_power computes the empirical probability that RD is significant, i.e. the empirical alpha of null hypothesis: $RD = 0$

Usage

```
mrd_power(num.rep = 100, sample.size = 100, x1.dist = "normal",
  x1.param = c(0, 1), x2.dist = "normal", x2.param = c(0, 1), x1.cut = 0,
  x2.cut = 0, x1.fuzzy = c(0, 0), x2.fuzzy = c(0, 0), x1.design = "1",
  x2.design = "1", coeff = c(0.1, 0.5, 0.5, 1, rep(0.1, 9)), eta.sq = 0.5,
  alpha.list = c(0.001, 0.01, 0.05))
```

Arguments

num.rep	Number of repetitions used to calculate the empirical alpha.
sample.size	Number of observations in each sample.
x1.dist	Distribution of the 1st assignment variable X1. "normal" distribution is the default. "uniform" distribution is the only other option.
x1.param	Parameters of the distribution of the 1st assignment variable X1. If x1.dist is "normal", then x1.param includes the mean and sd of normal distribution. If x1.dist is "uniform", then x1.param includes the upper and lower boundaries of uniform distribution.
x2.dist	Distribution of the 2nd assignment variable X2.
x2.param	Parameters of the distribution of the 2nd assignment variable X2.
x1.cut	Cutpoint of RD with respect to the 1st assignment variable X1.

<code>x2.cut</code>	Cutpoint of RD with respect to the 2nd assignment variable X2.
<code>x1.fuzzy</code>	Probabilities to be assigned to control in terms of the 1st assignment variable X1 for individuals in treatment based on cutoff, and to treatment for individuals in control based on cutoff. For a sharp design, by default, the 1st entry is 0, and the 2nd entry is 0. For a fuzzy design, the 1st entry is the probability to be assigned to control for individuals above the cutpoint, and the 2nd entry is the probability to be assigned to treatment for individuals below the cutpoint.
<code>x2.fuzzy</code>	Probabilities to be assigned to control in terms of the 2nd assignment variable X2 for individuals in treatment based on cutoff, and to treatment for individuals in control based on cutoff.
<code>x1.design</code>	The treatment option according to design. The entry is for X1: "g" means treatment is assigned if X1 is greater than its cutoff, " \geq " means treatment is assigned if X1 is greater than or equal to its cutoff, "l" means treatment is assigned if X1 is less than its cutoff, " \leq " means treatment is assigned if X1 is less than or equal to its cutoff.
<code>x2.design</code>	The treatment option according to design. The entry is for X2.
<code>coeff</code>	Coefficients of variables in the linear model to generate data The 1st entry is the intercept. The 2nd entry is the slope of treatment 1, i.e. treatment effect 1. The 3rd entry is the slope of treatment 2, i.e. treatment effect 2. The 4th entry is the slope of treatment, i.e. treatment effect. The 5th entry is the slope of assignment 1. The 6th entry is the slope of assignment 2. The 7th entry is the slope of interaction between assignment 1 and assignment 2. The 8th entry is the slope of interaction between treatment 1 and assignment 1. The 9th entry is the slope of interaction between treatment 2 and assignment 1. The 10th entry is the slope of interaction between treatment 1 and assignment 2. The 11th entry is the slope of interaction between treatment 2 and assignment 2. The 12th entry is the slope of interaction between treatment 1, assignment 1 and assignment 2. The 13th entry is the slope of interaction between treatment 2, assignment 1 and assignment 2.
<code>eta.sq</code>	Expected partial eta-squared of the linear model with respect to the treatment itself. It is used to control the variance of noise in the linear model.
<code>alpha.list</code>	List of significance levels used to calculate the empirical alpha.

Value

`mrd_power` returns the results of 6 estimators as a table, including mean, variance, and power of estimate. The 1st `Linear` results of the linear regression estimator of combined RD using the centering approach. The 2nd `Opt` results of the local linear regression estimator of combined RD using the centering approach, with the optimal bandwidth in the IK 2012 paper. The 3rd `Linear` results of the linear regression estimator of separate RD in terms of `x1` using the univariate approach. The 4th `Opt` results of the local linear regression estimator of separate RD in terms of `x1` using the univariate approach, with the optimal bandwidth in the IK 2012 paper. The 5th `Linear` results of the linear regression estimator of separate RD in terms of `x2` using the univariate approach. The 6th `Opt` results of the local linear regression estimator of separate RD in terms of `x2` using the univariate approach, with the optimal bandwidth in the IK 2012 paper.

Examples

```
## Not run:
mrd_power()
mrd_power(x1.dist = "uniform", x1.cut = 0.5)
```

```
mrd_power(x1.fuzzy = c(0.1, 0.1))

## End(Not run)
```

mrd_sens_bw	<i>Bandwidth Sensitivity Simulation for Multivariate Regression Discontinuity</i>
-------------	---

Description

mrd_sens_bw refits the supplemented model with varying bandwidth. Other estimation parameters are held constant.

Usage

```
mrd_sens_bw(object, approach = c("center", "univ1", "univ2"), bws)
```

Arguments

object	An object returned by mrd_est or mrd_impute.
approach	A string of the approaches to be refitted, choosing from c("center", "univ1", "univ2").
bws	A positive numeric vector of bandwidth for refitting an mrd object.

Value

A dataframe which contains the estimate `est` and standard error `se` for each supplemented bandwidth.

Examples

```
x1 <- runif(1000, -1, 1)
x2 <- rnorm(1000, 10, 2)
cov <- rnorm(1000)
y <- 3 + 2 * x1 + 1 * x2 + 3 * cov + 10 * (x1 >= 0) + 5 * (x2 >= 10) + rnorm(1000)
mrd <- mrd_est(y ~ x1 + x2 | cov, cutpoint = c(0, 10))
mrd_sens_bw(mrd, approach = "univ1", bws = seq(0.1, 1, length.out = 5))
```

mrd_sens_cutoff	<i>Cutoff Sensitivity Simulation for Multivariate Regression Discontinuity</i>
-----------------	--

Description

mrd_sens_cutoff refits the supplemented model with varying cutoff(s). Other estimation parameters, such as the automatically calculated bandwidth, are held constant.

Usage

```
mrd_sens_cutoff(object, cutoffs)
```

Arguments

object	An object returned by <code>mrd_est</code> or <code>mrd_impute</code> .
cutoffs	A two-column numeric matrix of paired cutoff values to be used for refitting an <code>mrd</code> object.

Value

A dataframe which contains the estimate `est` and standard error `se` for each pairs of cutoffs (A1 and A2). A1 contains varying cutoffs on assignment 1, and A2 assignment 2.

Examples

```
x1 <- runif(1000, -1, 1)
x2 <- rnorm(1000, 10, 2)
cov <- rnorm(1000)
y <- 3 + 2 * x1 + 1 * x2 + 3 * cov + 10 * (x1 >= 0) + 5 * (x2 >= 10) + rnorm(1000)
mrd <- mrd_est(y ~ x1 + x2 | cov, cutpoint = c(0, 10))
mrd_sens_cutoff(mrd, expand.grid(A1 = seq(-.5, .5, length.out = 5), A2 = 10))
```

plot.mfrd

*Plot the Multivariate Frontier Regression Discontinuity***Description**

`plot.mfrd` plots the 3D illustration of the bivariate frontier RDD.

Usage

```
## S3 method for class 'mfrd'
plot(x, model = c("m_s", "m_h", "m_t"), gran = 2,
     raw_data = TRUE, color_surface = FALSE, ...)
```

Arguments

x	An <code>mfrd</code> object returned by <code>mfrd_est</code> or contained in the object returned by <code>mrd_est</code> .
model	Option for the model specification, one of <code>c("m_s", "m_h", "m_t")</code> .
gran	Granularity of the surface grid.
raw_data	Whether the raw data points are plotted.
color_surface	Whether the treated surface is colored.
...	Additional graphic arguments passed to <code>persp</code> .

Examples

```
set.seed(12345)
x1 <- runif(1000, -1, 1)
x2 <- runif(1000, -1, 1)
cov <- rnorm(1000)
y <- 3 + 2 * x1 + 3 * cov + 10 * (x2 >= 0) + rnorm(1000)
model <- mfrd_est(y = y, x1 = x1, x2 = x2, c1 = 0, c2 = 0)
plot(model, "m_s")
```

plot.rd	<i>Plot the Regression Discontinuity</i> plot.rd plots the relationship between the running variable and the outcome. It is based on the plot.RD function in the rdd package.
---------	--

Description

Plot the Regression Discontinuity

plot.rd plots the relationship between the running variable and the outcome. It is based on the [plot.RD](#) function in the **rdd** package.

Usage

```
## S3 method for class 'rd'
plot(x, preds = NULL, fit_line = c("linear", "quadratic",
  "cubic", "optimal", "half", "double"), fit_ci = c("area", "dot", "hide"),
  fit_ci_level = 0.95, bin_n = 20, bin_level = 0.95,
  bin_size = c("shade", "size"), quant_bin = TRUE, xlim = NULL,
  ylim = NULL, include_rugs = FALSE, ...)
```

Arguments

x	An rd object, typically the result of rd_est .
preds	Predictions generated by predict.rd .
fit_line	Models to be shown as fitted lines.
fit_ci	Whether and how to plot prediction CIs around the fitted lines.
fit_ci_level	Confidence level of prediction CIs.
bin_n	Number of bins for binned data points (plot raw data points if = 0; suppress data points if < 0).
bin_level	Confidence level for CIs around binned data points.
bin_size	How to plot the number of observations in each bin.
quant_bin	Whether the data are binned per quantiles.
xlim	x-axis limits.
ylim	y-axis limits.
include_rugs	Whether to include 1d plot fo data for both axes.
...	Additional arguments affecting the plots produced.

Examples

```
dat <- data.frame(x = runif(1000, -1, 1), cov = rnorm(1000))
dat$tr <- as.integer(dat$x >= 0)
dat$y <- 3 + 2 * dat$x + 3 * dat$cov + 10 * (dat$x >= 0) + rnorm(1000)
rd <- rd_est(y ~ x + tr | cov, data = dat, cutpoint = 0)
plot(rd)
```


predict.rd

*Prediction the Regression Discontinuity***Description**

`predict.rd` makes predictions of mean and standard deviation of RDs at different cutoffs.

Usage

```
## S3 method for class 'rd'
predict(object, gran = 50, ...)
```

Arguments

<code>object</code>	An <code>rd</code> object, typically the result of <code>rd_est</code> .
<code>gran</code>	Granularity of the data points.
<code>...</code>	Additional arguments affecting the predictions produced.

Examples

```
x <- runif(1000, -1, 1)
cov <- rnorm(1000)
y <- 3 + 2 * x + 3 * cov + 10 * (x >= 0) + rnorm(1000)
tr <- as.integer(x >= 0)
rd <- rd_est(y ~ x + tr | cov, cutpoint = 0)
predict(rd)
```

print.mfrd

*Print the Multivariate Frontier Regression Discontinuity***Description**

`print.mfrd` prints a very basic summary of the multivariate frontier regression discontinuity. It is based on the `print.RD` function in the `rdd` package.

Usage

```
## S3 method for class 'mfrd'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

Arguments

<code>x</code>	An <code>mfrd</code> object, typically the result of <code>mfrd_est</code> .
<code>digits</code>	The number of digits to print.
<code>...</code>	Additional arguments.

<code>print.rd</code>	<i>Print the Regression Discontinuity</i>
-----------------------	---

Description

`print.rd` prints a very basic summary of the regression discontinuity. It is based on the `print.RD` function in the **rdd** package.

Usage

```
## S3 method for class 'rd'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

Arguments

<code>x</code>	An <code>rd</code> object, typically the result of <code>rd_est</code> .
<code>digits</code>	The number of digits to print.
<code>...</code>	Additional arguments.

<code>rd_est</code>	<i>Regression Discontinuity Estimation</i>
---------------------	--

Description

`rd_est` estimates both sharp and fuzzy RDD, using parametric and non-parametric (local linear) models. It is based on the `RDeestimate` function in the **rdd** package. Sharp RDDs (both parametric and non-parametric) are estimated using `lm` in the **stats** package. Fuzzy RDDs (both parametric and non-parametric) are estimated using two-stage least-squares `ivreg` in the **AER** package. For non-parametric models, Imbens-Kalyanaraman optimal bandwidths can be used,

Usage

```
rd_est(formula, data, subset = NULL, cutpoint = NULL, bw = NULL,
        kernel = "triangular", se.type = "HC1", cluster = NULL,
        verbose = FALSE, less = FALSE, est.cov = FALSE, est.itt = FALSE,
        t.design = "1")
```

Arguments

<code>formula</code>	The formula of the RDD. This is supplied in the format of $y \sim x$ for a simple sharp RDD, or $y \sim x \mid c1 + c2$ for a sharp RDD with two covariates. Fuzzy RDD may be specified as $y \sim x + z$ where x is the running variable, and z is the endogenous treatment variable. Covariates are then included in the same manner as in a sharp RDD.
<code>data</code>	An optional data frame.
<code>subset</code>	An optional vector specifying a subset of observations to be used
<code>cutpoint</code>	The cutpoint. If omitted, it is assumed to be 0.

bw	A numeric vector specifying the bandwidths at which to estimate the RD. If omitted or it is "IK12", the bandwidth is calculated using the Imbens-Kalyanaraman 2012 method. If it is "IK09", the bandwidth is calculated using the Imbens-Kalyanaraman 2009 method. Then it is estimated with that bandwidth, half that bandwidth, and twice that bandwidth. If only a single value is passed into the function, the RD will similarly be estimated at that bandwidth, half that bandwidth, and twice that bandwidth.
kernel	A string specifying the kernel to be used in the local linear fitting. "triangular" kernel is the default and is the "correct" theoretical kernel to be used for edge estimation as in RDD (Lee and Lemieux, 2010). Other options are "rectangular", "epanechnikov", "quartic", "triweight", "tricube", "gaussian" and "cosine".
se.type	This specifies the robust SE calculation method to use. Options are, as in <code>vcovHC</code> , "HC3", "const", "HC", "HC0", "HC1", "HC2", "HC4", "HC4m", "HC5". This option is overridden by <code>cluster</code> .
cluster	An optional vector specifying clusters within which the errors are assumed to be correlated. This will result in reporting cluster robust SEs. This option overrides anything specified in <code>se.type</code> . It is suggested that data with a discrete running variable be clustered by each unique value of the running variable (Lee and Card, 2008).
verbose	Will provide some additional information printed to the terminal.
less	Logical. If TRUE, return the estimates of linear and optimal, instead of linear, quadratic, cubic, optimal, half and double.
est.cov	Logical. If TRUE, the estimates of covariates will be included.
est.itd	Logical. If TRUE, the estimates of ITT will be returned.
t.design	The treatment option according to design. The entry is for X: "g" means treatment is assigned if X is greater than its cutoff, "geq" means treatment is assigned if X is greater than or equal to its cutoff, "l" means treatment is assigned if X is less than its cutoff, "leq" means treatment is assigned if X is less than or equal to its cutoff.

Value

`rd_est` returns an object of class "rd". The functions `summary` and `plot` are used to obtain and print a summary and plot of the estimated regression discontinuity. The object of class `rd` is a list containing the following components:

type	A string denoting either "sharp" or "fuzzy" RDD.
est	Numeric vector of the estimate of the discontinuity in the outcome under a sharp design, or the Wald estimator in the fuzzy design for each corresponding bandwidth.
se	Numeric vector of the standard error for each corresponding bandwidth.
z	Numeric vector of the z statistic for each corresponding bandwidth.
p	Numeric vector of the p value for each corresponding bandwidth.
ci	The matrix of the 95 for each corresponding bandwidth.
d	Numeric vector of the effective size (Cohen's d) for each estimate.
cov	The names of covariates.
bw	Numeric vector of each bandwidth used in estimation.

obs	Vector of the number of observations within the corresponding bandwidth.
call	The matched call.
na.action	The observations removed from fitting due to missingness.
impute	Whether multiple imputation is used or not.
model	For a sharp design, a list of the <code>lm</code> objects is returned. For a fuzzy design, a list of lists is returned, each with two elements: <code>firststage</code> , the first stage <code>lm</code> object, and <code>iv</code> , the <code>ivreg</code> object. A model is returned for each corresponding bandwidth.
frame	Returns the model frame used in fitting.

References

- Lee, D. S., Lemieux, T. (2010). Regression Discontinuity Designs in Economics. *Journal of Economic Literature*, 48(2), 281-355. <http://www.aeaweb.org/articles.php?doi=10.1257/jel.48.2.281>.
- Imbens, G., Lemieux, T. (2008). Regression discontinuity designs: A guide to practice. *Journal of Econometrics*, 142(2), 615-635. <http://dx.doi.org/10.1016/j.jeconom.2007.05.001>.
- Lee, D. S., Card, D. (2010). Regression discontinuity inference with specification error. *Journal of Econometrics*, 142(2), 655-674. <http://dx.doi.org/10.1016/j.jeconom.2007.05.003>.
- Angrist, J. D., Pischke, J.-S. (2009). *Mostly harmless econometrics: An empiricist's companion*. Princeton, NJ: Princeton University Press.

Examples

```
x <- runif(1000, -1, 1)
cov <- rnorm(1000)
y <- 3 + 2 * x + 3 * cov + 10 * (x >= 0) + rnorm(1000)
rd_est(y ~ x)
# Efficiency gains can be made by including covariates
rd_est(y ~ x | cov)
```

rd_impute

Multiple Imputation of Regression Discontinuity Estimation

Description

`rd_impute` estimates treatment effects in a RDD with imputed missing values.

Usage

```
rd_impute(formula, data, subset = NULL, cutpoint = NULL, bw = NULL,
  kernel = "triangular", se.type = "HC1", cluster = NULL, impute = NULL,
  verbose = FALSE, less = FALSE, est.cov = FALSE, est.itt = FALSE,
  t.design = "l")
```

Arguments

formula	The formula of the RDD. This is supplied in the format of $y \sim x$ for a simple sharp RDD, or $y \sim x \mid c1 + c2$ for a sharp RDD with two covariates. Fuzzy RDD may be specified as $y \sim x + z$ where x is the running variable, and z is the endogenous treatment variable. Covariates are then included in the same manner as in a sharp RDD.
data	An optional data frame.
subset	An optional vector specifying a subset of observations to be used
cutpoint	The cutpoint. If omitted, it is assumed to be 0.
bw	A numeric vector specifying the bandwidths at which to estimate the RD. If omitted or it is "IK12", the bandwidth is calculated using the Imbens-Kalyanaraman 2012 method. If it is "IK09", the bandwidth is calculated using the Imbens-Kalyanaraman 2009 method. Then it is estimated with that bandwidth, half that bandwidth, and twice that bandwidth. If only a single value is passed into the function, the RD will similarly be estimated at that bandwidth, half that bandwidth, and twice that bandwidth.
kernel	A string specifying the kernel to be used in the local linear fitting. "triangular" kernel is the default and is the "correct" theoretical kernel to be used for edge estimation as in RDD (Lee and Lemieux, 2010). Other options are "rectangular", "epanechnikov", "quartic", "triweight", "tricube", "gaussian" and "cosine".
se.type	This specifies the robust SE calculation method to use. Options are, as in vcovHC , "HC3", "const", "HC", "HC0", "HC1", "HC2", "HC4", "HC4m", "HC5". This option is overridden by cluster.
cluster	An optional vector specifying clusters within which the errors are assumed to be correlated. This will result in reporting cluster robust SEs. This option overrides anything specified in se.type. It is suggested that data with a discrete running variable be clustered by each unique value of the running variable (Lee and Card, 2008).
impute	An optional vector specifying the imputed variables with missing values.
verbose	Will provide some additional information printed to the terminal.
less	Logical. If TRUE, return the estimates of linear and optimal, instead of linear, quadratic, cubic, optimal, half and double.
est.cov	Logical. If TRUE, the estimates of covariates will be included.
est.itd	Logical. If TRUE, the estimates of ITT will be returned.
t.design	The treatment option according to design. The entry is for X: "g" means treatment is assigned if X is greater than its cutoff, "geq" means treatment is assigned if X is greater than or equal to its cutoff, "l" means treatment is assigned if X is less than its cutoff, "leq" means treatment is assigned if X is less than or equal to its cutoff.

Value

rd_impute returns an object of class "rd".

References

Stata: 64 mi estimate - Estimation using multiple imputations

Examples

```
x <- runif(1000, -1, 1)
cov <- rnorm(1000)
y <- 3 + 2 * x + 3 * cov + 10 * (x < 0) + rnorm(1000)
group <- rep(1:10, each = 100)
rd_impute(y ~ x, impute = group)
# Efficiency gains can be made by including covariates
rd_impute(y ~ x | cov, impute = group)
```

rd_power

Power Analysis of Regression Discontinuity

Description

rd_power computes the empirical probability that RD is significant, i.e. the empirical alpha of null hypothesis: $RD = 0$

Usage

```
rd_power(num.rep = 100, sample.size = 100, x.dist = "normal",
  x.param = c(0, 1), x.cut = 0, x.fuzzy = c(0, 0), x.design = "1",
  coeff = c(0.3, 1, 0.2, 0.3), eta.sq = 0.5, alpha.list = c(0.001, 0.01,
  0.05))
```

Arguments

num.rep	Number of repetitions used to calculate the empirical alpha.
sample.size	Number of observations in each sample.
x.dist	Distribution of the assignment variable X. "normal" distribution is the default. "uniform" distribution is the only other option.
x.param	Parameters of the distribution of the assignment variable X. If x.dist is "normal", then x.param includes the mean and sd of normal distribution. If x.dist is "uniform", then x.param includes the upper and lower boundaries of uniform distribution.
x.cut	Cutpoint of RD with respect to the assignment variable X.
x.fuzzy	Probabilities to be assigned to control for individuals in treatment based on cut-off, and to treatment for individuals in control based on cutoff. For a sharp design, by default, the 1st entry is 0, and the 2nd entry is 0. For a fuzzy design, the 1st entry is the probability to be assigned to control for individuals above the cutpoint, and the 2nd entry is the probability to be assigned to treatment for individuals below the cutpoint.
x.design	The treatment option according to design. The entry is for X: "g" means treatment is assigned if X is greater than its cutoff, "geq" means treatment is assigned if X is greater than or equal to its cutoff, "l" means treatment is assigned if X is less than its cutoff, "leq" means treatment is assigned if X is less than or equal to its cutoff.
coeff	Coefficients of variables in the linear model to generate data The 1st entry is the intercept. The 2nd entry is the slope of treatment, i.e. treatment effect. The 3rd entry is the slope of assignment. The 4th entry is the slope of interaction between treatment and assignment.

eta.sq	Expected partial eta-squared of the linear model with respect to the treatment itself. It is used to control the variance of noise in the linear model.
alpha.list	List of significance levels used to calculate the empirical alpha.

Value

rd_power returns the results of 2 estimators as a table, including mean, variance, and power of estimate. The 1st Linear results of the linear regression estimator The 2nd Opt results of the local linear regression estimator of RD, with the optimal bandwidth in the IK 2012 paper.

Examples

```
## Not run:
rd_power()
rd_power(x.dist = "uniform", x.cut = 0.5)
rd_power(x.fuzzy = c(0.1, 0.1))

## End(Not run)
```

rd_sens_bw

Bandwidth Sensitivity Simulation for Regression Discontinuity

Description

rd_sens_bw refits the supplemented model with varying bandwidth. Other estimation parameters are held constant.

Usage

```
rd_sens_bw(object, bws)
```

Arguments

object	An object returned by rd_est or rd_impute.
bws	A positive numeric vector of bandwidth for refitting an rd object.

Value

A dataframe which contains the estimate est and standard error se for each supplemented bandwidth.

Examples

```
x <- runif(1000, -1, 1)
cov <- rnorm(1000)
y <- 3 + 2 * x + 3 * cov + 10 * (x >= 0) + rnorm(1000)
rd <- rd_est(y ~ x | cov)
rd_sens_bw(rd, bws = seq(.1, 1, length.out = 5))
```

rd_sens_cutoff	<i>Cutoff Sensitivity Simulation for Regression Discontinuity</i>
----------------	---

Description

`rd_sens_cutoff` refits the supplemented model with varying cutoff(s). Other estimation parameters, such as the automatically calculated bandwidth, are held constant.

Usage

```
rd_sens_cutoff(object, cutoffs)
```

Arguments

<code>object</code>	An object returned by <code>rd_est</code> or <code>rd_impute</code> .
<code>cutoffs</code>	A numeric vector of cutoff values to be used in the refitting of an <code>rd</code> object.

Value

A dataframe contains the estimate `est` and standard error `se` for each cutoff values (A1). Column A1 contains varying cutoffs on the assignment variable.

Examples

```
x <- runif(1000, -1, 1)
cov <- rnorm(1000)
y <- 3 + 2 * x + 3 * cov + 10 * (x >= 0) + rnorm(1000)
rd <- rd_est(y ~ x | cov)
rd_sens_cutoff(rd, seq(-.5, .5, length.out = 10))
```

rd_type	<i>Determine Type of Regression Discontinuity Design</i>
---------	--

Description

`rd_type` cross-tabulates observations based on (1) a binary treatment and (2) one or two assignments and their cutoff values.

Usage

```
rd_type(data, treat, assign_1, cutoff_1, operator_1 = "g", assign_2 = NULL,
        cutoff_2 = NULL, operator_2 = NULL)
```


Arguments

<code>data</code>	A <code>data.frame</code> with each row representing an observation.
<code>treat</code>	The name of a numeric variable (treated = positive values).
<code>assign_1</code>	The variable name of the primary assignment.
<code>cutoff_1</code>	The cutoff value of the primary assignment.
<code>operator_1</code>	The operator for the primary assignment.
<code>assign_2</code>	The variable name of the secondary assignment.
<code>cutoff_2</code>	The cutoff value of the secondary assignment.
<code>operator_2</code>	The operator for the secondary assignment.

Value

A list of two elements:

<code>crosstab</code>	The cross-table as a <code>data.frame</code> .
<code>type</code>	The type of design as a string.

<code>sens_plot</code>	<i>Plot the Simulated Estimates for Sensitivity Analyses</i>
------------------------	--

Description

`sens_plot` plots the sensitivity analysis for cutpoint or bandwidth.

Usage

```
sens_plot(sim_results, level = 0.95, x = c("A1", "A2", "bw"),
  plot_models = unique(sim_results$model), yrange = NULL)
```

Arguments

<code>sim_results</code>	A <code>data.frame</code> returned by <code>rd_sens_cutoff</code> , <code>rd_sens_bw</code> , <code>mrd_sens_cutoff</code> , or <code>mrd_sens_bw</code> .
<code>level</code>	The confidence level for CIs (assuming a normal sampling distribution).
<code>x</code>	A string of the column name of the varying parameter in <code>sim_results</code> . This will be used as the x-axis in the plot. Possible values are <code>c("A1", "A2", "bw")</code> , which are column names in <code>sim_results</code> . A1 means the varying cutoffs are for assignment 1, and A2 assignment 2.
<code>plot_models</code>	A character vector specifying the models (i.e., models estimated with different approaches) to be plotted. Possible values are <code>unique(sim_results\$model)</code> .
<code>yrange</code>	A numeric vector of the range of y-axis

Examples

```
x <- runif(1000, -1, 1)
cov <- rnorm(1000)
y <- 3 + 2 * x + 3 * cov + 10 * (x >= 0) + rnorm(1000)
m <- rd_est(y ~ x | cov)
sim_cutoff <- rd_sens_cutoff(m, seq(-.5, .5, length.out = 10))
sens_plot(sim_cutoff, x = "A1", plot_models = c("linear", "optimal"))
sim_bw <- rd_sens_bw(m, seq(.1, 1, length.out = 10))
sens_plot(sim_bw, x = "bw")
```

summary.rd

Summarize the Regression Discontinuity

Description

summary.rd is a summary method for class "rd". It is based on [summary.RD](#) function in the **rdd** package.

Usage

```
## S3 method for class 'rd'
summary(object, digits = max(3, getOption("digits") - 3), ...)
```

Arguments

object	An object of class "rd", usually a result of a call to rd_est .
digits	Number of digits to display.
...	Additional arguments.

Value

summary.rd returns a list which has the following components:

coefficients	A matrix containing bandwidths, number of observations, estimates, SEs, z-values and p-values for each estimated bandwidth.
--------------	---

treat_assign

Treatment Assignment for Regression Discontinuity

Description

treat_assign computes the treatment variable T based on the cutoff of assignment variables X.

Usage

```
treat_assign(x, cut = 0, t.design = "1")
```

Arguments

x	The vector of assignment variable X.
cut	The cutoff of assignment variables X.
t.design	The treatment option according to design. The entry is for X: "g" means treatment is assigned if X is greater than its cutoff, "geq" means treatment is assigned if X is greater than or equal to its cutoff, "l" means treatment is assigned if X is less than its cutoff, "leq" means treatment is assigned if X is less than or equal to its cutoff.

Value

treat_assign returns the treatment variable as a vector according to the design, where 1 means the treated group, and 0 means the control group.

var_center	<i>Assignment Centering for Multivariate Frontier Regression Discontinuity</i>
------------	--

Description

var_center computes the univariate assignment variable X based on the cutoffs of

Usage

```
var_center(x, cut = c(0, 0), t.design = c("l", "l"), t.plot = FALSE)
```

Arguments

x	Data frame or matrix of two assignment variables, where the 1st column is X1, the 2nd column is X2
cut	Cutoffs of two assignment variables X1, X2.
t.design	The treatment option according to design. The 1st entry is for x1: "g" means treatment is assigned if x1 is greater than its cutoff, "geq" means treatment is assigned if x1 is greater than or equal to its cutoff, "l" means treatment is assigned if x1 is less than its cutoff, "leq" means treatment is assigned if x1 is less than or equal to its cutoff. The 2nd entry is for x2.
t.plot	Whether calculate the univariate treatment variable T and make a plot

Value

var_center returns the univariate assignment variable as a vector according to the design.

`wt_kern`*Kernel Weight Calculation*

Description

`wt_kern` calculates the appropriate kernel weights for a vector. This is useful when, for instance, one wishes to perform local regression. It is based on the `kernelwts` function in the **rdd** package.

Usage

```
wt_kern(X, center, bw, kernel = "triangular")
```

Arguments

<code>X</code>	The input x values. This variable represents the axis along which kernel weighting should be performed.
<code>center</code>	The point from which distances should be calculated.
<code>bw</code>	The bandwidth.
<code>kernel</code>	A string indicating the kernel to use. Options are "triangular" (the default), "epanechnikov", "quartic", "triweight", "tricube", "gaussian", and "cosine".

Value

A vector of weights with length equal to that of the `X` input (one weight per element of `X`).

Index

*Topic **datasets**

CARE, [5](#)

`attr_check`, [3](#)

`bw_ik09`, [4](#)

`bw_ik12`, [5](#)

CARE, [5](#)

`class`, [8](#), [10](#), [12](#), [19](#), [21](#)

`dc_test`, [6](#)

`DCdensity`, [6](#)

`IKbandwidth`, [4](#)

`kernelwts`, [28](#)

`mfrd_est`, [7](#), [17](#)

`mrd_est`, [8](#)

`mrd_impute`, [10](#)

`mrd_power`, [12](#)

`mrd_sens_bw`, [14](#)

`mrd_sens_cutoff`, [14](#)

`plot.mfrd`, [15](#)

`plot.RD`, [16](#)

`plot.rd`, [16](#)

`predict.rd`, [16](#), [17](#)

`print.mfrd`, [17](#)

`print.RD`, [17](#), [18](#)

`print.rd`, [18](#)

`rd_est`, [16](#), [17](#), [18](#), [18](#), [26](#)

`rd_impute`, [20](#)

`rd_power`, [22](#)

`rd_sens_bw`, [23](#)

`rd_sens_cutoff`, [24](#)

`rd_type`, [24](#)

`rdd_bw_ik`, [5](#)

`rddapp` (*rddapp-package*), [3](#)

rddapp-package, [3](#)

`RDestimate`, [18](#)

`sens_plot`, [25](#)

`summary.RD`, [26](#)

`summary.rd`, [26](#)

`treat_assign`, [26](#)

`var_center`, [27](#)

`vcovHC`, [9](#), [11](#), [19](#), [21](#)

`wt_kern`, [28](#)