

There's a particular function on lists that I'm a little obsessed with:

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conv : {A B : Set} → List A → List B → List (List (A × B))
conv _ [] = []
conv {A} {B} xs (yh :: ys) = foldr f [] xs
  where
    g : A
      → B
      → (List (List (A × B)) → List (List (A × B)))
      → List (List (A × B))
      → List (List (A × B))
    g x y a (z :: zs) = ((x , y) :: z) :: a zs
    g x y a [] = [(x , y)] :: a []
    f : A → List (List (A × B)) → List (List (A × B))
    f x zs = [ x , yh ] :: foldr (g x) id ys zs

```

It's an implementation of discrete convolution on lists. Previously I discussed it in relation to search patterns: it corresponds (somewhat) to breadth-first search (rather than depth-first).

Here though, I want to talk about its more traditional interpretation: the multiplication of two polynomials. Indeed, if you write out your polynomial backwards:

$$\begin{array}{ccccccc} & 2x^2 & +x & - & 4 & & (1) \end{array}$$

$$= \begin{array}{ccccccc} 2x^2 & +1x^1 & +- & 4x^0 \end{array} \{\text{With explicit powers of } x\} \quad (2)$$

$$= \begin{array}{ccccccc} -4x^0 & +1x^1 & + & 2x^2 \end{array} \{\text{Reversed}\} \quad (3)$$

[?]

References

- [1] E. Rivas, M. Jaskelioff, and T. Schrijvers, “From monoids to near-semirings: The essence of MonadPlus and Alternative,” in *Proceedings of the 17th International Symposium on Principles and Practice of Declarative Programming*. ACM, 2015, pp. 196–207, https://www.reddit.com/r/haskell/comments/3dlz6b/from_monoids_to_nearsemirings_the_essence_of/ [Online]. Available: <http://www.fceia.unr.edu.ar/~mauro/pubs/FromMonoidstoNearsemirings.pdf>