

Exercise 3

Data Preprocessing

Data Discretization

Discretizing continuous attributes in a dataset can be useful for handling outliers and smoothing the data. Discretization involves dividing the N possible values (typically $N > 9$) of an attribute into a finite number of categories.

Method 1: Discretization into Equal-Frequency Intervals (Quantiles, Equal-Frequency)

- This method divides the N possible values into Q quantiles (where Q is defined).
- The position of the i-th quantile is calculated as: $\text{Position} = N * i / Q$.
- All values that fall within the interval $[\text{Quantile } Q_i, \text{Quantile } Q_{i+1})$ are represented by the same category, where $0 \leq i < Q$.

Method 2: Discretization into Equal-Width Intervals

- Define or calculate the number of intervals, k, to use.
- The width of each interval is equal to: $(\text{MaxValue} - \text{MinValue}) / k$.
- All values falling within the same interval are represented by the same category.

Data Normalization

Data normalization is the process of adjusting the N possible values of each attribute to use a common scale.

Method 1: Min-Max Normalization

The formula for Min-Max normalization is:

$$\text{Value}_{(i, \text{new})} = \frac{\text{Value}_{(i, \text{old})} - \text{Value}_{(\text{min}, \text{old})}}{\text{Value}_{(\text{max}, \text{old})} - \text{Value}_{(\text{min}, \text{old})}} (\text{Value}_{(\text{max}, \text{new})} - \text{Value}_{(\text{min}, \text{new})}) + \text{Value}_{(\text{min}, \text{new})}$$

Method 2: Z-Score Normalization

The formula for Z-score normalization is:

$$\text{Value}_{(i, \text{new})} = \frac{\text{Value}_{(i, \text{old})} - \text{Value}_{(\text{mean}, \text{old})}}{S} \quad \text{with } S = \frac{1}{N} \sum_{i=1}^N |\text{Value}_{(i, \text{old})} - \text{Value}_{(\text{mean}, \text{old})}|$$

Questions :

- 1- Write a function to discretize the values of the "DatasetExos.csv" using Method 2 (Equal-width intervals). Use Huntsberger's formula to calculate the number of intervals $K = 1 + (10/3) * \log_{10}(n)$.
- 2- Replace the discretized values with the average of the corresponding interval.
- 3- Write a function to normalize the values of the "DatasetExos.csv" using Method 1. Use $\text{Value}_{\text{min}, \text{new}} = 0$ and $\text{Value}_{\text{max}, \text{new}} = 1$.

Dataset: DatasetExos.csv is available on this [link](#).