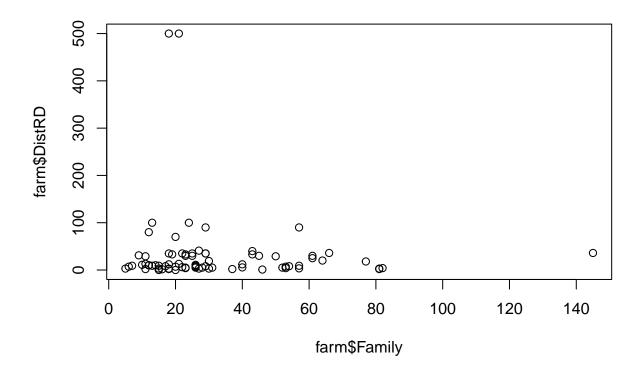
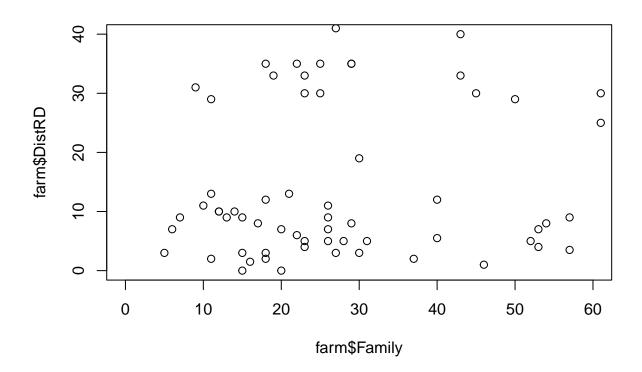
```
## Warning: package 'dplyr' was built under R version 4.1.2
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
##
cancer <- read.table("cancer.txt", header = TRUE, sep = "\t")</pre>
dev <- apply(cancer[, -1], 2, sd)</pre>
dev
## All.cancers
                                  Colon
                                           Melanoma
                                                       F.breast
                                                                    Pancreas
                      Lung
##
     47.857634
                 14.724588
                               7.262243
                                           5.245611
                                                        7.888396
                                                                    1.482258
##
      Leukemia
                   Ovarian
                                 Cervix
                                           Prostate
                                                           Liver
##
      2.255171
                  1.358915
                               1.421959
                                          16.858436
                                                        2.241009
#Unscaled Data
data <- cancer[,-1]</pre>
data <- data %>% mutate all(as.numeric)
c <- cov(data)</pre>
eig <- eigen(c)
evalue <- eig$values
evector <- eig$vectors</pre>
evector[,1:2]
##
                [,1]
                              [,2]
## [1,] 0.948911183 0.048606436
## [2,] 0.173707714 0.668729611
## [3,] 0.098867058 0.127018189
## [4,] 0.029715889 -0.112583098
## [5,] 0.077227953 -0.127033747
## [6,] 0.015969632 0.005649558
## [7,] 0.019995381 -0.039163522
## [8,] 0.004948948 -0.004370774
## [9,] 0.014052752 0.035246938
## [10,] 0.227792155 -0.708933677
## [11,] 0.002286687 0.008824253
```

library(dplyr)

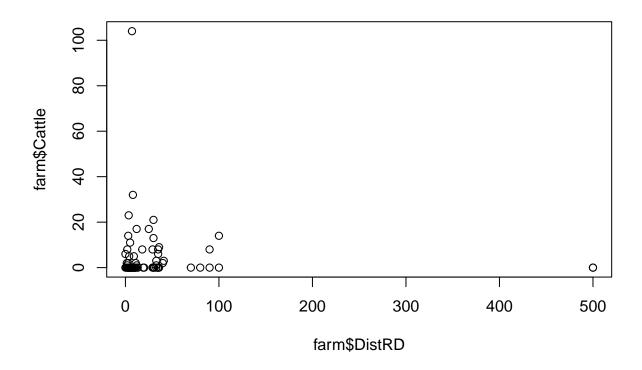
```
#Scaled Data
normal <- scale(data)
c <- cor(normal)</pre>
eig <- eigen(c)
evalue <- eig$values
evector <- eig$vectors</pre>
evector
                      [,2]
                               [,3]
                                         [, 4]
                                                   [,5]
                                                            [,6]
##
            [,1]
  [1,] -0.5010584 -0.03752827 0.13564906 0.10200653 0.00661866 0.10905402
##
  [4,] -0.1316843 -0.41857218 -0.05859752 0.60913595 0.15614063 -0.38162735
## [5,] -0.2764510 -0.37218720 -0.27254464 -0.03686353 0.14210375 0.57513296
## [6,] -0.3555025 0.02591798 -0.38107453 0.09964642 0.07993039 -0.45035470
  [7,] -0.2406797 -0.28184171 0.30247121 -0.48821395 -0.28970563 -0.27410672
  [8,] -0.1834695 -0.18665306 -0.48476086 -0.49457994 0.29556288 -0.06044586
  [9,] -0.3183348  0.43674873 -0.03254542  0.07805234 -0.10765380 -0.18024636
## [10,] -0.3061206 -0.30469450 0.22752557 0.19475514 -0.44400656 0.24994785
[,10]
##
             [,7]
                       [,8]
                                 [,9]
  [1,] 0.04374209 0.006792296 -0.11185970 -0.18508041 0.811210603
[3,] 0.37193300 0.131962267 0.70550259 -0.07120336 -0.162640106
## [4,] -0.30791519 0.098058275 0.31623819 -0.21670726 -0.107522730
## [5,] -0.04175042 0.414550768 0.10494771 0.40179558 -0.111317074
## [6,] 0.50502008 0.098916420 -0.43699136 0.16737802 -0.157430047
## [8,] -0.19263901 -0.503971154 0.13826954 -0.22490690 0.009368924
## [9,] -0.54255118 -0.168849994 0.04772674 0.57564539 0.012902563
## [10,] 0.15577866 -0.581436598 -0.09082973 0.03419142 -0.303946738
#Standardize all RV - Use correlation matrix (Cov of a standardized RV)
#Comparing the unscaled loadings to the standard deviations, we can observe that for most variables, th
farm <- read.csv("farmers.csv")</pre>
head(farm)
    Family DistRD Cotton Maize Sorg Millet Bull Cattle Goats
##
## 1
       12
            80
                               0.25
                                      2
                 1.5
                      1.0
                               1.00
## 2
       54
             8
                 6.0
                      4.0
                            0
                                     6
                                          32
                                                5
## 3
       11
            13
                 0.5
                      1.0
                               0.00
                                     0
                                           0
                                                0
                            0
## 4
       21
            13
                 2.0
                      2.5
                            1
                               0.00
                                      1
                                           0
                                                5
            30
                      5.0
                               0.00
                                                0
## 5
       61
                 3.0
                                          21
                               0.00
                                     2
                                                3
## 6
       20
            70
                 0.0
                      2.0
                            3
                                           0
```



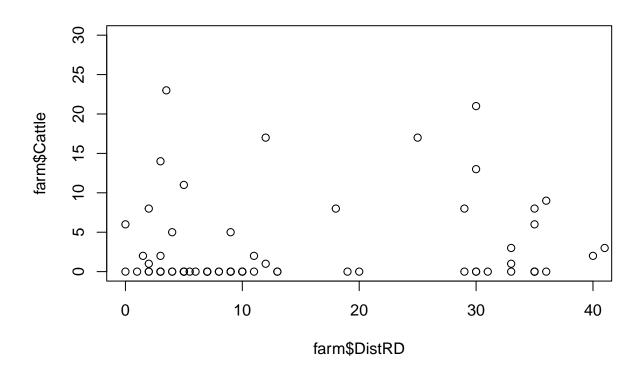
plot(farm\$Family, farm\$DistRD, ylim = c(0,40), xlim = c(0,60))



plot(farm\$DistRD, farm\$Cattle)



plot(farm\$DistRD, farm\$Cattle, ylim = c(0,30), xlim = c(0,40))



```
normal <- scale(farm)</pre>
c <- cor(normal)</pre>
eig <- eigen(c)
evalue <- eig$values
evector <- eig$vectors</pre>
evector[,1:5]
               [,1]
                           [,2]
                                        [,3]
##
                                                    [,4]
                                                               [,5]
   [1,] 0.44428879 -0.09567009 0.008833192 0.12789030 -0.09000166
    [2,] -0.03325733 -0.05415301 0.825143323 -0.51441340 -0.19338477
##
    [3,] 0.41179605 -0.33581984 0.083498728 -0.01627394 0.09170542
##
   [4,] 0.33247471 -0.56919455 -0.154619270 -0.15056819 -0.13415448
   [5,] 0.31097871 0.46059658
                                0.059319486 0.21998950 -0.35482566
   [6,] 0.26984647 0.07262355
                                0.392125115  0.59471442  -0.17451653
##
   [7,] 0.44047172 -0.04395364 -0.126521044 -0.19728624
##
##
   [8,]
         0.24794805 \quad 0.43776487 \quad -0.303032632 \quad -0.49033335 \quad -0.39511528
```

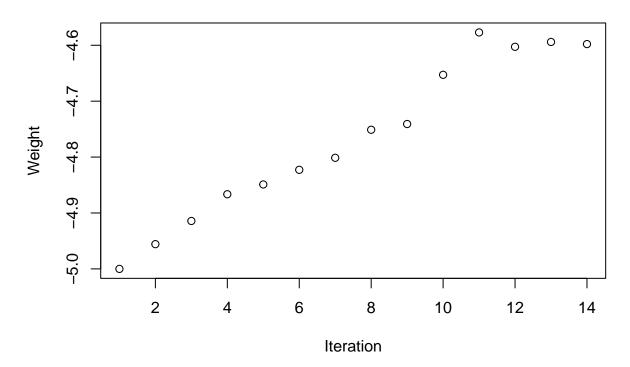
#The first principal component is a combination of all variables, as a majority are positive loadings.

```
g <- function(w) {
  return(sin(3 * w) + (1/3 * w)^2)
}</pre>
```

```
random_search1 <- function(g, alpha = 1, max_its = 100, n = 2, w0 = 0) {
  weight_history <- vector()</pre>
  cost_history <- vector()</pre>
  weight <- w0
  cost <- g(weight)</pre>
  weight history <- c(weight history, weight)</pre>
  cost_history <- c(cost_history, cost)</pre>
  if (alpha == "diminishing") {
    alpha <- 1
  } else {
    alpha <- alpha
  for (i in 1:max_its) {
    for (j in 1:n) {
      direction \leftarrow runif(1, -1, 1)
      a <- weight + (alpha * direction)</pre>
      a \leftarrow g(a)
      if (cost > a){
      weight <- weight + (alpha * direction)</pre>
      cost <- g(weight)</pre>
      weight_history <- c(weight_history, weight)</pre>
      cost_history <- c(cost_history, cost)</pre>
      }
    }
   if (alpha == "diminishing") {
      alpha <- alpha / sqrt(i)</pre>
    }
  }
  list(weight_history = weight_history, cost_history = cost_history)
}
# Example usage
results < random_search1(g, alpha = 0.1, max_its = 100, n = 2, w0 = -5)
results
## $weight_history
## [1] -5.000000 -4.955771 -4.914289 -4.866498 -4.848990 -4.822775 -4.801304
## [8] -4.751146 -4.740885 -4.652842 -4.577068 -4.602777 -4.594075 -4.597897
##
## $cost_history
## [1] 2.127490 1.983776 1.861254 1.736406 1.695324 1.638684 1.596757 1.514906
## [9] 1.500984 1.421351 1.409005 1.407532 1.407392 1.407372
```

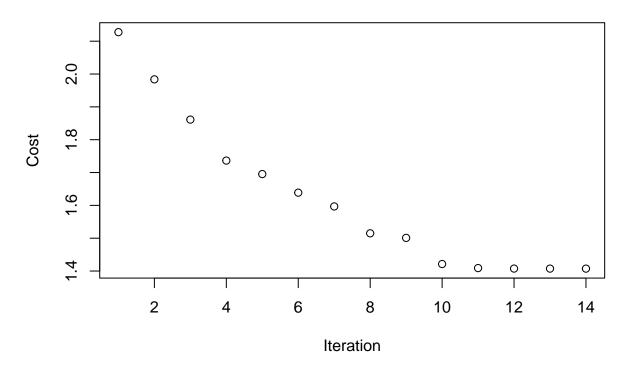
```
#random_search1(g, alpha = 0.1, max_its = 100, n = 2, w0 = 2.5)
plot(results$weight_history , xlab = "Iteration", ylab = "Weight", main = "Weight History")
```

Weight History



```
# Plot cost_history
plot(results$cost_history, xlab = "Iteration", ylab = "Cost", main = "Cost History")
```

Cost History



```
random_search <- function(g, a = "diminishing", max_its = 100, n = 1000, w0 = c(0, 0)) {
  weight_history <- list(w0)</pre>
  cost_history \leftarrow c(g(w0[1], w0[2]))
  if (a == "diminishing") {
    ap1 <- 1.0
  } else {
    ap1 <- a
  }
  for (i in 1:max_its) {
    directions <- matrix(rnorm(n * 2), ncol = 2)</pre>
    for (j in 1:n) {
      w <- weight_history[[length(weight_history)]]</pre>
      w_new <- w + ap1 * directions[j, ]</pre>
      cost <- g(w_new[1], w_new[2])</pre>
      if (cost < cost_history[length(cost_history)]) {</pre>
         weight_history <- c(weight_history, list(w_new))</pre>
        cost_history <- c(cost_history, cost)</pre>
      }
    }
    if (a == "diminishing") {
      ap1 <- ap1 / 2.0
```

```
}
}

return(list(weight_history = do.call(rbind, weight_history), cost_history = cost_history))

g <- function(w1, w2) {
    return(100 * (w2 - w1^2)^2 + (1 - w1)^2)
}

result <- random_search(g, a = 1, max_its = 100, w0 = c(-3, -3))

# Plot cost history
plot(result$cost_history, xlab = "Iteration", ylab = "Cost", main = "Cost History")
</pre>
```

Cost History

