

Finite Element Analysis of Rock Deformation in Deep Twin Tunnels

Felipe P. M. Quevedo¹, Carlos A. M. M. Colombo¹, Bianca M. Girardi¹, Denise Bernaud¹, Samir Maghous¹

¹Federal University of Rio Grande do Sul Av. Osvaldo Aranha, 99, Porto Alegre, 90.035-190, RS, Brazil motta.quevedo@ufrgs.br, ca-colombo@hotmail.com, eng.biancagirardi@gmail.com denise.bernaud@ufrgs.br, samir.maghous@ufrgs.br

Abstract. Relying upon a three-dimensional finite element analysis, this contribution investigates the instantaneous irreversivel response induced by the constitutive behavior of the rock mass in the convergence profile of twin tunnels. At the rock material level, elastoplastic state equations based on a Drucker-Prager yield surface with an associated flow rule are adopted in the modeling. As regards the tunnel support, the formulation accounts for the presence of an elastic shotcrete-like lining. From a computational point of view, the deactivation-activation method is used to simulate the excavation process and the installation of the lining. The accuracy of the finite element predictions is assessed through comparisons with the available analytical solutions formulated in a simplified scenario for the twin tunnel configuration. A parametric study investigates the mutual interaction induced by the proximity of the tunnels.

Keywords: Twin tunnels, Elastoplasticity, Finite element modeling

1 Introduction

Many design methods often focus on single tunnels, but twin tunnels are a common occurrence. The interaction between tunnels can be significant, especially when the spacing between them is minimal. Additionally, many twin tunnels incorporate transverse galleries, introducing a localized effect on displacements and stresses. While the simulation of tunnel convergence in single tunnels has been widely investigated and reported in published literature, few works have addressed the computational evaluation of deformation in twin tunnels. Some studies on deep twin tunnels can be found at Spyridis and Bergmeister [1], Chen et al. [2], Ma et al. [3], Fortsakis et al. [4], Chortis and Kavvadas [5], Chortis and Kavvadas [6], Guo et al. [7], Chortis and Kavvadas [8], Chortis and Kavvadas [9]. But less attention has been dedicated to assessing the mutual mechanical interaction induced by the excavation of the transverse gallery connecting the twin tunnels.

In this context, the main contributions of this paper can be summarized at both the material and tunnel analysis levels. At the material level, the constitutive state equations of the rock mass are developed using a plasticity framework, which is suitable for clayey rocks. For the mechanical behavior of the concrete lining, the traditional linear elastic model are employed. At the structural analysis level, the deformation of the highly interactive components of the material system (i.e., rock mass and lining) resulting from the excavation of twin tunnels and transverse gallery is simulated using three-dimensional finite element simulations. The excavation and lining placement processes are simulated through the activation/deactivation technique. The constitutive models for the rock mass and the associated numerical integration schemes, are implemented into the UPF/USERMAT customization tool [10] of the ANSYS standard software. This three-dimensional finite element analysis is specifically designed to address the interactions induced by the construction process, the proximity of twin tunnels, and the presence of the transverse gallery.

2 Constitutive Models

The constitutive model for the rock mass corresponds to the associated Drucker-Prager elastoplastic model. The local strain rate $\dot{\varepsilon}$ is split into two contributions $\dot{\varepsilon} = \dot{\varepsilon}^e + \dot{\varepsilon}^p$, so that the constitutive relationships relating the Cauchy stress rate $\dot{\sigma}$ and strain rate components can be written as:

$$\dot{\boldsymbol{\sigma}} = \boldsymbol{D} : \dot{\boldsymbol{\varepsilon}}^e = \boldsymbol{D} : (\dot{\boldsymbol{\varepsilon}} - \dot{\boldsymbol{\varepsilon}}^p). \tag{1}$$

In the above relationship, $\dot{\varepsilon}^e$ and $\dot{\varepsilon}^p$, represent respectively the elastic and plastic strain rate, and D denote the fourth-order isotropic elastic linear constitutive tensor defined by the rock mass elastic Young modulus E and Poisson ratio ν . The plastic strain rate is given by flow rule:

$$\dot{\varepsilon}^{p} = \begin{cases} \dot{\lambda} \frac{\partial g}{\partial \sigma} & \text{for } f > 0 \\ \mathbf{0}, & \text{for } f \leq 0 \end{cases} , \tag{2}$$

where $\dot{\lambda}$ is the plasticity multiplier (obtained through the consistency condition $\dot{f}=0$) and g is a potential flow function analogous to f used to simulate the volume dilatation during the evolution of plastic deformations. However, for this analysis, was used associated plasticity, i.e., g=f. In this model the Drucker-Prager plastic flow surface is given by

$$f(\sigma, q) = f(I_1, J_2, q) = \beta_1 I_1 + \beta_2 \sqrt{J_2} - q(\alpha), \tag{3}$$

which I_1 is the first invariant of the stress tensor, J_2 the second invariant of the deviator tensor and β_1, β_2 and $q(\alpha)$ are strength parameters related to the friction angle ϕ and cohesion $c(\alpha)$, respectively. In the present model Drucker-Prager surface been inner of the Mohr-Coulomb surface [16], that is,

$$\beta_1 = \frac{(k-1)}{3}, \quad \beta_2 = \frac{(2k+1)}{\sqrt{3}}, \quad q(\alpha) = 2\sqrt{k} c(\alpha),$$
 (4)

where $k = (1 + \sin \phi)/(1 - \sin \phi)$. The internal variable α is the equivalent plastic strain $\bar{\epsilon}^p$ used to simulate strain hardening/softening phenomena. However, for this study, we adopt perfect plasticity, meaning that c is a constant.

A linear elastic constitutive model is used for the concrete lining, which can be expressed, within the framework of infinitesimal analysis, as:

$$\dot{\boldsymbol{\sigma}} = \boldsymbol{D} : \dot{\boldsymbol{\varepsilon}}^e, \tag{5}$$

where, $\dot{\varepsilon}^e$ and D are respectively the elastic strain rate and the fourth-order isotropic elastic constitutive tensor defined by the concrete lining Poisson ratio $\nu_c = 0.2$ and elastic Young modulus E_c .

3 Spatial and time discretization of the domain

The geometry material domain Ω considered for the finite element simulations, including tunnelling and deformation analysis, is defined by a parallelepiped volume of dimensions $(L_1 + L_2) \times L_3 \times d_3$ (Fig. 1). Owing to the symmetry of the problem, only the material portion $\{x \le 0, y \ge 0\}$ is considered for F.E discretization and analysis. Referring to the notations of Fig. 1, d_1 is the distance between the axes of longitudinal tunnels, L_2 represents the total length along longitudinal direction e_z of the cylindrical volume to be excavated that is considered in the numerical simulation, d_3 is the thickness along vertical direction e_y of material domain Ω , L_1 stands for the length of unexcavated region after total excavation process, L_3 is the total length along transversal direction e_x of discretized material domain, d_2 characterizes the location of the circular transverse axis gallery that intersects the longitudinal tunnel at $z = L_1 + d_2$. The length of the excavation step adopted will be denoted by L_{vt} . The mesh used in the simulations consists of 119740 or 221104 total elements (hexahedra and tetrahedra), depending on the value of spacing between longitudinal tunnels. To increase the accuracy of the model predictions in the intersection zone, the region surrounding the transverse gallery (including part of the longitudinal tunnel) is discretized by means 10-node quadratic tetrahedral elements, whereas 8-node trilinear hexahedral elements are used for the remaining part of the structure. Furthermore, a refined meshing is used for discretizing the zones surrounding the longitudinal and transverse gallery. These zones whose mechanical state is significantly affected by the tunnelling process are indicated by light gray color in Fig. 1. Two values shall be considered for the spacing d_1 in the numerical simulations, namely $d_1 = 16R_t$ and $4R_t$. The layer of concrete lining of thickness e_q installed along the gallery wall is indicated by red color in the figure. Without introducing additional modeling restriction and for the sake of simplicity, the value of the gallery radius is fixed to $R_g = 2/3R_t$. The same lining system (same concrete material and layer thickness) is considered for both longitudinal tunnels and gallery. As regards the discretization of the region surrounding the gallery, parameters d_5 and d_1 define the size in a yz plane of the transition region involving the tetrahedral finite elements.

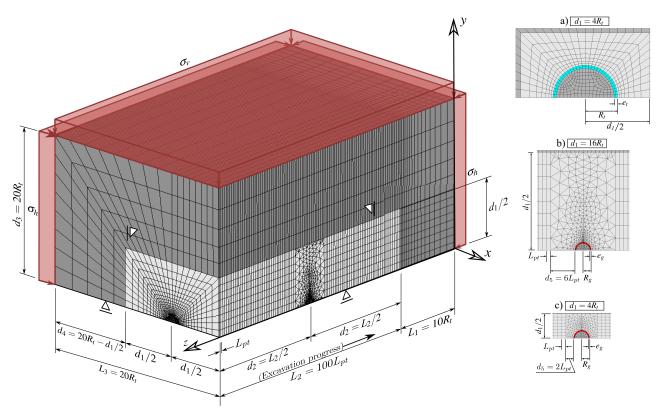


Figure 1. Geometry, mesh and boundary conditions of domain and details of a) longitudinal tunnel cross-section for configuration $d_1 = 4R_t$ and gallery cross-section for configurations b) $d_1 = 16R_t$ and c) $d_1 = 4R_t$.

As mentioned previously, the tunnelling process, including the excavation steps and lining installation, is simulated resorting to the activation-deactivation method shown in the schematic representation in Fig. 2. Each excavation step is modeled by deactivation of the corresponding elements (the elements stiffness is reduced by a factor 1E8), whereas installation of elements of lining at a distance d_{0t} from the excavation face (unlined length) is achieved through activation of the corresponding elements by assigning them concrete properties. In this Figure, n_p is the total number of excavation steps and n_{pig} represents the number of longitudinal tunnel excavation steps prior to gallery excavation. After achievement of the n_{pig} excavation steps, the excavation of the gallery is initiated starting from the longitudinal tunnel wall. Referring to the notation of Fig. 2, L_{pg} is the considered step length for the gallery excavation, V_{pg} is the speed of the gallery excavation, and d_{0g} is the unlined length of the gallery. Each gallery excavation step is associated with pseudotime interval $t_{pg} = V_{pg}/L_{pg}$. After the gallery excavation is completed, we proceed to further excavation steps of the longitudinal tunnel. The main parameters defining the geometry domain as well as and excavation process and lining installation are summarized in Table 1.

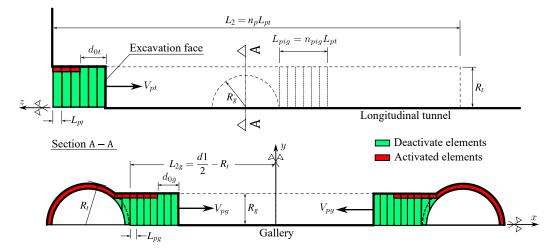


Figure 2. Schematic representation of the excavation process.

| Table 1. Parameters related to the geometry of the domain, excavati | on and installation of the lining. |
|---|------------------------------------|
|---|------------------------------------|

| PARAMETERS | SYMBOL | UNIT | VALUES | |
|--|-----------|-------|-----------------|--|
| Longitudinal tunnels | | | | |
| Radius of the longitudinal tunnel | R_t | m | R_t | |
| Thickness of the lining | e_t | m | $0.1R_t$ | |
| Step length of the excavation process | L_{pt} | m | $1/3R_t$ | |
| Unlined length | d_{0t} | m | $2L_{pt}$ | |
| Speed of the excavation face | V_{pt} | m/day | 12.5 | |
| Excavation step time | t_p | day | L_{pt}/V_{pt} | |
| Gallery | | | | |
| Radius of the gallery | R_g | m | $2/3R_t$ | |
| Thickness of the concrete lining | e_g | m | $0.1R_t$ | |
| Step length of the excavation process | L_{pg} | m | $1/3R_g$ | |
| Unlined length | d_{0g} | m | $2L_{pg}$ | |
| Speed of the excavation face | V_{pg} | m/day | 12.5 | |
| Number of steps that starts gallery excavation | n_{pig} | un | 15 | |
| Rest of domain | | | | |
| Distance between longitudinal tunnel axes | d_1 | m | $4R_t, 16R_t$ | |
| Length of the unexcavated region | L_1 | m | $10R_t$ | |
| Total excavated length | L_2 | m | $100L_{pt}$ | |
| Domain height | L_3 | m | $20R_t$ | |

4 Verification with unlined twin tunnel in elastoplastic medium

In the context of plane strain conditions, Ma et al. [3] developed an approximate analytical solution for the stresses and the plastic zone boundary around deep twin circular tunnels excavated in a homogeneous elastoplastic medium. This solution does not assume necessarily equal initial stresses, and the initial stress along the tunnel axis is assumed as the middle stress, i.e., $\sigma_{zz}=(\sigma_v+\sigma_h)/2$. For the constitutive model, the authors considered perfectly plastic Mohr-Coulomb criterion with associated plastic flow rule. In this analytical solution, it is assumed that the plastic zones around each tunnel are isolated from each other and completely surround each tunnel.

Fig. 3 shows the comparison between the 3D F.E. Solution (from a far behind the excavation face) and the analytical solution for plastic zone boundary provided in [3]. For these analysis, $R_t=1$ m, $d_1/2R_t=2.5$, Young's modulus E=20 GPa, Poisson's ratio $\nu=0.3$ and, friction angle $\phi=30^\circ$. The boundary of the plastic zone agrees very well with the elements that have reached the plasticity criterion.

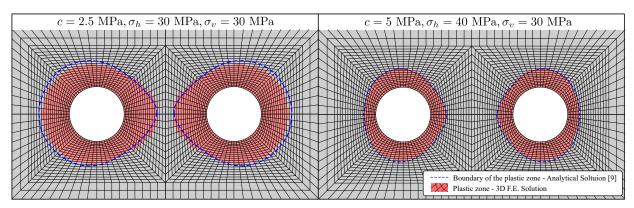


Figure 3. Comparisons between the numerical and analytical solution for the plastic zones considering $d_1/2R_t = 2.5$ and $\phi = 30^{\circ}$ for different initial conditions and cohesion values.

The stresses obtained in the 3D numerical simulation are compared quantitatively in Fig. 4 with the stresses

derived from the elastoplastic analytical solution in [3]. In this figure, the stresses are given in polar coordinates $(r, \theta = 45^{\circ}, 90^{\circ})$ and 135° . Although the criterion adopted for numerical simulation is the Drucker-Prager inscribed in Mohr-Coulomb, the solution agrees very well with the analytical solution in the plastic zone.

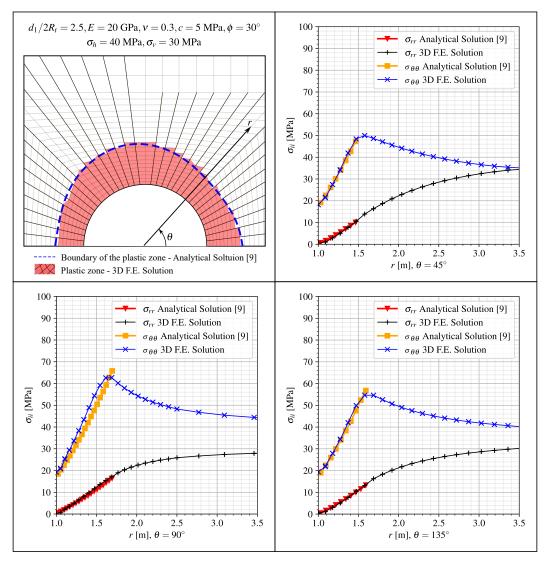


Figure 4. Comparisons between the numerical and analytical solution for differents stress-paths.

5 Numerical Results and Discussion

5.1 Writing style

Please limit your paper by writing concisely, rather than by reducing figures or tables to a size at which symbols or labels would become difficult to read.

5.2 More detailed specifications

The first page must include the paper's title (in sentence case), authors, affiliations, abstract, keywords, as well as the beginning of the text itself (i.e., the first section, which is usually the introduction). Do not insert a page break in between the keywords and the beginning of the text. Please follow strictly the line spacing defined next: either exactly 13pt-spaced lines (preferred) or single-spaced lines for the body of the text, with 20pt space before and 12pt space after first-level and second-level headings. If you use the pre-defined styles of this template, these specifications will be automatically applied.

Remark 1: Author(s) and affiliation(s). Type the authors' names in regular (plain) type, flush left, including first name, middle initial(s) and last name. Group the authors by their affiliations with a superscript number. Each name or group of names must be followed by the corresponding affiliations and emails, which should be both in italics. A 12pt space must be left between the names and affiliations. If you use the pre-defined styles of this template, these specifications will be automatically applied.

Remark 2: Abstract and keywords. Type "Abstract" in boldface, flush left, followed by a period. On the same line, type the abstract in regular (plain) format, justified alignment. The abstract should not exceed 200 words. Please pay attention to the line spacing between the authors affiliations and the abstract, as well as between the abstract and the keywords. If you use the pre-defined styles of this template, these specifications will be automatically applied. For the keywords, type "Keywords", followed by a colon, in boldface, flush left and type 3 to 5 keywords, separated by commas.

Remark 3: Headings. First-level headings must be typed in sentence letters, 13 pt boldface type, flush left, as in Section 2 above. Use Arabic numbering (if you use the pre-defined styles of this template, automatic numbering is already built-in in the "1st Heading Cilamce-2024" style). Notice the line spacing before and after first-level headings. For second-level headings, use sentence letters, 10pt boldface type, flush left, with Arabic double numbering (if you use the pre-defined styles of this template, automatic double numbering is already defined). Notice the line spacing before and after second-level headings. Do not use third-level headings. Instead, use, at most, "Remarks" (or the like), as shown here. These shall start with the word "Remark" (or the like) in boldface italics, followed by a number and a title (optional). The text that follows must be in regular (plain) format. Notice the line spacing before and after such paragraphs.

Remark 4: Body of text. As said before, the body of the text should be typed in 10pt Times New Roman, using either exactly 13pt spaced lines (preferred) or single-spaced lines, with justified alignment. Start each paragraph with an indentation of 0.75 cm from the left margin, and allow no space between paragraphs. If you use the pre-defined styles of this template, these specifications will be automatically applied.

5.3 Equations, symbols and units

Equations must be centered, right-numbered, with numbers enclosed in parentheses and placed flush right. Allow 6 pt line spacing before and after an equation. For example:

$$q_r = -4pr^2k\frac{dT}{dr}. (6)$$

Please pay attention to the punctuation after the equations, as equations are part of the text and must be punctuated accordingly. When referring to an equation in the text, write eq. (6), except at the beginning of a sentence, wherein Equation (6) should be used. Please describe the notation adopted and be careful as to define all quantities, variables and symbols as soon as they first appear in the text. A nomenclature section is not necessary.

All data, including those shown in tables and figures, must be reported in SI units. Use decimal points rather than commas to indicate decimals.

5.4 Figures and tables

Figures and tables should be inserted as close as possible to their first mentioning in the text. Embedded text and symbols must be clearly readable; avoid exceedingly small fonts. Supply good quality pictures and illustrations. Figures and tables and their captions should be centered in the text. Place figure captions below the figures and allow 12pt line spacing between both, and 20pt line spacing after the caption (i.e., before the subsequent text). Place table title above the table, leaving 20pt line spacing before the title and 6pt between the title and the table. Leave 20pt line spacing after the table (i.e., before the subsequent text). Examples are shown next:

Arabic numerals should be used in figures and tables (e.g., Figure 5, Figure 2, Table 2, Table 2, etc). Refer to them in the text as Table 2 and Fig. 5, except at the beginning of a sentence, wherein Figure 5 should be used.

When constructing graphs or plots, do not forget to label coordinates and state the corresponding units.

Table 2. Coefficients in constitutive relations

| Constitutive relation | Nomenclature | Value |
|-----------------------|--------------|-------|
| Turbulent tensor | C_{μ} | 0.09 |
| Turbulent tensor | $C_{\mu b}$ | 0.69 |
| Lateral lift | C_L | 0.08 |
| Virtual mass | C_{VM} | 0.8 |

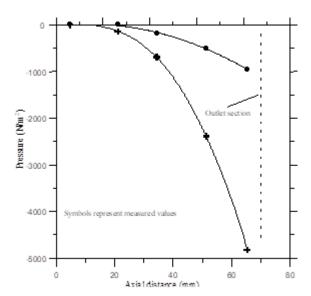


Figure 5. Pressure variation along the nozzle: experimental data

Similarly, label all columns/rows in tables and state corresponding units whenever applicable.

5.5 Permission

You are the sole responsible for making sure that you have the right to publish everything in your paper. If you use material from a copyrighted source, or from other authors, you may need to obtain permission from the copyright holder or the respective authors. An "authorship statement" must be placed at the end of your paper, immediately before the list of references, as shown further below.

5.6 References

References should be cited in the text by Last Name [number]. For example: "In a recent work,?] proposed the method of?]". Numbers must be Arabic, enclosed in square brackets and used consecutively. References must be listed at the end of the paper, in a separate section entitled "References". They must be listed consecutively by the order of citation in the text. Type the word "References" in boldface, 13 pt Times New Roman type from the left margin, leaving 20 pt line spacing before and 12pt after. Then type the reference 9pt below it, in 9pt Times New Roman, with single-spaced lines (please do not leave blank spaces between references). See examples below. The list should only include works that are cited in the text.

6 Conclusions

Type your conclusions or closing remarks here. Please be as concise and objective as possible. Do not make a summary of the paper, but instead list the main findings and results, even if these are only partial conclusions so far.

Acknowledgements. This section should be positioned immediately after the Conclusion section. Type Acknowledgements in boldface, 10 pt Times New Roman type from left margin, leaving 20 pt line spacing before and 12pt after.

Authorship statement. This section is mandatory and should be positioned immediately before the References section. The text should be exactly as follows: The authors hereby confirm that they are the sole liable persons responsible for the authorship of this work, and that all material that has been herein included as part of the present paper is either the property (and authorship) of the authors, or has the permission of the owners to be included here.

References

- [1] P. Spyridis and K. Bergmeister. Analysis of lateral openings in tunnel linings. *Tunnelling and Underground Space Technology*, vol. 50, pp. 376–395, 2015.
- [2] F. Chen, L.-b. Lin, and D. Li. Analytic solutions for twin tunneling at great depth considering liner installation and mutual interaction between geomaterial and liners. *Applied Mathematical Modelling*, vol. 73, 2019.
- [3] Y. Ma, A. Lu, X. Zeng, and H. Cai. Analytical solution for determining the plastic zones around twin circular tunnels excavated at great depth. *International Journal of Rock Mechanics and Mining Sciences*, vol. 136, pp. 104475, 2020.
- [4] P. Fortsakis, E. Bekri, G. Prountzopoulos, and P. Marinos. Numerical analysis of twin tunnels interaction. In *Proc. 1st Eastern European Tunnelling Conference*, Budapest, Hungary, 2012.
- [5] F. Chortis and M. Kavvadas. Three-dimensional numerical analyses of perpendicular tunnel intersections. *Geotechnical and Geological Engineering*, vol. 39, pp. 1771–1793, 2021a.
- [6] F. Chortis and M. Kavvadas. Three-dimensional numerical investigation of the interaction between twin tunnels. *Geotechnical and Geological Engineering*, vol. 39, pp. 5559–5585, 2021b.
- [7] Z. Guo, X. Liu, and Z. Zhu. An elastic solution for twin circular tunnels' stress in hydrostatic stress field. *Geotechnical and Geological Engineering*, vol. 39, pp. 1–11, 2021.
- [8] F. Chortis and M. Kavvadas. 3D numerical investigation of the axial forces acting on tunnel junctions constructed in fractured/weathered to very blocky rockmass. In *Expanding Underground-Knowledge and Passion to Make a Positive Impact on the World*, pp. 1574–1582. CRC Press, 2023a.
- [9] F. Chortis and M. Kavvadas. 3D numerical investigation of the bending moments acting on tunnel junctions constructed in fractured/weathered to very blocky rockmass. In *Expanding Underground-Knowledge and Passion to Make a Positive Impact on the World*, pp. 1583–1591. CRC Press, 2023b.
- [10] ANSYS. ANSYS Programmer's Reference, release 15.0. Canonsburg, Pennsylvania, 2013.
- [11] G. Rousset. *Comportement mecanique des argiles profondes: Application au stockage de déchets radioactifts.* Ph.D. Thesis (in french), Ecole Nationale des Ponts et Chaussées, Paris, France, 1988.
- [12] D. Nguyen Minh and G. Rousset. Influence of instantaneous failure on time dependent behavior of underground galleries. In *The 28th U.S. Symposium on Rock Mechanics (USRMS)*, pp. ARMA–87–0663, Tucson, Arizona, 1987.
- [13] A. Giraud and G. Rousset. Time-dependent behaviour of deep clays. *Engineering Geology*, vol. 41, n. 1, pp. 181–195, 1996.
- [14] F. P. M. Quevedo, D. Bernaud, and S. Maghous. Numerical integration scheme for coupled elastoplastic-viscoplastic constitutive law for tunnels. *International Journal of Geomechanics*, vol. 22, n. 10, 2022.
- [15] F. P. M. Quevedo. *Análise computacional das deformações em túneis profundos considerando o acoplamento plasticidade-viscoplasticidade*. Ph.D. Thesis (in portuguese), Federal University of Rio Grande do Sul, Porto Alegre, Brazil, 2021.
- [16] D. Bernaud. *Tunnels profonds dans les milieux viscoplastiques: approches expérimentale et numérique*. Ph.D. Thesis (in french), Ecole Nationale des Ponts et Chaussées, Paris, France, 1991.
- [17] P. Perzyna. Fundamental problems in viscoplasticity. In *Advances in applied mechanics*, volume 9, pp. 243–377. Elsevier, 1966.