



Introduction to backpropagation

In this lesson

- Virginia Tech Hokies
- Matrices
- Gradient descent flavors (full, batch, sgd)
- Correlation
- Overfitting
- Backpropagation

Hokies

Let's learn how a network learns entire datasets



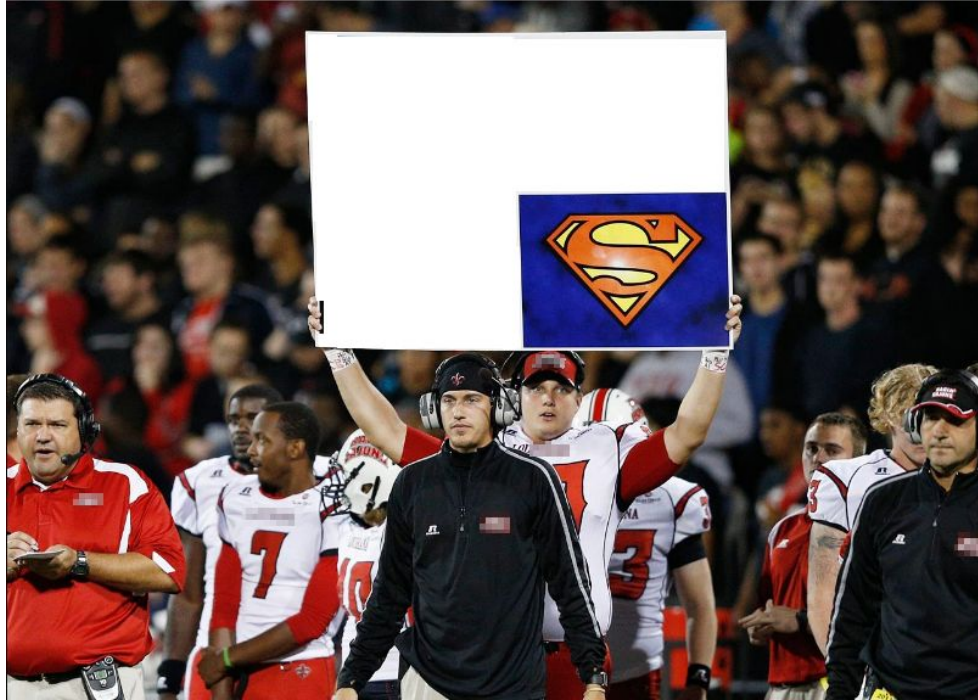
Run



PASS!!!



Run



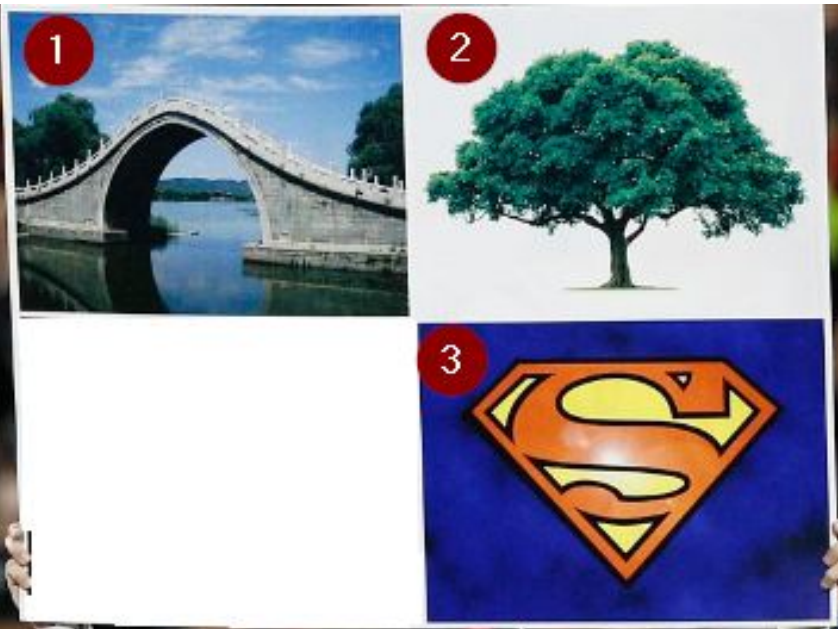


Image 1	Image 2	Image 3	Label
YES	NO	YES	Run
NO	YES	YES	Pass
NO	NO	YES	Run
YES	YES	YES	Pass
No	YES	YES	Pass
YES	NO	YES	Run



How to think about data

Neural networks don't read football placards.



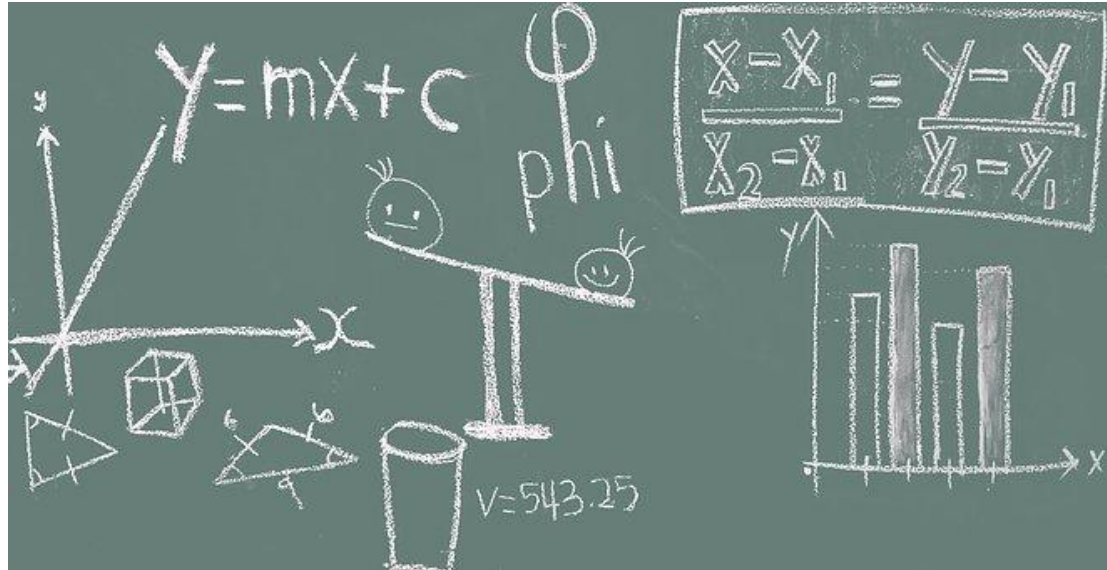
What you know

What you
wanna know

Image 1	Image 2	Image 3	Label
YES	NO	YES	Run
NO	YES	YES	Pass
NO	NO	YES	Run
YES	YES	YES	Pass
No	YES	YES	Pass
YES	NO	YES	Run

How to think about data

We need to see this in a math context.












How to think about data

Poster Boards				Board Pattern		
Image 1	Image 2	Image 3		Image 1	Image 2	Image 3
YES	NO	YES	→	1	0	1
NO	YES	YES	→	0	1	1
NO	NO	YES	→	0	0	1
YES	YES	YES	→	1	1	1
No	YES	YES	→	0	1	1
YES	NO	YES	→ 10	1	0	1










How to think about data

Poster Boards				Board Pattern		
Image 1	Image 2	Image 3		Image 1	Image 2	Image 3
YES	BOTH	YES		1	.5	1
NO	YES	YES		0	1	1
NO	NO	YES		0	0	1
YES	YES	YES		1	1	1
No	BOTH	YES		0	.5	1
YES	NO	YES	 	1	0	1



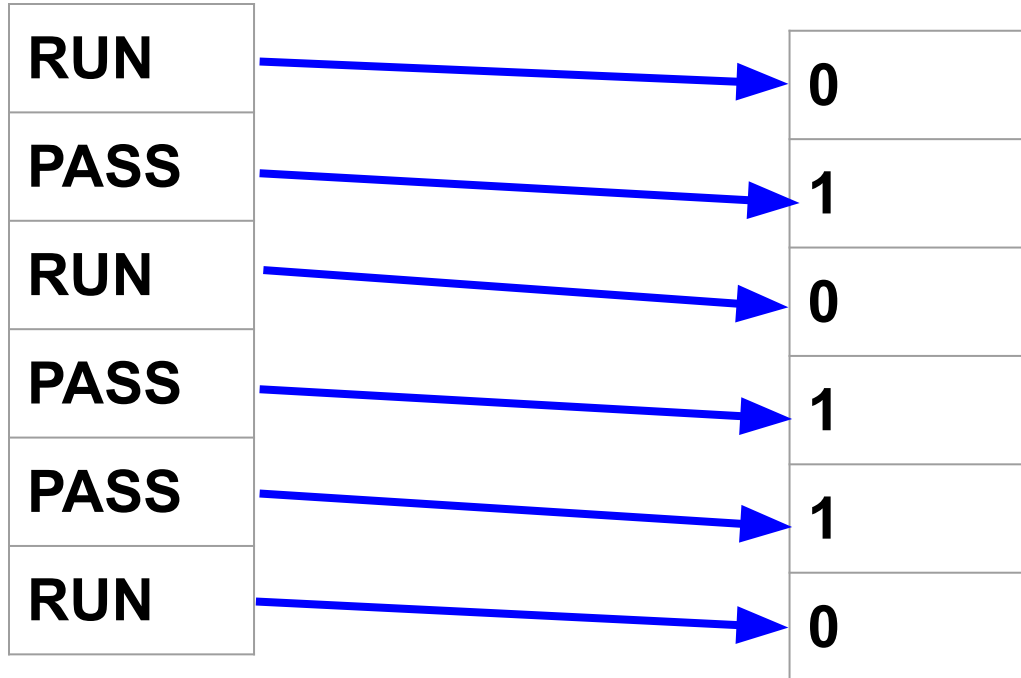
How to think about data

Poster Boards				Board Pattern		
Image 1	Image 2	Image 3		Image 1	Image 2	Image 3
YES	BOTH	YES		10	5	10
NO	YES	YES		0	10	10
NO	NO	YES		0	0	10
YES	YES	YES		10	10	10
No	BOTH	YES		0	5	10
YES	NO	YES	 	10	0	10

How to think about data

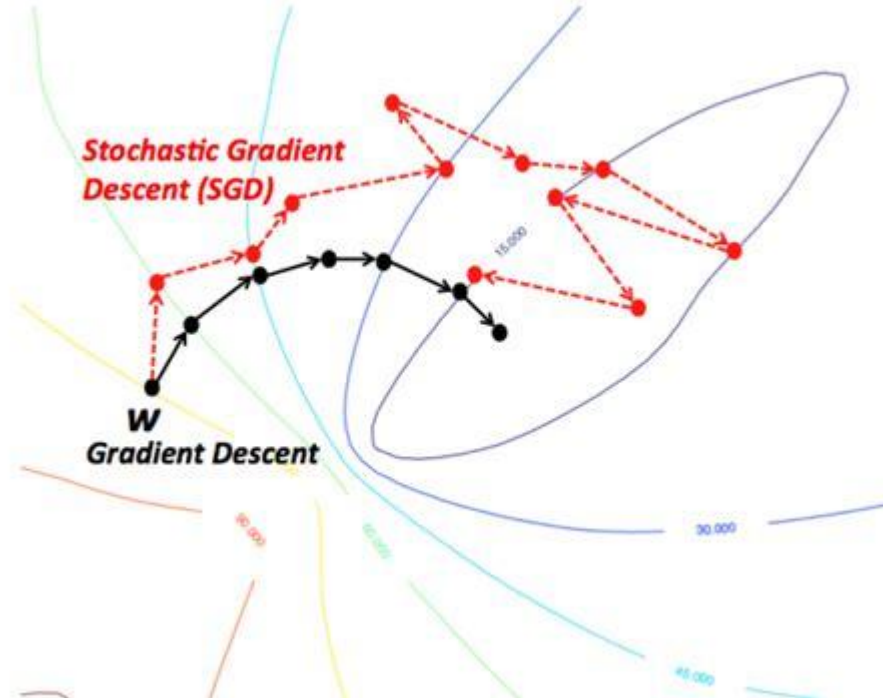


How to think about data



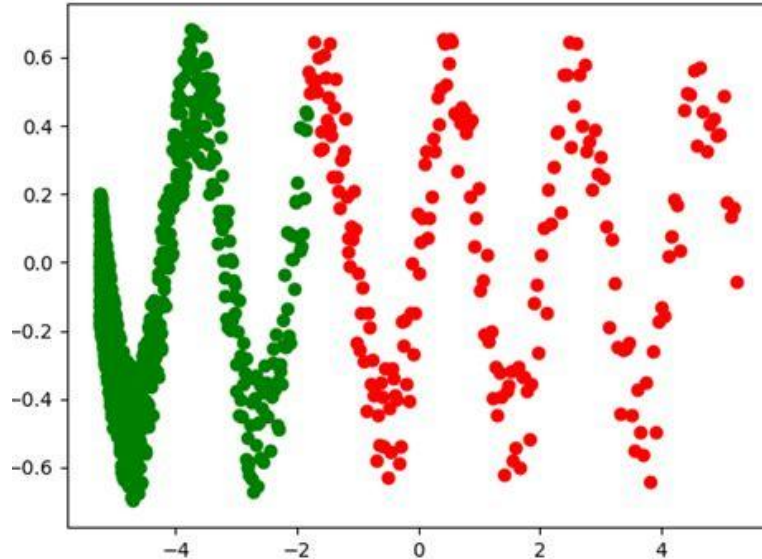
stochastic gradient descent

Stochastic gradient descent updates weights one example



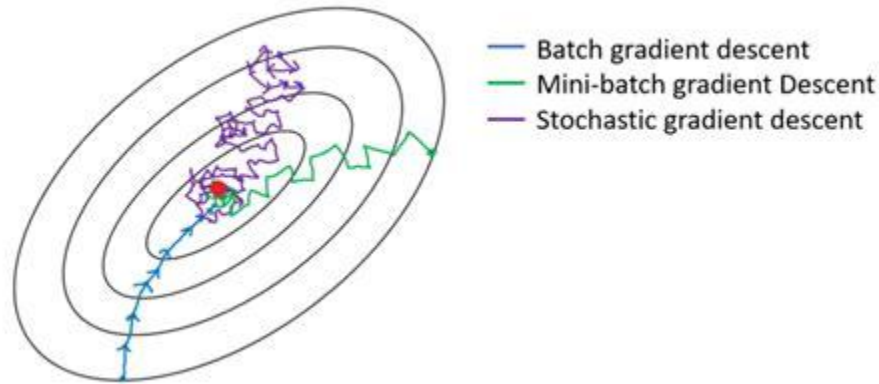
regular gradient descent

(Average/Regular/Full) gradient descent updates weights
one dataset at a time.



batch/mini batch gradient descent

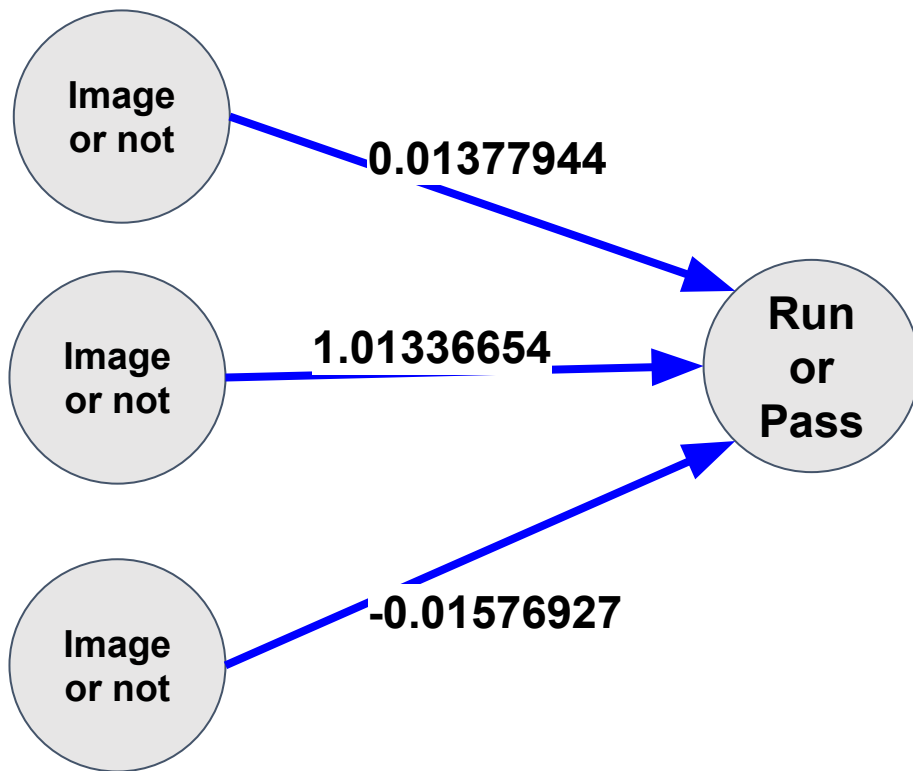
(BATCH) gradient descent updates weights one dataset at a time.



TRUISM: Neural Networks Learn Correlations

What did the neural network learn?





Push/Pull of weights comes from the data

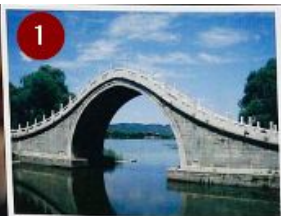
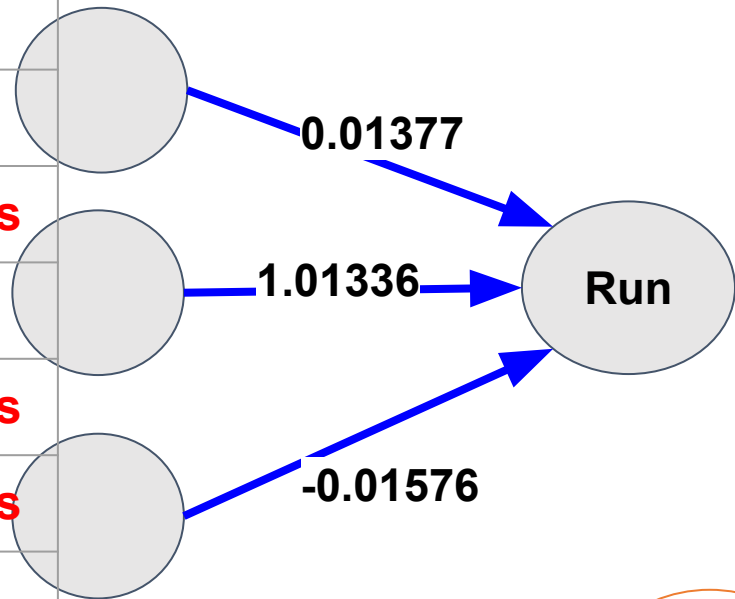


Image 1	Image 2	Image 3	Label
YES	NO	YES	Run
NO	YES	YES	Pass
NO	NO	YES	Run
YES	YES	YES	Pass
No	YES	YES	Pass
YES	NO	YES	Run



Push/Pull of weights comes from the data

Image 1	Image 2	Image 3	Label
1	0	1	Run
0	1	1	Pass
0	0	1	Run
1	1	1	Pass
0	1	1	Pass
1	0	1	Run



Image 1	Image 2	Image 3	Label
-	0	-	Run
0	+	+	Pass
0	0	-	Run
+	+	+	Pass
0	+	+	Pass
-	0	-	Run

Up and down pressure

Image 1	Image 2	Image 3	Label
1	0	1	Run
0	1	1	Pass
0	0	1	Run
1	1	1	Pass
0	1	1	Pass
1	0	1	Run



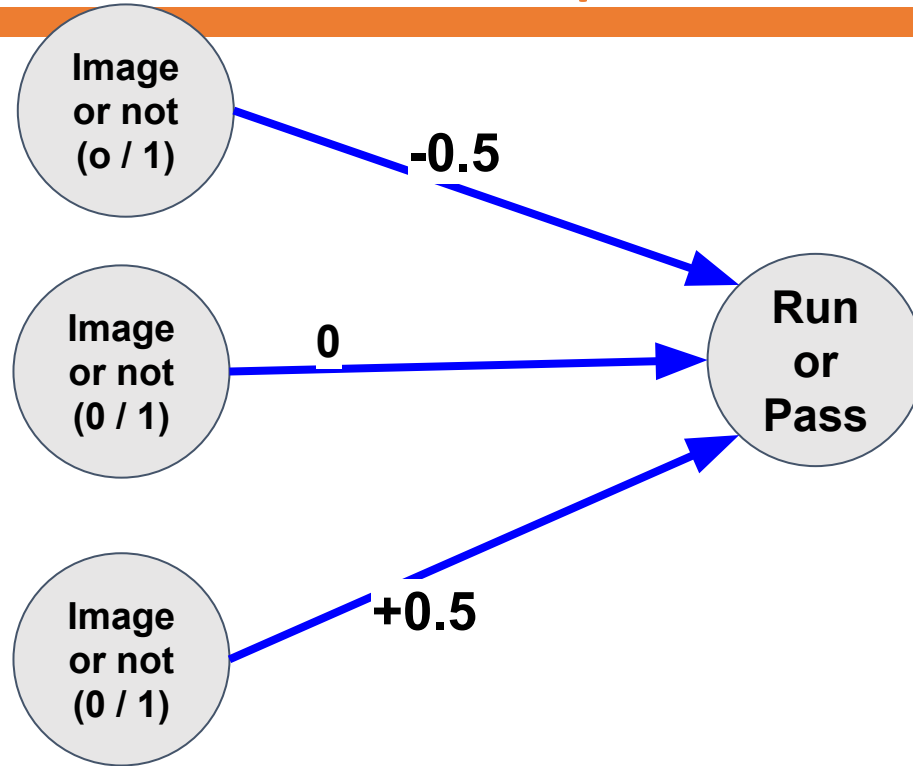
Image 1	Image 2	Image 3	Label
-	0	-	Run
0	+	+	Pass
0	0	-	Run
+	+	+	Pass
0	+	+	Pass
-	0	-	Run

Up and down pressure



Overfitting

Correlation Oops...





Overfitting



How does it learn with all the conflicts?

Know thyself - correlation

Image 1	Image 2	Image 3	Label
1	0	1	Run
0	1	1	Pass
0	0	1	Run
1	1	1	Pass
0	1	1	Pass
1	0	1	Run



Image 1	Image 2	Image 3	Label
-	0	-	Run
0	+	+	Pass
0	0	-	Run
+	+	+	Pass
0	+	+	Pass
-	0	-	Run

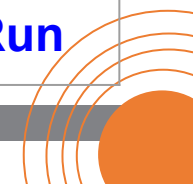




Image 1	Image 2	Image 3	Label
1	0	1	Run
0	1	1	Pass
0	0	1	Run
1	1	1	Pass
0	1	1	Pass
1	0	1	Run



Image 1	Image 2	Image 3	Label
-	0	-	Run
0	+	+	Pass
0	0	-	Run
+	+	+	Pass
0	+	+	Pass
-	0	-	Run

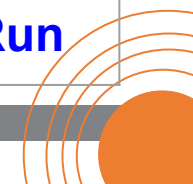




Image 1	Image 2	Image 3	Label
1	0	1	Run
0	1	1	Pass
0	0	1	Run
1	1	1	Pass
0	1	1	Pass
1	0	1	Run



Image 1	Image 2	Image 3	Label
-	0	-	Run
0	+	+	Pass
0	0	-	Run
+	+	+	Pass
0	+	+	Pass
-	0	-	Run



Edge case: Conflicting pressure

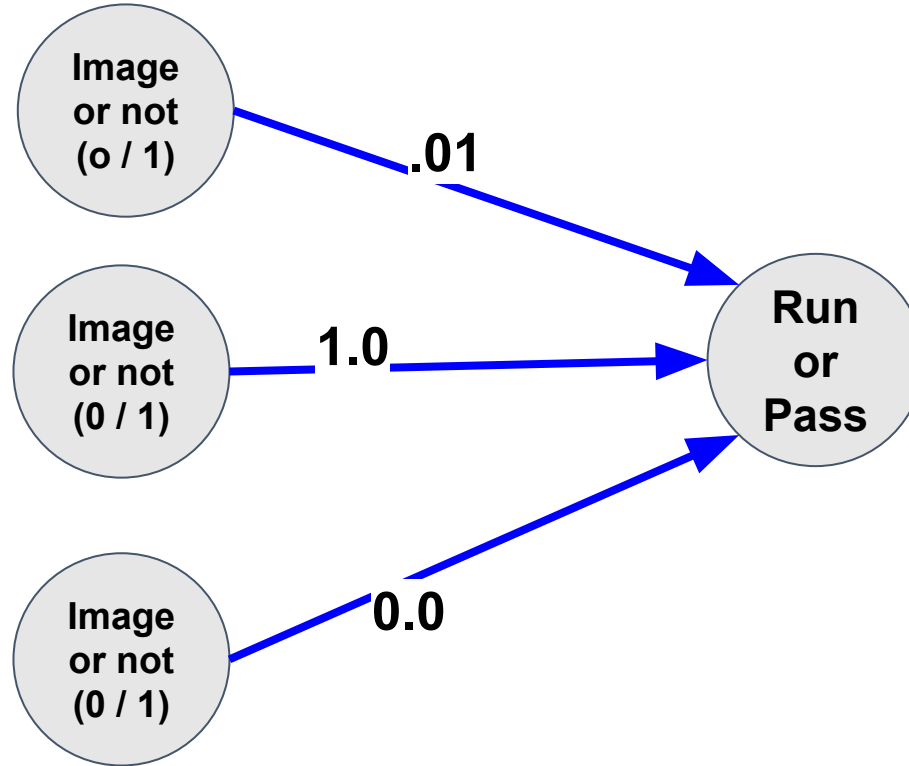
Image 1	Image 2	Image 3	Label
1	0	1	Pass
0	1	1	Pass
0	0	1	Run
1	1	1	Run



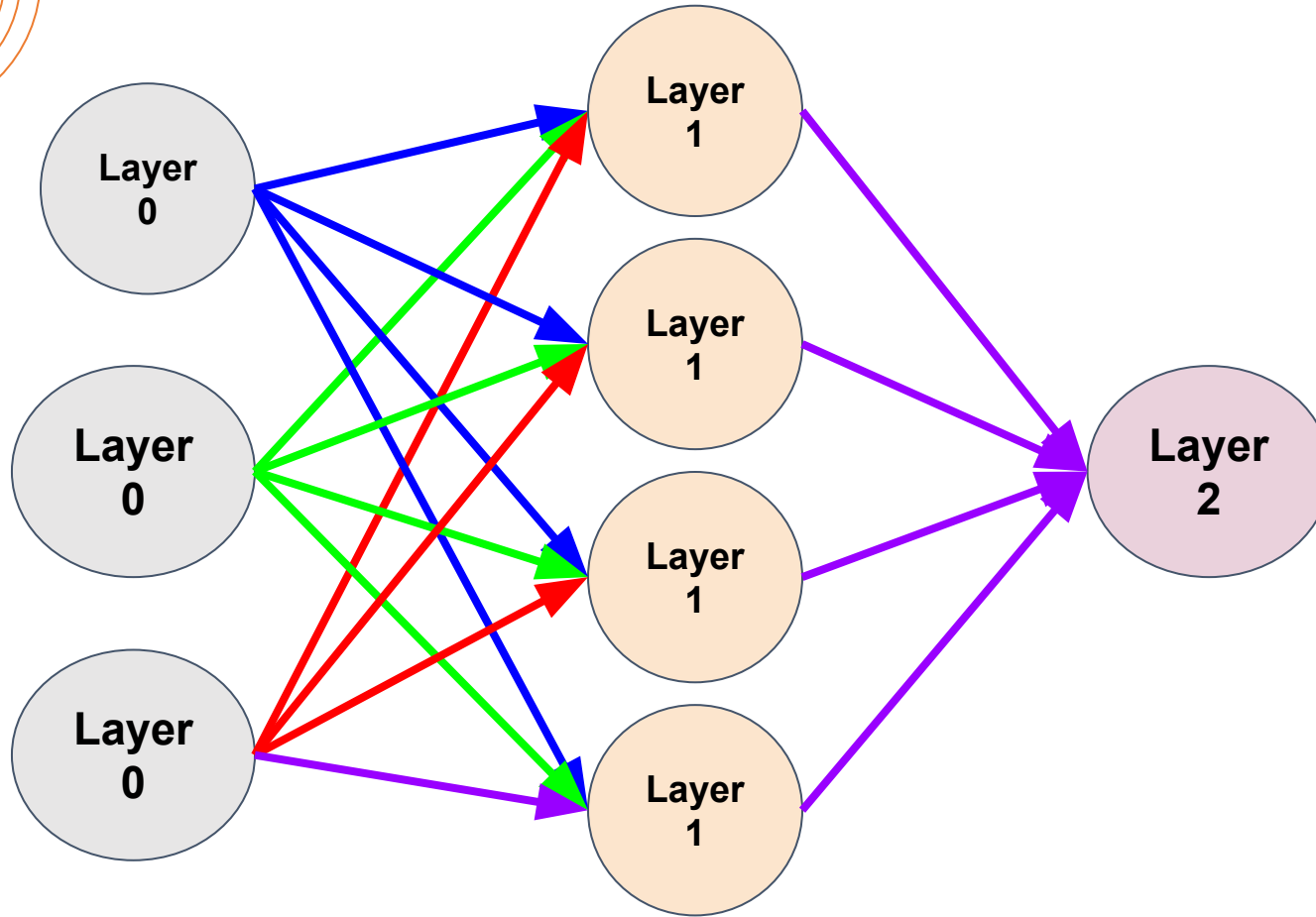
Image 1	Image 2	Image 3	Label
+	0	+	Pass
0	+	+	Pass
0	0	-	Run
-	-	-	Run

Learning indirect correlation

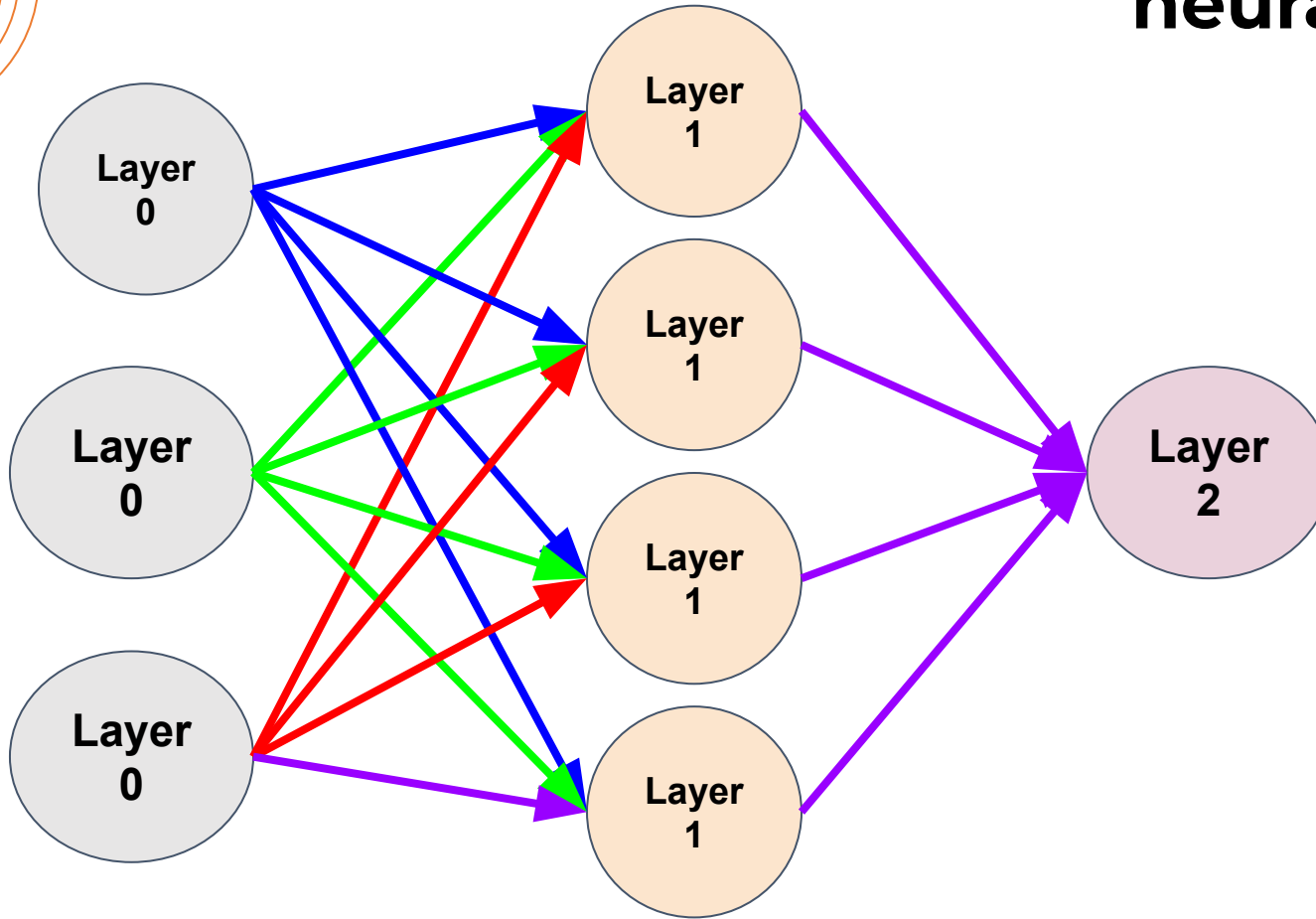
create an intermediate data set



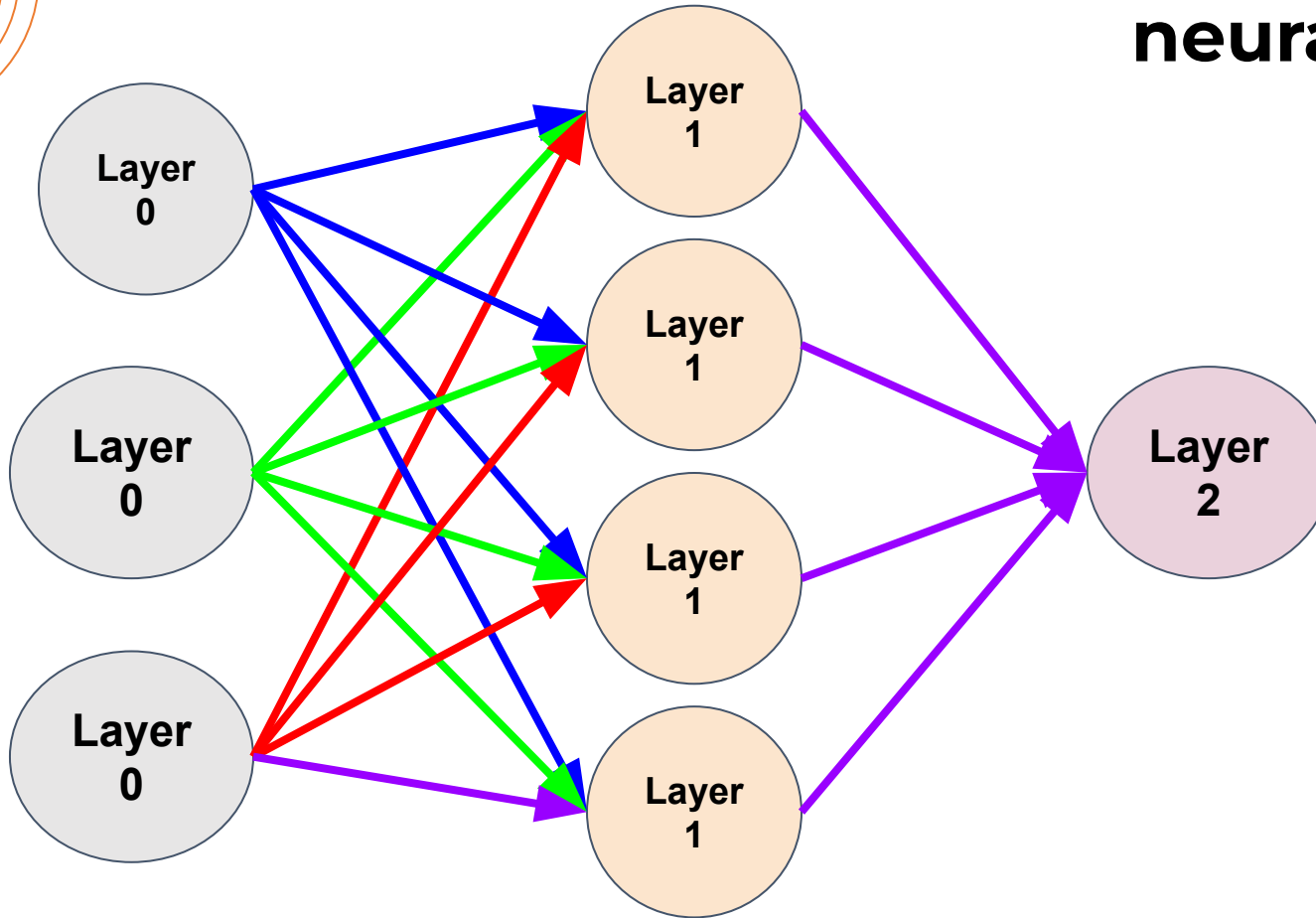
Intermediate Layer



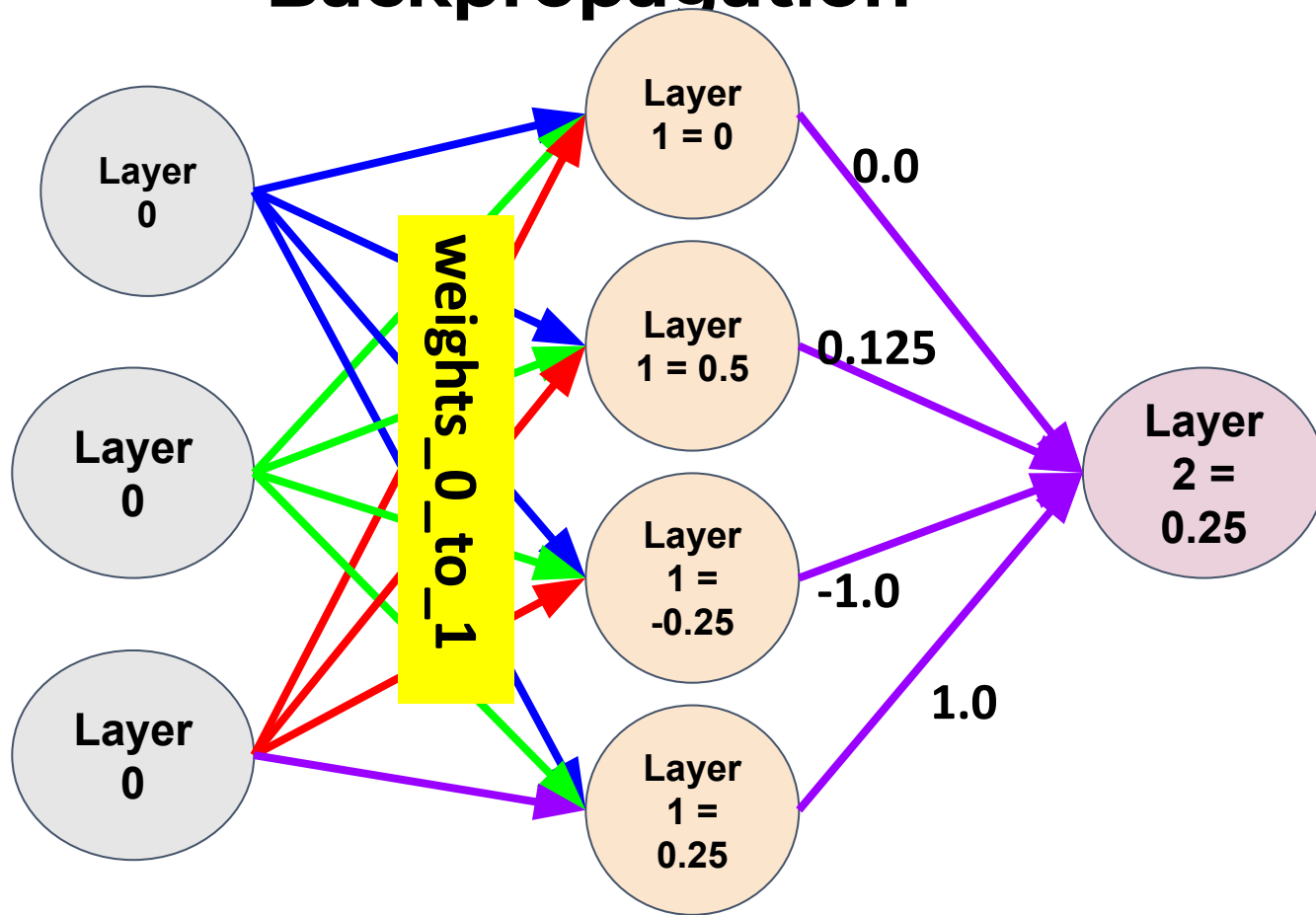
neural networks



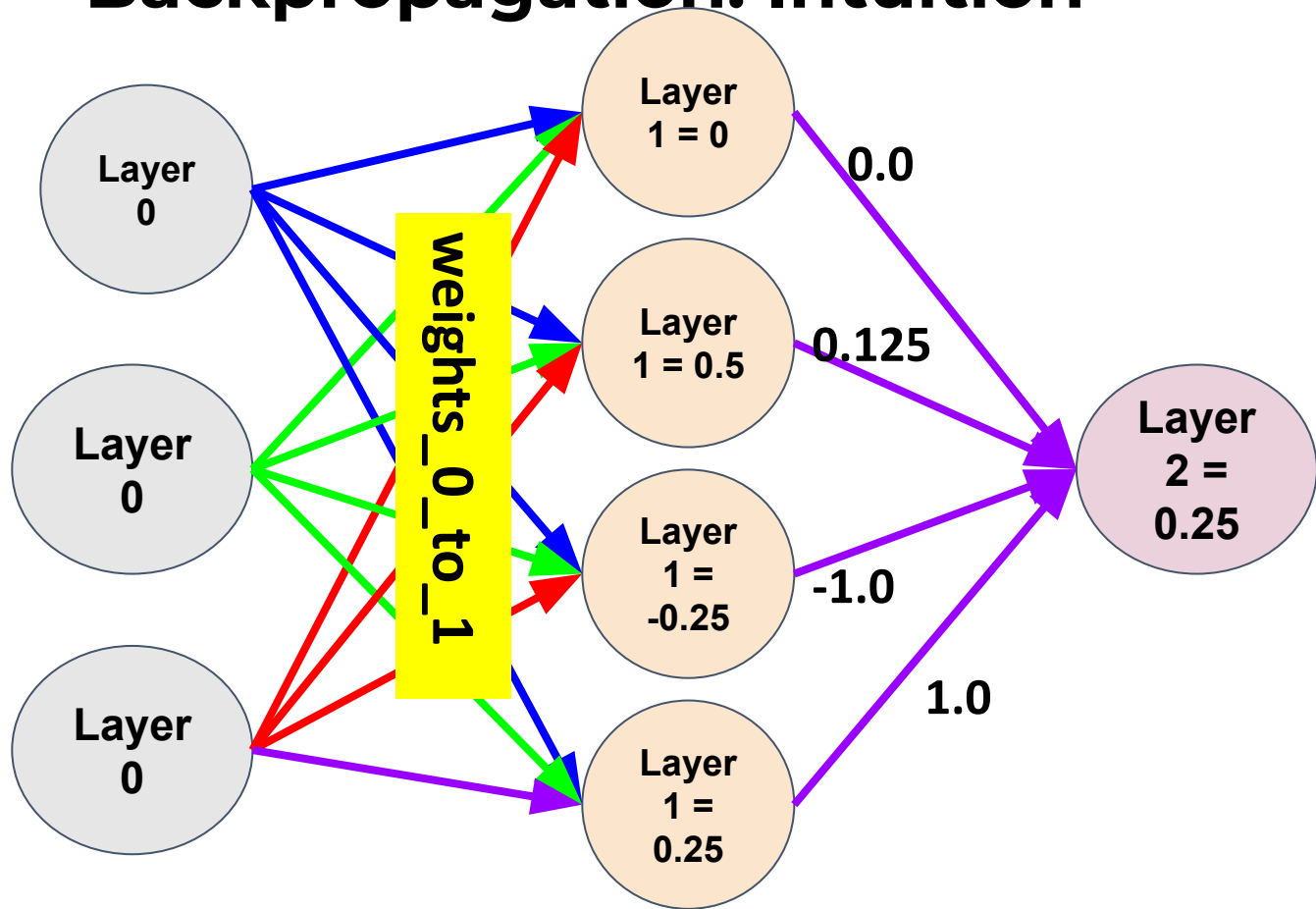
neural networks



Backpropagation



Backpropagation: Intuition



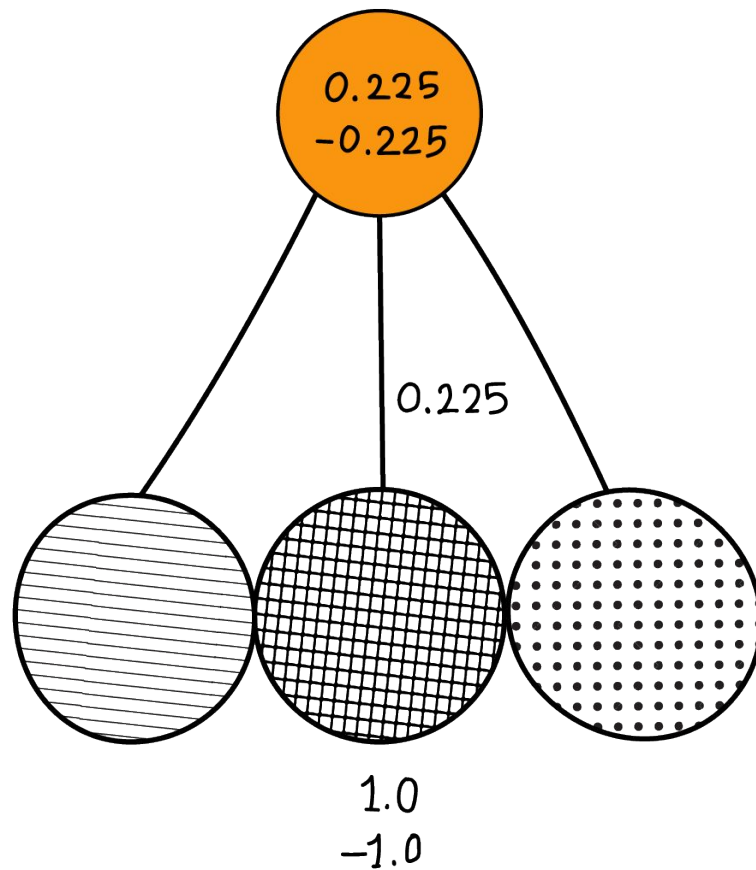
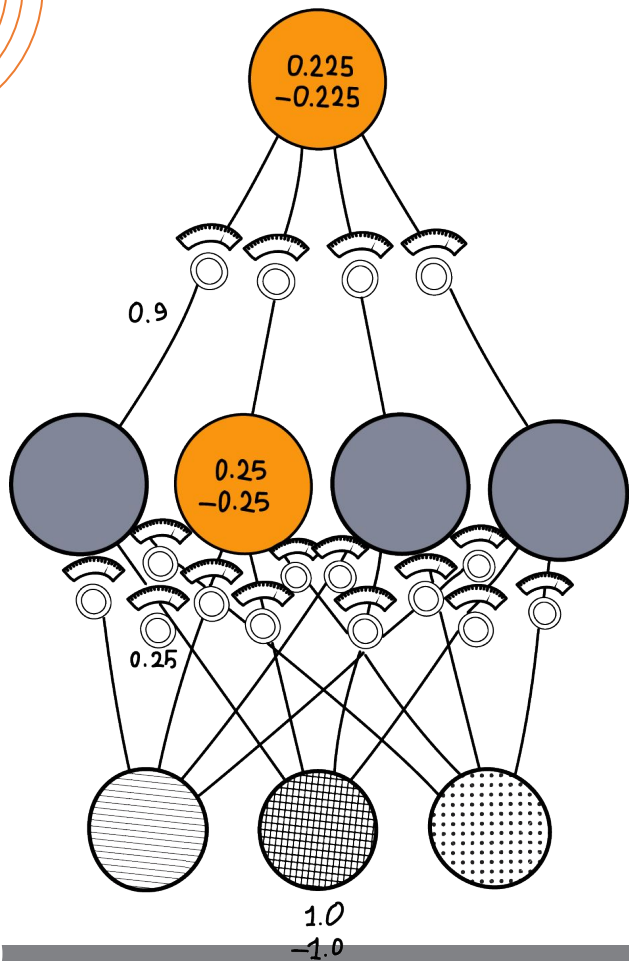


Linear vs. nonlinear

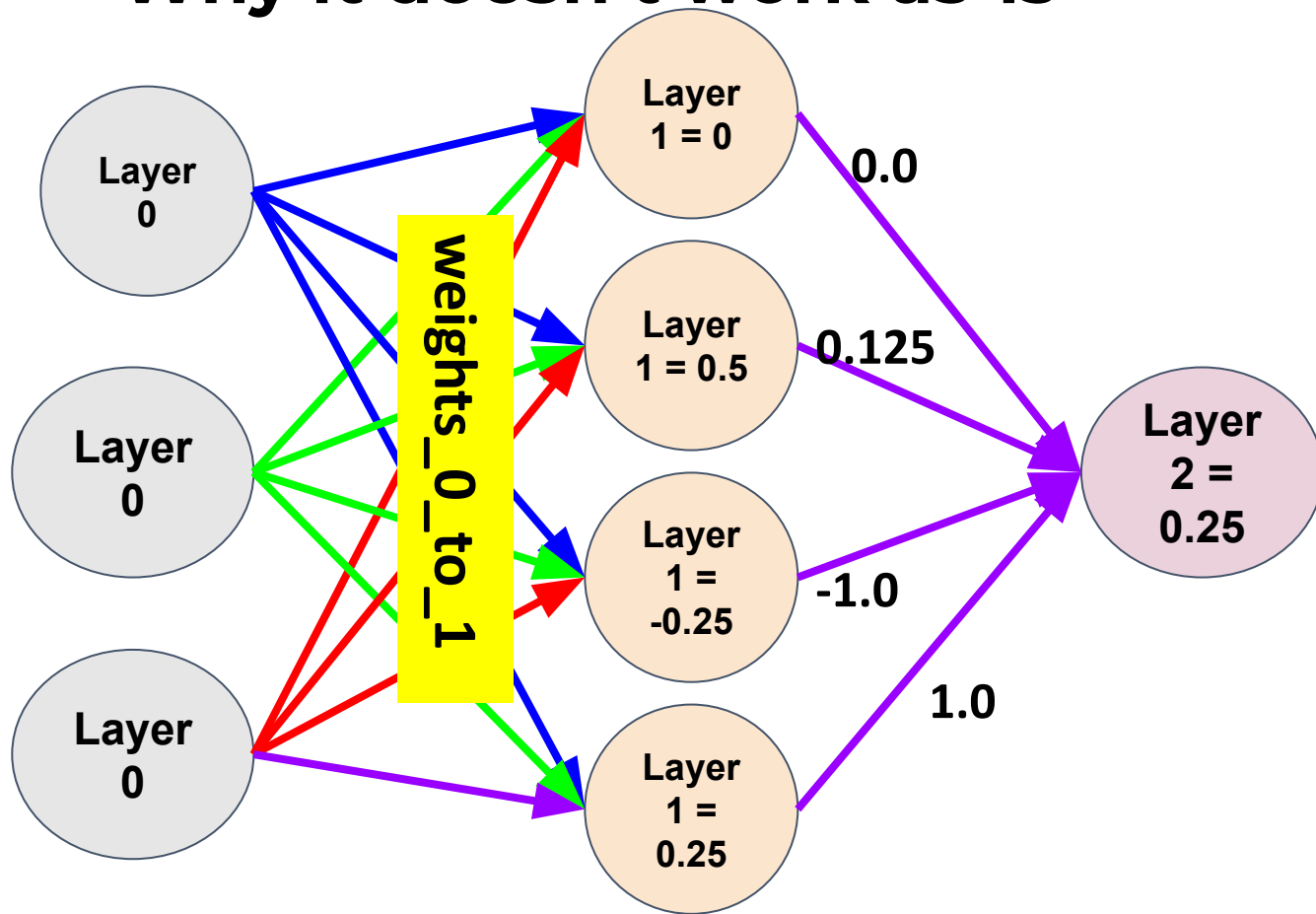
$$12 \times 1 = \mathbf{12} = 2 \times 5 \times 1.2$$

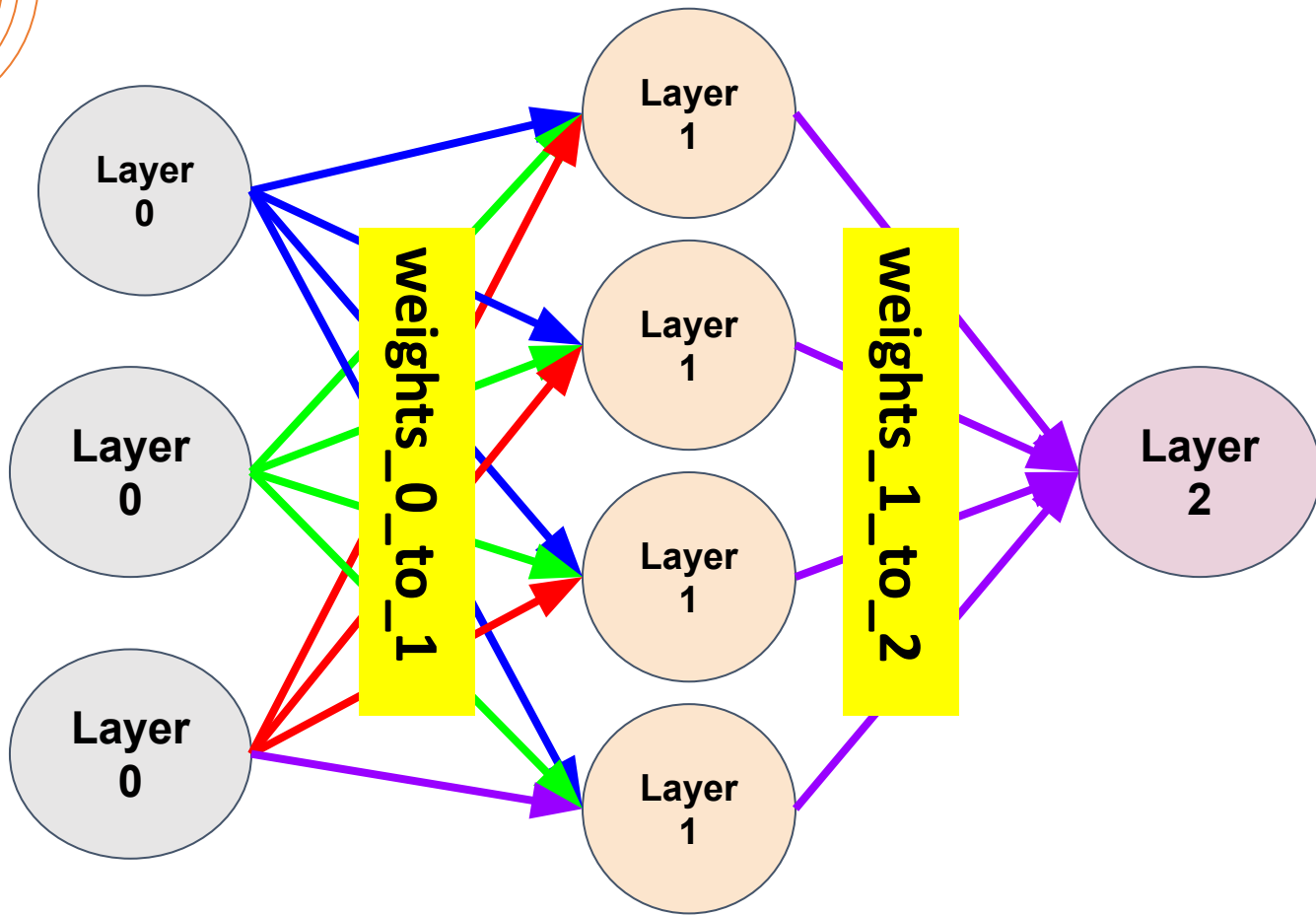
$$6 \times 2 = \mathbf{12} = 9 \times .25 \times 4$$

$$3 \times 4 = \mathbf{12} = 6 \times .5 \times 4$$

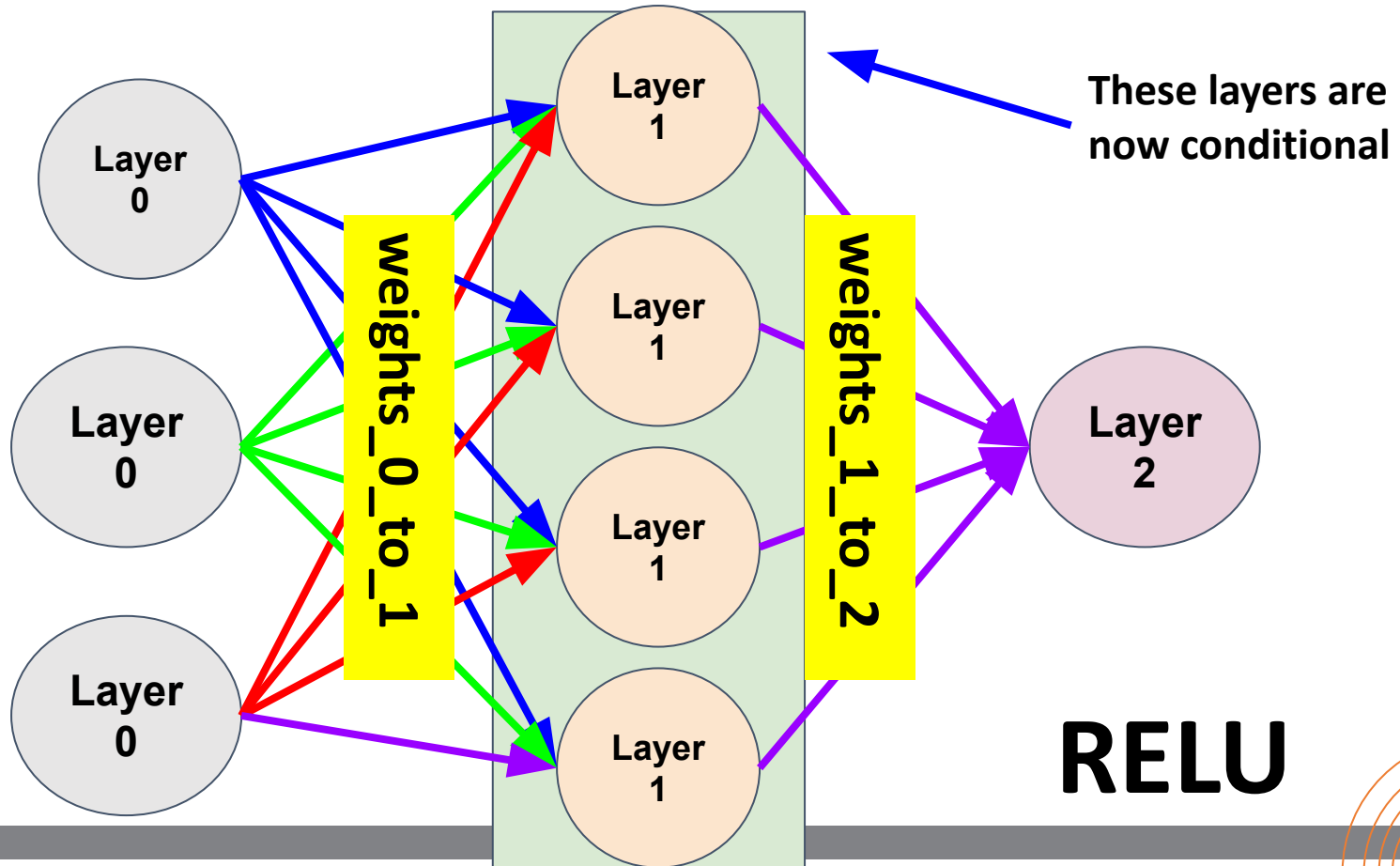


Why it doesn't work as-is





The Insight





ABSORB



Why do deep networks matter?

- No individual pixel correlates with whether there's a dog in the picture.
- Only different configurations of pixels correlate with whether Daisy is in the picture.

