

Lesson 3 Introduction to neural prediction: forward propagation





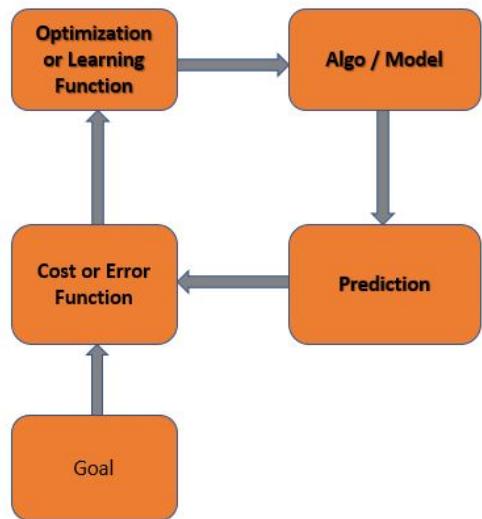
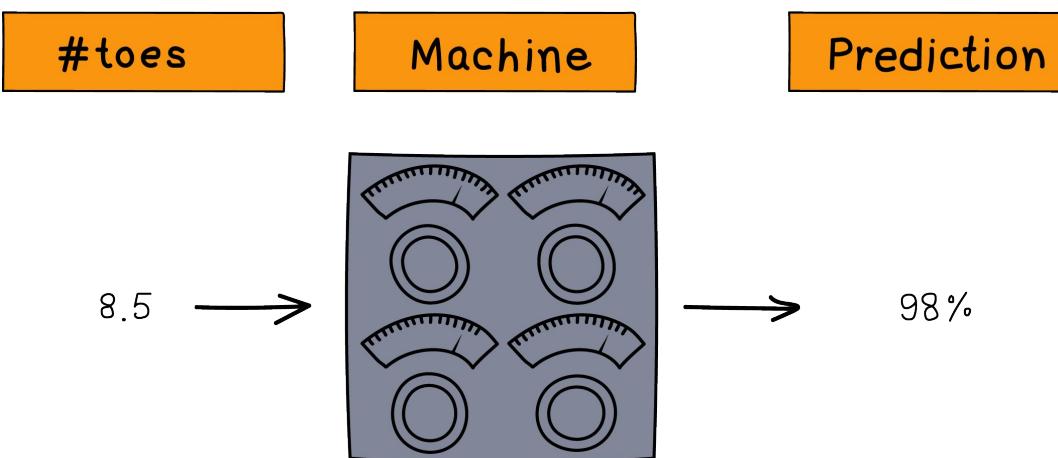
Forward propagation

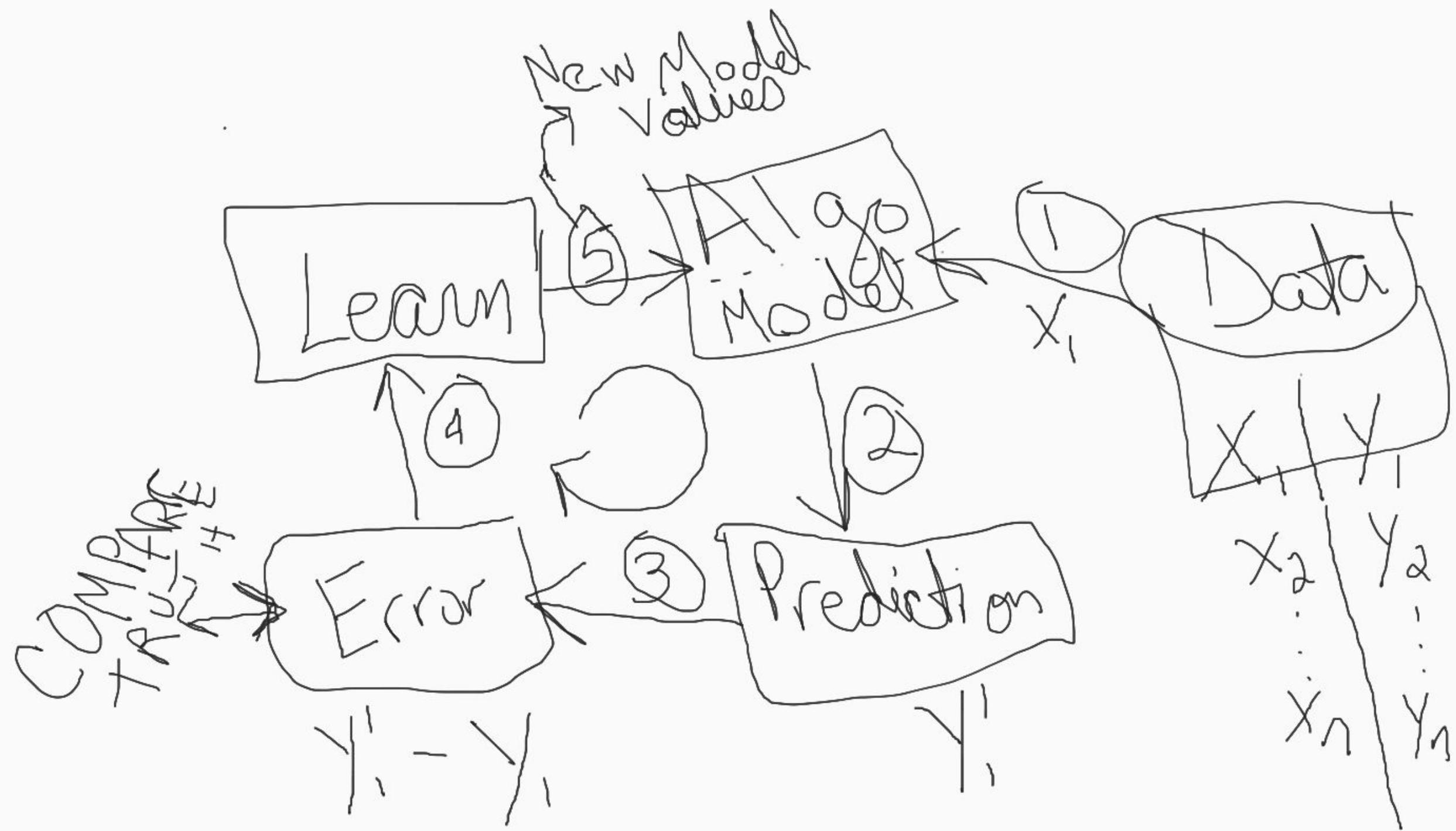


In this lesson we learn

- A simple network making a prediction
- What is a neural network, and what does it do?
- Making a prediction with multiple inputs
- Making a prediction with multiple outputs
- Making a prediction with multiple inputs and outputs
- Predicting on predictions

Forward propagation





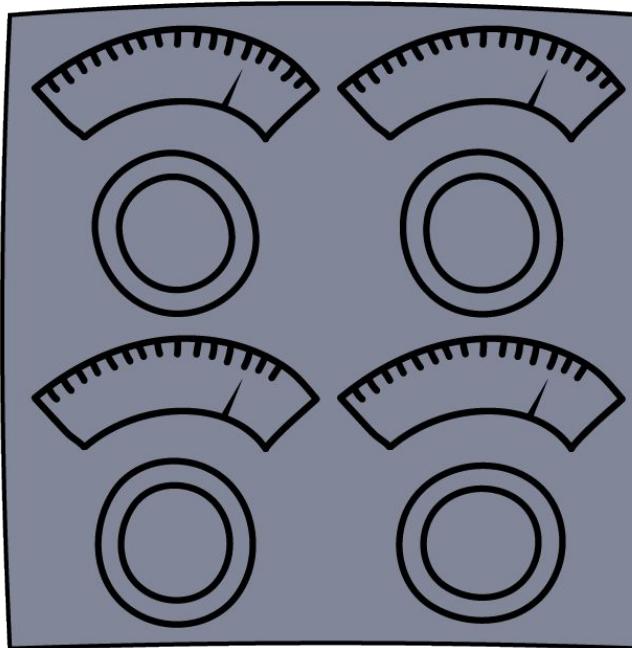
Forward propagation

- # Asking Price

Machine

Selling probability

8.5

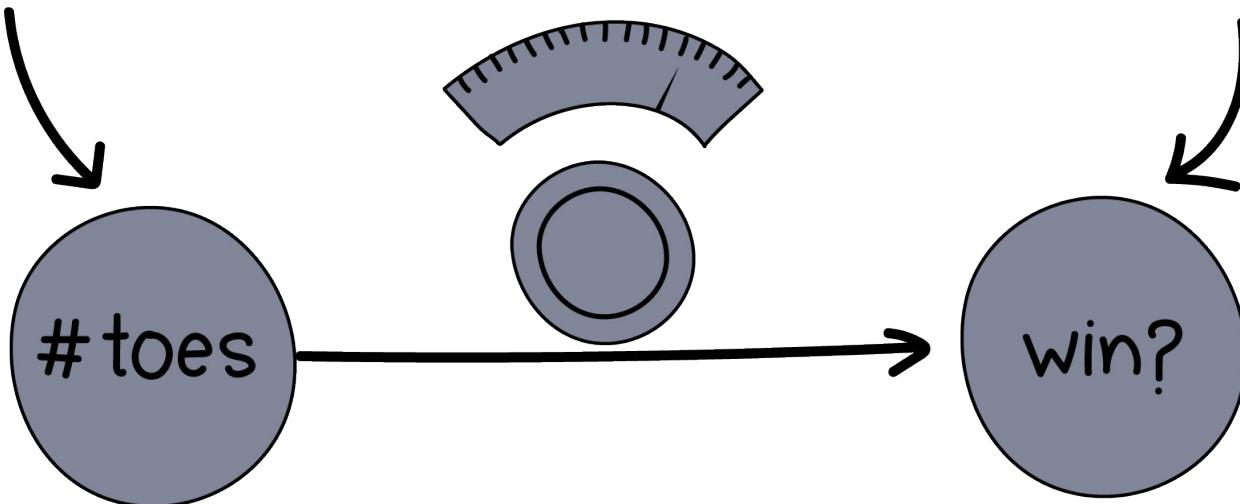


98 %

Forward propagation

① An empty network

Input data
enters here.



Predictions
come out here.



A simple neural network making a prediction





What is a neural network?



```
# The network:  
weight = 0.2  
def neural_network(input, weight):  
    prediction = input * weight  
    return prediction
```



What is a neural network?



```
# How we use the network to predict something:  
number_of_bedrooms = [3, 2, 4, 3, 5]  
input = number_of_bedrooms[0]  
pred = neural_network(input,weight)  
print(pred)
```



What does this neural network do?

-



What does this neural network do?



-



What does this neural network do?

-



What does this neural network do?

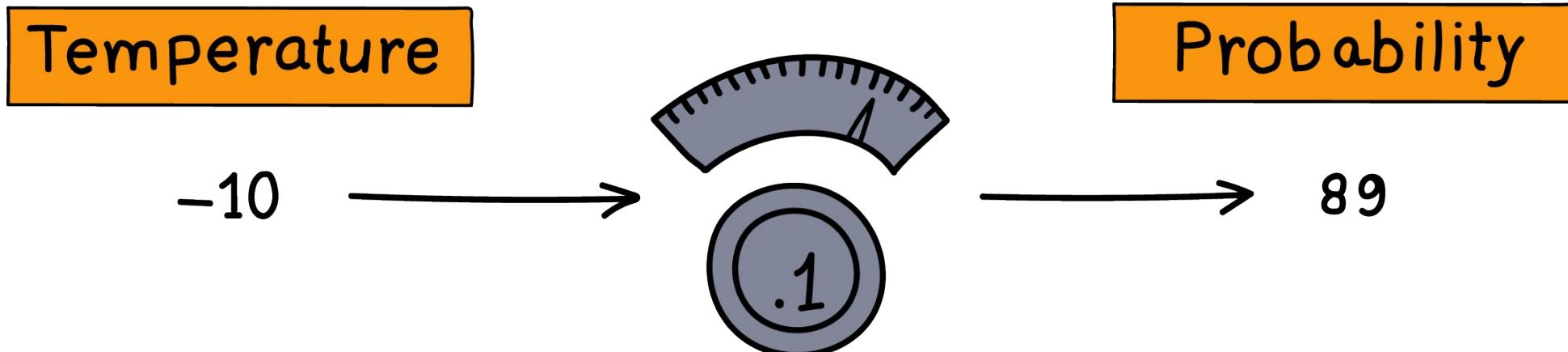




What does this neural network do?



What does this neural network do?



Making a prediction with multiple inputs

-



Making a prediction with multiple inputs



- Take a look at the next prediction:



Making a prediction with multiple inputs





Making a prediction with multiple inputs





Multiple inputs: What does this neural network do?



-



Multiple inputs: What does this neural network



Multiple inputs: What does this neural network do?

-

Multiple inputs: What does this neural network do?





Multiple inputs: What does this neural network do?

-



Multiple inputs: What does this neural network do?

-

```
a = [ 0, 1, 0, 1]
b = [ 1, 0, 1, 0]
c = [ 0, 1, 1, 0]
d = [.5, 0, .5, 0]
e = [ 0, 1, -1, 0]
```

```
w_sum(a,b) = 0
w_sum(b,c) = 1
w_sum(b,d) = 1
w_sum(c,c) = 2
w_sum(d,d) = .5
w_sum(c,e) = 0
```

Multiple inputs: What does this neural network do?

- These assume you're performing `w_sum(input,weights)` and the "then" to these if statements is an abstract "then give high score":

```
weights = [ 1, 0, 1] => if input[0] OR input[2]
weights = [ 0, 0, 1] => if input[2]
weights = [ 1, 0, -1] => if input[0] OR NOT input[2]
weights = [ -1, 0, -1] => if NOT input[0] OR NOT input[2]
weights = [ 0.5, 0, 1] => if BIG input[0] or input[2]
```



Multiple inputs: What does this neural network do?



Multiple inputs: Complete runnable code

- The code snippets from this example come together in the following code, which creates and executes a neural network.

```
weights = [0.2, 0.01, 0.2, -0.2]
```

```
def neural_network(input, weights):  
    pred = w_sum(input,weights)  
    return pred
```

```
bedrooms = [3, 2, 4, 3, 5]
```

```
bathrooms = [1, 1, 3, 2, 4]
```

```
floors = [1, 1, 2, 2, 1]
```

```
condition = [0.48, 0.85, 0.56, 0.2, 0.1]
```

Input corresponds to the first house

```
input = [bedrooms[0], bathrooms[0], floors[0], condition[0]]  
pred = neural_network(input,weights)  
print(pred)
```

Multiple inputs: Complete runnable code

```
import numpy as np
weights = np.array([0.2, 0.01, 0.2, -0.2])
def neural_network(input, weights):
    pred = input.dot(weights)
    return pred

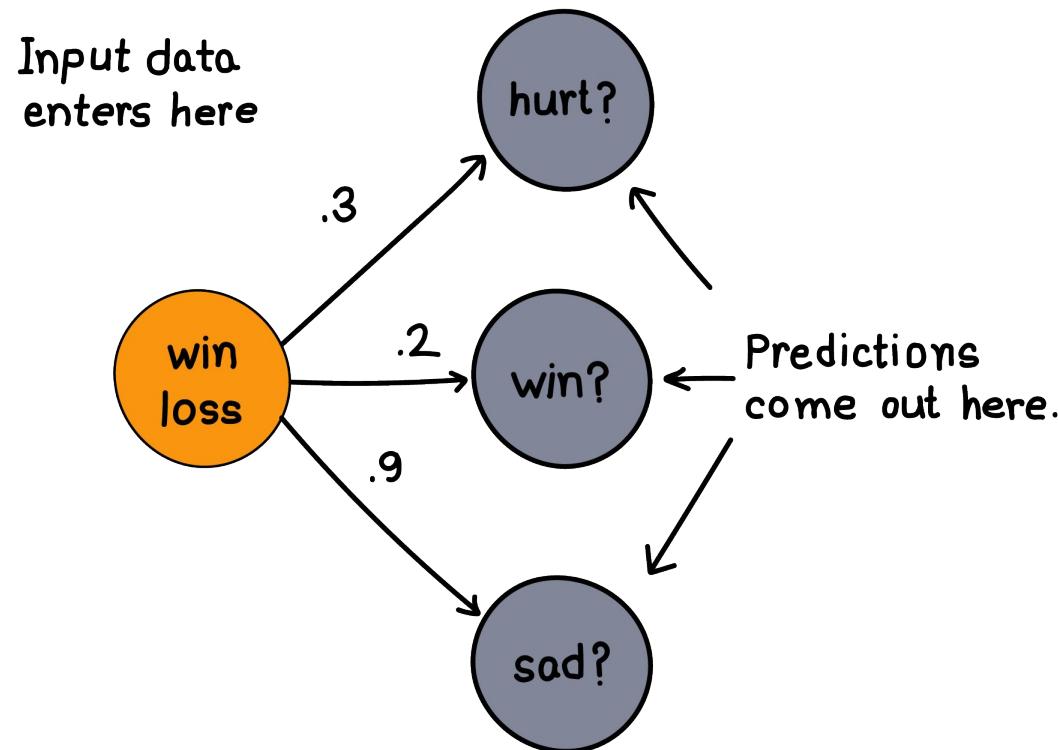
bedrooms = np.array([3, 2, 4, 3, 5])
bathrooms = np.array([1, 1, 3, 2, 4])
floors = np.array([1, 1, 2, 2, 1])
condition = np.array([0.48, 0.85, 0.56, 0.2, 0.1])

# Input corresponds to the first house in the dataset.
input = np.array([bedrooms[0], bathrooms[0], floors[0], condition[0]])
pred = neural_network(input,weights)
print(pred)
```

Making a prediction with multiple outputs

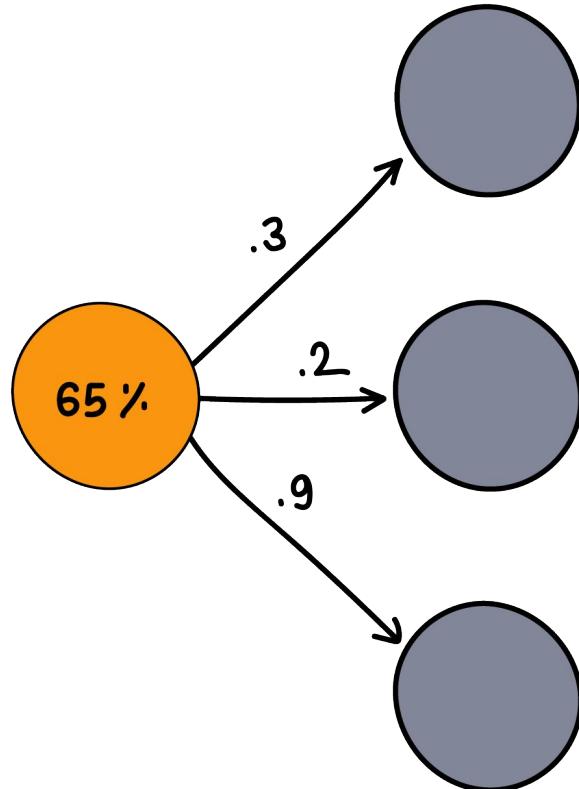
Neural networks can also make multiple predictions using only a single input.

① An empty network with multiple outputs



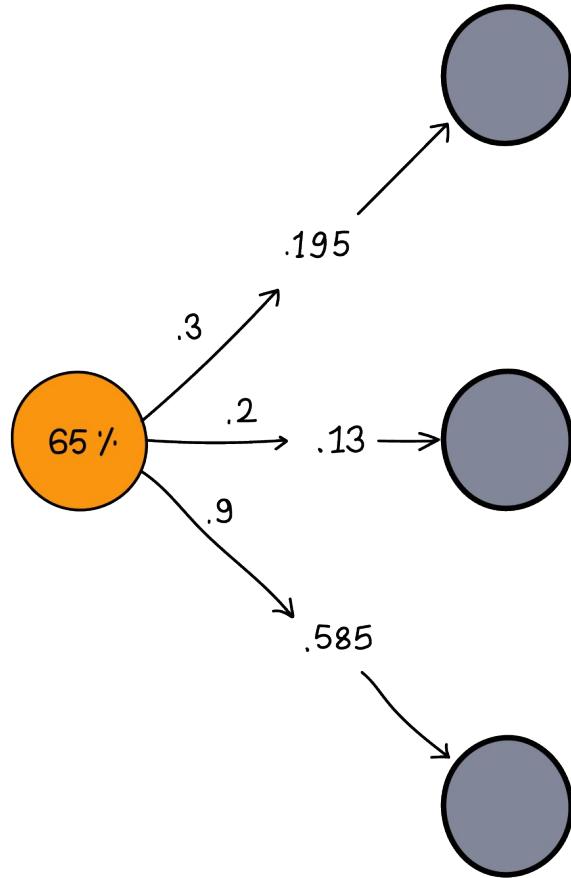
Making a prediction with multiple outputs

② Inserting one input datapoint



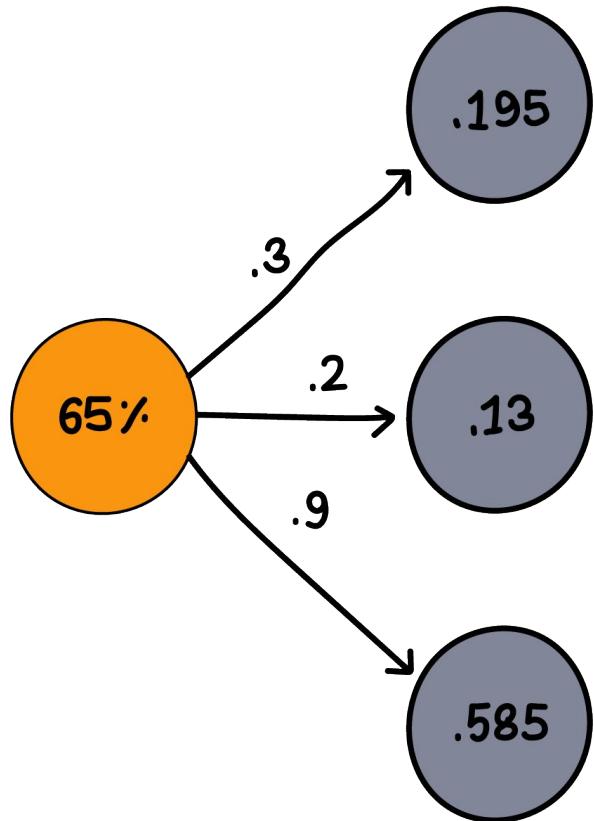
Making a prediction with multiple outputs

③ Performing elementwise multiplication



Making a prediction with multiple outputs

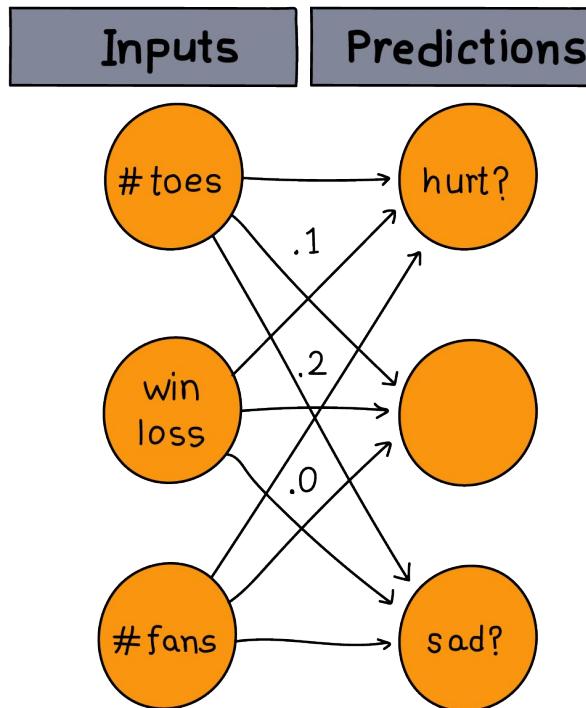
④ Depositing predictions



Predicting with multiple inputs and outputs

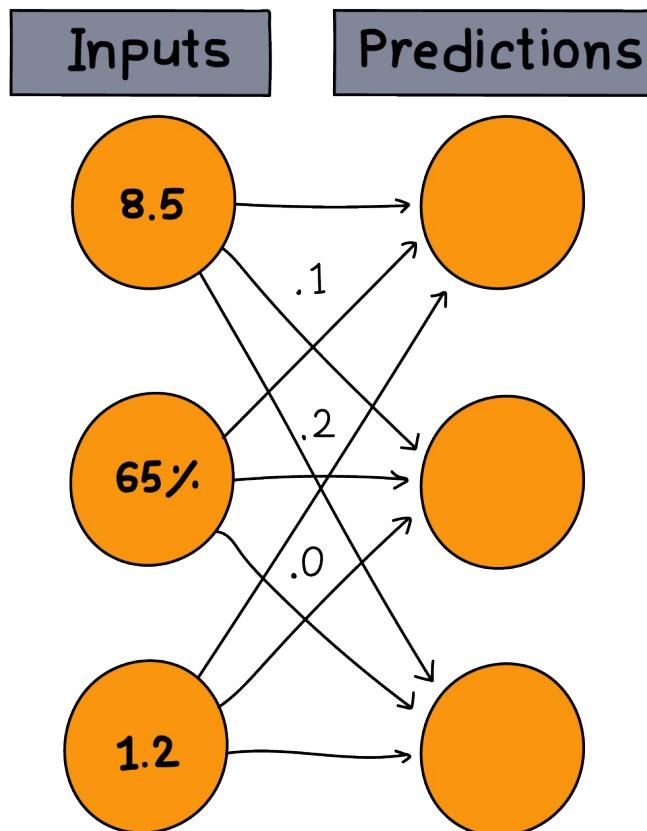
Neural networks can predict multiple outputs given multiple inputs

① An empty network with multiple inputs and outputs

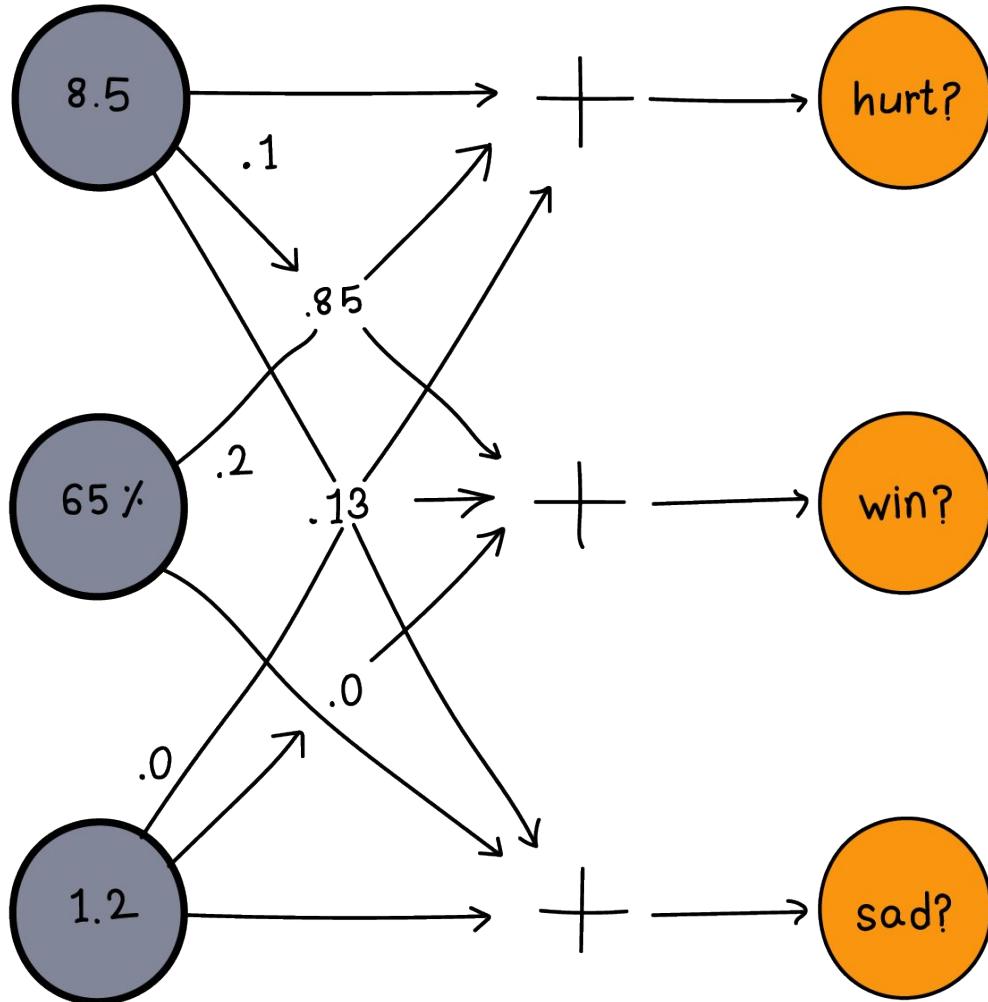


Predicting with multiple inputs and outputs

② Inserting one input datapoint

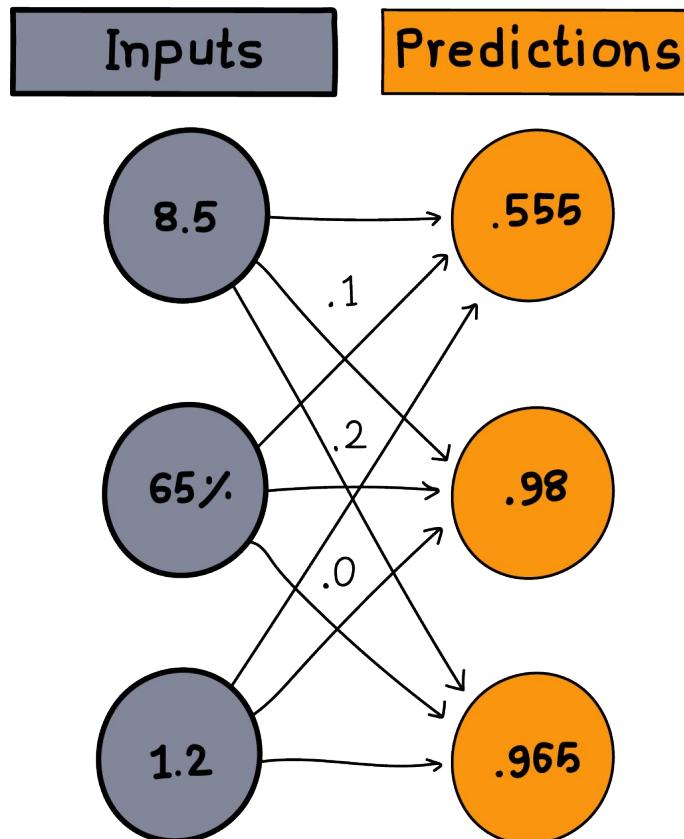


③ For each output, performing a weighted sum of inputs



Predicting with multiple inputs and outputs

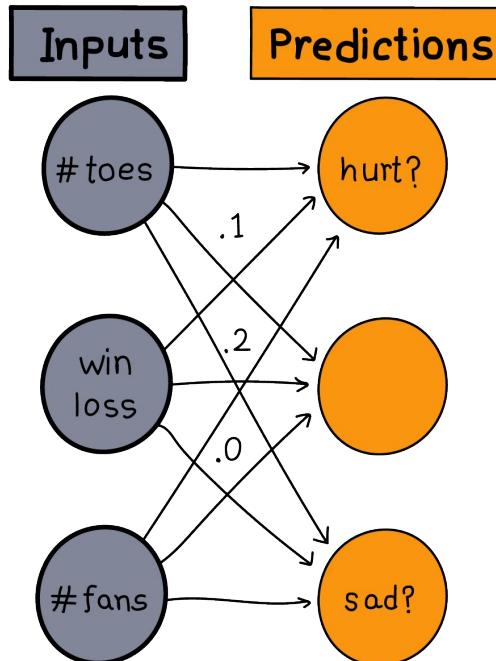
Depositing predictions



Multiple inputs and outputs: How does it work?

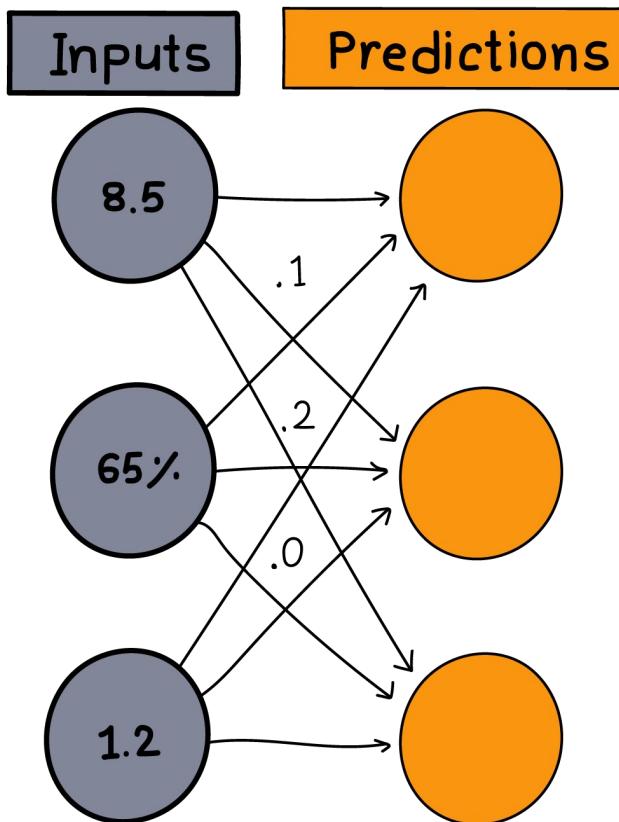
It performs three independent weighted sums of the input to make three predictions.

① An empty network with multiple inputs and outputs

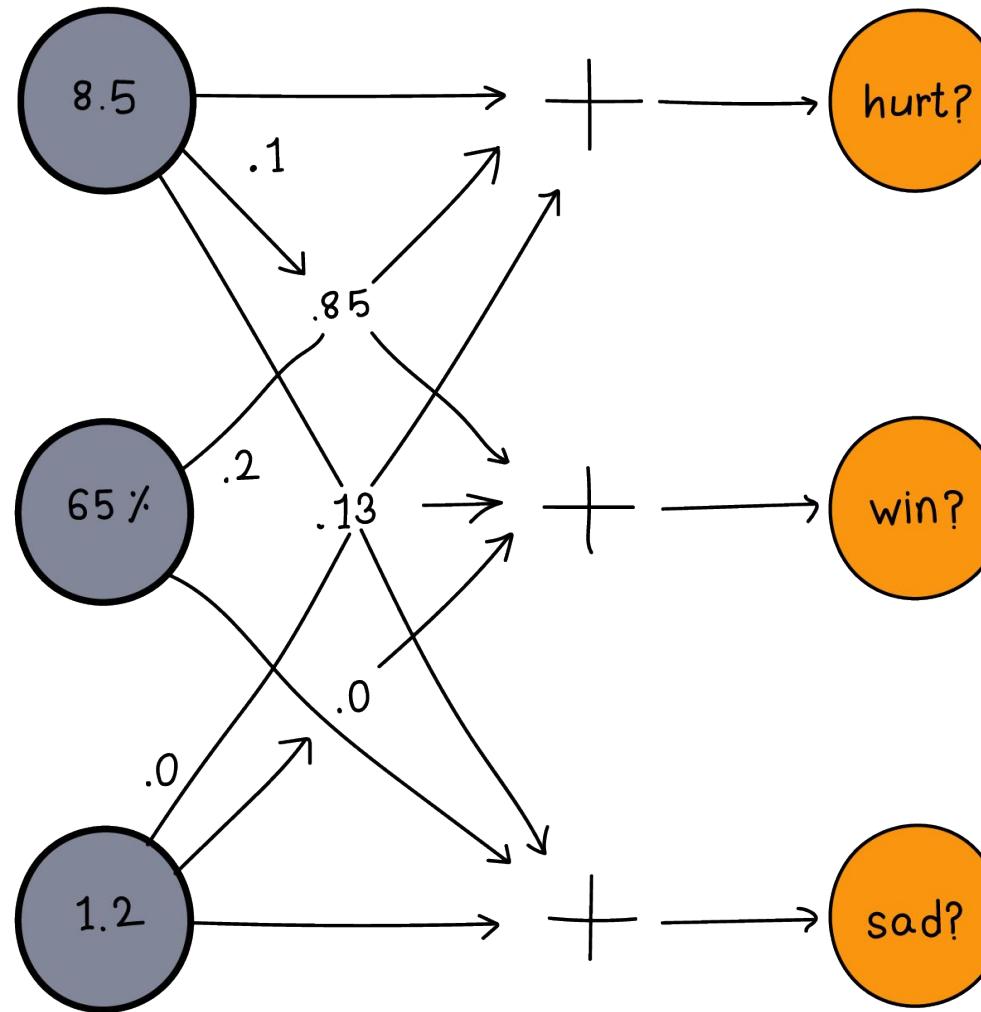


Multiple inputs and outputs: How does it work?

② Inserting one input datapoint



③ For each output, performing a weighted sum of inputs



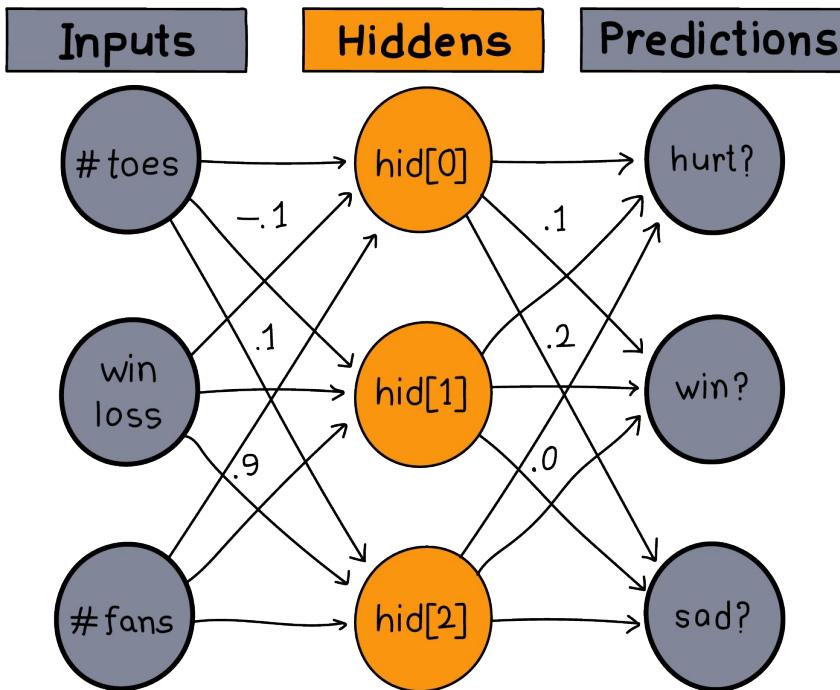
Multiple inputs and outputs: How does it work?

-

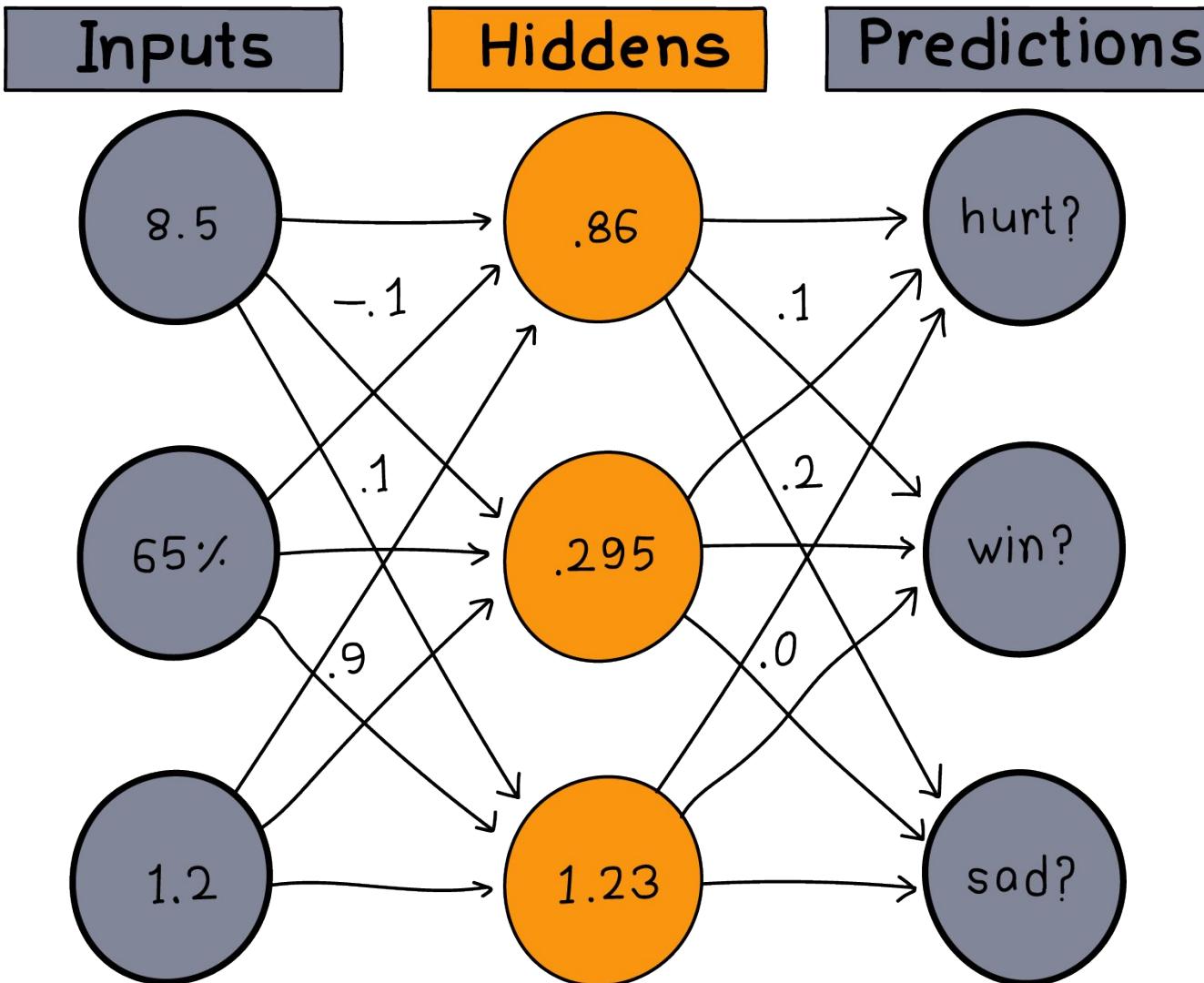
Predicting on predictions

Neural networks can be stacked!

① An empty network with multiple inputs and outputs

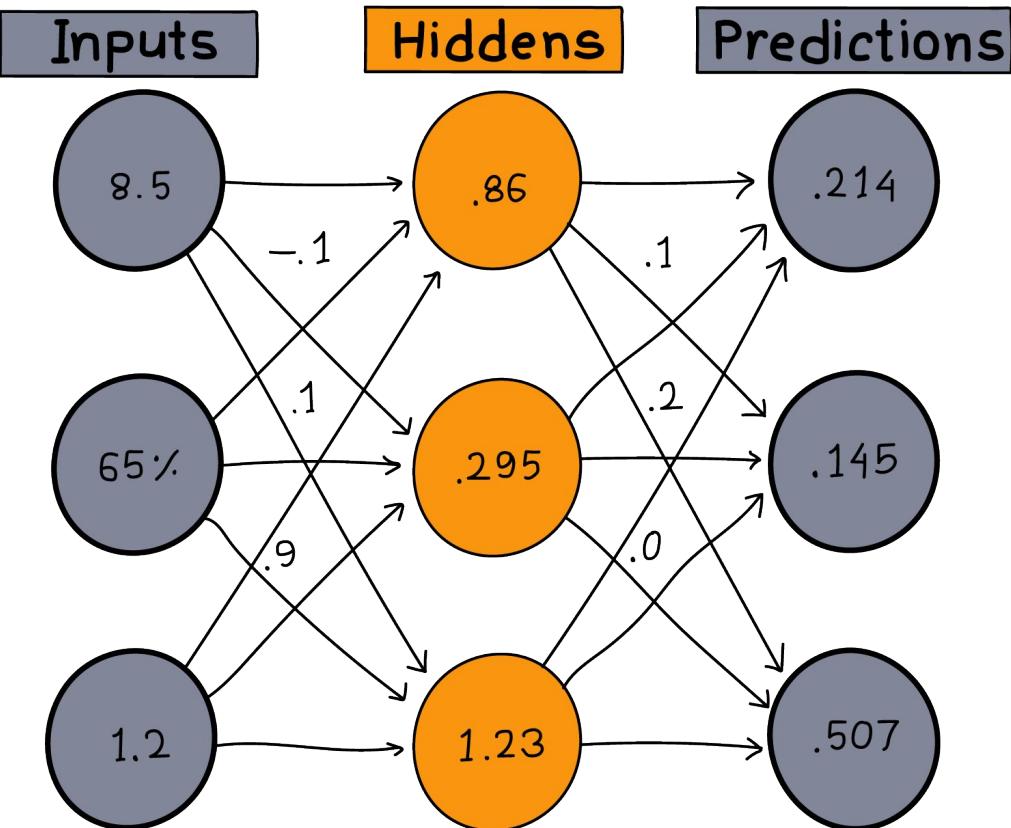


② Predicting the hidden layer



Predicting on predictions

Predicting the output layer (and depositing the prediction)





```
import numpy as np

# toes % win # fans
ih_wgt = np.array([
    [0.1, 0.2, -0.1], # hid[0]
    [-0.1, 0.1, 0.9], # hid[1]
    [0.1, 0.4, 0.1]]).T # hid[2]

# hid[0] hid[1] hid[2]
hp_wgt = np.array([
    [0.3, 1.1, -0.3], # hurt?
    [0.1, 0.2, 0.0], # win?
    [0.0, 1.3, 0.1]]).T # sad?

weights = [ih_wgt, hp_wgt]

def neural_network(input, weights):

    hid = input.dot(weights[0])
    pred = hid.dot(weights[1])
    return pred

toes = np.array([8.5, 9.5, 9.9, 9.0])
wlrec = np.array([0.65, 0.8, 0.8, 0.9])
nfans = np.array([1.2, 1.3, 0.5, 1.0])

input = np.array([toes[0], wlrec[0], nfans[0]])

pred = neural_network(input, weights)
print(pred)
```

NumPy version



A quick primer on NumPy

NumPy does a few things for you. Let's reveal the magic.

- You've also learned about different operations that occur on vectors and matrices, including dot products, elementwise multiplication and addition, and vector-matrix multiplication.
- For these operations, you've written Python functions that can operate on simple Python list objects.



A quick primer on NumPy



- You can create vectors and matrices in multiple ways in NumPy.
- Most of the common techniques for neural networks are listed in the previous code.

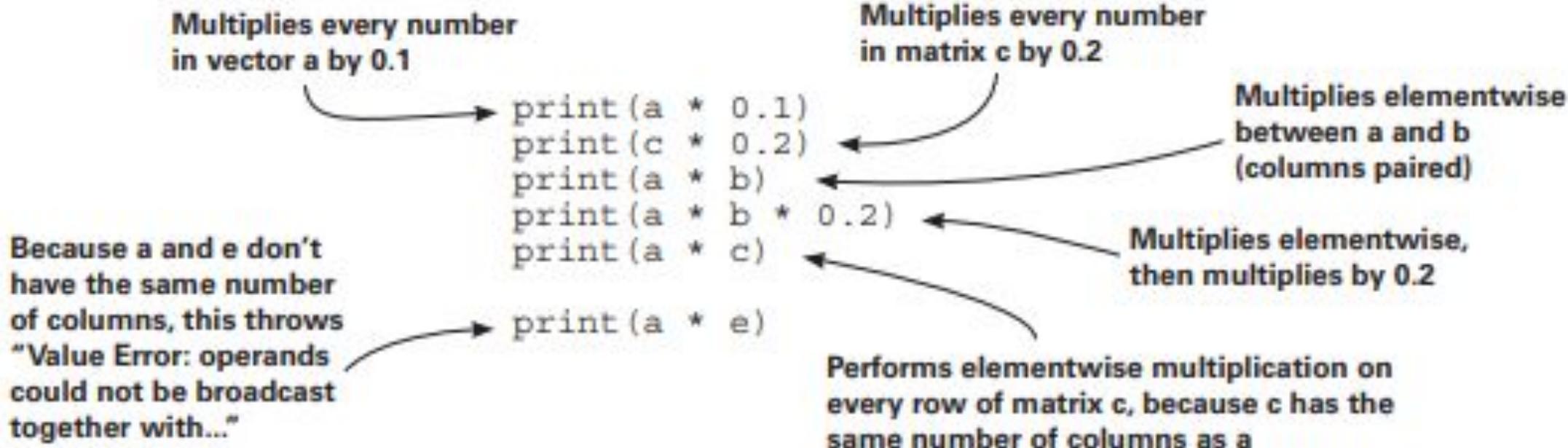
A quick primer on NumPy

```
import numpy as np  
  
a = np.array([0,1,2,3])           ← A vector  
b = np.array([4,5,6,7])           ← Another vector  
c = np.array([[0,1,2,3],  
             [4,5,6,7]])          ← A matrix  
  
d = np.zeros((2,4))              ← 2 × 4 matrix  
e = np.random.rand(2,5)           ← of zeros  
  
print(a)  
print(b)  
print(c)  
print(d)  
print(e)
```

Output

```
[0 1 2 3]  
[4 5 6 7]  
[[0 1 2 3]  
 [4 5 6 7]]  
[[ 0.  0.  0.  0.]  
 [ 0.  0.  0.  0.]]  
[[ 0.22717119  0.39712632  
  0.0627734   0.08431724  
  0.53469141]  
 [ 0.09675954  0.99012254  
  0.45922775  0.3273326  
  0.28617742]]
```

A quick primer on NumPy





A quick primer on NumPy

- The general rule of thumb for anything elementwise (+, -, *, /) is that either the two variables must have the same number of columns, or one of the variables must have only one column.
 - For example, `print(a * 0.1)` multiplies a vector by a single number (a scalar). NumPy says, “Oh, I bet I’m supposed to do vector-scalar multiplication here,” and then multiples the scalar (0.1) by every value in the vector.
 - This looks exactly the same as `print(c * 0.2)`, except NumPy knows that `c` is a matrix.
- 



A quick primer on NumPy



- Again, the most confusing part is that all of these operations look the same if you don't know which variables are scalars, vectors, or matrices.
- When you “read NumPy,” you’re really doing two things: reading the operations and keeping track of the shape (number of rows and columns) of each operation.

A quick primer on NumPy

- Let's look at a few examples of matrix multiplication in NumPy, noting the input and output shapes of each matrix.

```
a = np.zeros((1,4))
b = np.zeros((4,3))

c = a.dot(b)           ← Vector of length 4
print(c.shape)         ← Matrix with
                        4 rows and
                        3 columns

Output
(1, 3)
```

```
a = np.zeros( (2, 4)) ← Matrix with 2 rows  
b = np.zeros( (4, 3)) ← and 4 columns  
  
c = a.dot(b) ← Matrix with 4 rows  
print(c.shape) ← and 3 columns Outputs (2,3)  
  
e = np.zeros( (2, 1)) ← Matrix with 2 rows and 1 column  
f = np.zeros( (1, 3)) ← Matrix with 1 row and 3 columns  
  
g = e.dot(f)  
print(g.shape) ← Outputs (2,3)  
← Throws an error; .T flips the rows and columns of a matrix.  
  
h = np.zeros( (5, 4)).T ← Matrix with 4 rows and 5 columns  
i = np.zeros( (5, 6)) ← Matrix with 6 rows and 5 columns  
  
j = h.dot(i)  
print(j.shape) ← Outputs (4,6)  
← Matrix with 5 rows and 4 columns  
  
h = np.zeros( (5, 4)) ← Matrix with 5 rows and 4 columns  
i = np.zeros( (5, 6)) ← Matrix with 5 rows and 6 columns  
j = h.dot(i)  
print(j.shape) ← Throws an error
```



Summary



To predict, neural networks perform repeated weighted sums of the input.

- You've seen an increasingly complex variety of neural networks in this lesson.
 - I hope it's clear that a relatively small number of simple rules are used repeatedly to create larger, more advanced neural networks.
 - The network's intelligence depends on the weight values you give it.
- 