

**TABLE S1:** Seasonality indices used in intercomparison. The variable name “B” can refer to either the annual total of either precipitation (P) or potential evapotranspiration (E),  $b_m$  is the amount in month  $m$  of either P or E.

Abbreviation	Name in original publication	Equation & brief description	Reference
ASI	Asynchronicity index, ASI	$ASI = \sqrt{JS_{obs} - JS_{min}}$ <p>Difference between the observed Jensen-Shannon distance of P and PET at a location and its minimized Jensen-Shannon distance. Ranges [0,1].</p>	This paper, equation (2)
SI	Seasonality index, S	$S = D \cdot \frac{P}{P_{max}}, \quad D = \sum_{m=1}^{12} p_m \log_2 \left( \frac{p_m}{1/12} \right)$ <p>Product of relative entropy D (of monthly rainfall with respect to the uniform distribution) and mean annual rainfall normalized with respect to observed maximum within the stations. Ranges [0,∞].</p>	Feng et al. (2013), equation (1)
Imr	Moisture index seasonality, $I_{m,r}$	$I_{m,r} = \max(MI(t)) - \min(MI(t)), \quad MI(t) = \begin{cases} 1 - \frac{E(t)}{P(t)} & , P(t) > E(t) \\ 0 & , P(t) = E(t) \\ \frac{E(t)}{P(t)} - 1 & , P(t) < E(t) \end{cases}$ <p>Range [0, 2]. 0 indicates no intra-annual changes in the water/energy budget, and 2 indicates the climate switches between fully arid and fully saturated within a single year</p>	Knoben et al. (2018), equations (1) and (3)
dP*	Seasonality of precipitation in relation to seasonality of temperature, $\delta_p^*$	$\delta_p^* = \delta_p \cos(2\pi(s_p - s_E)/\tau)$ <p><math>\delta_p</math> is the normalized amplitude of the seasonal precipitation signal, approximated here by <math>\delta_p = \frac{\max(p_m) - \min(p_m)}{2P}</math> to avoid assuming sinusoidality. <math>s_p</math> and <math>s_E</math> are the phases of the precipitation and PET, approximated by <math>s_B = \text{argmax}(b_m)</math>. Value of <math>\delta_p^*</math> ranges from -1 (winter dominant P) through 0 (uniform P) to 1 (summer dominant P).</p>	Woods (2009), equation (14)
WalshS	Seasonality index (for relative seasonality), SI	$SI = \frac{1}{P} \sum_{m=1}^{12} \left  r_m - \frac{P}{12} \right $ <p>Sum of the absolute deviations of mean monthly rainfalls from the overall monthly mean, divided by the mean annual rainfall. Ranges [0,∞].</p>	Walsh & Lawler (1981)
dCentroid	Difference of centroids, $\Delta\tau$	$\Delta\tau = \tau_P - \tau_E, \quad \tau_B = \frac{1}{B} \sum_{m=1}^{12} m b_m$ <p>Difference in the first moments of monthly precipitation and PET distributions. Ranges [0,6]</p>	This paper
MillyS	Seasonality index, S	$S =  \delta_p - \delta_E R $ <p>R is the dryness index, <math>\delta</math> are amplitudes of sinusoidal climatologies for precipitation and PET. The amplitudes are approximated in this paper using <math>\delta_B = \frac{\max(b_m) - \min(b_m)}{2B}</math> to avoid assuming sinusoidality. Ranges [0,∞].</p>	Milly (1994), equation (23)