

电子学基础——第十一次作业

LXQ

2019.12.20

11.4 Construct the Bode plot of $|V_{out}/V_{in}|$ for the stages depicted in Fig. 11-62.

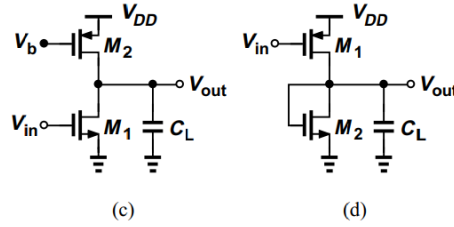


Figure 11-62

解 (c) M_2 电流稳定, 可视为 r_{o1} 电阻。则

$$A_0 = -g_m(r_{o2}/r_{o1}), \omega_p = \frac{1}{r_{o2}C_L}$$

波特图如图 p11-4-c 所示。

(d) M_2 可视为 $\frac{1}{g_{m2}}$, 则有极点 $\omega_p = \frac{g_{m2}}{C_L}$

$$A_0 = -\frac{g_{m1}}{g_{m2}}$$

波特图如图 p11-4-d。

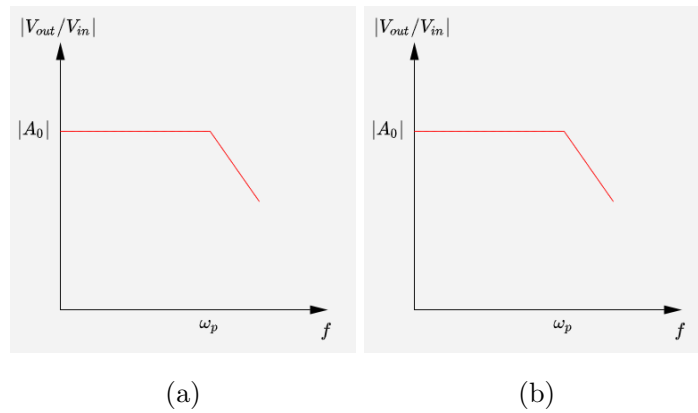


Figure p11-4

11.6 An amplifier exhibits two poles at 100MHz and 10GHz and a zero at 1GHz. Construct the Bode plot of $|V_{out}/V_{in}|$.

解 如图 p11-6 所示。其中三个斜率发生改变的点为 $\omega_{p1} = 100\text{MHz}$, $\omega_z = 1\text{GHz}$, $\omega_{p2} = 10\text{GHz}$ 。

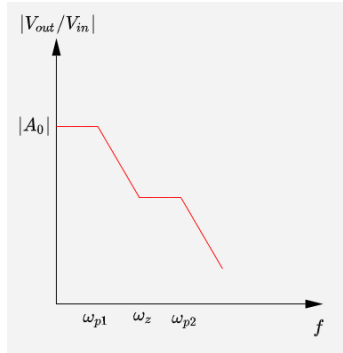


Figure p11-6

11.12 Due to a manufacturing error, a parasitic resistance R_P has appeared in series with the source of M_1 in Fig. 11-65. Assuming $\lambda = 0$ and neglecting other capacitances, determine the input and output poles of the circuit.

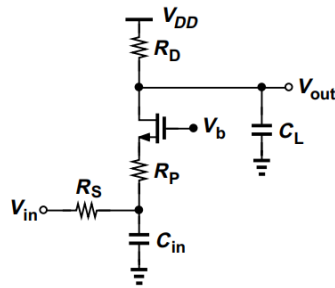


Figure 11-65

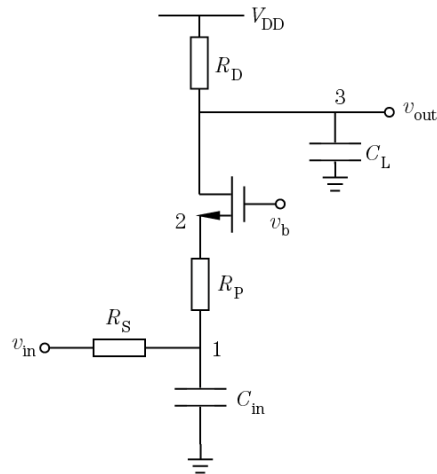


Figure p11-12

解 如图 p11-12 所示。对于节点一，

$$\omega_{p1} = \frac{1}{C_{in}[R_S // (R_P + \frac{1}{g_m})]}$$

节点二仅有分压效果，不产生极点。

对于节点三，

$$\omega_{p2} = \frac{1}{C_L R_D}$$

11.13 Repeat Problem 12 for the circuit shown in Fig. 11-66.

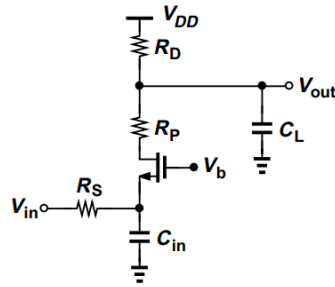


Figure 11-66

解 在输入端，

$$\omega_{p1} = \frac{1}{C_{in}(R_S // \frac{1}{g_m})}$$

在输出端，

$$\omega_{p2} = \frac{1}{C_L(R_D // R_P)}$$

11.14 Repeat Problem 12 for the CS stage depicted in Fig. 11-67.

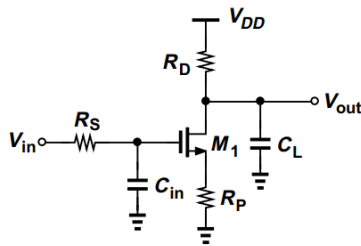


Figure 11-67

解 在输入端，

$$\omega_{p1} = \frac{1}{C_{in} R_S}$$

在输出端，

$$\omega_{p2} = \frac{1}{C_L R_D}$$

11.19 Using Miller's theorem, estimate the input capacitance of the circuit depicted in Fig. 11-71. Assume $\lambda > 0$ but neglect other capacitances. What happens if $\lambda \rightarrow 0$?

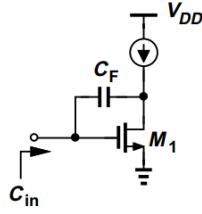


Figure 11-71

解 M_1 内部可看作并联电阻 r_o ，则在小信号电路中可看作 r_o 连接漏端与地，从而可对 C_F 应用密勒定理。

$$C_{in} = (1 + g_m r_o) C_F$$

当 $\lambda \rightarrow 0$ ，则 $C_{in} \rightarrow \infty$

11.38 Assuming $\lambda > 0$ and using Miller's theorem, determine the input and output poles of the stages depicted in Fig. 11-80.

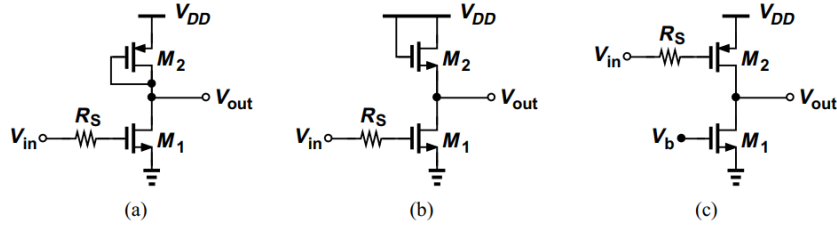


Figure 11-80

解 (a) 画出所有电容的电路以及简化后的电路如图 p11-38-a 所示。其中

$$R_D = \frac{1}{g_{m2}} // r_{o2}$$

$$A_0 = g_{m1} \left(\frac{1}{g_{m2}} // r_{o2} // r_{o1} \right)$$

$$C_{in} = C_{GS1} + C_{GD1} \left(1 + g_{m1} \left(\frac{1}{g_{m2}} // r_{o2} // r_{o1} \right) \right)$$

$$C_{out} = C_{DB1} + C_{DB2} + C_{GS2} + C_{GD1} \left[1 + \frac{1}{g_{m1} \left(\frac{1}{g_{m1}} // r_{o2} // r_{o1} \right)} \right]$$

其中 A_0 为电路低频增益，从而

$$\omega_{p1} = \left[R_S \left[C_{GS1} + C_{GD1} \left(1 + g_{m1} \left(\frac{1}{g_{m2}} // r_{o2} // r_{o1} \right) \right) \right] \right]^{-1}$$

$$\omega_{p2} = \left[\left(\frac{1}{g_{m2}} // r_{o2} \right) \left[C_{DB1} + C_{DB2} + C_{GS2} + C_{GD1} \left(1 + \frac{1}{g_{m1} \left(\frac{1}{g_{m1}} // r_{o2} // r_{o1} \right)} \right) \right] \right]^{-1}$$

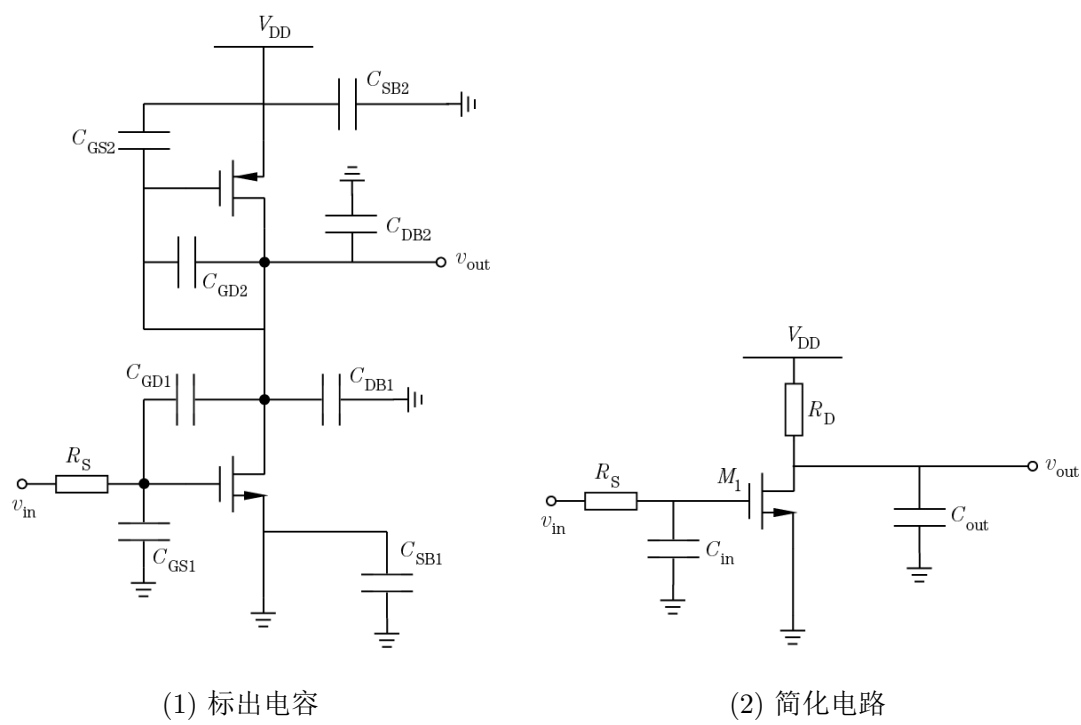


Figure p11-38-a

(b) 画出所有电容后的电路以及简化后的电路如图 p11-38-b 所示。其中

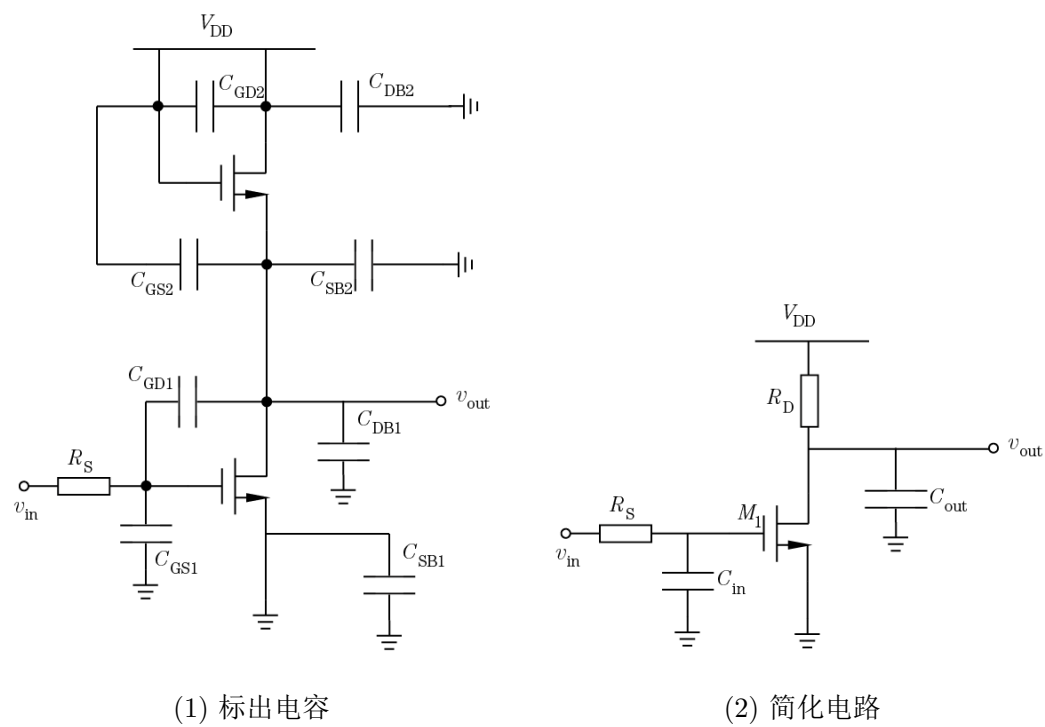


Figure p11-38-b

$$R_D = \frac{1}{g_{m2}} // r_{o2}$$

$$A_0 = g_{m1} \left(\frac{1}{g_{m2}} // r_{o2} // r_{o1} \right)$$

$$C_{in} = C_{GS1} + C_{GD1} \left[1 - g_{m1} \left(\frac{1}{g_{m2}} // r_{o2} // r_{o1} \right) \right]$$

$$C_{out} = C_{DB1} + C_{GS2} + C_{SB2} + C_{GD1} \left[1 - \frac{1}{g_{m1} \left(\frac{1}{g_{m2}} // r_{o2} // r_{o1} \right)} \right]$$

其中 A_0 为电路低频增益，从而

$$\omega_{p1} = \left[R_S \left[C_{GS1} + C_{GD1} \left(1 - g_{m1} \left(\frac{1}{g_{m2}} // r_{o2} // r_{o1} \right) \right) \right] \right]^{-1}$$

$$\omega_{p2} = \left[\left(\frac{1}{g_{m2}} // r_{o2} \right) \left[C_{DB1} + C_{GS2} + C_{SB2} + C_{GD1} \left(1 - \frac{1}{g_{m1} \left(\frac{1}{g_{m2}} // r_{o2} // r_{o1} \right)} \right) \right] \right]^{-1}$$

(c) 画出所有电容后的电路以及简化后的电路如图 p11-38-c 所示。其中

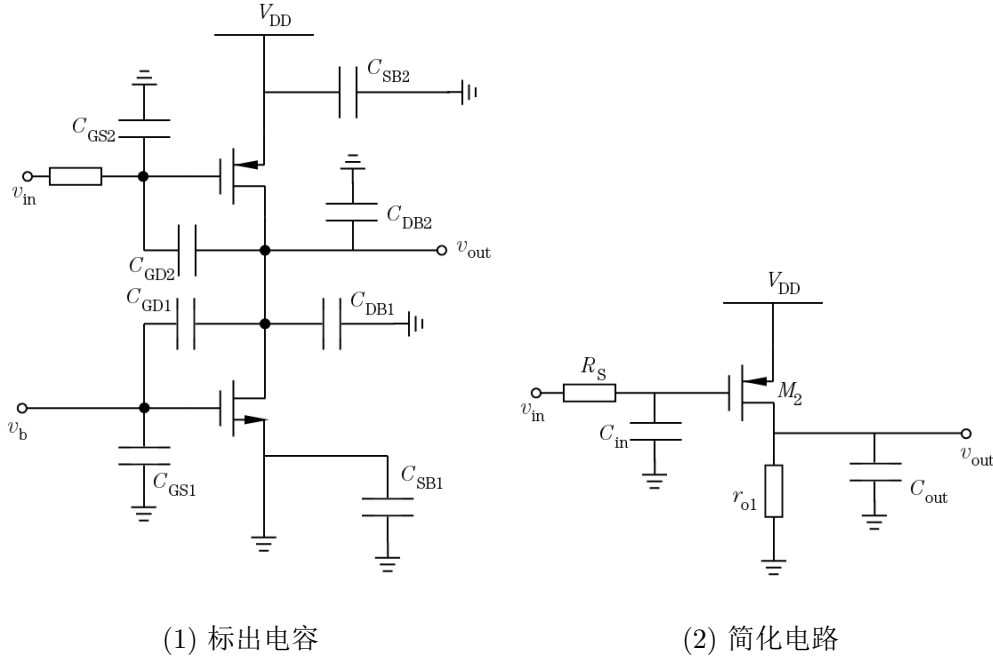


Figure p11-38-c

$$A_0 = -g_{m1} (r_{o2} // r_{o1})$$

$$C_{in} = C_{GS2} + C_{GD2} [1 + g_{m1} (r_{o2} // r_{o1})]$$

$$C_{out} = C_{DB1} + C_{DB2} + C_{GD1} + C_{GD2} \left[1 + \frac{1}{g_{m1} (r_{o2} // r_{o1})} \right]$$

其中 A_0 为电路低频增益，从而

$$\omega_{p1} = [R_S [C_{GS2} + C_{GD2} (1 + g_{m1} (r_{o2}/r_{o1}))]]^{-1}$$

$$\omega_{p2} = \left[r_{o1} \left[C_{DB1} + C_{DB2} + C_{GD1} + C_{GD2} \left(1 + \frac{1}{g_{m1} (r_{o2}/r_{o1})} \right) \right] \right]^{-1}$$

11.42 The circuit depicted in Fig. 11-82 is called an "active inductor". Neglecting other capacitances and assuming $\lambda = 0$, compute Z_{in} . Use Bode's rule to plot $|Z_{in}|$ as a function of frequency and explain why it exhibits inductive behavior.

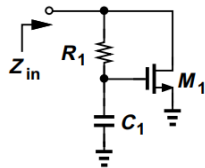


Figure 11-82

解

$$Z_{in} = (R_1 - j \frac{1}{\omega C_1}) // \frac{1}{g_m} = \frac{1}{g_m} \cdot \frac{1 + j\omega R_1 C_1}{1 + j\omega C_1 (\frac{1}{g_m} + R_1)}$$

$$\omega_z = \frac{1}{R_1 C_1}, \omega_p = \frac{1}{C_1 (\frac{1}{g_m} + R_1)}$$

从而可作波特图如图 p11-42 所示，在高频下 $|Z_{in}|$ 更小，显出电导性。

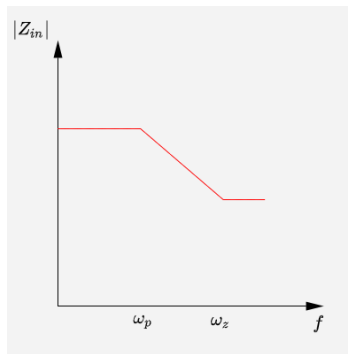


Figure p11-42

11.46 Determine the transfer function of the circuits shown in Fig. 11-86. Assume $\lambda = 0$ for M_1 .

解 (a) 画出所有电容后的电路以及简化后的电路如图 p11-46-a 所示。其中

$$R_D = \frac{1}{g_{m2}} // r_{o2}$$

$$A_0 = g_{m1} (\frac{1}{g_{m2}} // r_{o2})$$

$$C_{in} = C_{SB1} + C_{GS1}$$

$$C_{out} = C_{DB1} + C_{DB2} + C_{GD2} + C_{GD1}$$

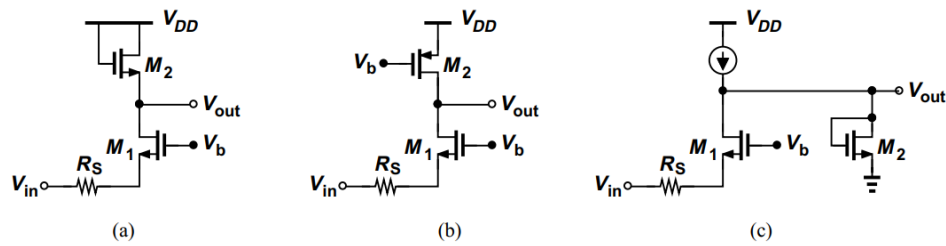


Figure 11-86

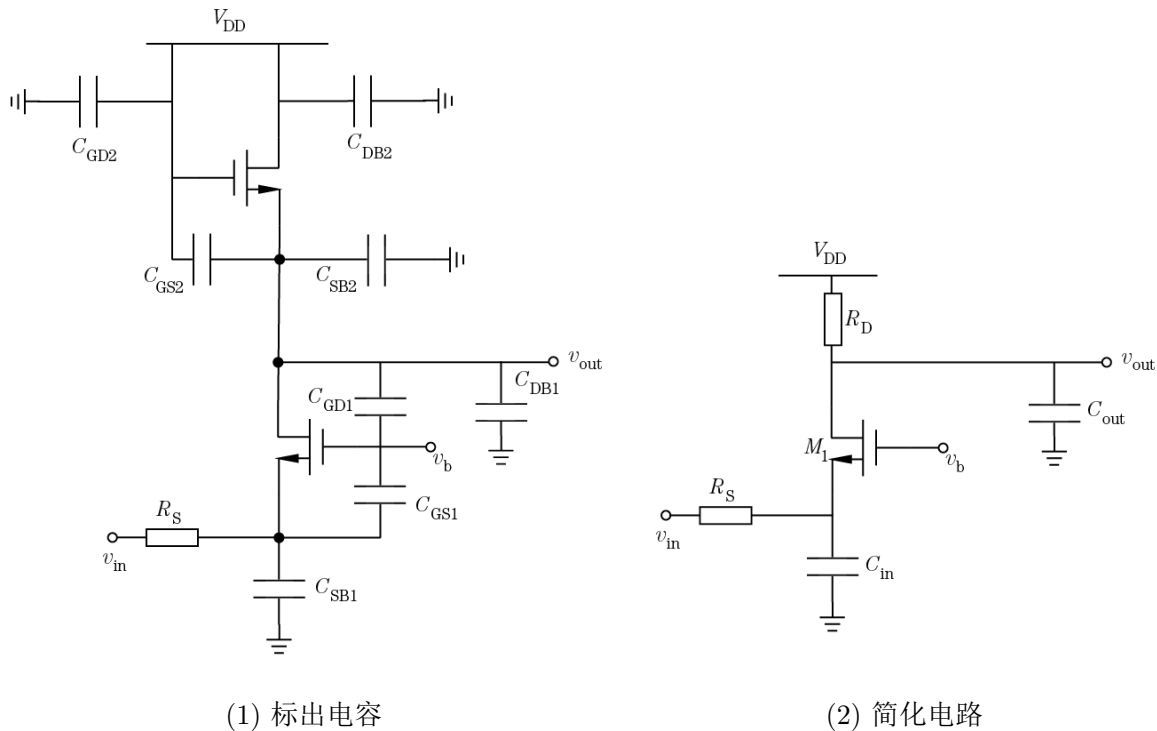


Figure p11-46-a

其中 A_0 为电路低频增益，从而

$$\begin{aligned}
 \omega_{p1} &= [R_S(C_{SB1} + C_{GS1})]^{-1} \\
 \omega_{p2} &= \left[\left(\frac{1}{g_{m2}} // r_{o2} \right) (C_{DB1} + C_{DB2} + C_{GD2} + C_{GD1}) \right]^{-1} \\
 A &= \frac{A_0}{\left(1 + \frac{j\omega}{\omega_{p1}} \right) \left(1 + \frac{j\omega}{\omega_{p2}} \right)} \\
 &= \frac{g_{m1} \left(\frac{1}{g_{m2}} // r_{o2} \right)}{[1 + j\omega R_S(C_{SB1} + C_{GS1})] \left[1 + j\omega \left(\frac{1}{g_{m2}} // r_{o2} \right) (C_{DB1} + C_{DB2} + C_{GD2} + C_{GD1}) \right]}
 \end{aligned}$$

(b) 画出所有电容后的电路以及简化后的电路如图 p11-46-b 所示。其中

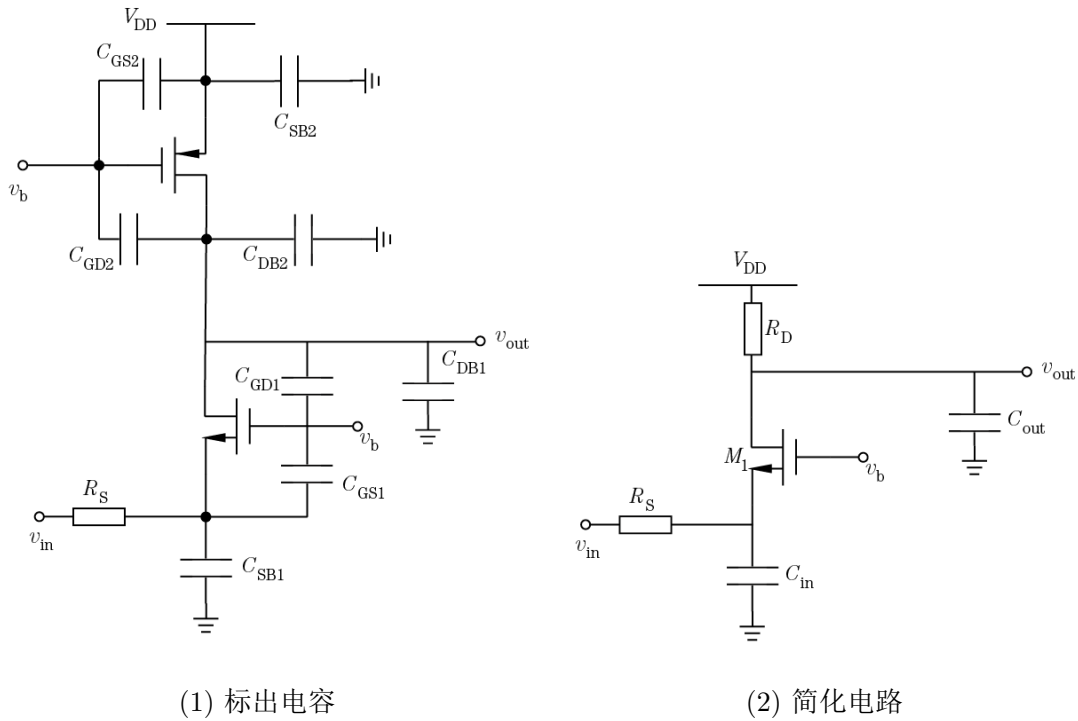


Figure p11-46-b

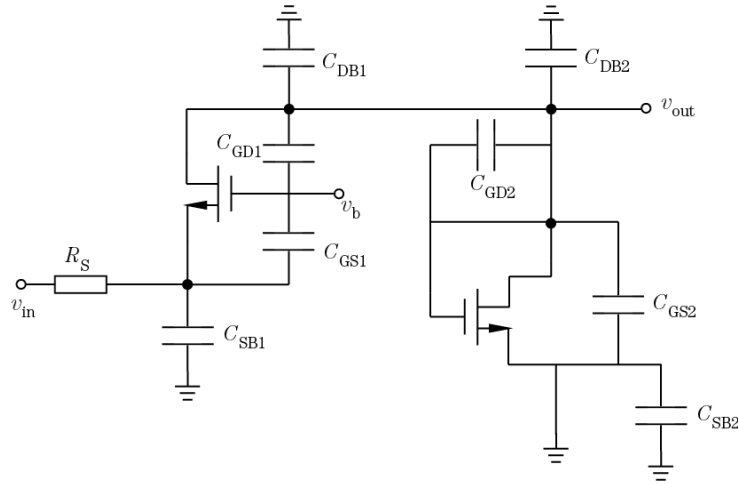
$$\begin{aligned}
 A_0 &= g_{m1}r_{o2} \\
 C_{in} &= C_{SB1} + C_{GS1} \\
 C_{out} &= C_{DB1} + C_{DB2} + C_{GD2} + C_{GD1}
 \end{aligned}$$

其中 A_0 为电路低频增益，从而

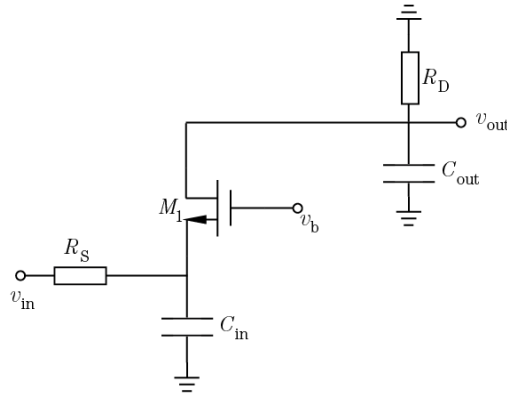
$$\begin{aligned}
 \omega_{p1} &= [R_S(C_{SB1} + C_{GS1})]^{-1} \\
 \omega_{p2} &= [r_{o2}(C_{DB1} + C_{DB2} + C_{GD2} + C_{GD1})]^{-1} \\
 A &= \frac{A_0}{\left(1 + \frac{j\omega}{\omega_{p1}}\right) \left(1 + \frac{j\omega}{\omega_{p2}}\right)} \\
 &= \frac{g_{m1}r_{o2}}{[1 + j\omega R_S(C_{SB1} + C_{GS1})][1 + j\omega r_{o2}(C_{DB1} + C_{DB2} + C_{GD2} + C_{GD1})]}
 \end{aligned}$$

(c) 画出所有电容后的电路以及简化后的电路如图 p11-46-c 所示。其中

$$\begin{aligned}
 R_D &= \frac{1}{g_{m2}} // r_{o2} \\
 A_0 &= g_{m1} \left(\frac{1}{g_{m2}} // r_{o2} \right) \\
 C_{in} &= C_{SB1} + C_{GS1} \\
 C_{out} &= C_{DB1} + C_{DB2} + C_{GS2} + C_{GD1}
 \end{aligned}$$



(1) 标出电容



(2) 简化电路

Figure p11-46-c

其中 A_0 为电路低频增益，从而

$$\begin{aligned}
 \omega_{p1} &= [R_S(C_{SB1} + C_{GS1})]^{-1} \\
 \omega_{p2} &= \left[\left(\frac{1}{g_{m2}} // r_{o2} \right) (C_{DB1} + C_{DB2} + C_{GS2} + C_{GD1}) \right]^{-1} \\
 A &= \frac{A_0}{\left(1 + \frac{j\omega}{\omega_{p1}} \right) \left(1 + \frac{j\omega}{\omega_{p2}} \right)} \\
 &= \frac{g_{m1} \left(\frac{1}{g_{m2}} // r_{o2} \right)}{[1 + j\omega R_S(C_{SB1} + C_{GS1})] \left[1 + j\omega \left(\frac{1}{g_{m2}} // r_{o2} \right) (C_{DB1} + C_{DB2} + C_{GS2} + C_{GD1}) \right]}
 \end{aligned}$$

11.50 Due to manufacturing error, a parasitic resistor R_P has appeared in the cascode stage of Fig. 11-90. Assuming $\lambda = 0$ and using Miller's theorem, determine the poles of the circuit.

解 画出所有电容后的电路以及简化后的电路如图 p11-50 所示。其中

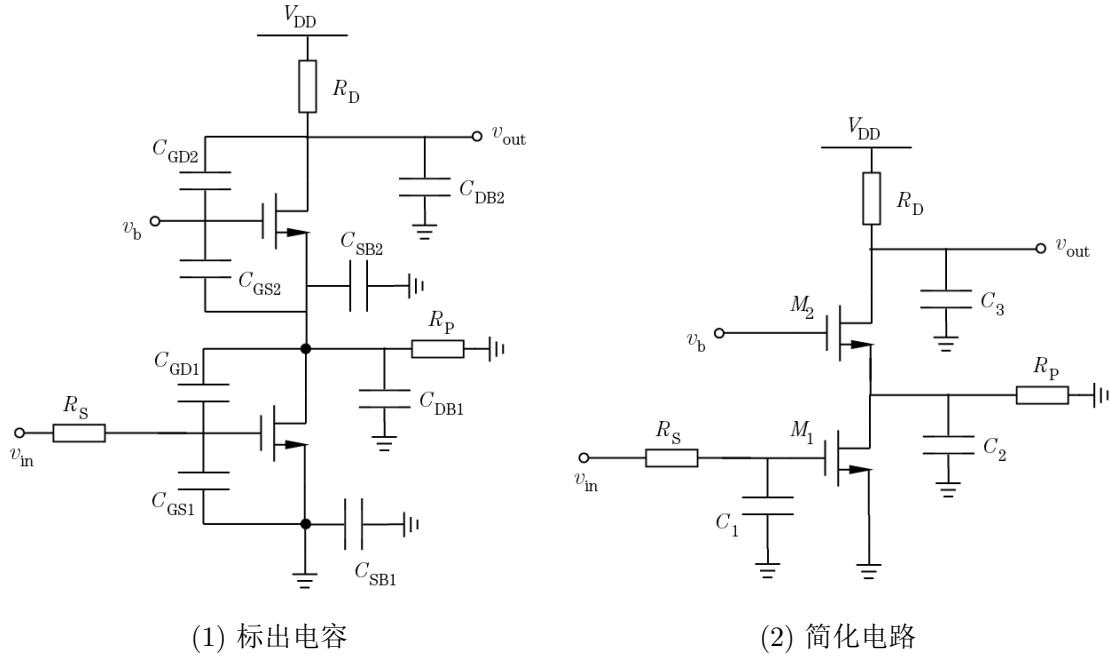


Figure 11-50

$$\begin{aligned}
 A_0 &= -g_{m1}g_{m2}R_D \left(\frac{1}{g_{m2} // R_P} \right) \\
 C_1 &= C_{GS1} + C_{GD1} \left(1 + g_{m1}g_{m2}R_D \left(\frac{1}{g_{m2} // R_P} \right) \right) \\
 C_2 &= C_{SB2} + C_{DB1} + C_{GS2} + C_{GD1} \left(1 + \frac{1}{g_{m1}g_{m2}R_D \left(\frac{1}{g_{m2} // R_P} \right)} \right) \\
 C_3 &= C_{DB2} + C_{GD2}
 \end{aligned}$$

其中 A_0 为电路低频增益，从而

$$\begin{aligned}
 \omega_{p1} &= \left[R_S \left(C_{GS1} + C_{GD1} \left(1 + g_{m1}g_{m2}R_D \left(\frac{1}{g_{m2} // R_P} \right) \right) \right) \right]^{-1} \\
 \omega_{p2} &= \left[\left(\frac{1}{g_{m2} // R_P} \right) \left(C_{SB2} + C_{DB1} + C_{GS2} + C_{GD1} \left(1 + \frac{1}{g_{m1}g_{m2}R_D \left(\frac{1}{g_{m2} // R_P} \right)} \right) \right) \right]^{-1} \\
 \omega_{p3} &= [R_D(C_{DB2} + C_{GD2})]^{-1} \\
 A &= \frac{A_0}{\left(1 + \frac{j\omega}{\omega_{p1}} \right) \left(1 + \frac{j\omega}{\omega_{p2}} \right) \left(1 + \frac{j\omega}{\omega_{p3}} \right)}
 \end{aligned}$$