

SWEN304

Assignment three

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- a) [4 marks] Consider a relation schema $N(R, F)$ where $R = \{A, B, C\}$. Suppose we find the following two tuples in an instance of this relation schema.

A	B	C
3	5	9
3	4	9

Determine if the following functional dependencies hold over the relation schema N ? Justify your answer.

- 1) $A \rightarrow C$
- 2) $B \rightarrow A$
- 3) $B \rightarrow AC$
- 4) $AC \rightarrow B$

- 1) A can hold C
- 2) B can hold A
- 3) B can hold AC
- 4) AC cannot hold B, AC have multiple Bs.

- b) [16 marks] Consider a relation schema $N(R, F)$ where $R = \{A, B, C, D\}$. For each of the following sets F of functional dependencies, determine which normal form (1NF, 2NF, 3NF, BCNF) the relation schema N is in. Justify your answer.

Hint: Note that in all four cases AB is the only minimal key for N .

- 1) $F = \{AB \rightarrow C, AB \rightarrow D\}$
- 2) $F = \{AB \rightarrow C, C \rightarrow D\}$
- 3) $F = \{AB \rightarrow D, B \rightarrow C\}$
- 4) $F = \{AB \rightarrow CD, C \rightarrow B\}$

- 1) It is BCNF, AB is the super key for C and D .
- 2) It is in 2NF, it has transitive dependency. Key AB could hold D directly. Thus, it is not 3NF.
- 3) It is in 1NF, it has partial dependency. Because C is partially depends on AB .
- 4) it is in 3NF, it have neither partial dependency nor transitive dependency. Meanwhile, AB is key and CD is non-prime attributes and C is non-prime attribute and B is prime attribute.

Question 2. Minimal Cover of a set of Functional Dependencies [20 marks]

Consider the set of functional dependencies $F = \{A \rightarrow D, C \rightarrow D, AD \rightarrow C\}$. Compute a minimal cover of F . Justify your answer.

$A^+ = ADC$

$C^+ = CD$

$D^+ = D$

$AD^+ = ADC$

$AC^+ = ADC$

$CD^+ = CD$

Step 1: As we can see above, $A^+ = ADC$, thus, $A \rightarrow C$ directly. D cannot hold C because $C \rightarrow D$. hence, $AD \rightarrow C$ can be removed. $\{A \rightarrow D, C \rightarrow D, A \rightarrow C\}$ is equal to $\{A \rightarrow D, C \rightarrow D, AD \rightarrow C\}$. I update $F = \{A \rightarrow D, C \rightarrow D, A \rightarrow C\}$.

$A \rightarrow D$ and $C \rightarrow D$ have same prime attributes D . However, $A \rightarrow C$ and $C \rightarrow D$ can use transitive rule to infer $A \rightarrow D$. $A \rightarrow D$ is considered as redundant FD. I removed $A \rightarrow D$ update F to $\{A \rightarrow C, C \rightarrow D\}$.

Question 3. Lossless Third Normal Form Normalization

[25 marks]

Consider a relation schema $N(R, F)$ where $R = \{A, B, C, D\}$ and $F = \{B \rightarrow C, D \rightarrow A\}$. Perform the following tasks. *Justify your answers.*

- 1) Identify all minimal keys for N . Show your process.
- 2) Identify the highest normal form (1NF, 2NF, 3NF, BCNF) that N satisfies.
- 3) If N is not in 3NF, compute a lossless transformation into a set of 3NF relation schemas that preserve attributes and functional dependencies.
- 4) Verify explicitly that your result has the lossless property, satisfies 3NF, and that all attributes and functional dependencies are preserved.

1)

$A^+ = A$

$B^+ = BC$

$C^+ = C$

$D^+ = DA$

$AB^+ = ABC$

$AC^+ = AC$

$AD^+ = AD$

$BC^+ = BC$

$BD^+ = BDCA$

$CD^+ = CDA$

$ABC^+ = ABC$

$ABD^+ = ABCD$

$ACD^+ = ACD$

$BCD^+ = ABCD$

BCD, ABD , and BD all infer $ABCD$. Hence, the key will be the minimal attributes then it will be BD .

2) it is in 1NF, Because the minimal key is BD which is verified in last process, thus, $BD^+ = ABCD$ which means $BD \rightarrow A$ and $BD \rightarrow C$. Meanwhile $B \rightarrow C$ and $D \rightarrow A$ is given. it has partial dependency, then it is in 1NF.

3)

Step 1: $\{B \rightarrow C\}, \{D \rightarrow A\}$

Step 2: $\{BC\}\{B \rightarrow C\}, \{DA\}\{D \rightarrow A\}$

Step 3: add key to the function $\{\{BC\}\{B, C\}, \{DA\}\{D, A\}, \{BD\}\{B, D\}\}$

4) To make sure it is lossless, we should construct a relation schema (U, F) where $U =$ union of all R s and $F =$ union of all F s

In this question, $U = BC \cup DA \cup BD = \{A, B, C, D\}$ and $F = \{B \rightarrow C\} \cup \{D \rightarrow A\} = \{B \rightarrow C, D \rightarrow A\}$. Hence, compared with given U and F . We didn't lost anything. Then It is lossless.

Question 4. BCNF Normalization

[35 marks]

Suppose you are given a relation schema $N(R, F)$, where $R = \{A, B, C, D\}$ and $F = \{AB \rightarrow CD, C \rightarrow A, D \rightarrow B\}$.

- 1) Identify all minimal keys for N . *Justify your answer.*
- 2) Identify the highest normal form that N satisfies (1NF, 2NF, 3NF, BCNF). Justify your answer.
- 3) If N is not in BCNF, transform it into a set of at least BCNF relation schemas that preserve attributes and functional dependencies and have a lossless join property.
- 4) Check whether your decomposition preserves all the functional dependencies. Justify your answer.

1)

$A^+ = A$

$B^+ = B$

$C^+ = CA$

$D^+ = DB$

$AB^+ = ABCD$

$AC^+ = AC$

$AD^+ = ADBC$

$BC^+ = BCAD$

$CD^+ = ABCD$

$ABC^+ = ABCD$

$ABD^+ = ABCD$

$BCD^+ = ABCD$

As we can see above, There four minimal keys they are $\{AB, AD, BC, CD\}$

2) For this question, I consider AB as my key. Thus, C and D will be non-prime attributes. Thus, It should be 3NF. Because C and D is non-prime attributes and A and B are part of key (prime attribute). Hence, it should be 3NF.

3)

$R = \{A, B, C, D\}$

$F = \{AB \rightarrow CD, C \rightarrow A, D \rightarrow B\}$

As we can see $C \rightarrow A$, $D \rightarrow B$ both violates the rule of BCNF

Let's start with $C \rightarrow A$

$N_1 = (BCD \{D \rightarrow B\})$ $N_2 = (AC \{C \rightarrow A\})$

$B^+ = B$

$C^+ = C$

$D^+ = BD$

$BC^+ = ABCD$

$BD^+ = BD$

$CD^+ = CDAB$

$N_3 = (CD \{D \rightarrow B\})$ $N_4 = (BD \{D \rightarrow B\})$

$BC^+ = ABCD$ is key thus It hasn't violated BCNF.

$CD^+ = CDAB$ $CD \rightarrow B$ is not minimal. we

replace $CD \rightarrow B$ by $D \rightarrow B$.

After BC Normalization we got

$(AC \{C \rightarrow A\}), (CD \{D \rightarrow B\}), (BD \{D \rightarrow B\})$

4) We construct a relation schema (U, F) where U = union of all R_s and F = union of all F_s . We can get $U = \{A, C\} \cup \{C, D\} \cup \{B, D\} = \{A, B, C, D\}$ $F = \{\text{null}\} \cup \{C \rightarrow A\} \cup \{D \rightarrow B\} = \{C \rightarrow A, D \rightarrow B\}$. Compared with original $F = \{AB \rightarrow CD, C \rightarrow A, D \rightarrow B\}$, We lost function $\{AB \rightarrow CD\}$.