

From Soulsby's book

## 1 Total Shear Stress

Total shear stress induced by wave and currents can be calculated by (p92, (69))

$$\tau_m = \tau_c \left[ 1 + 1.2 \left( \frac{\tau_w}{\tau_c + \tau_w} \right)^{3.2} \right] \quad (1)$$

where  $\tau_c$  and  $\tau_w$  represent current and wave-induced shear stresses, respectively.

## 2 Calculating $\tau_c$ and $\tau_w$

### 2.1 $\tau_c$

For current-induced shear stress (p53, (30))

$$\tau_c = \rho C_D \bar{U}^2 \quad (2)$$

where  $\bar{U}$  is depth-averaged velocity, and  $C_D$  has two forms (p48):

$$C_D = \alpha \left( \frac{z_0}{h} \right)^\beta \quad (3)$$

and

$$C_D = \left[ \frac{0.40}{1 + \ln(z_0/h)} \right] \quad (4)$$

The latter one may be popular one used in sediment transport formulas.

### 2.2 $\tau_w$

In p76, (57):

$$\tau_w = \frac{1}{2} \rho f_w U_w^2 \quad (5)$$

where  $U_w$  is wave orbital velocity amplitude.

There are several formulas which can be used to calculate  $f_w$  Soulsby, p78, (62):

$$f_w = 1.39 \left( \frac{A}{z_0} \right)^{-0.52} \quad (6)$$

and Swart (1974) which is used for example

$$f_{wr} = 0.3 \quad \text{for } r < 1.57 \quad (7)$$

$$f_{wr} = 0.00251 \exp(5.21r^{-0.19}) \quad \text{for } r > 1.57 \quad (8)$$

where  $r = A/k_s$ , in which  $A$  is semi-orbital excursion ( $U_w T/2\pi$ ) and  $k_s = 30z_0$ , Nikuradse equivalent sand grain roughness

$$k_s = 30z_0 \quad (9)$$

### 3 calculating roughness length $z_0$

$z_0$  is total roughness length

$$z_0 = z_{0s} + z_{0f} + z_{0t} \quad (10)$$

in which  $z_{0s}$ ,  $z_{0f}$  and  $z_{0t}$  are roughness length corresponding to skin friction, form drag, and sediment transport (mobilization). p48, (25)

$$z_{0s} = d_{50}/12 \quad (11)$$

For both wave/current generated ripples (p123, (90))

$$z_{0f} = a_r \frac{\Delta_r^2}{\lambda_r} \quad (12)$$

where  $\Delta_r$  and  $\lambda_r$  are ripple height and length, respectively. For current-only case, in p59, (42)

$$z_{0t} = \frac{5\tau_{0s}}{30g(\rho_s - \rho)} \quad (13)$$

where  $\tau_{0s}$  is skin-friction shear stress.

For wave generated ripples Nielsen's formula may be used (p124, (92)),

$$z_{0t} = 5.67(\theta_{ws} - 0.05)^{0.5} d_{50} \quad (14)$$

where  $\theta_{ws}$  is skin-friction Shields parameter. When using Nielsen's formula, ripple height and length have to be evaluated using p122 (89) and  $a_r = 0.269$ .