A Block-sorting Lossless Data Compression Algorithm

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Authors' abstract

We describe a block-sorting, lossless data compression algorithm, and our implementation of that algorithm. We compare the performance of our implementation with widely available data compressors running on the same hardware.

The algorithm works by applying a reversible transformation to a block of input text. The transformation does not itself compress the data, but reorders it to make it easy to compress with simple algorithms such as move-to-front coding.

Our algorithm achieves speed comparable to algorithms based on the techniques of Lempel and Ziv, but obtains compression close to the best statistical modelling techniques. The size of the input block must be large (a few kilobytes) to achieve good compression.

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1 Introduction

The most widely used data compression algorithms are based on the sequential data compressors of Lempel and Ziv [1, 2]. Statistical modelling techniques may produce superior compression [3], but are significantly slower.

In this paper, we present a technique that achieves compression within a percent or so of that achieved by statistical modelling techniques, but at speeds comparable to those of algorithms based on Lempel and Ziv's.

Our algorithm does not process its input sequentially, but instead processes a block of text as a single unit. The idea is to apply a reversible transformation to a block of text to form a new block that contains the same characters, but is easier to compress by simple compression algorithms. The transformation tends to group characters together so that the probability of finding a character close to another instance of the same character is increased substantially. Text of this kind can easily be compressed with fast locally-adaptive algorithms, such as move-to-front coding [4] in combination with Huffman or arithmetic coding.

Briefly, our algorithm transforms a string S of N characters by forming the N rotations (cyclic shifts) of S, sorting them lexicographically, and extracting the last character of each of the rotations. A string L is formed from these characters, where the ith character of L is the last character of the ith sorted rotation. In addition to L, the algorithm computes the index I of the original string S in the sorted list of rotations. Surprisingly, there is an efficient algorithm to compute the original string S given only L and I.

The sorting operation brings together rotations with the same initial characters. Since the initial characters of the rotations are adjacent to the final characters, consecutive characters in L are adjacent to similar strings in S. If the context of a character is a good predictor for the character, L will be easy to compress with a simple locally-adaptive compression algorithm.

In the following sections, we describe the transformation in more detail, and show that it can be inverted. We explain more carefully why this transformation tends to group characters to allow a simple compression algorithm to work more effectively. We then describe efficient techniques for implementing the transformation and its inverse, allowing this algorithm to be competitive in speed with Lempel-Ziv-based algorithms, but achieving better compression. Finally, we give the performance of our implementation of this algorithm, and compare it with well-known compression programmes.

The algorithm described here was discovered by one of the authors (Wheeler) in 1983 while he was working at AT&T Bell Laboratories, though it has not previously been published.

2 The reversible transformation

This section describes two sub-algorithms. Algorithm C performs the reversible transformation that we apply to a block of text before compressing it, and Algorithm D performs the inverse operation. A later section suggests a method for compressing the transformed block of text.

In the description below, we treat strings as vectors whose elements are characters.

Algorithm C: Compression transformation

This algorithm takes as input a string S of N characters $S[0], \ldots, S[N-1]$ selected from an ordered alphabet X of characters. To illustrate the technique, we also give a running example, using the string S = `abraca', N = 6, and the alphabet $X = \{\text{'a'}, \text{'b'}, \text{'c'}, \text{'r'}\}$.

C1. [sort rotations]

Form a conceptual $N \times N$ matrix M whose elements are characters, and whose rows are the rotations (cyclic shifts) of S, sorted in lexicographical order. At least one of the rows of M contains the original string S. Let I be the index of the first such row, numbering from zero.

In our example, the index I = 1 and the matrix M is

row 0 aabrac 1 abraca 2 acaabr 3 bracaa 4 caabra 5 racaab

C2. [find last characters of rotations]

Let the string L be the last column of M, with characters $L[0], \ldots, L[N-1]$ (equal to $M[0, N-1], \ldots, M[N-1, N-1]$). The output of the transformation is the pair (L, I).

In our example, L = `caraab' and I = 1 (from step C1).

Algorithm D: Decompression transformation

We use the example and notation introduced in Algorithm C. Algorithm D uses the output (L, I) of Algorithm C to reconstruct its input, the string S of length N.

D1. [find first characters of rotations]

This step calculates the first column F of the matrix M of Algorithm C. This is done by sorting the characters of L to form F. We observe that any column of the matrix M is a permutation of the original string S. Thus, L and F are both permutations of S, and therefore of one another. Furthermore, because the rows of M are sorted, and F is the first column of M, the characters in F are also sorted.

In our example, F = 'aaabcr'.

D2. [build list of predecessor characters]

To assist our explanation, we describe this step in terms of the contents of the matrix M. The reader should remember that the complete matrix is not available to the decompressor; only the strings F, L, and the index I (from the input) are needed by this step.

Consider the rows of the matrix M that start with some given character ch. Algorithm C ensured that the rows of matrix M are sorted lexicographically, so the rows that start with ch are ordered lexicographically.

We define the matrix M' formed by rotating each row of M one character to the right, so for each i = 0, ..., N - 1, and each j = 0, ..., N - 1,

$$M'[i, j] = M[i, (j-1) \mod N]$$

In our example, M and M' are:

row	M	M'
0	aabrac	caabra
1	abraca	aabrac
2	acaabr	racaab
3	bracaa	abraca
4	caabra	acaabr
5	racaab	bracaa

Like M, each row of M' is a rotation of S, and for each row of M there is a corresponding row in M'. We constructed M' from M so that the rows

of M' are sorted lexicographically starting with their *second* character. So, if we consider only those rows in M' that start with a character ch, they must appear in lexicographical order relative to one another; they have been sorted lexicographically starting with their second characters, and their first characters are all the same and so do not affect the sort order. Therefore, for any given character ch, the rows in M that begin with ch appear in the *same order* as the rows in M' that begin with ch.

In our example, this is demonstrated by the rows that begin with 'a'. The rows 'aabrac', 'abraca', and 'acaabr' are rows 0, 1, 2 in M and correspond to rows 1, 3, 4 in M'.

Using F and L, the first columns of M and M' respectively, we calculate a vector T that indicates the correspondence between the rows of the two matrices, in the sense that for each $j = 0, \ldots, N-1$, row j of M' corresponds to row T[j] of M.

If L[j] is the kth instance of ch in L, then T[j] = i where F[i] is the kth instance of ch in F. Note that T represents a one-to-one correspondence between elements of F and elements of F, and F[T[j]] = L[j].

In our example, T is: $(4 \ 0 \ 5 \ 1 \ 2 \ 3)$.

D3. [form output *S*]

Now, for each i = 0, ..., N - 1, the characters L[i] and F[i] are the last and first characters of the row i of M. Since each row is a rotation of S, the character L[i] cyclicly precedes the character F[i] in S. From the construction of T, we have F[T[j]] = L[j]. Substituting i = T[j], we have L[T[j]] cyclicly precedes L[j] in S.

The index I is defined by Algorithm C such that row I of M is S. Thus, the last character of S is L[I]. We use the vector T to give the predecessors of each character:

for each
$$i = 0, ..., N - 1$$
: $S[N - 1 - i] = L[T^{i}[I]]$.

where $T^0[x] = x$, and $T^{i+1}[x] = T[T^i[x]]$. This yields S, the original input to the compressor.

In our example, S = 'abraca'.

We could have defined T so that the string S would be generated from front to back, rather than the other way around. The description above matches the pseudo-code given in Section 4.2.

The sequence $T^i[I]$ for $i=0,\ldots,N-1$ is not necessarily a permutation of the numbers $0,\ldots,N-1$. If the original string S is of the form Z^p for some substring Z and some p>1, then the sequence $T^i[I]$ for $i=0,\ldots,N-1$ will also be of the form Z'^p for some subsequence Z'. That is, the repetitions in S will be generated by visiting the same elements of T repeatedly. For example, if S= 'cancan', Z= 'can' and p=2, the sequence $T^i[I]$ for $i=0,\ldots,N-1$ will be [2,4,0,2,4,0].

3 Why the transformed string compresses well

Algorithm C sorts the rotations of an input string S, and generates the string L consisting of the last character of each rotation.

To see why this might lead to effective compression, consider the effect on a single letter in a common word in a block of English text. We will use the example of the letter 't' in the word 'the', and assume an input string containing many instances of 'the'.

When the list of rotations of the input is sorted, all the rotations starting with 'he' will sort together; a large proportion of them are likely to end in 't'. One region of the string L will therefore contain a disproportionately large number of 't' characters, intermingled with other characters that can proceed 'he' in English, such as space, 's', 'T', and 'S'.

The same argument can be applied to all characters in all words, so any localized region of the string L is likely to contain a large number of a few distinct characters. The overall effect is that the probability that given character ch will occur at a given point in L is very high if ch occurs near that point in L, and is low otherwise. This property is exactly the one needed for effective compression by a move-to-front coder [4], which encodes an instance of character ch by the count of distinct characters seen since the next previous occurrence of ch. When applied to the string L, the output of a move-to-front coder will be dominated by low numbers, which can be efficiently encoded with a Huffman or arithmetic coder.

Figure 1 shows an example of the algorithm at work. Each line is the first few characters and final character of a rotation of a version of this document. Note the grouping of similar characters in the column of final characters.

For completeness, we now give details of one possible way to encode the output of Algorithm C, and the corresponding inverse operation. A complete compression algorithm is created by combining these encoding and decoding operations with Algorithms C and D.

final char	sorted rotations		
(<i>L</i>)	202300 200000000		
a	n to decompress. It achieves compression		
0	n to perform only comparisons to a depth		
0	n transformation This section describes		
0	n transformation} We use the example and		
0	n treats the right-hand side as the most		
a	n tree for each 16 kbyte input block, enc		
a	n tree in the output stream, then encodes		
i	n turn, set $L[i]$ to be the		
i	n turn, set \$R[i]\$ to the		
0	n unusual data. Like the algorithm of Man		
a	n use a single set of probabilities table		
е	n using the positions of the suffixes in		
i	n value at a given point in the vector \$R		
е	n we present modifications that improve t		
е	n when the block size is quite large. Ho		
i	n which codes that have not been seen in		
i	n with ch appear in the ϵ		
i	n with \$ch\$. In our exam		
0	n with Huffman or arithmetic coding. Bri		
0	n with figures given by Bell~\cite{bell}.		

Figure 1: Example of sorted rotations. Twenty consecutive rotations from the sorted list of rotations of a version of this paper are shown, together with the final character of each rotation.

Algorithm M: Move-to-front coding

This algorithm encodes the output (L, I) of Algorithm C, where L is a string of length N and I is an index. It encodes L using a move-to-front algorithm and a Huffman or arithmetic coder.

The running example of Algorithm C is continued here.

M1. [move-to-front coding]

This step encodes each of the characters in L by applying the move-to-front technique to the individual characters. We define a vector of integers $R[0], \ldots, R[N-1]$, which are the codes for the characters $L[0], \ldots, L[N-1]$.

Initialize a list Y of characters to contain each character in the alphabet X exactly once.

For each i = 0, ..., N - 1 in turn, set R[i] to the number of characters preceding character L[i] in the list Y, then move character L[i] to the front of Y.

Taking Y = ['a', 'b', 'c', 'r'] initially, and L = 'caraab', we compute the vector R: $(2 \ 1 \ 3 \ 1 \ 0 \ 3)$.

M2. [encode]

Apply Huffman or arithmetic coding to the elements of R, treating each element as a separate token to be coded. Any coding technique can be applied as long as the decompressor can perform the inverse operation. Call the output of this coding process OUT. The output of Algorithm C is the pair (OUT, I) where I is the value computed in step C1.

Algorithm W: Move-to-front decoding

This algorithm is the inverse of Algorithm M. It computes the pair (L, I) from the pair (OUT, I).

We assume that the initial value of the list *Y* used in step M1 is available to the decompressor, and that the coding scheme used in step M2 has an inverse operation.

W1. [decode]

Decode the coded stream OUT using the inverse of the coding scheme used in step M2. The result is a vector R of N integers.

In our example, R is: (2 1 3 1 0 3).

W2. [inverse move-to-front coding]

The goal of this step is to calculate a string L of N characters, given the move-to-front codes $R[0], \ldots, R[N-1]$.

Initialize a list Y of characters to contain the characters of the alphabet X in the same order as in step M1.

For each i = 0, ..., N-1 in turn, set L[i] to be the character at position R[i] in list Y (numbering from 0), then move that character to the front of Y. The resulting string L is the last column of matrix M of Algorithm C. The output of this algorithm is the pair (L, I), which is the input to Algorithm D.

Taking Y = ['a', 'b', 'c', 'r'] initially (as in Algorithm M), we compute the string L = `caraab'.

4 An efficient implementation

Efficient implementations of move-to-front, Huffman, and arithmetic coding are well known. Here we concentrate on the unusual steps in Algorithms C and D.

4.1 Compression

The most important factor in compression speed is the time taken to sort the rotations of the input block. A simple application of quicksort requires little additional space (one word per character), and works fairly well on most input data. However, its worst-case performance is poor.

A faster way to implement Algorithm C is to reduce the problem of sorting the rotations to the problem of sorting the suffixes of a related string.

To compress a string S, first form the string S', which is the concatenation of S with EOF, a new character that does not appear in S. Now apply Algorithm C to S'. Because EOF is different from all other characters in S', the suffixes of S' sort in the same order as the rotations of S'. Hence, to sort the rotations, it suffices to sort the suffixes of S'. This can be done in linear time and space by building a suffix tree, which then can be walked in lexicographical order to recover the sorted suffixes. We used McCreight's suffix tree construction algorithm [5] in an implementation of Algorithm C. Its performance is within 40% of the fastest technique we have found when operating on text files. Unfortunately, suffix tree algorithms need space for more than four machine words per input character.

Manber and Myers give a simple algorithm for sorting the suffixes of a string in $O(N \log N)$ time [6]. The algorithm they describe requires only two words per

input character. The algorithm works by sorting suffixes on their first i characters, then using the positions of the suffixes in the sorted array as the sort key for another sort on the first 2i characters. Unfortunately, the performance of their algorithm is significantly worse than the suffix tree approach.

The fastest scheme we have tried so far uses a variant of quicksort to generate the sorted list of suffixes. Its performance is significantly better than the suffix tree when operating on text, and it uses significantly less space. Unlike the suffix tree however, its performance can degrade considerably when operating on some types of data. Like the algorithm of Manber and Myers, our algorithm uses only two words per input character.

Algorithm Q: Fast quicksorting on suffixes

This algorithm sorts the suffixes of the string S, which contains N characters $S[0, \ldots, N-1]$. The algorithm works by applying a modified version of quicksort to the suffixes of S.

First we present a simple version of the algorithm. Then we present modifications that improve the speed and make bad performance less likely.

Q1. [form extended string]

Let *k* be the number of characters that fit in a machine word.

Form the string S' from S by appending k additional EOF characters to S, where EOF does not appear in S.

Q2. [form array of words]

Initialize an array W of N words W[0, ..., N-1], such that W[i] contains the characters S'[i, ..., i+k-1] arranged so that integer comparisons on the words agree with lexicographic comparisons on the k-character strings.

Packing characters into words has two benefits: It allows two prefixes to be compared k bytes at a time using aligned memory accesses, and it allows many slow cases to be eliminated (described in step Q7).

Q3. [form array of suffixes]

In this step we initialize an array V of N integers. If an element of V contains j, it represents the suffix of S' whose first character is S'[j]. When the algorithm is complete, suffix V[i] will be the ith suffix in lexicographical order.

Initialize an array V of integers so that for each i = 0, ..., N-1: V[i] = i.

Q4. [radix sort]

Sort the elements of V, using the first two characters of each suffix as the sort key. This can be done efficiently using radix sort.

Q5. [iterate over each character in the alphabet]

For each character *ch* in the alphabet, perform steps Q6, Q7.

Once this iteration is complete, V represents the sorted suffixes of S, and the algorithm terminates.

Q6. [quicksort suffixes starting with ch]

For each character ch' in the alphabet: Apply quicksort to the elements of V starting with ch followed by ch'. In the implementation of quicksort, compare the elements of V by comparing the suffixes they represent by indexing into the array W. At each recursion step, keep track of the number of characters that have compared equal in the group, so that they need not be compared again.

All the suffixes starting with ch have now been sorted into their final positions in V.

Q7. [update sort keys]

For each element V[i] corresponding to a suffix starting with ch (that is, for which S[V[i]] = ch), set W[V[i]] to a value with ch in its high-order bits (as before) and with i in its low-order bits (which step Q2 set to the k-1 characters following the initial ch). The new value of W[V[i]] sorts into the same position as the old value, but has the desirable property that it is distinct from all other values in W. This speeds up subsequent sorting operations, since comparisons with the new elements cannot compare equal.

This basic algorithm can be refined in a number of ways. An obvious improvement is to pick the character ch in step Q5 starting with the least common character in S, and proceeding to the most common. This allows the updates of step Q7 to have the greatest effect.

As described, the algorithm performs poorly when *S* contains many repeated substrings. We deal with this problem with two mechanisms.

The first mechanism handles strings of a single repeated character by replacing step Q6 with the following steps.

Q6a. [quicksort suffixes starting ch, ch' where $ch \neq ch'$]

For each character $ch' \neq ch$ in the alphabet: Apply quicksort to the elements of V starting with ch followed by ch'. In the implementation of quicksort,

compare the elements of V by comparing the suffixes they represent by indexing into the array W. At each recursion step, keep track of the number of characters that have compared equal in the group, so that they need not be compared again.

Q6b. [sort low suffixes starting ch, ch]

This step sorts the suffixes starting runs which would sort before an infinite string of *ch* characters. We observe that among such suffixes, long initial runs of character *ch* sort after shorter initial runs, and runs of equal length sort in the same order as the characters at the ends of the run. This ordering can be obtained with a simple loop over the suffixes, starting with the shortest.

Let V[i] represent the lexicographically least suffix starting with ch. Let j be the lowest value such that suffix V[j] starts with ch, ch.

```
while not (i = j) do
   if (V[i] > 0) and (S[V[i]-1] = ch) then
      V[j] := V[i]-1;
      j := j + 1
   end;
   i := i + 1
end;
```

All the suffixes that start with ch, ch and that are lexicographically less than an infinite sequence of ch characters are now sorted.

Q6c. [sort high suffixes starting ch, ch]

This step sorts the suffixes starting runs which would sort after an infinite string of *ch* characters. This step is very like step Q6b, but with the direction of the loop reversed.

Let V[i] represent the lexicographically greatest suffix starting with ch. Let j be the highest value such that suffix V[j] starts with ch, ch.

```
while not (i = j) do
   if (V[i] > 0) and (S[V[i]-1] = ch) then
      V[j] := V[i]-1;
      j := j - 1
   end;
   i := i - 1
end;
```

All the suffixes that start with ch, ch and that are lexicographically greater than an infinite sequence of ch characters are now sorted.

The second mechanism handles long strings of a repeated substring of more than one character. For such strings, we use a doubling technique similar to that used in Manber and Myers' scheme. We limit our quicksort implementation to perform comparisons only to a depth D. We record where suffixes have been left unsorted with a bit in the corresponding elements of V.

Once steps Q1 to Q7 are complete, the elements of the array W indicate sorted positions up to $D \times k$ characters, since each comparison compares k characters. If unsorted portions of V remain, we simply sort them again, limiting the comparison depth to D as before. This time, each comparison compares $D \times k$ characters, to yield a list of suffixes sorted on their first $D^2 \times k$ characters. We repeat this process until the entire string is sorted.

The combination of radix sort, a careful implementation of quicksort, and the mechanisms for dealing with repeated strings produce a sorting algorithm that is extremely fast on most inputs, and is quite unlikely to perform very badly on real input data.

We are currently investigating further variations of quicksort. The following approach seems promising. By applying the technique of Q6a–Q6c to all overlapping repeated strings, and by caching previously computed sort orders in a hash table, we can produce an algorithm that sorts the suffixes of a string in approximately the same time as the modified algorithm Q, but using only 6 bytes of space per input character (4 bytes for a pointer, 1 byte for the input character itself, and 1 byte amortized space in the hash table). This approach has poor performance in the worst case, but bad cases seem to be rare in practice.

4.2 Decompression

Steps D1 and D2 can be accomplished efficiently with only two passes over the data, and one pass over the alphabet, as shown in the pseudo-code below. In the first pass, we construct two arrays: C[alphabet] and P[0, ..., N-1]. C[ch] is the total number of instances in L of characters preceding character ch in the alphabet. P[i] is the number of instances of character L[i] in the prefix L[0, ..., i-1] of L. In practice, this first pass could be combined with the move-to-front decoding step. Given the arrays L, C, P, the array T defined in step D2 is given by:

for each
$$i = 0, ..., N - 1$$
: $T[i] = P[i] + C[L[i]]$

In a second pass over the data, we use the starting position I to complete Algorithm D to generate S.

Initially, all elements of C are zero, and the last column of matrix M is the vector $L[0, \ldots, N-1]$.

```
for i := 0 to N-1 do
   P[i] := C[L[i]];
   C[L[i]] := C[L[i]] + 1
end;
```

Now C[ch] is the number of instances in L of character ch. The value P[i] is the number of instances of character L[i] in the prefix L[0, ..., i-1] of L.

```
sum := 0;
for ch := FIRST(alphabet) to LAST(alphabet) do
    sum := sum + C[ch];
    C[ch] := sum - C[ch];
end;
```

Now C[ch] is the total number of instances in L of characters preceding ch in the alphabet.

```
i := I;
for j := N-1 downto 0 do
    S[j] := L[i];
    i := P[i] + C[L[i]]
end
```

The decompressed result is now S[0, ..., N-1].

5 Algorithm variants

In the example given in step C1, we treated the left-hand side of each rotation as the most significant when sorting. In fact, our implementation treats the right-hand side as the most significant, so that the decompressor will generate its output *S* from left to right using the code of Section 4.2. This choice has almost no effect on the compression achieved.

The algorithm can be modified to use a different coding scheme instead of move-to-front in step M1. Compression can improve slightly if move-to-front is replaced by a scheme in which codes that have not been seen in a very long time are moved only part-way to the front. We have not exploited this in our implementations.

Although simple Huffman and arithmetic coders do well in step M2, a more complex coding scheme can do slightly better. This is because the probability of a certain value at a given point in the vector R depends to a certain extent on the immediately preceding value. In practice, the most important effect is that zeroes tend to occur in runs in R. We can take advantage of this effect by representing each run of zeroes by a code indicating the length of the run. A second set of Huffman codes can be used for values immediately following a run of zeroes, since the next value cannot be another run of zeroes.

	Size	CPU time/s		Compressed	bits/
File	(bytes)	compress	decompress	size (bytes)	char
bib	111261	1.6	0.3	28750	2.07
book1	768771	14.4	2.5	238989	2.49
book2	610856	10.9	1.8	162612	2.13
geo	102400	1.9	0.6	56974	4.45
news	377109	6.5	1.2	122175	2.59
obj1	21504	0.4	0.1	10694	3.98
obj2	246814	4.1	0.8	81337	2.64
paper1	53161	0.7	0.1	16965	2.55
paper2	82199	1.1	0.2	25832	2.51
pic	513216	5.4	1.2	53562	0.83
progc	39611	0.6	0.1	12786	2.58
progl	71646	1.1	0.2	16131	1.80
progp	49379	0.8	0.1	11043	1.79
trans	93695	1.6	0.2	18383	1.57
Total	3141622	51.1	9.4	856233	-

Table 1: Results of compressing fourteen files of the Calgary Compression Corpus.

Block size	bits/character		
(bytes)	book1	Hector corpus	
1k	4.34	4.35	
4k	3.86	3.83	
16k	3.43	3.39	
64k	3.00	2.98	
256k	2.68	2.65	
750k	2.49	-	
1M	-	2.43	
4M	-	2.26	
16M	-	2.13	
64M	-	2.04	
103M	-	2.01	

Table 2: The effect of varying block size (N) on compression of book1 from the Calgary Compression Corpus and of the entire Hector corpus.

6 Performance of implementation

In Table 1 we give the results of compressing the fourteen commonly used files of the Calgary Compression Corpus [7] with our algorithm. Comparison of these figures with those given by Bell, Witten and Cleary [3] indicate that our algorithm does well on non-text inputs as well as text inputs.

Our implementation of Algorithm C uses the techniques described in Section 4.1, and a simple move-to-front coder. In each case, the block size N is the length of the file being compressed.

We compress the output of the move-to-front coder with a modified Huffman coder that uses the technique described in Section 5. Our coder calculates new Huffman trees for each 16 kbyte input block, rather than computing one tree for its whole input.

In Table 1, compression effectiveness is expressed as output bits per input character. The CPU time measurements were made on a DECstation 5000/200, which has a MIPS R3000 processor clocked at 25MHz with a 64 kbyte cache. CPU time is given rather than elapsed time so the time spent performing I/O is excluded.

In Table 2, we show the variation of compression effectiveness with input block size for two inputs. The first input is the file book1 from the Calgary Compression Corpus. The second is the entire Hector corpus [8], which consists of a little over 100 MBytes of modern English text. The table shows that compression improves with increasing block size, even when the block size is quite large. However, increasing the block size above a few tens of millions of characters has only a small effect.

If the block size were increased indefinitely, we expect that the algorithm would not approach the theoretical optimum compression because our simple byte-wise move-to-front coder introduces some loss. A better coding scheme might achieve optimum compression asymptotically, but this is not likely to be of great practical importance.

Comparison with other compression programmes

Table 3 compares our implementation of Algorithm C with three other compression programmes, chosen for their wide availability. The same fourteen files were compressed individually with each algorithm, and the results totalled. The bits per character values are the *means* of the values for the individual files. This metric was chosen to allow easy comparison with figures given by Bell [3].

	Total CPU time/s		Total compressed	mean
Programme	compress	decompress	size (bytes)	bits/char
compress	9.6	5.2	1246286	3.63
gzip	42.6	4.9	1024887	2.71
Alg-C/D	51.1	9.4	856233	2.43
comp-2	603.2	614.1	848885	2.47

compress is version 4.2.3 of the well-known LZW-based tool [9, 10]. gzip is version 1.2.4 of Gailly's LZ77-based tool [1, 11]. Alg-C/D is Algorithms C and D, with our back-end Huffman coder.

Table 3: Comparison with other compression programmes.

comp-2 is Nelson's comp-2 coder, limited to a fourth-order model [12].

7 Conclusions

We have described a compression technique that works by applying a reversible transformation to a block of text to make redundancy in the input more accessible to simple coding schemes. Our algorithm is general-purpose, in that it does well on both text and non-text inputs. The transformation uses sorting to group characters together based on their contexts; this technique makes use of the context on only one side of each character.

To achieve good compression, input blocks of several thousand characters are needed. The effectiveness of the algorithm continues to improve with increasing block size at least up to blocks of several million characters.

Our algorithm achieves compression comparable with good statistical modellers, yet is closer in speed to coders based on the algorithms of Lempel and Ziv. Like Lempel and Ziv's algorithms, our algorithm decompresses faster than it compresses.

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