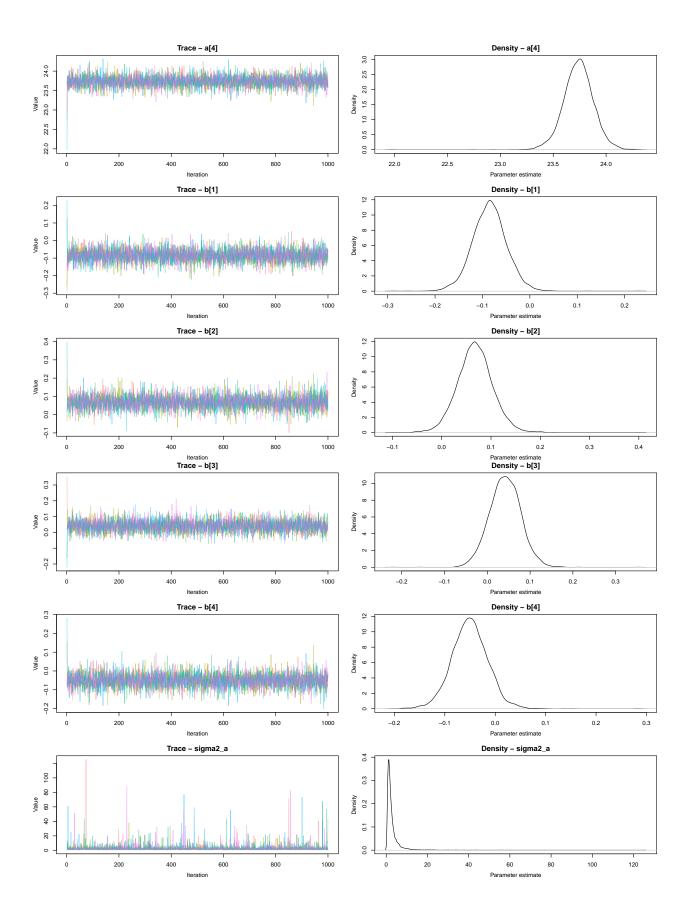
682hw5

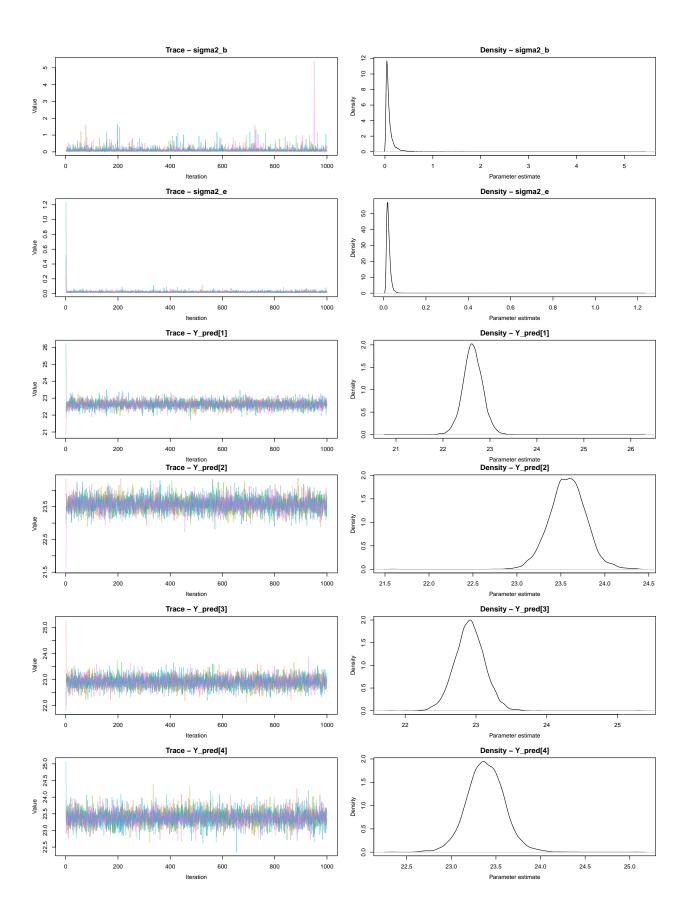
Zheng Xu

December 2, 2017

```
knitr::opts_chunk$set(fig.width=12, fig.height=8, warning=FALSE, message=FALSE)
library(R2jags)
library(MASS)
library(ggplot2)
library(mcmcplots)
library(MCMCvis)
library(geoR)
load("swim_time.RData")
    <- nrow(Y)
ns
     <- ncol(Y)
nt
JAGS_swimmer_model = function(){
  for (i in 1:ns) {
    for (j in 1:nt) {
      Y[i, j]
              ~ dnorm(mean[i, j], tau_e)
      mean[i, j] \leftarrow a[i] + b[i] *j
    }
  for (i in 1:ns){
    a[i]~ dnorm(22, tau_a)
   b[i]~ dnorm(0, tau_b)
    Y_pred[i] ~ dnorm(a[i] + b[i] * 7, tau_e)
    z[i] <- (Y_pred[i] == min(Y_pred))</pre>
  tau_a~ dgamma(0.1, 0.1)
  tau_b ~ dgamma(0.1, 0.1)
  tau_e ~ dgamma(0.1, 0.1)
  sigma2_a <- 1/tau_a
  sigma2_b <- 1/tau_b
  sigma2_e <- 1/tau_e
}
fit_swimmer_model = jags(
  data = list(Y = Y, ns = ns, nt = nt),
  inits = list(list(a = rep(20,4), b = rep(0,4)),
               list(a = rep(30,4), b = rep(1,4)),
               list(a = rep(25,4), b = rep(-1,4)),
               list(a = rep(10,4), b = rep(0,4)),
               list(a = rep(15,4), b = rep(0,4))),
parameters.to.save = c("a","b","sigma2_a","sigma2_b", "sigma2_e", "Y_pred","z"),
  n.chains = 5,
  n.iter = 10000,
 n.burnin = 1000,
  model.file = JAGS_swimmer_model
)
```

```
## Compiling model graph
 ##
            Resolving undeclared variables
 ##
            Allocating nodes
 ## Graph information:
            Observed stochastic nodes: 24
 ##
            Unobserved stochastic nodes: 15
 ##
            Total graph size: 158
 ##
 ##
 ## Initializing model
 chains = as.mcmc(fit_swimmer_model)
 MCMCtrace(chains, pdf = FALSE, params = c("a","b","sigma2_a","sigma2_b", "sigma2_e", "Y_pred"))
                                                                                                                    Density - a[1]
                                                                                   3.0
                                                                                   2.5
    23.5
            t keesta kala kassa addi is ka addi is ad armaa adaiil daa aylad. Armaa saa gaad oo laa data saa dada
Jarahe ya ayyyy a saa yiyy gaay gaalaa ya ayaa a ay ga ahay caasaa ay oo ay aa ay ay a ay ay ay ay ay b
                                                                                   1.0 1.5 2.0
 Value
22.0 22.5 23.0 2
                                                                                   0.5
                                                                                   0.0
                      200
                                                             800
                                                                          1000
                                                                                           21.5
                                                                                                      22.0
                                                                                                                  22.5
                                                                                                                                                     24.0
                                     Trace - a[2]
                                                                                                                    Density - a[2]
                                                                                   1.0 1.5 2.0 2.5 3.0
    23.0
                                                                                 Density
 Value
    22.0
                                                                                   0.5
                                                                                   0.0
                                   400
                                                                          1000
                                                                                                                           22.5
                                                                                                                    Density - a[3]
                                     Trace - a[3]
                                                                                   2.5
    23.5
Value
23.0
                                                                                   2.0
                                                                                   -5.
    22.5
                                                                                   1.0
    22.0
                                                                                   0.5
                                                                                   0.0
```





gelman.diag(chains, multivariate = FALSE)

```
## Potential scale reduction factors:
##
##
              Point est. Upper C.I.
## Y_pred[1]
                     1.00
                                 1.00
## Y_pred[2]
                     1.00
                                 1.00
## Y_pred[3]
                     1.00
                                 1.01
## Y_pred[4]
                     1.00
                                 1.01
## a[1]
                     1.00
                                 1.00
## a[2]
                     1.00
                                 1.00
## a[3]
                     1.00
                                 1.00
## a[4]
                     1.00
                                 1.00
## b[1]
                     1.00
                                 1.00
## b[2]
                     1.00
                                 1.00
## b[3]
                     1.00
                                 1.00
## b[4]
                     1.00
                                 1.00
## deviance
                     1.00
                                 1.01
## sigma2_a
                     1.01
                                 1.01
## sigma2_b
                     1.09
                                 1.10
## sigma2_e
                     1.00
                                 1.00
## z[1]
                     1.00
                                 1.00
## z[2]
                      \mathtt{NaN}
                                  \mathtt{NaN}
## z[3]
                     1.00
                                 1.00
## z[4]
                     1.06
                                 1.06
```

b. PPD

To obtain PPD, draw Y_pred in the JAGS model, densityplots shown for Y_pred is the posterior predictive distribution. We also obtain mean and 95% CI for Y_pred.

summary(chains)

```
##
## Iterations = 1:8992
## Thinning interval = 9
## Number of chains = 5
## Sample size per chain = 1000
##
## 1. Empirical mean and standard deviation for each variable,
##
      plus standard error of the mean:
##
##
                             SD Naive SE Time-series SE
## Y_pred[1]
              22.63421 0.21431 0.0030308
                                               0.0031274
## Y_pred[2]
              23.57707 0.20651 0.0029205
                                               0.0028497
## Y_pred[3]
              22.91268 0.21203 0.0029986
                                               0.0029293
## Y_pred[4]
              23.38329 0.20896 0.0029551
                                               0.0029547
## a[1]
              23.22786 0.14225 0.0020117
                                               0.0019784
## a[2]
              23.10830 0.14413 0.0020383
                                               0.0020386
## a[3]
              22.61924 0.14266 0.0020175
                                               0.0020678
## a[4]
              23.73894 0.14266 0.0020175
                                               0.0020173
## b[1]
              -0.08508 0.03608 0.0005102
                                               0.0004979
## b[2]
               0.06775 0.03614 0.0005111
                                               0.0005176
               0.04161 0.03659 0.0005174
## b[3]
                                               0.0005210
```

```
## b[4]
               -0.05055 0.03612 0.0005108
                                                 0.0005108
## deviance
             -33.65562 8.04383 0.1137570
                                                 0.1135954
## sigma2_a
                2.98535 5.00851 0.0708311
                                                 0.0708179
## sigma2_b
                0.09813 0.14151 0.0020013
                                                 0.0020009
## sigma2_e
                0.02346 0.02180 0.0003083
                                                 0.0003065
## z[1]
                0.82980 0.37585 0.0053153
                                                 0.0052624
## z[2]
                0.00020 0.01414 0.0002000
                                                 0.0002000
## z[3]
                0.16680 0.37283 0.0052727
                                                 0.0052203
## z[4]
                0.00320 0.05648 0.0007988
                                                 0.0008346
##
## 2. Quantiles for each variable:
##
##
                    2.5%
                                25%
                                           50%
                                                     75%
                                                              97.5%
                          22.50143
## Y_pred[1]
               22.220277
                                     22.63117
                                                22.76883
                                                           23.04825
## Y_pred[2]
               23.172336
                          23.44412
                                     23.57878
                                                23.71040
                                                           23.98216
## Y_pred[3]
               22.503286
                          22.77686
                                     22.91214
                                                23.04770
                                                           23.31816
## Y_pred[4]
               22.971321
                          23.24831
                                     23.38051
                                                23.51728
                                                           23.79680
## a[1]
               22.953355
                          23.14013
                                     23.22810
                                                23.31931
                                                           23.50335
               22.822348
## a[2]
                          23.02151
                                     23.11209
                                                23.20047
                                                           23.38406
## a[3]
               22.345367
                          22.52860
                                     22.61770
                                                22.71080
                                                           22.90192
## a[4]
               23.452953
                          23.65010
                                     23.74043
                                                23.82952
                                                           24.01211
               -0.156986
                          -0.10829
                                                -0.06244
                                                           -0.01451
## b[1]
                                     -0.08505
## b[2]
               -0.001405
                            0.04518
                                      0.06733
                                                 0.08976
                                                            0.13957
               -0.029914
## b[3]
                            0.01772
                                      0.04159
                                                 0.06588
                                                            0.11344
## b[4]
               -0.120128
                          -0.07376
                                     -0.05106
                                                -0.02755
                                                            0.01954
## deviance
              -46.608882 -39.19464
                                    -34.48124
                                               -28.93283
                                                         -16.36224
## sigma2_a
                0.538198
                            1.13404
                                      1.80302
                                                 3.09261
                                                           12.18865
## sigma2_b
                0.019433
                            0.03938
                                      0.06230
                                                 0.10741
                                                            0.40388
## sigma2_e
                0.011224
                            0.01666
                                      0.02096
                                                 0.02703
                                                            0.04622
## z[1]
                0.000000
                            1.00000
                                      1.00000
                                                 1.00000
                                                            1.00000
## z[2]
                0.000000
                            0.00000
                                      0.00000
                                                 0.00000
                                                            0.00000
## z[3]
                0.000000
                            0.00000
                                      0.00000
                                                 0.00000
                                                            1.00000
## z[4]
                0.000000
                            0.00000
                                      0.00000
                                                 0.00000
                                                            0.00000
```

c.

In the JAGS model, we define Z as indicator function that individual i has the fastest posterior predictive value. In this case, we output the posterior mean of Z, as the probablity $Pr(Y_i^* = min(Y_1^*, ..., Y_4^*)|\mathbf{Y})$. Based on posterior mean of z = (0.8364, 0.0012, 0.1594, 0.003), we would recommend swimmer 1.

Problem 2.

a.

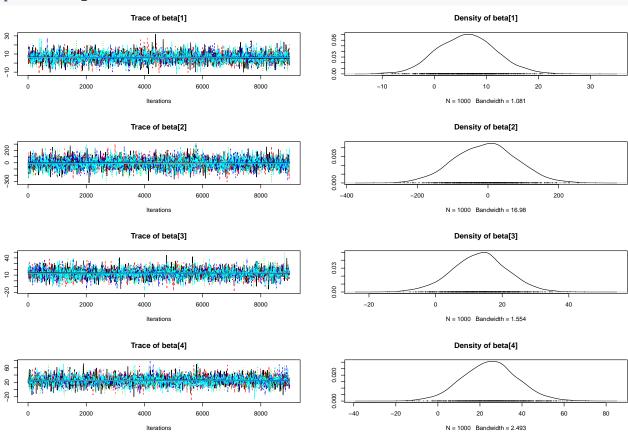
Linear regression.

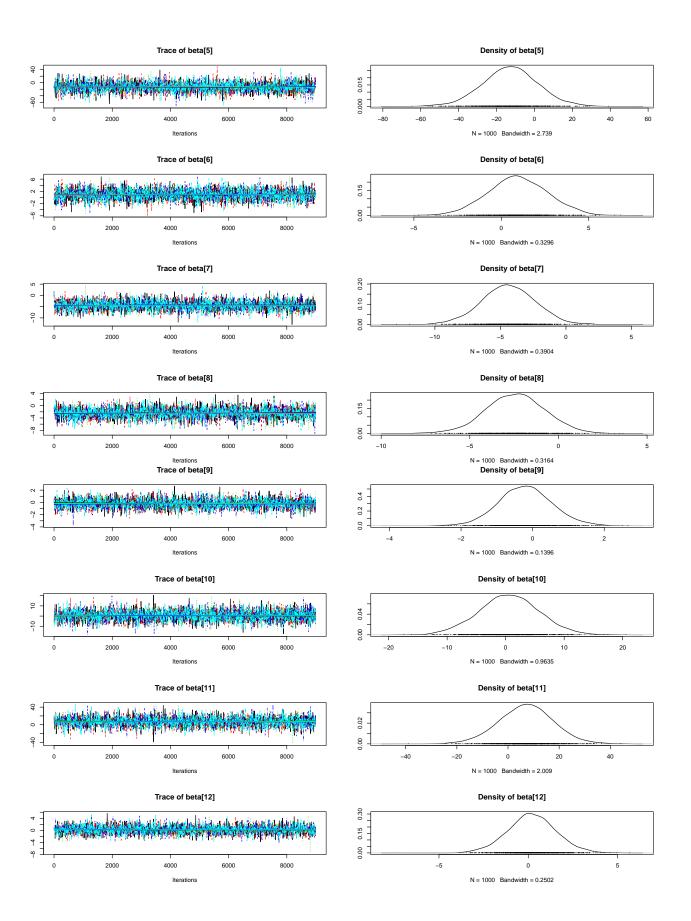
```
#import data
X = UScrime[,1:15]
Y = UScrime[,16]
n = nrow(UScrime)
p = ncol(UScrime) - 1
df = list()
```

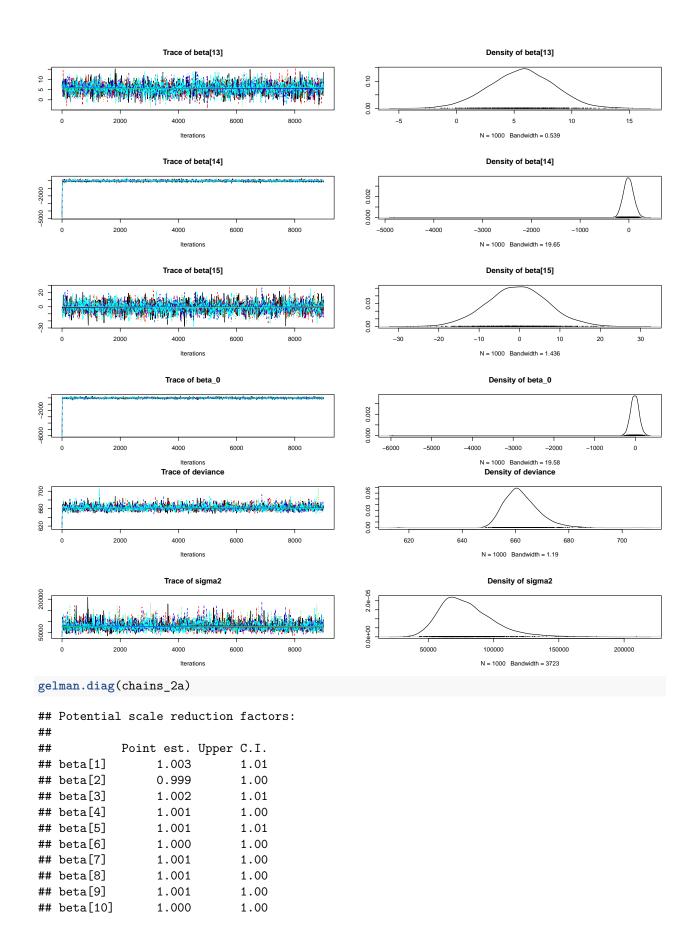
```
df$X = X
df\$Y = Y
dfn = n
df$p = p
JAGS_BLR_flat = function(){
  # Likelihood
  for(i in 1:n){
    Y[i] ~ dnorm(mu[i],inv_sigma2)
    mu[i] <- beta_0 + inprod(X[i,],beta)</pre>
  # Prior for beta
  for(j in 1:p){
    beta[j] ~ dnorm(0,0.0001)
    #non-informative priors
  }
  # Prior for intercept
  beta_0 ~ dnorm(0, 0.0001)
  # Prior for the inverse variance
  inv_sigma2 ~ dgamma(0.0001, 0.0001)
  sigma2 <- 1.0/inv_sigma2
fit_JAGS_flat = jags(data=df,
                inits=list(list(beta = rnorm(p),
                                 beta_0 = 0,
                                 inv_sigma2 = 1),
                         list(beta = rnorm(p),
                                 beta_0 = 1,
                                 inv_sigma2 = 2),
                           list(beta = rnorm(p),
                                 beta_0 = 2,
                                 inv_sigma2 = 2),
                           list(beta = rnorm(p),
                                 beta_0 = 10,
                                 inv_sigma2 = 5),
                         list(beta = rnorm(p),
                                 beta_0 = 20,
                                 inv_sigma2 = 1)),
                parameters.to.save = c("beta_0", "beta", "sigma2"),
                n.chains=5,
                n.iter=10000,
                n.burnin=1000,
                model.file=JAGS_BLR_flat)
## Compiling model graph
##
      Resolving undeclared variables
      Allocating nodes
##
## Graph information:
##
      Observed stochastic nodes: 47
##
      Unobserved stochastic nodes: 17
      Total graph size: 950
##
```

##
Initializing model

chains_2a = as.mcmc(fit_JAGS_flat)
plot(chains_2a)







```
## beta[11]
                  1.000
                              1.00
## beta[12]
                  1.001
                              1.00
## beta[13]
                  1.001
                              1.00
## beta[14]
                  1.000
                              1.00
## beta[15]
                  1.000
                              1.00
                              1.00
## beta 0
                  1.000
## deviance
                  1.001
                              1.00
## sigma2
                  1.005
                              1.01
##
## Multivariate psrf
## 1.01
##output 95% credible interval
summary(chains_2a)
##
## Iterations = 1:8992
## Thinning interval = 9
## Number of chains = 5
## Sample size per chain = 1000
##
## 1. Empirical mean and standard deviation for each variable,
##
      plus standard error of the mean:
##
                                   Naive SE Time-series SE
##
                   Mean
                               SD
## beta[1]
                6.2665
                            5.600
                                     0.07919
                                                     0.07773
## beta[2]
                -6.2477
                           87.991
                                     1.24438
                                                     1.22961
## beta[3]
                13.2462
                            8.368
                                     0.11835
                                                     0.11490
## beta[4]
                24.8543
                           13.238
                                     0.18721
                                                     0.18716
## beta[5]
              -12.7524
                           14.686
                                     0.20769
                                                     0.20759
## beta[6]
                0.9395
                            1.712
                                     0.02421
                                                     0.02328
               -4.3958
## beta[7]
                            2.046
                                     0.02894
                                                     0.02829
## beta[8]
                -2.4215
                            1.678
                                     0.02373
                                                     0.02372
## beta[9]
               -0.1999
                            0.745
                                     0.01054
                                                     0.01004
## beta[10]
                0.5547
                            5.136
                                     0.07264
                                                     0.07169
## beta[11]
                7.0196
                           10.712
                                     0.15148
                                                     0.15147
## beta[12]
                 0.2036
                            1.353
                                     0.01913
                                                     0.01952
## beta[13]
                5.6415
                            2.805
                                     0.03966
                                                     0.03790
## beta[14]
              -13.6725
                          182.689
                                     2.58361
                                                     2.58445
## beta[15]
                -0.4990
                            7.564
                                     0.10696
                                                     0.10700
## beta 0
              -23.4653
                          213.148
                                     3.01437
                                                     3.01544
## deviance
              662.2543
                            6.606
                                     0.09343
                                                     0.09352
## sigma2
            79533.4483 20590.852 291.19863
                                                   290.99404
##
## 2. Quantiles for each variable:
##
##
                   2.5%
                                           50%
                                                       75%
                                                                97.5%
                               25%
## beta[1]
            -4.327e+00
                         2.391e+00
                                        6.2105
                                                    9.9408
                                                            1.747e+01
## beta[2]
            -1.797e+02 -6.666e+01
                                                   51.5321
                                                            1.662e+02
                                       -4.6218
## beta[3]
            -3.784e+00 7.825e+00
                                       13.4183
                                                   18.6130
                                                            2.945e+01
## beta[4]
                                                   33.3070
                                                            5.166e+01
            -9.218e-01 1.599e+01
                                       24.8460
## beta[5]
                                      -12.7385
                                                   -3.1869
            -4.161e+01 -2.221e+01
                                                            1.700e+01
## beta[6]
            -2.428e+00 -1.824e-01
                                        0.9265
                                                    2.1062
                                                            4.268e+00
```

beta[7]

-8.468e+00 -5.753e+00

-3.0418 -4.739e-01

-4.4165

```
-1.3297 8.129e-01
## beta[8] -5.781e+00 -3.527e+00
                                   -2.4091
## beta[9] -1.640e+00 -6.926e-01
                                   -0.2052
                                              0.2767 1.312e+00
## beta[10] -9.464e+00 -2.802e+00
                                  0.5451
                                             3.8889 1.066e+01
                                           13.8972 2.812e+01
## beta[11] -1.439e+01 -5.498e-02
                                   7.2358
## beta[12] -2.517e+00 -6.659e-01
                                  0.1811
                                              1.0713 2.925e+00
## beta[13] 9.149e-02 3.803e+00
                                             7.5454 1.104e+01
                                  5.7142
## beta[14] -2.036e+02 -7.807e+01 -10.3631 58.3941 1.889e+02
## beta[15] -1.551e+01 -5.458e+00
                                             4.5134 1.476e+01
                                  -0.4843
          -2.134e+02 -8.536e+01
## beta 0
                                  -16.9771
                                             50.5969 1.781e+02
## deviance 6.519e+02 6.577e+02
                                  661.4326
                                            666.0076 6.771e+02
## sigma2
            4.852e+04 6.488e+04 76334.0844 90729.4792 1.284e+05
```

b.

Cross validation

```
#split data into training and test set
split_data = function(df,train_test_ratio = 1,random=TRUE){
 n_train = floor(df$n*train_test_ratio/(1+train_test_ratio))
 n_{test} = df n - n_{train}
  if(random){
   train_idx = sample(1:n,n_train,replace = FALSE)
   test idx = setdiff(1:n,train idx)
  else{
   train_idx = 1:n_train
    test_idx = n_train+1:n_test
  df_t = list()
  df_t$Y_train = df$Y[train_idx]
  df_t$X_train = df$X[train_idx,,drop=FALSE]
  df_t$X_test = df$X[test_idx,,drop=FALSE]
  df_t$n_train = n_train
  df_t$n_test = n_test
  df_t = dfp
  return(list(df_t=df_t,Y_test=df$Y[test_idx]))
}
pred = split_data(df, random = FALSE)
##define a predictive JAGS
JAGS_BLR_flat_pred = function(){
  # Likelihood
  for(i in 1:n_train){
   Y_train[i] ~ dnorm(mu_train[i],inv_sigma2)
   mu_train[i] <- beta_0 + inprod(X_train[i,],beta)</pre>
    # same as beta_0 + X[i,1]*beta[1] + \dots + X[i,p]*beta[p]
  # Prior for beta
 for(j in 1:p){
   beta[j] \sim dnorm(0,0.0001)
  #non-informative priors
```

```
# Prior for intercept
  beta_0 ~ dnorm(0, 0.0001)
  # Prior for the inverse variance
  inv_sigma2 ~ dgamma(0.0001, 0.0001)
  sigma2 <- 1.0/inv_sigma2</pre>
  #prediction
   # Predictions
  for(i in 1:n_test){
    Y_test[i] ~ dnorm(mu_test[i],inv_sigma2)
    mu_test[i] <- beta_0 + inprod(X_test[i,],beta)</pre>
}
fit_JAGS_flat_pred = jags(data=pred$df_t,
                inits=list(list(beta = rnorm(p),
                                 beta_0 = 0,
                                 inv_sigma2 = 1),
                         list(beta = rnorm(p),
                                 beta_0 = 1,
                                 inv_sigma2 = 2),
                          list(beta = rnorm(p),
                                 beta 0 = 2,
                                 inv_sigma2 = 2),
                          list(beta = rnorm(p),
                                 beta_0 = 10,
                                 inv_sigma2 = 5),
                         list(beta = rnorm(p),
                                 beta_0 = 20,
                                 inv_sigma2 = 1)),
                parameters.to.save = c("beta_0","beta","sigma2", "Y_test"),
                n.chains=5,
                n.iter=10000,
                n.burnin=1000,
                model.file=JAGS_BLR_flat_pred)
## Compiling model graph
      Resolving undeclared variables
##
      Allocating nodes
##
## Graph information:
      Observed stochastic nodes: 23
##
      Unobserved stochastic nodes: 41
##
##
      Total graph size: 951
##
## Initializing model
chains_2b = as.mcmc(fit_JAGS_flat_pred)
##plot the predictive values
result = summary(chains_2b)
q = result$quantiles
dtfr = as.data.frame(cbind(result$quantiles))
```

```
##compare
pred$Y_test

## [1] 968 523 1993 342 1216 1043 696 373 754 1072 923 653 1272 831
## [15] 566 826 1151 880 542 823 1030 455 508 849

fit_JAGS_flat_pred$BUGSoutput$median$Y_test

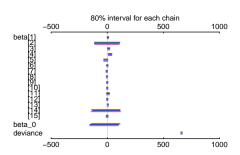
## [1] 702.3189 911.1052 1694.7808 190.2616 861.1977 2098.1610 798.2761
## [8] 289.2185 1290.1620 658.4909 761.7653 1272.8585 764.8326 562.4828
## [15] 745.2396 995.5814 1403.8654 534.4566 503.4575 887.8674 580.6554
## [22] 550.1389 1331.0586 592.6950
```

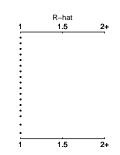
c. Slab and spike

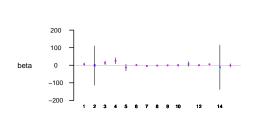
```
JAGS BLR SpikeSlab = function(){
  # Likelihood
  for(i in 1:n){
    Y[i] ~ dnorm(mu[i],inv_sigma2)
    mu[i] <- beta_0 + inprod(X[i,],beta)</pre>
    # same as beta_0 + X[i,1]*beta[1] + \dots + X[i,p]*beta[p]
  #Prior for beta_j
 for(j in 1:p){
    beta[j] ~ dnorm(0,inv_tau2[j])
    inv_tau2[j] <- (1-gamma[j])*1000+gamma[j]*0.01</pre>
    gamma[j] ~ dbern(0.5)
  # Prior for intercept
  beta_0 ~ dnorm(0, 0.0001)
  # Prior for the inverse variance
  inv_sigma2 ~ dgamma(0.0001, 0.0001)
  sigma2 <- 1.0/inv_sigma2
fit_JAGS_SpikeSlab = jags(data=df,
                inits=list(list(beta = rnorm(p),
                                 beta_0 = 0,
                                 inv_sigma2 = 1),
                          list(beta = rnorm(p),
                                 beta_0 = 1,
                                 inv_sigma2 = 2),
                          list(beta = rnorm(p),
                                 beta 0 = 2,
                                 inv_sigma2 = 2),
                          list(beta = rnorm(p),
                                 beta_0 = 10,
                                 inv_sigma2 = 5),
                          list(beta = rnorm(p),
                                 beta_0 = 20,
                                 inv_sigma2 = 1)),
                parameters.to.save = c("beta_0","beta","sigma2"),
```

```
n.chains=5,
                n.iter=10000,
                n.burnin=1000,
                model.file=JAGS_BLR_flat)
## Compiling model graph
##
      Resolving undeclared variables
##
      Allocating nodes
##
  Graph information:
##
      Observed stochastic nodes: 47
      Unobserved stochastic nodes: 17
##
##
      Total graph size: 950
##
## Initializing model
plot(fit_JAGS_SpikeSlab)
```

Bugs model at "/tmp/RtmpqEqWQS/model7195a6a6033.txt", fit using jags, 5 chains, each with 10000 iterations (first 1000 discarded)







medians and 80% intervals







```
chains_2c = as.mcmc(fit_JAGS_SpikeSlab)
summary(chains_2c)
```

```
##
## Iterations = 1:8992
## Thinning interval = 9
## Number of chains = 5
```

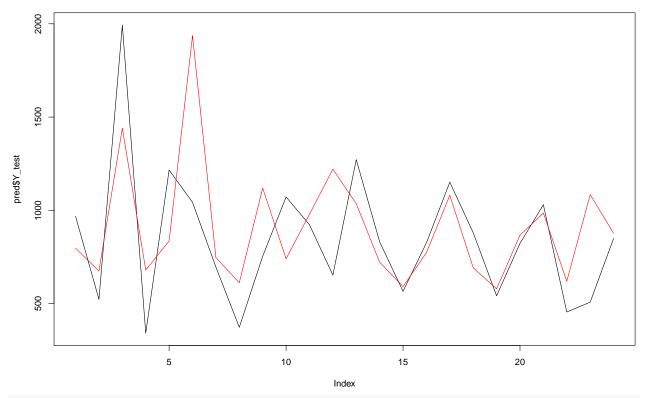
```
## Sample size per chain = 1000
##
  1. Empirical mean and standard deviation for each variable,
##
##
     plus standard error of the mean:
##
##
                               Naive SE Time-series SE
                             SD
                 Mean
## beta[1]
               6.3092
                          5.400
                                  0.07637
                                                0.07628
## beta[2]
              -2.6117
                         88.419
                                  1.25043
                                                1.25034
## beta[3]
              13.2802
                          8.259
                                  0.11680
                                                0.11681
## beta[4]
              25.1446
                         13.178
                                  0.18636
                                                0.18134
## beta[5]
             -13.0849
                         14.577
                                  0.20615
                                                0.20049
## beta[6]
               0.9506
                          1.692
                                  0.02392
                                                0.02419
## beta[7]
              -4.3264
                          1.991
                                  0.02815
                                                0.02816
## beta[8]
              -2.3521
                          1.654
                                  0.02339
                                                0.02338
## beta[9]
              -0.2120
                          0.739
                                  0.01045
                                                0.01053
## beta[10]
               0.3355
                          5.068
                                  0.07167
                                                0.07170
                                                0.14843
## beta[11]
               7.4999
                         10.496
                                  0.14843
## beta[12]
               0.1314
                          1.325
                                  0.01874
                                                0.01846
## beta[13]
               5.4855
                          2.782
                                  0.03934
                                                0.03935
## beta[14]
             -17.3998
                        182.078
                                  2.57497
                                                2.57593
## beta[15]
              -0.7892
                          7.525
                                  0.10642
                                                0.10578
## beta 0
                        213.578
             -27.1134
                                  3.02045
                                                3.02106
## deviance
             662.0127
                          6.519
                                  0.09219
                                                0.09116
           79143.6611 20658.342 292.15307
                                              306.47839
## sigma2
##
## 2. Quantiles for each variable:
##
##
                 2.5%
                             25%
                                       50%
                                                  75%
                                                           97.5%
## beta[1]
           -4.554e+00
                          2.7418
                                                       1.670e+01
                                     6.3351
                                               9.9140
## beta[2]
           -1.759e+02
                        -61.6151
                                    -4.4024
                                              55.8237
                                                       1.725e+02
## beta[3]
           -3.055e+00
                          7.8237
                                    13.3335
                                              18.6867
                                                       2.982e+01
## beta[4]
            1.121e-01
                         16.3637
                                    25.0514
                                              33.8903
                                                       5.097e+01
## beta[5]
           -4.198e+01
                        -22.7576
                                   -13.1229
                                              -3.4576
                                                       1.527e+01
                                               2.0783
## beta[6]
           -2.346e+00
                         -0.1727
                                    0.9546
                                                       4.264e+00
## beta[7]
           -8.164e+00
                         -5.6202
                                    -4.3302
                                              -3.0469 -4.070e-01
                                              -1.2744 9.474e-01
## beta[8]
           -5.645e+00
                         -3.4453
                                   -2.3590
## beta[9]
           -1.653e+00
                         -0.6958
                                    -0.1988
                                               0.2833 1.220e+00
## beta[10] -9.754e+00
                         -3.0409
                                    0.4276
                                               3.7375
                                                       1.029e+01
## beta[11] -1.295e+01
                          0.6334
                                    7.4273
                                              14.4106
                                                       2.804e+01
## beta[12] -2.517e+00
                                                       2.759e+00
                         -0.7261
                                    0.1227
                                               1.0188
## beta[13] 9.279e-02
                          3.5854
                                    5.4443
                                               7.3662 1.102e+01
## beta[14] -2.079e+02
                        -80.9641
                                   -14.8048
                                              53.8219
                                                       1.900e+02
## beta[15] -1.534e+01
                         -5.6004
                                   -0.9122
                                               4.1580
                                                       1.398e+01
## beta_0
           -2.216e+02
                        -89.2852
                                   -19.9943
                                              46.1587
                                                       1.732e+02
## deviance 6.518e+02
                        657.5149
                                   661.2607
                                             665.6451
                                                       6.771e+02
            4.816e+04 64411.3123 76117.5539 89902.4117
                                                       1.282e+05
##Prediction
JAGS_BLR_SpikeSlab_pred = function(){
# Likelihood
```

```
for(i in 1:n_train){
    Y_train[i] ~ dnorm(mu_train[i],inv_sigma2)
    mu_train[i] <- beta_0 + inprod(X_train[i,],beta)</pre>
    # same as beta_0 + X[i,1]*beta[1] + ... + X[i,p]*beta[p]
  }
  # Prior for beta
 for(j in 1:p){
    beta[j] ~ dnorm(0,inv tau2[j])
    inv_tau2[j] <- (1-gamma[j])*1000+gamma[j]*0.01
    gamma[j] ~ dbern(0.5)
  }
  # Prior for intercept
  beta_0 ~ dnorm(0, 0.0001)
  # Prior for the inverse variance
  inv_sigma2 ~ dgamma(0.0001, 0.0001)
  sigma2 <- 1.0/inv_sigma2
  #prediction
   # Predictions
  for(i in 1:n_test){
    Y_test[i] ~ dnorm(mu_test[i],inv_sigma2)
    mu_test[i] <- beta_0 + inprod(X_test[i,],beta)</pre>
  }
}
fit_JAGS_SpikeSlab_pred = jags(data = pred$df_t,
                inits=list(list(beta = rnorm(p),
                                 beta_0 = 0,
                                 inv_sigma2 = 1),
                         list(beta = rnorm(p),
                                 beta_0 = 1,
                                 inv_sigma2 = 2),
                          list(beta = rnorm(p),
                                 beta_0 = 2,
                                 inv_sigma2 = 2),
                          list(beta = rnorm(p),
                                 beta_0 = 10,
                                 inv_sigma2 = 5),
                         list(beta = rnorm(p),
                                 beta_0 = 20,
                                 inv_sigma2 = 1)),
                parameters.to.save = c("beta_0","beta","sigma2","Y_test"),
                n.chains=5,
                n.iter=10000,
                n.burnin=1000,
                model.file=JAGS_BLR_SpikeSlab_pred)
## Compiling model graph
##
      Resolving undeclared variables
      Allocating nodes
##
## Graph information:
##
      Observed stochastic nodes: 23
```

##

Unobserved stochastic nodes: 56

```
Total graph size: 1071
##
##
## Initializing model
cbind(pred$Y_test, fit_JAGS_SpikeSlab_pred$BUGSoutput$median$Y_test)
         [,1]
                  [,2]
##
   [1,] 968 796.8714
##
   [2,] 523 674.8399
   [3,] 1993 1440.6227
   [4,] 342 680.0654
##
##
   [5,] 1216 835.9979
##
  [6,] 1043 1936.1407
  [7,] 696 746.9942
##
   [8,] 373 611.9618
##
## [9,] 754 1119.7948
## [10,] 1072 740.4464
## [11,] 923 979.5285
## [12,] 653 1220.9262
## [13,] 1272 1035.2173
## [14,] 831 722.1332
## [15,] 566 591.3444
## [16,] 826 773.2865
## [17,] 1151 1080.8901
## [18,] 880 692.0879
## [19,] 542 579.3675
## [20,] 823 867.2079
## [21,] 1030 985.5025
## [22,] 455 619.7641
## [23,] 508 1084.4153
## [24,] 849 877.1035
plot(pred$Y_test, type = 'l')
lines(fit_JAGS_SpikeSlab_pred$BUGSoutput$median$Y_test, col= 'red')
```



v_loc = unique(gambia[,"x"])
v = match(gambia[,"x"],v_loc)