

## Chapter 3

# Optimization

### 3.1 Optimization Problems

Problem 3.1

$$\begin{aligned} f(x, y) &= (1 - y)^2 + 100 * (x - y^2)^2 \\ (x_0, y_0) &= [-0.5, -1.5]; \\ Interval \quad &-2 : 0.01 : 2; y = -2 : 0.01 : 2; \\ \alpha_g &= 0.001; \quad \alpha_n = 0.5; \end{aligned} \tag{3.1}$$

Problem 3.2

$$\begin{aligned} f(x, y) &= x^2 + x * y + 3 * y^2 \\ (x_0, y_0) &= [-0.5, -1.5]; \\ Interval \quad &x = -3 : 0.1 : 3; y = -3 : 0.1 : 3; \\ \alpha_g &= 0.1; \quad \alpha_n = 0.5; \end{aligned} \tag{3.2}$$

Problem 3.3

$$\begin{aligned} f(x, y) &= \sin(0.5 * x^2 - 0.25 * y^2 + 3) * \cos(2 * x + 1 - \exp(y)); \\ (x_0, y_0) &= [-0.2, 0.2]; \\ Interval \quad &x = -2 : 0.01 : 2; y = -2 : 0.01 : 2; \\ \alpha_g &= 0.1; \quad \alpha_n = 0.5; \end{aligned} \tag{3.3}$$

Problem 3.4

$$\begin{aligned} f(x, y) &= x^2 - x + \sin(y); \\ (x_0, y_0) &= [3, -1]; \\ Interval \quad &x = -5 : 0.1 : 5; y = -5 : 0.1 : 5; \\ \alpha_g &= 0.1; \quad \alpha_n = 0.5; \end{aligned} \tag{3.4}$$

Problem 3.5

$$\begin{aligned} f(x, y) &= x * e^{(-x^2/0.25 - y^2/0.25)}; \\ (x_0, y_0) &= [-0.2, 0.1]; \\ Interval \quad &x = -1 : 0.01 : 1; y = -1 : 0.01 : 1; \\ \alpha_g &= 0.1; \quad \alpha_n = 0.5; \end{aligned} \tag{3.5}$$

Problem 3.6

$$\begin{aligned}
 f(x, y) &= (x - y)^4 + 2 * x^2 + y^2 - x + 2 * y; \\
 (x_0, y_0) &= [1, 1]; \\
 \text{Interval } x &= -1 : 0.01 : 1; y = -1 : 0.01 : 1; \\
 \alpha_g &= 0.1; \quad \alpha_n = 0.5;
 \end{aligned} \tag{3.6}$$

Problem 3.7

$$\begin{aligned}
 f(x, y) &= -\ln(1 - x - y) - \ln(x) - \ln(y); \\
 (x_0, y_0) &= [0.1, 0.1]; \\
 \text{Interval } x &= 0.01 : 0.001 : 0.5; y = 0.01 : 0.001 : 0.5; \\
 \alpha_g &= 0.01; \quad \alpha_n = 0.5;
 \end{aligned} \tag{3.7}$$

Problem 3.8

$$\begin{aligned}
 f(x, y) &= x * y * e^{(16 * x^2 + 9 * y^2) / 288} \\
 (x_0, y_0) &= [2, 2]; \\
 \text{Interval } x &= -3 : 0.1 : 3; y = -3 : 0.1 : 3; \\
 \alpha_g &= 0.01; \quad \alpha_n = 0.5;
 \end{aligned} \tag{3.8}$$

Problem 3.9

$$\begin{aligned}
 f(x, y) &= e^{(x^2 + y^2 - 6y)}; \\
 (x_0, y_0) &= [1.25, 4.5]; \\
 \text{Interval } x &= -1.5 : 0.1 : 1.5; y = 1 : 0.1 : 5; \\
 \alpha_g &= 0.5; \quad \alpha_n = 0.5;
 \end{aligned} \tag{3.9}$$

Problem 3.10

$$\begin{aligned}
 f(x, y) &= -x * \ln(y^2 / x) - 3 * x + x * y^2; \\
 (x_0, y_0) &= [2.5, 1.25]; \\
 \text{Interval } x &= 1.5 : 0.1 : 4; y = -1 : 0.1 : 5; \\
 \alpha_g &= 0.1; \quad \alpha_n = 0.5;
 \end{aligned} \tag{3.10}$$

Problem 3.11

$$\begin{aligned}
 f(x, y) &= \frac{x}{(x^2 + y^2 + 4)} \\
 (x_0, y_0) &= [-1.0, -0.5]; \\
 \text{Interval } x &= -3 : 0.1 : 3; y = -3 : 0.1 : 3; \\
 \alpha_g &= 0.5; \quad \alpha_n = 0.5;
 \end{aligned} \tag{3.11}$$

Problem 3.12

$$\begin{aligned}
 f(x, y) &= \frac{-(2xy)}{(x^2 + y^2 + 4)^2} \\
 (x_0, y_0) &= [0.5, 0.75]; \\
 \text{Interval } x &= -2 : 0.1 : 2; y = -2 : 0.1 : 2; \\
 \alpha_g &= 0.5; \quad \alpha_n = 0.5;
 \end{aligned} \tag{3.12}$$

Problem 3.13

$$\begin{aligned}
f(x, y) &= \frac{-1}{(x^2 + y^2 + 3x - 2y + 1)} \\
(x_0, y_0) &= [-1.8, 1.6]; \\
Interval \quad x &= -2 : 0.01 : -1.0; y = 0.0 : 0.01 : 2.0; \\
\alpha_g &= 0.5; \quad \alpha_n = 0.5;
\end{aligned} \tag{3.13}$$

Problem 3.14

$$\begin{aligned}
f(x, y) &= \frac{1}{(\sqrt{x} + \sqrt{y} - x - y)} \\
(x_0, y_0) &= [0.6, 0.6]; \\
Interval \quad x &= -0.0 : 0.01 : 1; y = -0.0 : 0.01 : 1; \\
\alpha_g &= 0.15; \quad \alpha_n = 0.5;
\end{aligned} \tag{3.14}$$

Problem 3.15

$$\begin{aligned}
f(x, y) &= x * \exp(-(x^2 + y^2)) \\
(x_0, y_0) &= [-1.0, 0.45]; \\
Interval \quad x &= -2.0 : 0.1 : 2.0; y = -2.0 : 0.1 : 2.0; \\
\alpha_g &= 0.5; \quad \alpha_n = 0.5;
\end{aligned} \tag{3.15}$$

Problem 3.16

$$\begin{aligned}
f(x, y) &= 3(1 - x)^2 e^{-x^2 - (y+1)^2} - 10\left(\frac{x}{5} - x^3 - y^5\right) e^{-x^2 - y^2} - \frac{1}{3} e^{-y^2 - (x+1)^2} \\
(x_0, y_0) &= [0.75, -1.25]; \\
Interval \quad x &= -2.5 : 0.1 : 2.5; y = -3.0 : 0.1 : 3.0; \\
\alpha_g &= 0.015; \quad \alpha_n = 0.1;
\end{aligned} \tag{3.16}$$

## 3.2 Matlab

$$\begin{aligned}
S_e &= \sum_{i=1}^n (y - y_o)^2 \\
S_e &= \sum_{i=1}^n \left( y - \sum_{j=0}^m a_j x^j \right)^2
\end{aligned}$$

## 3.3 Example

A neural network with two inputs, two hidden neurons, two output neurons. Additionally, the hidden and output neurons will include a bias. The input and target values for this network are  $i_1 = 0.05$ ,  $i_2 = 0.10$ ,  $t_1 = 0.01$  and  $t_2 = 0.99$  respectively:

### 3.3.1 Forward Pass

First Layer

$$\begin{aligned}
net_{h_1} &= \omega_1 \cdot i_1 + \omega_2 \cdot i_2 + b_1 \cdot 1 \\
net_{h_1} &= 0.15 \cdot 0.05 + 0.2 \cdot 0.1 + 0.35 \cdot 1 = 0. \\
h_1 &= \frac{1}{1 + e^{-net_{h_1}}} = \frac{1}{1 + e^{-0}} = 0.
\end{aligned}$$