# Bayesian Demographic Trajectory analysis tutorial: BaSTA and $$\operatorname{BaFTA}$$

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# Introduction

This is a general introduction to the R packages BaSTA and BAFTA. The aim is to provide a simple tutorial that allows users to start running survival and fertility analyses with both packages. For a more in depth description of the models and methods, please refer to the relevant papers (Colchero and Clark 2012, Colchero et al. 2012, Colchero et al. 2021, Colchero 2025), and the two vignettes, available under "01docs/Vignettes/".

Together with this tutorial, I provide R scripts with all the commands provided here. They also include additional analyses to give you a better idea of the kinds of analyses you can carry out with both packages. You can find both under "02code/BaSTAtutorialRcode.R" and "02code/BaFTAtutorialRcode.R".

In Fig. 1 I show the file structure for the workshop materials.

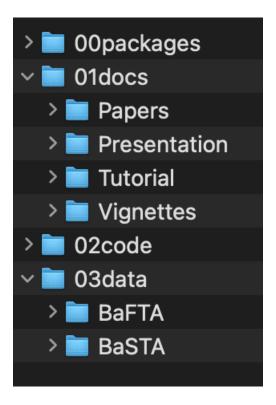


Figure 1: A caption

# Installing packages and loading additional code

First, make sure to point R to the workshop's working directory as:

```
# Set WD to workshop directory:
setwd("Path to Workshop directory/ColcheroWorkshopEvoDemoS2025/")
```

BaSTA version 2.02 is available in CRAN, although I recommend that you install the latest version from my GitHub repository. To install BaSTA and BaFTA from GitHub, use the following commands:

```
# Install and load 'devtools':
install.packages("devtools")
library(devtools)

# Install BaSTA:
install_git("https://github.com/fercol/basta2.0", subdir = "pkg/")

# Install BaFTA:
install_git("https://github.com/fercol/BaFTA", subdir = "pkg/")
```

In case installing from GitHub doesn't work, you can install them from the versions available in the workshop's directory as

```
repos = NULL)
```

For both packages, you will also need to install snowfall for parallel computing:

```
# Install snowfall:
install.packages("snowfall")
```

In addition to the libraries, I provide two R scripts with additional code to complement both packages. Load the additional functions as:

```
# Load extra functions for BaSTA:
source("02code/BaSTAextraFunctions.R")

# Load additional functions for BaFTA:
source("02code/BaFTAextraFunctions.R")
```

## BaSTA: Bayesian Survival Trajectory Analysis

Here I will briefly show how to run analyses on **capture-mark-recapture (CMR)** and on **census** data. CMR it the type of data that was traditionally used with BaSTA, while the package has been recently extended to allow the use of census data. These type of data are relevant for studies where individuals are followed constantly and for which constructing a recapture matrix is unnecessary.

You can find the R code file associated to this section at "02code/BaSTAtutorialRcode.R'.'

#### Capture-mark-recapture (CMR) data

#### Loading and checking data

To illustrate the use of BaSTA on CMR data, I provide the capture-mark-recapture data on Eurasian sparrowhawk (*Accipiter nisus*), compiled by the British ornithologist Ian Newton. Until recently, this dataset was hosted in the Long-term Individual-basedTime Series (LITS) database (Jones et al. 2008). Load the data as:

```
# Sparrowhawk:
sphDat <- read.csv(file = "03data/BaSTA/tables/SparrowhawkData.csv")</pre>
```

Any CMR dataset to be analyzed with BaSTA needs to be structured as: a) the first three columns are the individual ID, and the times of birth and death, commonly in years; b) these are followed by the capture-recapture-matrix; and c) any covariates to be included in the analysis. Here is the structure for the sparrowhawk data:

Table 1: Example of CMR table for BaSTA based on the sparrowhawk dataset.

ID	birth	death	X1971	CMR.cols.	X1999	sex	repr	wing	mass
DA53804	1986	NA	0	-	0	f	4	0.4677805	0.4689179
DA53824	NA	NA	0	-	0	$\mathbf{f}$	4	0.9210977	0.1701786
DA53825	1984	NA	0	-	0	$\mathbf{f}$	4	1.1477563	0.9917118
DS85729	1974	NA	0	-	0	$\mathbf{f}$	4	0.6944391	0.1390599
EB01503	1974	NA	0	-	0	f	0	0.1844573	0.4191280

Note that only the first and last columns of the capture matrix in Table 1 are visible here. To verify that

there are not issues with the data, use function **DataCheck** as:

```
sphCheck <- DataCheck(object = sphDat, studyStart = 1971, studyEnd = 1999)</pre>
```

You can use function **summary** to print the results to the console as:

```
summary(sphCheck)
```

```
> DATA CHECK: 2025-09-16 06:09:49.664401
 _____
> DATA SUMMARY:
> =========
> - Number of individuals:
                                572
> - Number with known birth year:
                               378
> - Number with known death year:
> - Number with known birth
   AND death years:
                                 0
> - Number of recaptures:
                                948
> - Earliest detection year:
                               1971
> - Latest detection year:
                               1999
> - Earliest birth year:
                               1969
> - Latest birth year:
                               1996
> - Earliest death year:
                                 NA
> - Latest death year:
                                 NA
> NUMBER OF PROBLEMATIC RECORDS:
> - Death < Entry: 0
> - No obs.:
> - Birth > Death: 0
> - Death < Depart: 0
> - Birth > Entry: 0
> - Birth = 1 in Y: 1
> Note: you can use function FixCMRdata() to fix issues.
```

#### Single runs

To run a single analysis you should use function **basta**. For instance, to run an analysis with a Weibull hazard rate or mortality function, you can use:

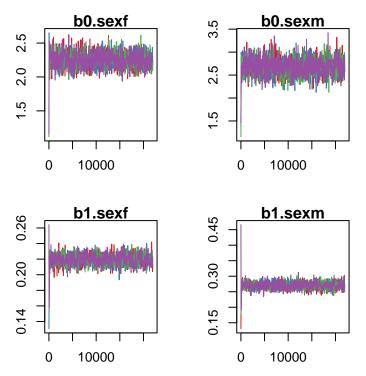
Here, arguments **model** and **shape** specify the main mortality function (here Weibull) and the general shape (options are *simple*, *Makeham*, and *bathtub*). The output can be visualized by printing it to the console or with function **summary** as:

```
summary(outSph1, digits = 3)
> Call:
> Model : WE
```

```
> Shape
                          : simple
> Minimum age
                          : 0
> Covars. structure
                          : fused
> Cat. covars.
                          : sexf, sexm
> Cont. covars.
> Model settings:
    niter burnin thinning
                                nsim
>
     22000
              2001
                         40
> Mean Kullback-Leibler
> discrepancy calibration (KLDC):
                b0 b1
> sexm - sexf 0.985 1
> Coefficients:
          Mean StdErr Lower95%CI Upper95%CI SerAutocorr UpdateRate
> b0.sexf 2.250 0.11027 2.042
                                      2.469
                                                 0.0715
                                                             0.253
> b0.sexm 2.672 0.18280
                            2.334
                                      3.039
                                                 0.0143
                                                             0.246
> b1.sexf 0.219 0.00694
                            0.206
                                      0.233
                                                             0.263
                                                 0.1581
                                  0.233
0.292
0.533
> b1.sexm 0.270 0.01133
                            0.249
                                                 0.0820
                                                             0.252
> pi 0.503 0.01547
                            0.474
                                                 0.1362
                                                             1.000
         PotScaleReduc
> b0.sexf
> b0.sexm
> b1.sexf
> b1.sexm
                     1
> pi
> Convergence:
> Appropriate convergence reached for all parameters.
> DIC:
> 2382.077
```

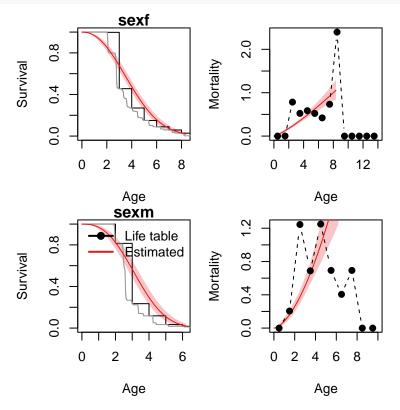
To plot the traces you can use the built-in function  ${f plot}$  as:

#### plot(outSph1)



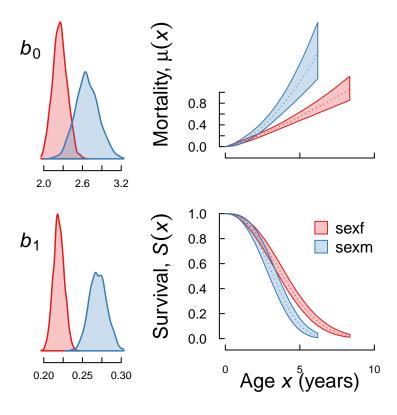
While you can visually inspect the goodness of fit as:

plot(outSph1, type = 'gof')



You can now also produce the "fancy" plots available in previous versions as:

plot(outSph1, type = 'fancy')



#### Multiple runs

# Summary of results:

You can use function **multibasta** to test multiple models and shapes. Here's an example comparing the Gompertz, Weibull and logistic models with all shapes:

To inspect the results, use function **summary**, which provides a table with the sorted DICs, as:

```
summary(multiout)
>
> Call:
                             : 0
> Covars. structure
> Minimum age
                             : fused
                             : sexf, sexm
 Cat. covars.
>
 Cont. covars.
>
> Model settings:
     niter
             burnin thinning
                                   nsim
>
     22000
                2001
                           40
                                      4
> DICs:
     model
             shape D.ave D.mode pD k DIC DICdiff Rank
```

```
> 3
        WE simple
                             1749 211
                                       4 2382
                                                  0.00
                     2171
                                                           1
> 9
        WE bathtub
                             1761 208 10 2385
                                                  2.81
                                                           2
                     2177
> 6
        WE Makeham
                     2176
                             1721 228
                                       6 2403
                                                 21.11
                                                           3
> 10
        LO bathtub
                     2057
                             1219 419 12 2476
                                                 93.74
                                                           4
 7
        LO Makeham
                     2050
                             1180 435
                                       8 2485
                                                103.38
                                                           5
> 4
        LO
            simple
                     2046
                             1163 442
                                       6 2488
                                                105.74
                                                           6
> 8
        GO bathtub
                     2359
                             2098 130 10 2489
                                                107.34
                                                           7
            simple
> 2
        GO
                     2352
                             2078 137
                                        4 2490
                                                107.52
                                                           8
> 5
        GO Makeham
                     2357
                             2059 149
                                       6 2506
                                                123.98
                                                           9
```

#### Census data

One of the lateset additions is to include what can be described as **census** data. This is typical of studies where individuals are followed constantly (e.g., lab studies, captive populations, primate field studies).

#### Loading and checking data

To illustrate the structure of the data, load the elephant data provided by Crawley et al. (2020):

```
# Elephant data (from Crawley et al (2020) Sci Reps):
eleDat <- read.csv(file = "03data/BaSTA/tables/elephantData.csv")</pre>
```

The structure of the data is as follows

Table 2: Example of census table for BaSTA based on the elephant dataset.

ID	Birth.Date	Min.Birth.Date	Max.Birth.Date	Entry.Date	Depart.Date	Depart.Type	Sex
1	1962-03-28	1962-03-28	1962-03-28	1962-03-28	2005-09-26	D	Male
2	1986 - 02 - 15	1986-02-15	1986-02-15	1986 - 02 - 15	2019-07-22	$^{\mathrm{C}}$	Female
3	1974 - 02 - 13	1974-02-13	1974-02-13	1974 - 02 - 13	2020-01-26	D	Female
4	1996 - 08 - 02	1996-08-02	1996-08-02	1996 - 08 - 02	2000-12-08	$^{\mathrm{C}}$	Female
5	1960 - 02 - 15	1960-02-15	1960-02-15	1960 - 02 - 15	2005 - 11 - 12	D	Female

As you can see in Table 2, the data uses several date columns in 'YYYY-mm-dd' format, three for the birth date, including a minimum and maximum birth date, and columns for the entry and departure dates. The minimum and maximum birth dates allow to account for ranges in the potential ages when the birth date is uncertain or unknown. The **Entry.Date** and **Depart.Date** columns, as their names suggest, show the first and last time the individual was recorded. When the entry date is later than the birth date, then the individual is treated as truncated. The column **Depart.Type** uses two categories: **C** for censored (i.e., still alive by the departure date), and **D** for death at the departure date.

To detect whether there are issues with the data, use function **DataCheck** as:

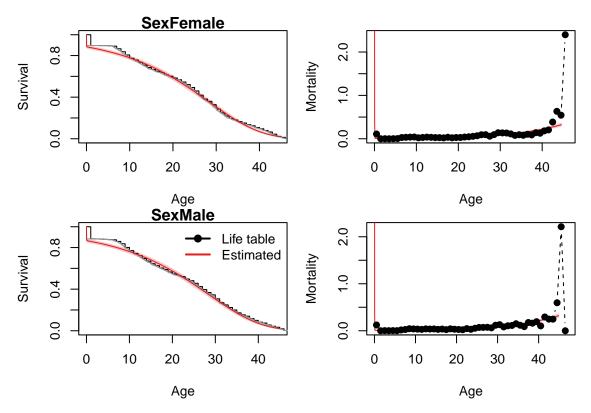
```
> Total number of records : 2962
> Number censored (C) : 1031
> Number uncensored (D)
                     : 1931
> Number with unknown birth: 0
> NAs IN DATES COLUMNS:
> -----
> No NAs found in dates columns.
> DATES RANGES:
> Birth.Date
           Min.Birth.Date Max.Birth.Date Entry.Date Depart.Date
> 1950-01-01 1950-01-01 1950-01-01 1950-01-01 1950-05-06
> INCONSISTENCIES BETWEEN DATES COLUMNS:
> None.
> INCONSISTENCIES IN DEPARTURE TYPES:
```

#### Analysis from birth and older ages

To run a basic analysis using a Siler (1979) model (i.e., **model = "GO"** and **shape = "bathtub"**) with sex as a covariate, run function basta as:

While inspecting the goodness of fit graphically, you can see that the fit is poor for the first 10 years:

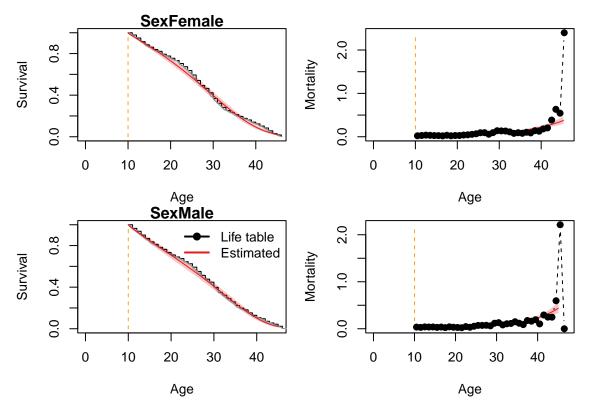
```
plot(outEle1, type = 'gof')
```



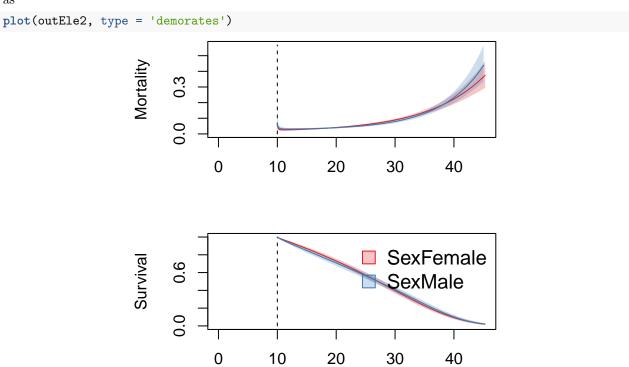
This is a common issue with many datasets for which infant and early mortality records may be unreliable. A way to improve the fit, particularly when interested on senescence, is to fit the mortality model to data at older ages using argument **minAge** as:

Which produces a considerably better goodness of fit plot:

```
plot(outEle2, type = 'gof')
```



To visualize the survival and mortality curves by categorical covariates use argument  $\mathbf{type} = \mathbf{``demorates''}$  as



### BaFTA: Bayesian Fertility Trajectory Analysis

#### Aggregated data

Here I provide data from 12 studies on the same number of mammalian species. You can find the metadata at "03data/BaFTA/tables/speciesFertMeta.csv'. Load the data and extract the list of species as

```
# Load aggregated data:
datAggr <- read.csv(file = "03data/BaFTA/tables/speciesFert.csv")
# Extract species:
species <- unique(datAggr$species)</pre>
```

As an example, here is the data for northern fur seals (Callorhinus ursinus) from Lander (1998):

```
# Select one of the species:
isp <- 1

# Subset data:
spDat <- datAggr[which(datAggr$species == species[isp]), ]</pre>
```

The aggregated data needed to run BaFTA are:

Table 3: Example of aggregated data table for BaFTA based on the northern fur seal data. Only the first five rows are shown.

Age	Fertility	nParents	nOffspring
4	0.04	1450	58
5	0.37	1303	483
6	0.70	1217	852
7	0.80	1235	988
8	0.85	1270	1080

As shown in Table 3, the columns required are the **Age**, commonly in years, **nParents** for the number of adult individuals available at the corresponding age, **nOffspring** for the number of offspring produced by parents of that age, and **Fertility** commonly calculated as the ratio between the offspring and parents. Note that inference is carried out on the **nParents** and **nOffspring** columns; the **Fertility** column is only use as references.

#### Single run

To run an analysis using the gamma function, simply use function **bafta** as:

```
# Quadratic:
outAggr1 <- bafta(object = spDat, model = "gamma", nsim = 6, ncpus = 6)</pre>
```

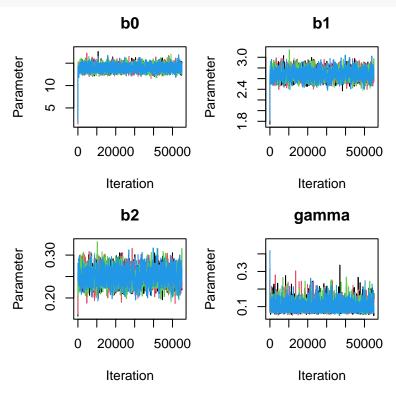
Note that it is not necessary to specify \*\*dataType = "aggregated" since it is the default. You can print the output to the screen:

```
outAggr1
> Call:
> Model : gamma
> Data type : aggregated
```

```
: 55000
> Num. iterations
                     : 5001
> Burnin
> Thinning
                     : 20
> Number of sims.
                     : 4
>
  Computing time
                     : 11.45 secs
  Coefficients:
>
                       SD
                             Lower
                                     Upper Neff Rhat
> b0
        13.92966 0.67957 12.68534 15.3622 4443 1.000
         2.68495 0.09275
                           2.50902
                                    2.8741 2759 1.001
>
 b1
> b2
         0.25034 0.01853
                           0.21504
                                    0.2883 2632 1.001
         0.09386 0.02657
                           0.06397
                                    0.1634 7981 1.000
>
 Convergence:
 All parameter chains converged.
> Model fit:
> DIC = 218.31
> Predictive loss:
   Good. Fit Penalty Deviance
>
      122922 117549
                        240471
```

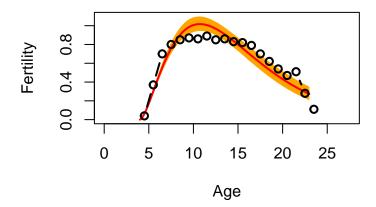
To inspect the traces, use the built-in function  ${f plot}$  as:

#### plot(outAggr1)



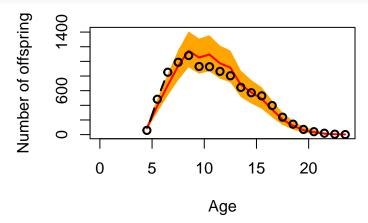
To inspect the fit to the Fertility data, modify the function with argument type as:

```
plot(outAggr1, type = "fertility")
```



while you can check the fit on the number of offspring as:





#### Multiple runs

As with BaSTA, in the extra code I provide a **multibafta** function. For illustration, let's select the models we wish to run on the aggregated data:

We can then run the function as:

```
# Run multi-BaFTA:
multiout <- multibafta(object = spDat, models = models)</pre>
```

To visualize the output, simply print it to the console as:

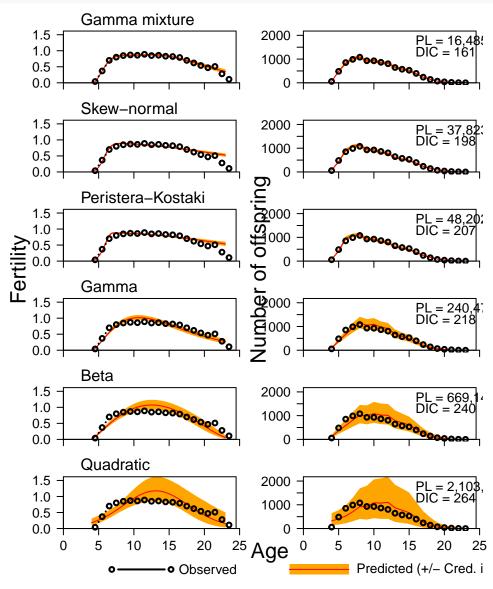
```
# Print output:
multiout
```

```
> Sorted by DIC:
>
               model DIC PredLoss
> 5
        gammaMixture 161
                             16485
> 6
          skewNormal 198
                             37823
> 2 PeristeraKostaki 207
                             48202
> 3
               gamma 218
                            240471
> 4
                 beta 240
                            669149
```

```
quadratic 264 2103748
> 1
  Sorted by PredLoss:
>
               model DIC PredLoss
>
 5
        gammaMixture 161
                             16485
>
 6
          skewNormal 198
                             37823
 2 PeristeraKostaki 207
                             48202
                            240471
> 3
               gamma 218
> 4
                beta 240
                            669149
           quadratic 264
                          2103748
```

You can also use the built-in plot function to compare the fits of each model:

```
# Plot output:
plot(multiout, sortBy = "PredLoss")
```



#### Individual level data with seasonal reproduction

Here I provide simulated data to illustrate how to prepare the data and run BaFTA on individual level data where reproduction is seasonal, and thus records are organized by age as integers. First load the data as:

```
# Load individual data:
datIndivSimp <- read.csv(file = "03data/BaFTA/tables/indivSimpFert.csv")</pre>
```

The data should include the following columns:

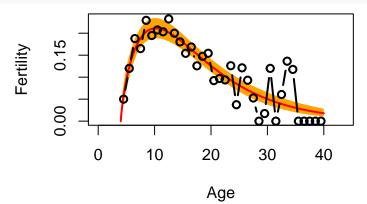
Table 4: Example of individual data with seasonal reproduction ('indivSimp') for BaFTA. Only the first five rows are shown.

indID	Age	nOffspring
I0002	4	0
10002	5	0
10002	6	0
10002	7	0
10002	8	0

As with the aggretated data, use function **bafta** to test for instance the gamma model as shown here:

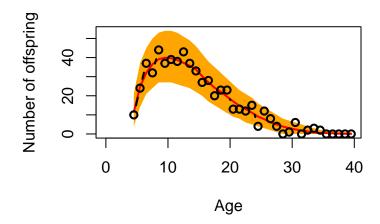
Note that we had to specify **dataType = 'indivSimple'**. To visually inspect the fit to the fertility data, use **plot** as:

```
plot(outIndSimp1, type = "fertility")
```



To check the goodness of fit, modify the plot as:

```
plot(outIndSimp1, type = "predictive")
```



#### Individual level data with variable IBI

In many species, particularly mammals, reproduction is not seasonal, while inter-birth intervals (IBIs) can be variable. Here I provide an example on simulated data. Load the data as:

```
# Load individual data:
datIndivExt <- read.csv(file = "03data/BaFTA/tables/indivExtFert.csv")</pre>
```

The data includes the following columns:

Table 5: Example of individual data with continuous reproduction ('indivExt') and variable IBIs for BaFTA. Only the first five rows are shown.

indID	Age	nOffspring	IBI	Time	First
I0020	6.251	0	1.251	1.251	0
10020	8.232	0	1.982	3.232	0
I0020	9.530	0	1.298	4.530	0
I0020	10.571	1	1.041	5.571	0
10020	11.863	0	1.292	6.863	0

As you can see from Table 5, there are three additional columns to those in Table 4. These are the time between reproductive events (**IBI**), the time since the minimum age at birth in the population (**Time**), and whether this was the first reproductive event (**First**). These additional columns are needed, since the model not only makes inferences on age-specific fertility, but also on the times to first offspring from the age at minimum birth, and on IBIs. To run, for example the Peristera-Kostaki (2007) model, modify the **dataType** and **model** arguments as:

As with the other types of data, check the output with functions **print** or **summary** as:

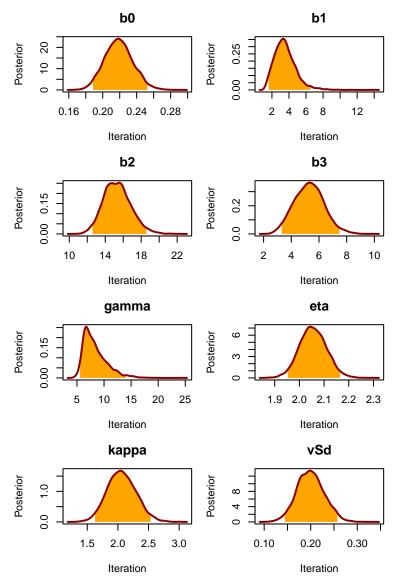
```
summary(outIndExt2, digist = 3)
```

> Call:

```
> Num. iterations : 20000
         : 1001
> Burnin
> Thinning
                 : 20
> Number of sims. : 4
> Computing time
                : 3.36 mins
> Coefficients:
                                Upper Neff Rhat
          Mean
                    SD
                       Lower
> b0
        0.2190 0.01663 0.1885 0.2530 171 1.000
> b1
       3.5508 1.25793 1.5976 6.5438 1178 1.002
> b2
       15.3379 1.51734 12.5797 18.5858 1729 1.000
       5.2924 1.06398 3.3050 7.4975 1125 1.001
> b3
> gamma 8.3451 2.19242 5.5639 14.0497 3436 1.000
        2.0556 0.05461 1.9525 2.1647 2743 1.001
> kappa 2.0634 0.23336 1.6253 2.5361 1266 1.000
> vSd
        0.1998 0.02920 0.1441 0.2577 1026 1.001
> Convergence:
> All parameter chains converged.
> Model fit:
> DIC = 3169.02
> Predictive loss:
  Good. Fit Penalty Deviance
        316
                314
                        630
```

You can check the posterior density plots for the parameters as:

```
# Plot parameter posterior densities:
plot(outIndExt2, type = "density")
```



In the additional code, I provide a function that shows both the posterior densities and traces:

# Combined plot of posterior densities and traces:
PlotDensTrace(out = outIndExt2)

