

## APPLICATION

# BaSTA: an R package for Bayesian estimation of age-specific survival from incomplete mark–recapture/recovery data with covariates

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## Summary

1. Understanding age-specific survival in wild animal populations is crucial to the study of population dynamics and is therefore an essential component of several fields including evolution, management and conservation.
2. We present Bayesian survival trajectory analysis (BaSTA), a free open-source software package for estimating age-specific survival from capture–recapture/recovery data under a Bayesian framework.
3. The method copes with low recapture probabilities, unknown ages (e.g. because of left-truncation) and unknown ages at death (e.g. because of right-censoring). It estimates survival and detection parameters as well as the unknown birth and death times (i.e. latent states) while allowing users to test a range of survival models. In addition, the effect of continuous or categorical covariates can be evaluated.
4. This tool facilitates the analysis of age patterns of survival in long-term animal studies and will enable researchers to robustly infer the effect of covariates, even with large amounts of missing data.

**Key-words:** Bayesian inference, capture–recapture, capture–recovery, free software, long-term individual-based data sets, R project, survival analysis

## Introduction

Understanding how survival trajectories change with age is crucial to population dynamics and is therefore an essential component of ecology, evolutionary biology and conservation science (Martin 1995; Clutton-Brock & Sheldon 2010). Commonly, survival in wild animal populations is inferred from capture–recapture and capture–recovery data (Catchpole *et al.* 1998). However, these data often include numerous records with missing birth and death times, which makes inference on age patterns of survival challenging (Ricklefs & Scheuerlein 2001; Metcalf *et al.* 2009). Recently, ecologists and evolutionary biologists have acknowledged the importance of developing analytical methods that account for these limitations. As a consequence, several alternative models have been developed (Schofield & Barker 2008; Pledger *et al.* 2009; Zajitschek *et al.* 2009; Colchero & Clark 2012). Unfortunately, these methods are not easily implemented and require considerable conceptual and computational investments. This highlights the need to provide user-friendly software.

Here we present Bayesian Survival Trajectory Analysis (BaSTA), a free open-source package that runs on the R platform (R Development Core Team 2011) and implements the hierarchical Bayesian model described by Colchero & Clark (2012). This package facilitates drawing inference on age-specific survival from capture–recapture/recovery (CRR) data when large proportions (or even all) of the records have missing information about times of birth and death. In addition, BaSTA allows users to evaluate the effect of both continuous and categorical covariates on survival as well as time differences in recapture probabilities.

## Missing data in CRR data sets

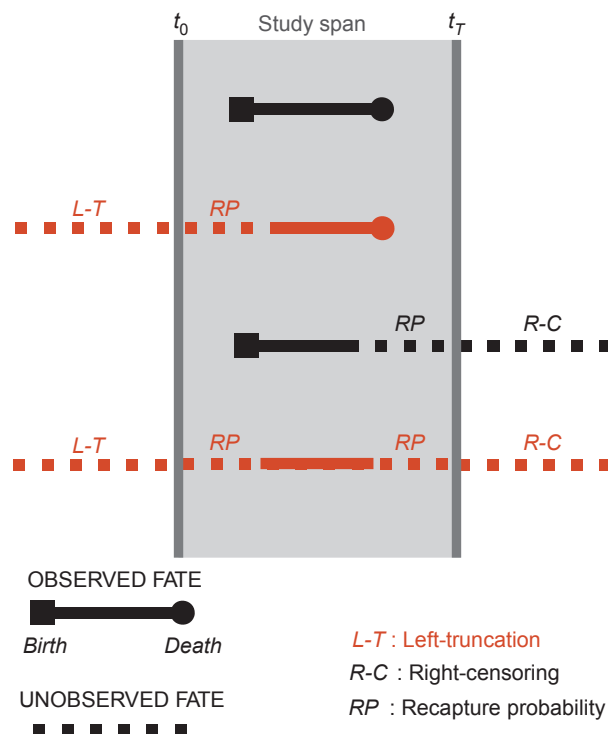
In CRR studies, a population is sampled repeatedly for a number of periods (e.g. years), where each sampling occasion is regarded as a discrete snapshot in time of the state of the population. Typically at each sampling occasion, the sampling scheme consists of marking newborns and individuals that have not previously been tagged and then, in the following occasions, these individuals are either recaptured, not detected, or recovered if found dead (Catchpole *et al.* 1998). As a

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result, CRR data sets commonly include not only records of individuals with known birth and death times (i.e. uncensored), but also numerous records from individuals for which times of birth are unknown, for example because they were born before the study (i.e. left-truncated), and individuals for which times of death are unknown, for instance those dying after the study has ended (i.e. right-censored; Fig. 1). In addition, low recapture probabilities can reduce the number of years an individual is observed, while the probability of finding dead individuals is commonly low, extending censoring within the study. For some very long-term studies (e.g. Jones *et al.* 2008) these issues are alleviated somewhat, but generally, such problems are commonplace and are particularly troublesome to shorter studies (Nisbet 2001; Colchero & Clark 2012). Our package, BaSTA, has been designed to address these unavoidable problems, allowing users to retain the entire data set without needing to discard records from individuals with unknown age.

### Components of BaSTA

BaSTA consists of routines initialized by the user through data input and the definition of basic model settings (Fig. 2). Although BaSTA provides default values, users can define additional variables such as initial parameters, jump standard errors, priors and general setup variables for the main algorithm. The package then performs a range of error checks on the input data and the user-defined settings. If no errors are found, the model runs one or multiple Markov chain Monte

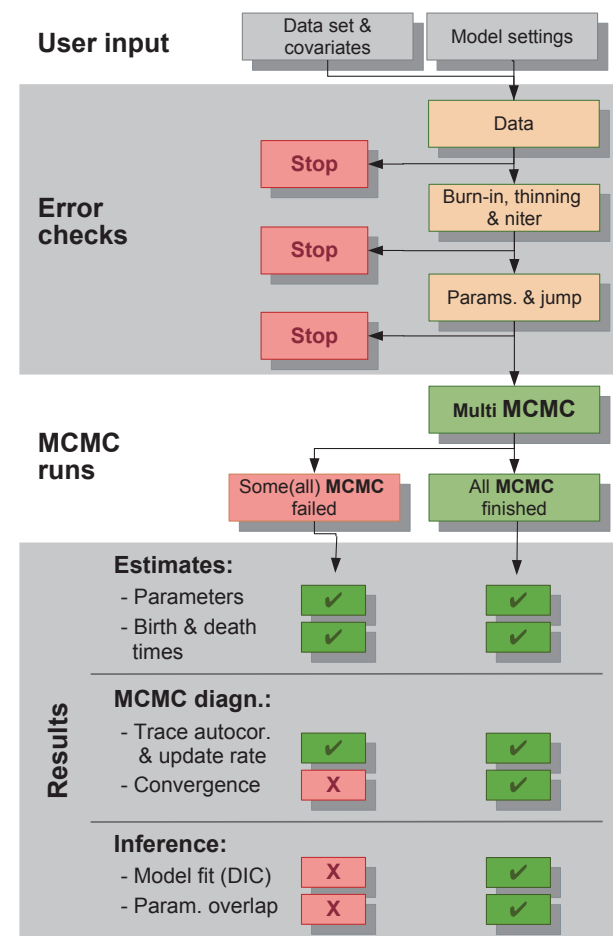


**Fig. 1.** Types of capture histories commonly found in ecological studies. Histories outlined in red are usually discarded from studies of age-specific survival. Bayesian Survival Trajectory Analysis includes these records into the inference process.

Carlo (MCMC) algorithms (see Colchero & Clark 2012). When the MCMC runs finish, BaSTA calculates diagnostics that include measures of serial autocorrelation on parameter traces, parameter update rates, convergence, parameter overlap and preliminary model selection. See the Supporting Information for an extended description of the models and a step-by-step tutorial where every section below is described in detail.

### DATA FORMAT

BaSTA's input data format is compatible with other CRR programs such as MARK (White & Burnham 1999). The data takes the form of a table (i.e. an R data frame) where each row represents one individual. This table includes individual times of birth and death (if known) and the recapture history matrix that assigns 1 for every year an individual is detected and 0 otherwise (Table 1). If users wish to evaluate covariates, an optional covariate matrix can be included (see pages 3–4 in Supporting Information). BaSTA provides functions to coerce conventional individual survey tables and covariate matrices into the proper format.



**Fig. 2.** Work flow of Bayesian Survival Trajectory Analysis main function after data input and argument definition from the user. During the initial 'error check' sequence, if an error is found, the function is stopped and an error message is printed.

**Table 1.** Data format required by Bayesian Survival Trajectory Analysis. Column 1 refers to each individual's ID, columns 2 and 3 are the times of birth and death, columns 4–7 are the capture-history matrix and the last two columns correspond to covariates for location

ID	Birth	Death	Year 1	Year 2	Year 3	Year 4	Location 1	Location 2
1	$b_1$	$d_1$	1	0	1	1	1	0
2	$b_2$	0	0	1	1	1	1	0
3	0	$d_3$	1	1	1	1	0	1
4	0	0	0	1	1	0	0	1

#### MORTALITY MODELS AND RECAPTURE PROBABILITIES

BaSTA includes four basic mortality functions: (i) exponential (Cox & Oakes 1984); (ii) Gompertz (Gompertz 1825; Pletcher 1999); (iii) Weibull (Pinder *et al.* 1978); and (iv) logistic (Vaupel *et al.* 1979; Pletcher 1999) (see Table S3 in Supporting Information). Each function can describe different trends in age-specific mortality, giving BaSTA considerable flexibility when estimating these vital rates (Fig. 3).

In addition, BaSTA allows users to extend these basic functions to include more complex shapes (Fig. 3). Specifically, three general forms can be defined: (i) *simple*, which uses only the basic functions described above; (ii) *Makeham* (Pletcher 1999); and (iii) *bathtub* (e.g. Siler 1979).

Also, BaSTA allows the user to test whether recapture probabilities should be constant or whether they should change as a function of time. This could be useful when the recapture effort is not equal every year.

#### CONDITIONING ON A MINIMUM AGE

In some species, fates of individuals younger than a certain age are typically unknown. For example, after fledging, juvenile seabirds disperse for several years, during which they can experience high mortality. After this time, they may settle in a different colony from the colony where they were born and are thus never detected again. Consequently, uncertainty in the fate of juveniles can inflate early mortality estimates. Accordingly, BaSTA allows users to condition survival estimation on having reached a minimum age while keeping the integrity of the data set (i.e. no records need to be discarded).

#### COVARIATES

BaSTA also allows users to define three optional structures to evaluate the effect of covariates on age patterns of survival: (i)

*fused*, where categorical covariates are included as linear functions of the survival parameters (analogous to generalized linear models) and continuous covariates are evaluated under a proportional hazards framework (Klein & Moeschberger 2003); (ii) all covariates as *proportional hazards*; and (iii) *all-in-mortality*, where all covariates are evaluated as linear functions of the survival parameters (see Fig. S1 in Supporting Information).

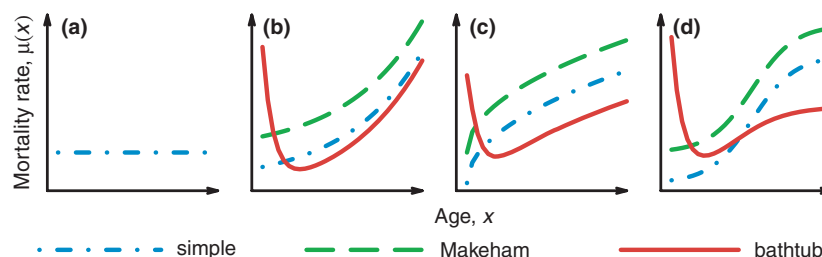
#### MULTIPLE RUNS AND DIAGNOSTICS

##### Multiple runs

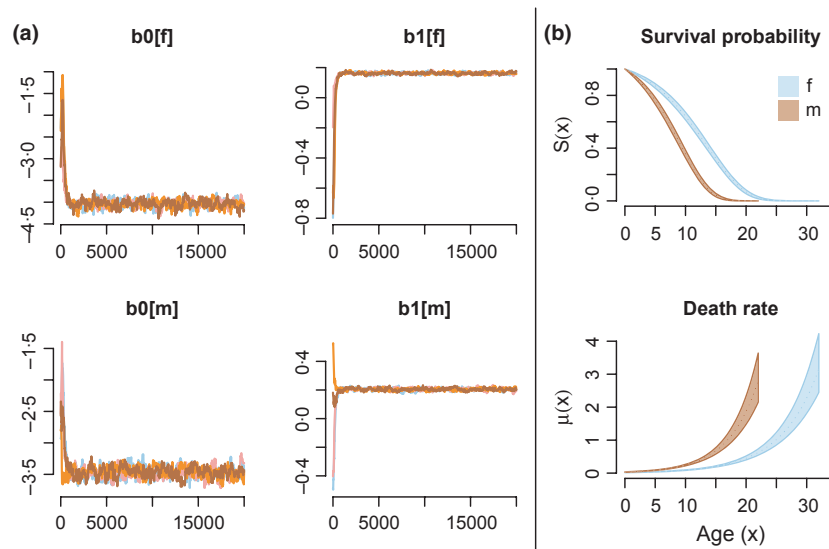
An important feature of BaSTA is the ability to run multiple simulations, in parallel or in series. Running multiple simulations allows users to test whether the final MCMC parameter chains (i.e. traces) all converged to the same final values, irrespective of initial parameters (Gelman *et al.* 2004). BaSTA performs these multiple runs in parallel with the SNOWFALL package (Knaus 2010), which reduces computing time proportionally to the number of processors or cores used.

##### Diagnostics

If multiple simulations are implemented and they all run to completion, BaSTA calculates potential scale reduction for each parameter to estimate convergence (Gelman *et al.* 2004). If all parameters have converged, BaSTA calculates the deviance information criterion (DIC; Spiegelhalter *et al.* 2002), which has been described as a measure of predictive power and criterion for model fit. However, we emphasize that the use of DICs is still controversial and the results should be taken with caution (see responses in Spiegelhalter *et al.* 2002). BaSTA's DIC is calculated as an approximation to the group-marginalized DIC presented by Millar (2009). Additionally, BaSTA includes a diagnostic based on Kullback–Leibler discrepancies



**Fig. 3.** Mortality rates,  $\mu(x|\theta)$ , resulting from the four basic models included in Bayesian Survival Trajectory Analysis (BaSTA): (a) exponential; (b) Gompertz; (c) Weibull; and (d) logistic. The three different lines in each plot (except in a) show examples of the shapes that can be tested with BaSTA, namely: 'simple'; 'Makeham'; and 'bathtub'.



**Fig. 4.** Plots produced from a Bayesian Survival Trajectory Analysis output with the generic R function `plot()`: (a) trace plots for mortality parameters; and (b) predicted mortality (death rates) and survival probabilities. The model ran for 20 000 iterations and four parallel simulations. Each colour in (a) corresponds to a parallel run.

(KLD; Kullback & Leibler 1951; McCulloch 1989), which provides users with a measure of how differently (or similarly) each categorical covariate affects survival (e.g. effects of males and females on mortality parameters). This measure is based on a calibration proposed by McCulloch (1989), which simplifies the interpretation of KLD values.

### Retrieving and visualizing results

The outputs of BaSTA can be explored using R's generic functions (`print()`, `summary()` and `plot()`) to obtain summary statistics, parameter trace plots and figures of the predicted mortality and survival probabilities (Fig. 4). Furthermore, BaSTA can optionally produce life tables from the predicted ages at death for each of the categorical covariates.

### Conclusions

Data from wild populations are often characteristically 'messy'. For numerous records, the variables of interest are either masked (e.g. measurement error) or hidden (e.g. non-detection vs. death). Consequently, researchers are forced to choose between reducing the data set to complete records, or using analytical methods that, although powerful, require a great deal of investment and can be challenging to implement. To bridge the gap between developers and potential users, we have produced BaSTA as a 'user-friendly' option for the analysis of CRR data when the aim is to understand age patterns of survival in wild populations.

BaSTA is available at CRAN ([cran.r-project.org/](http://cran.r-project.org/)) and can be installed in R with the following command: `install.packages('BaSTA')`.

Users are encouraged to join and submit enquiries or comments to the BaSTA users mailing list at: <http://lists.r-forge.r-project.org/mailman/listinfo/basta-users>.

[r-forge.r-project.org/mailman/listinfo/basta-users](http://lists.r-forge.r-project.org/mailman/listinfo/basta-users).

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## Supporting Information

Additional Supporting Information may be found in the online version of this article.

**Data S1.** Tutorial and technical details of the models used in BaSTA.

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