

Mata Kuliah	: Matematika Diskrit 1 (Teori)
Kode Mata Kuliah	: KKT14143
Waktu	: Selasa (07.00 – 08.40)
Jumlah SKS	: 3 SKS
Nama Dosen	: Suprihanto
Minggu ke	: 12 (Dua Belas)
Tanggal	: 01-12-2015
Judul Materi	: Latihan Soal 2

Lanjutan latihan soal dari minggu ke 11

30. Can you conclude that $A = B$ if A, B , and C are sets such that
- $A \cup C = B \cup C$
 - $A \cap C = B \cap C$
 - $A \cup C = B \cup C$ and $A \cap C = B \cap C$
31. Let A and B be subsets of a universal set U . Show that $A \subseteq B$ if and only if $\overline{B} \subseteq \overline{A}$.
- The **symmetric difference** of A and B , denoted by $A \oplus B$, is the set containing those elements in either A or B , but not in both A and B .
32. Find the symmetric difference of $\{1, 3, 5\}$ and $\{1, 2, 3\}$.
33. Find the symmetric difference of the set of computer science majors at a school and the set of mathematics majors at this school.
34. Draw a Venn diagram for the symmetric difference of the sets A and B .
35. Show that $A \oplus B = (A \cup B) - (A \cap B)$.
36. Show that $A \oplus B = (A - B) \cup (B - A)$.
37. Show that if A is a subset of a universal set U , then
- $A \oplus A = \emptyset$
 - $A \oplus \emptyset = A$
 - $A \oplus U = \overline{A}$
 - $A \oplus \overline{A} = U$
38. Show that if A and B are sets, then
- $A \oplus B = B \oplus A$
 - $(A \oplus B) \oplus B = A$
39. What can you say about the sets A and B if $A \oplus B = A$?
- *40. Determine whether the symmetric difference is associative; that is, if A, B , and C are sets, does it follow that $A \oplus (B \oplus C) = (A \oplus B) \oplus C$?
- *41. Suppose that A, B , and C are sets such that $A \oplus C = B \oplus C$. Must it be the case that $A = B$?
42. If A, B, C , and D are sets, does it follow that $(A \oplus B) \oplus (C \oplus D) = (A \oplus C) \oplus (B \oplus D)$?
43. If A, B, C , and D are sets, does it follow that $(A \oplus B) \oplus (C \oplus D) = (A \oplus D) \oplus (B \oplus C)$?
44. Show that if A and B are finite sets, then $A \cup B$ is a finite set.
45. Show that if A is an infinite set, then whenever B is a set, $A \cup B$ is also an infinite set.
- *46. Show that if A, B , and C are sets, then
- $$|A \cup B \cup C| = |A| + |B| + |C| - |A \cap B| - |A \cap C| - |B \cap C| + |A \cap B \cap C|.$$
- (This is a special case of the inclusion-exclusion principle, which will be studied in Chapter 8.)
47. Let $A_i = \{1, 2, 3, \dots, i\}$ for $i = 1, 2, 3, \dots$. Find
- $\bigcup_{i=1}^n A_i$
 - $\bigcap_{i=1}^n A_i$
48. Let $A_i = \{\dots, -2, -1, 0, 1, \dots, i\}$. Find
- $\bigcup_{i=1}^n A_i$
 - $\bigcap_{i=1}^n A_i$
49. Let A_i be the set of all nonempty bit strings (that is, bit strings of length at least one) of length not exceeding i . Find
- $\bigcup_{i=1}^n A_i$
 - $\bigcap_{i=1}^n A_i$
50. Find $\bigcup_{i=1}^{\infty} A_i$ and $\bigcap_{i=1}^{\infty} A_i$ if for every positive integer i ,
- $A_i = \{i, i+1, i+2, \dots\}$
 - $A_i = \{0, i\}$
 - $A_i = (0, i)$, that is, the set of real numbers x with $0 < x < i$
 - $A_i = (i, \infty)$, that is, the set of real numbers x with $x > i$
51. Find $\bigcup_{i=1}^{\infty} A_i$ and $\bigcap_{i=1}^{\infty} A_i$ if for every positive integer i ,
- $A_i = \{-i, -i+1, \dots, -1, 0, 1, \dots, i-1, i\}$
 - $A_i = \{-i, i\}$
 - $A_i = [-i, i]$, that is, the set of real numbers x with $-i \leq x \leq i$
 - $A_i = [i, \infty)$, that is, the set of real numbers x with $x \geq i$
52. Suppose that the universal set is $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$. Express each of these sets with bit strings where the i th bit in the string is 1 if i is in the set and 0 otherwise.
- $\{3, 4, 5\}$
 - $\{1, 3, 6, 10\}$
 - $\{2, 3, 4, 7, 8, 9\}$
53. Using the same universal set as in the last problem, find the set specified by each of these bit strings.
- 11 1100 1111
 - 01 0111 1000
 - 10 0000 0001
54. What subsets of a finite universal set do these bit strings represent?
- the string with all zeros
 - the string with all ones
55. What is the bit string corresponding to the difference of two sets?
56. What is the bit string corresponding to the symmetric difference of two sets?
57. Show how bitwise operations on bit strings can be used to find these combinations of $A = \{a, b, c, d, e\}$, $B = \{b, c, d, g, p, t, v\}$, $C = \{c, e, i, o, u, x, y, z\}$, and $D = \{d, e, h, i, n, o, t, u, x, y\}$.
- $A \cup B$
 - $A \cap B$
 - $(A \cup D) \cap (B \cup C)$
 - $A \cup B \cup C \cup D$
58. How can the union and intersection of n sets that all are subsets of the universal set U be found using bit strings?
- The **successor** of the set A is the set $A \cup \{A\}$.
59. Find the successors of the following sets.
- $\{1, 2, 3\}$
 - \emptyset
 - $\{\emptyset\}$
 - $\{\emptyset, \{\emptyset\}\}$

Melanjutkan latihan dengan pembahasan tentang symmetric difference yaitu jika ada himpunan A dan B maka symmetric differencenya adalah anggota yang ada di A atau B namun tidak ada di keduanya (hanya salah satu). Contohnya mulai dari soal nomor 32.