

# CSE 222 - SPRING 2020 - HW 7

Ferd! SONMER

16104406

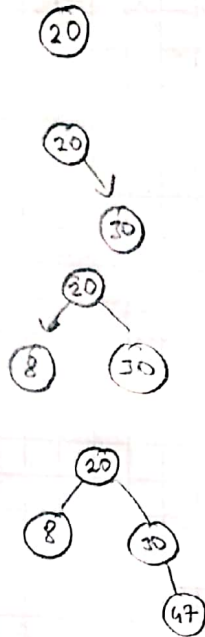
1 AVL TREE =

insert → 20

insert → 30

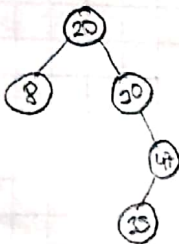
insert → 8

insert → 47

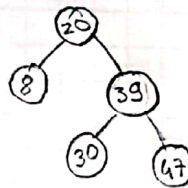


AVL Tree  
insert

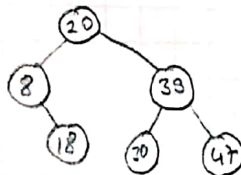
insert → 33



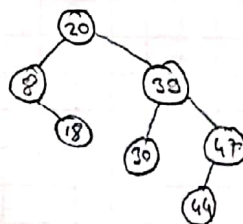
Left  
Rotate  
⇒



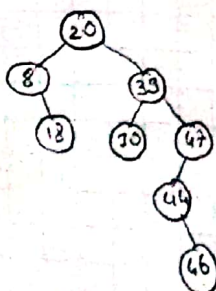
insert → 18



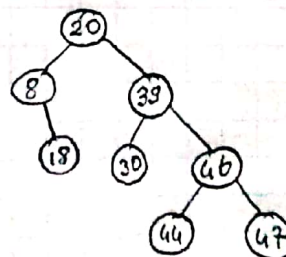
insert → 44



insert → 46

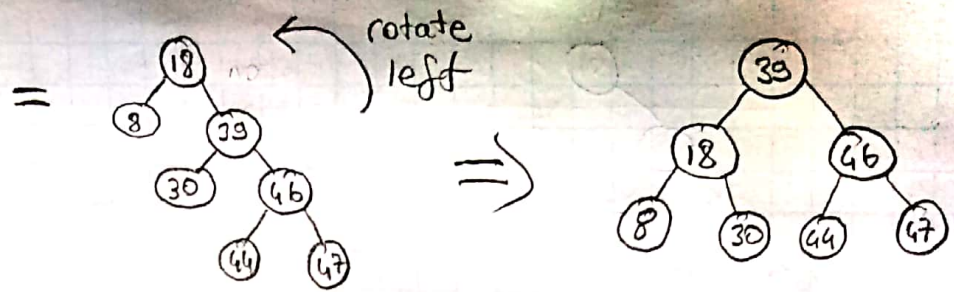


Right  
Rotate  
⇒



Delete = 20

(Find largest node in left subtree)



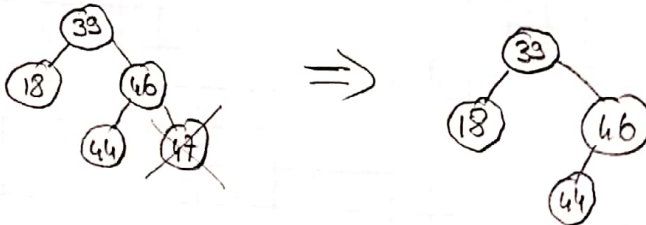
Delete = 30



Delete = 8

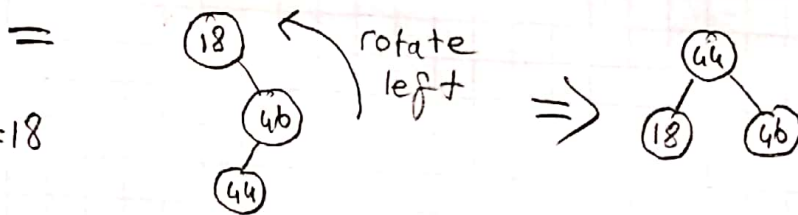


Delete = 47

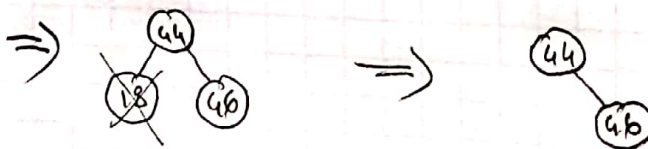


Delete = 39

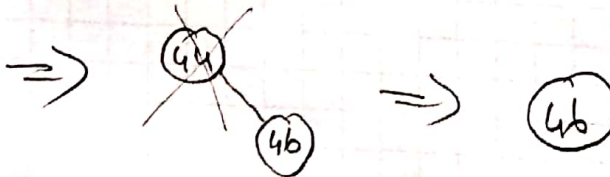
(Find largest node in left subtree) = 18



Delete = 18



Delete = 44



Delete = 46 =>

AVL Tree Delete



# Red/Black Tree =>

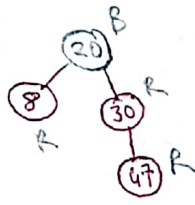
insert = 20

insert = 30

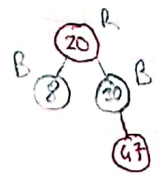
insert = 8

insert = 47 =>

(Node and parent are both red)



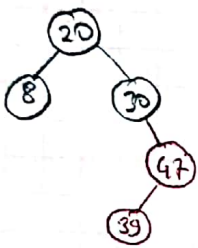
Recoloring



Root is red recoloring

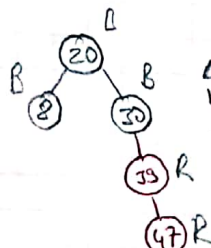


insert = 39 =>

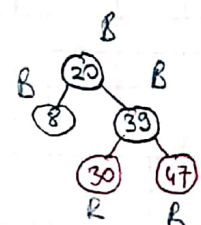
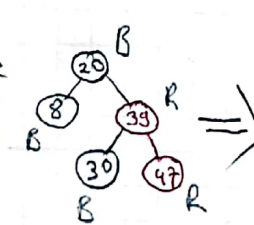


(Node and parent are both red)

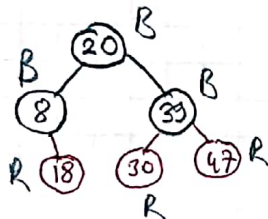
(rotate right)



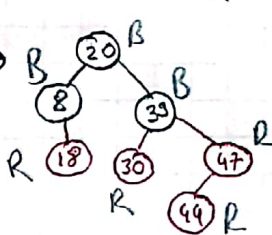
rotate left



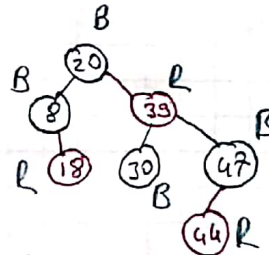
insert = 18



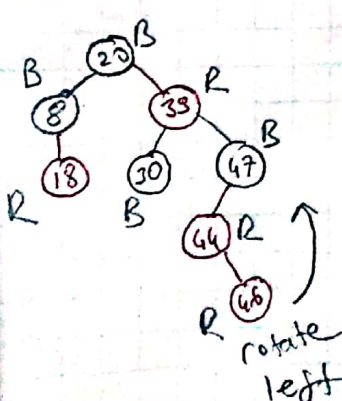
insert = 44



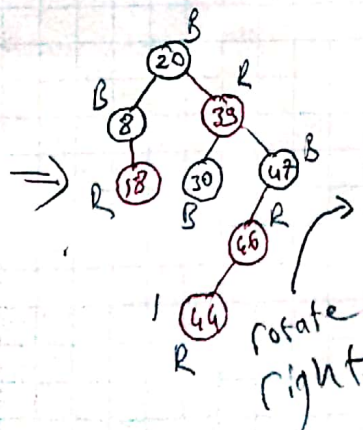
Recoloring



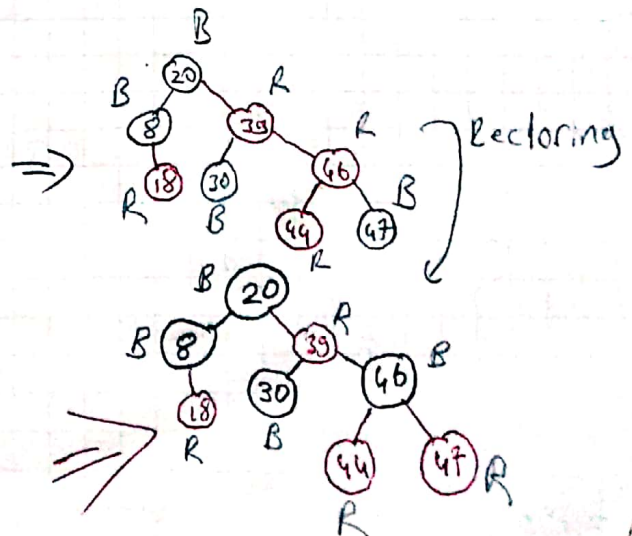
insert = 46



rotate left



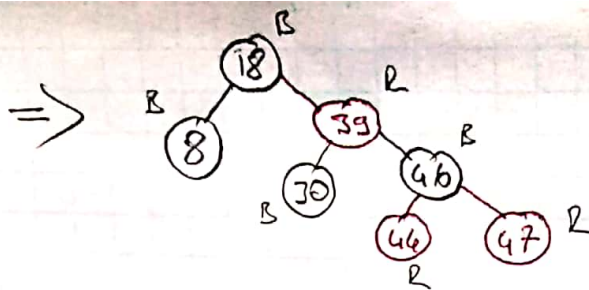
rotate right



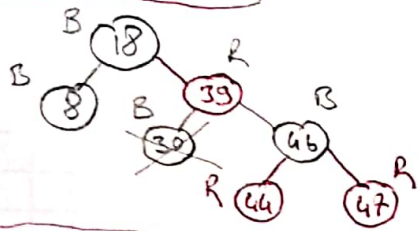
Recoloring

Delete = 20

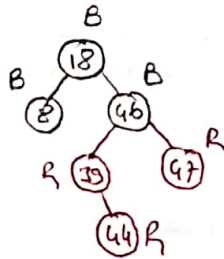
(Find largest node in left subtree) = 18



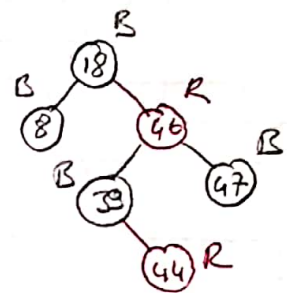
Delete = 30



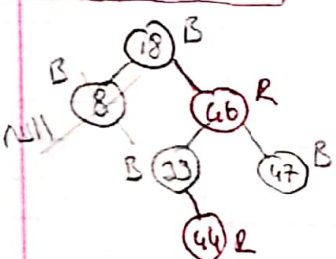
Rotate left



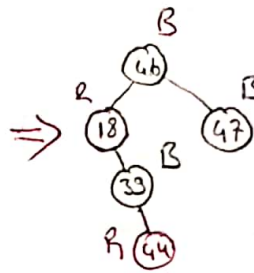
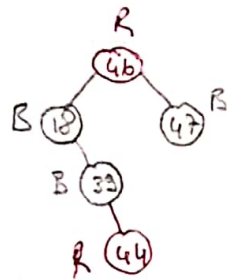
Recoloring



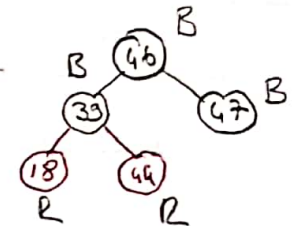
Delete = 8



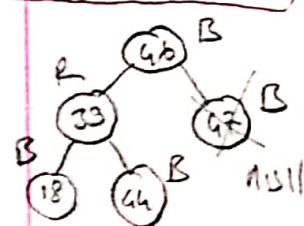
Rotate left



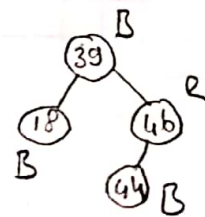
Rotate left



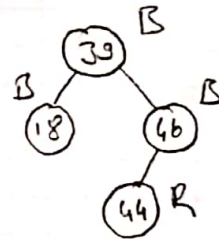
Delete = 47



Rotate Right

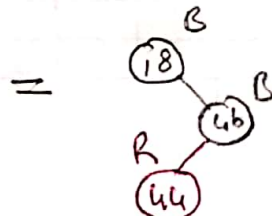


Recoloring

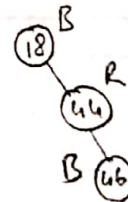


Delete = 39

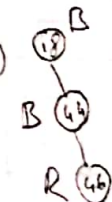
(Find largest node in left subtree)



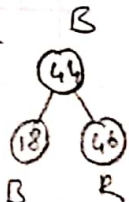
Rotate Right



Recoloring



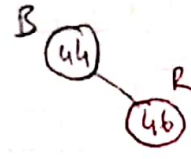
Rotate left



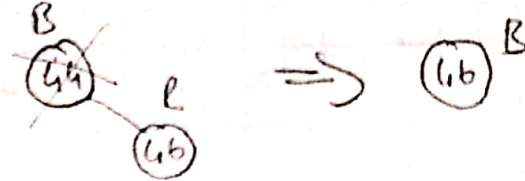
Delete = 18



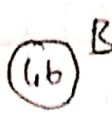
Recoloring



Delete = 44



Recoloring



Delete = 46

Red/Black Tree Delete

2-3 Tree  $\Rightarrow$

insert = 20  $\longrightarrow$

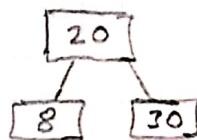
20

insert = 30  $\longrightarrow$

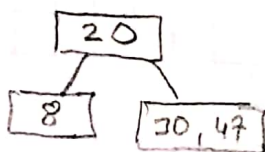
20, 30

insert = 8  $\longrightarrow$

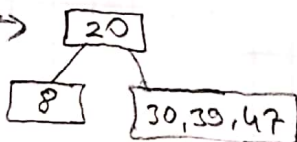
8, 20, 30



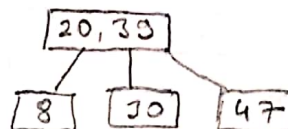
insert = 47  $\longrightarrow$



insert = 39  $\longrightarrow$



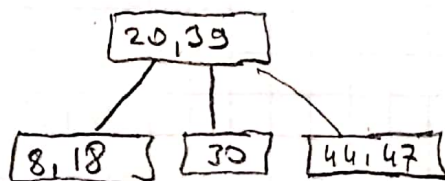
$\Rightarrow$



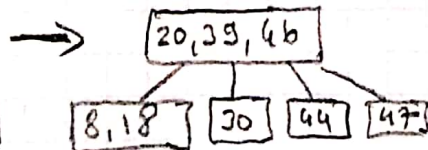
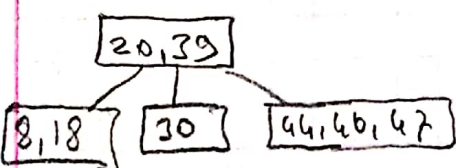
insert = 18  $\hookrightarrow$



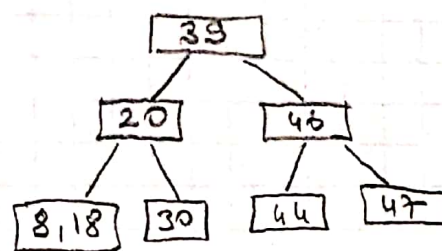
insert = 44  $\hookrightarrow$



insert = 46  $\hookrightarrow$



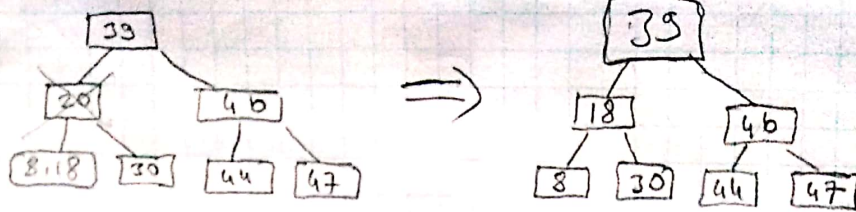
$\Rightarrow$



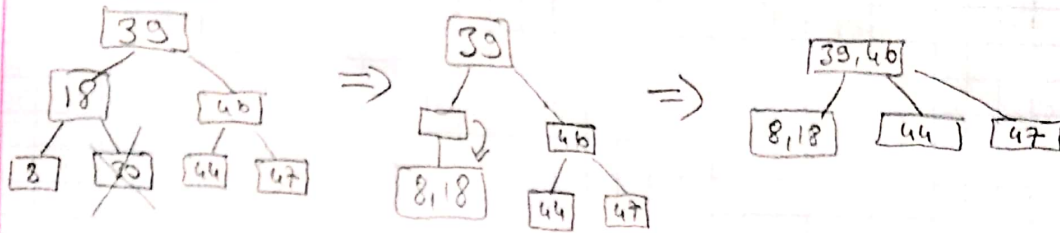
2-3 Tree  
insert



Delete = 20



Delete = 30



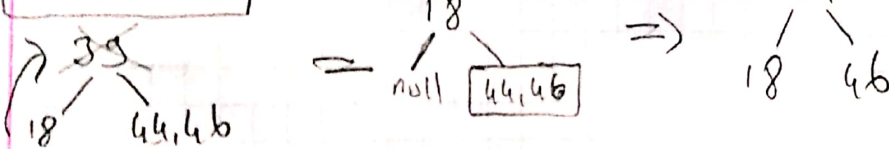
Delete = 8



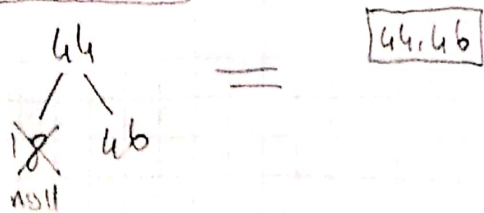
Delete = 47



Delete = 39



Delete = 18



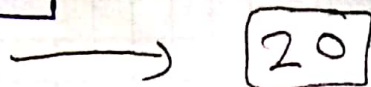
Delete = 44 → 46

Delete = 46 → null

2-3 Tree Delete

# B-Tree with order 4

insert = 20



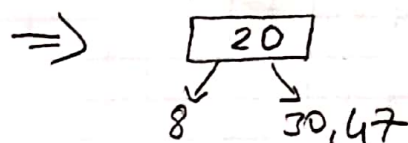
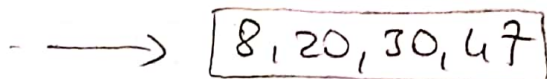
insert = 30



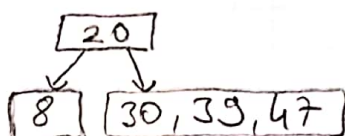
insert = 8



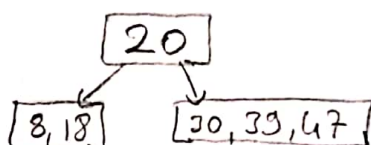
insert = 47



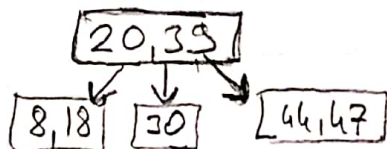
insert = 39



insert = 18

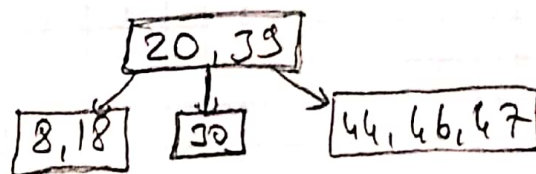


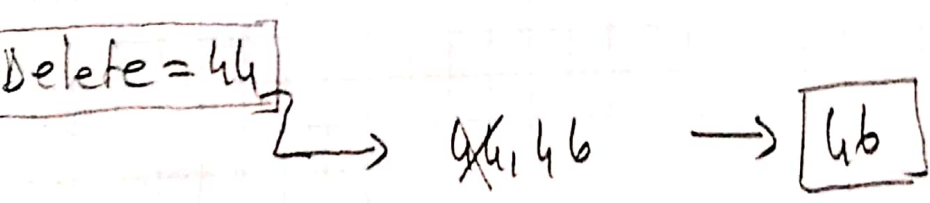
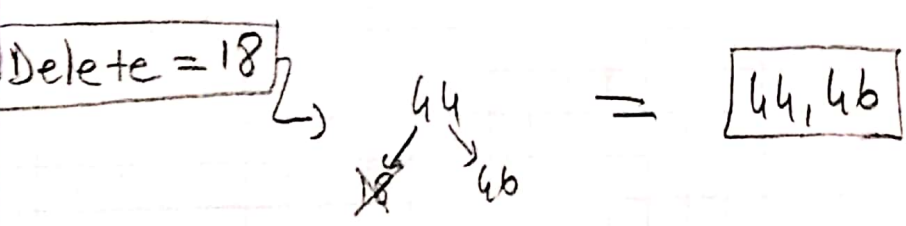
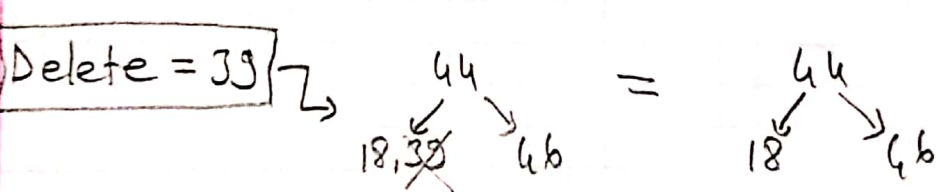
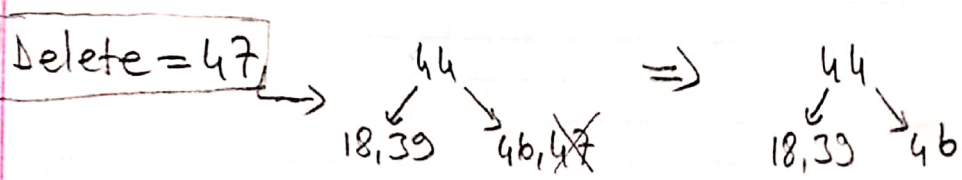
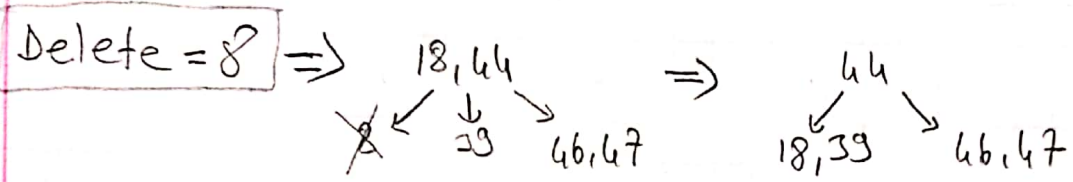
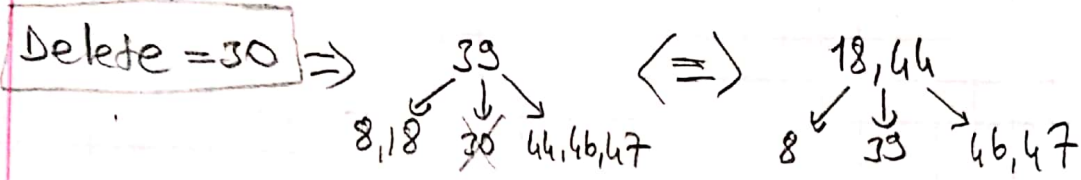
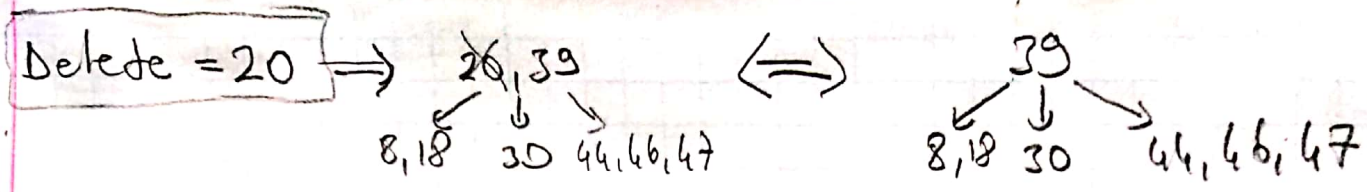
insert = 44



B-Tree with 4  
insert

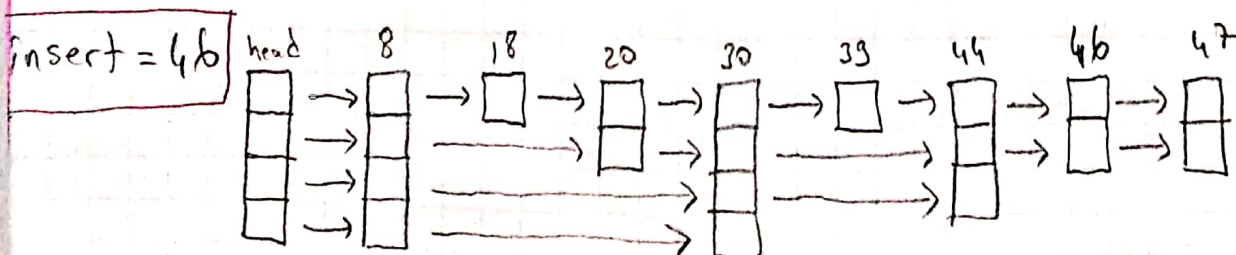
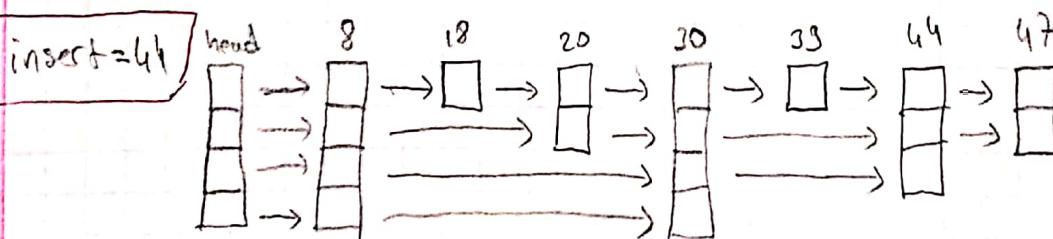
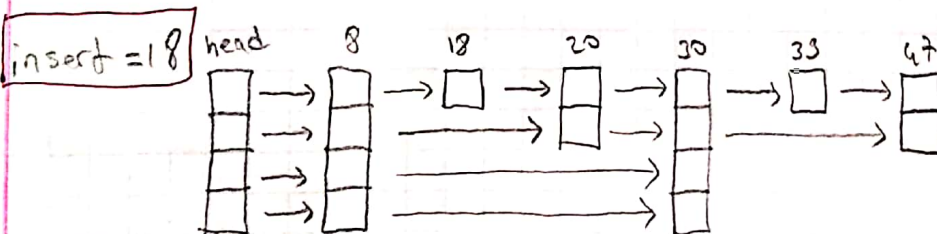
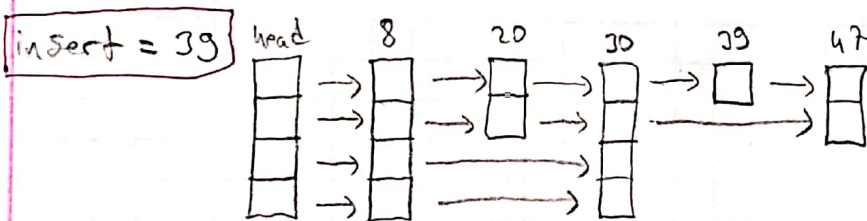
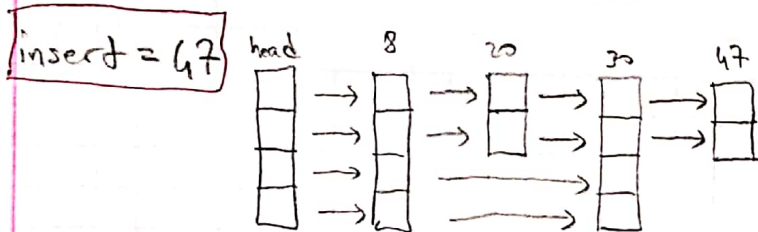
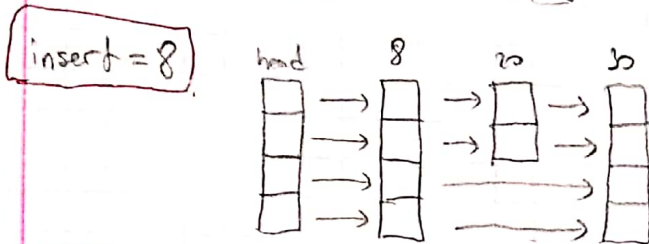
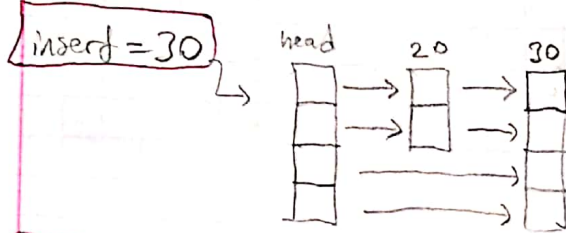
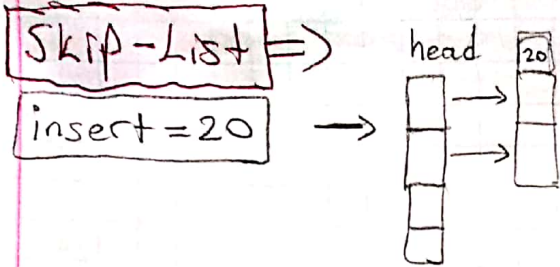
insert = 46





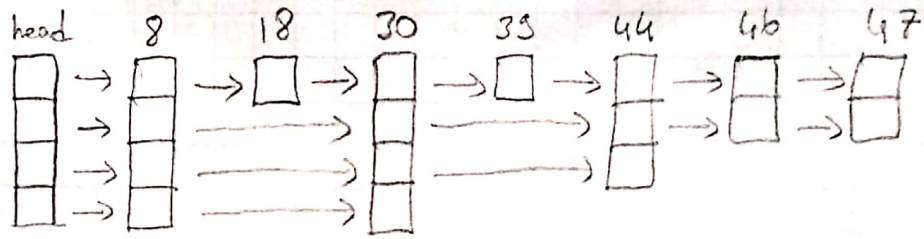
B-Tree with 4 Delete



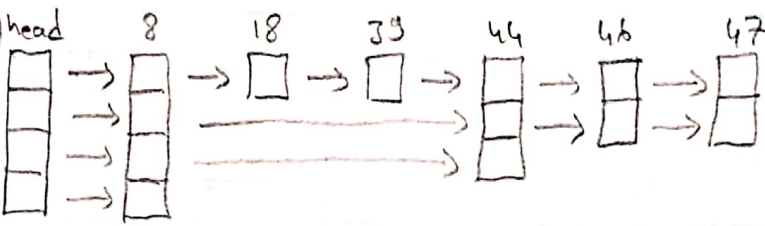


Skip-List  
insert

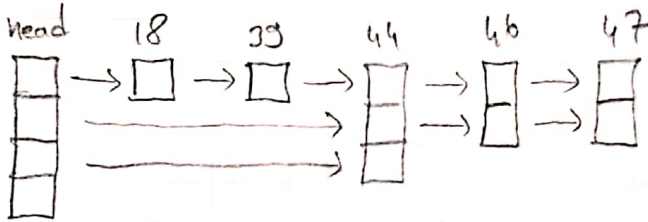
Delete = 20



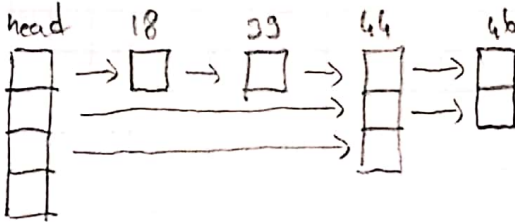
Delete = 30



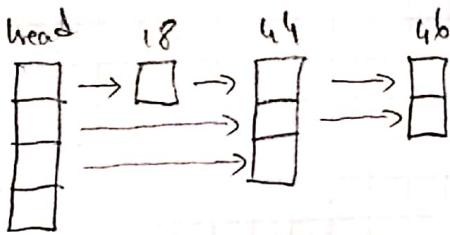
Delete = 8



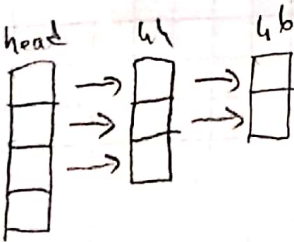
Delete = 47



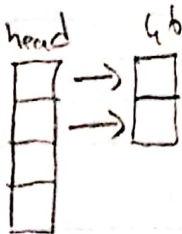
Delete = 39



Delete = 18



Delete = 44



Delete = 46

Skip-List  
Delete