Prob. 1	Prob. 2	Prob. 3	Prob. 4

## Problem 1.

We can use contradiction or construction:

max: sth like suppose there is another binary tree with greater potential than the binary list but with the same n number of nodes that would mean that at some height of the tree there is one node having more nodes in its sublist than the equivalent node in the linked list however this would be impossible since in a linked list the only nodes of a tree that are not included in a node's subtree are its parent nodes

well we can just say that the w(root) = n-1, and the biggest weight for its child is n-2 constructing such a tree will end up with a linked list

min: well summing n/2 + n/2 or (n/2)-1 + (n/2)+1, doesnt matter, we get n BUT by doing n/2 + n/2 we will have the tree with the smallest height -i smallest number of element in the sum

and besides this way we maximize the number of nodes with no children

## Problem 2.

Let's say we have a request of m elements with n distinct elements in it. Then if m = n, any order of the list with those n elements would give the same cost: 1 + 2 + ... + n.

Now assume we have elements in the request that appear more than once, then the order matters. The goal to minimize the cost is that the access cost of an element appearing often in the request should be low. Thus if we order the list given the number of time it appears in the request (frequency), we get the static optimal ordering. The optimized cost is:

$$X_1 * F_1 + X_2 * F_2 + ... + X_n * F_n$$

Where  $X_i$  is the access cost of element i such that  $X_i = i$  and  $F_i$  the frequency of i in the request such that  $\forall i, F_i \geq F_{i+1}$ . It's clear that if this last inequality is not satisfied we can only get a larger sum because  $\forall i, X_i < X_{i+1}$ .

Problem 3.

Problem 4.