QUESTION 3 SECANT METHOD AND THE METHOD OF FALSE POSITION

$$f(x) = -x^3 - \cos(x)$$

The Secant Method

$$p_{n} = p_{n-1} - \frac{f(p_{n-1})(p_{n-1} - p_{n-2})}{f(p_{n-1}) - f(p_{n-2})}$$

$$p_0 = -1$$
 $p_1 = 0$

$$p_2 = 0 - \frac{f(0)(0 - (-1))}{f(0) - f(-1)} = -0.685073$$

$$p_3 = -0.685073 - \frac{f \ (-0.685073) \ (-0.685073 - 0)}{f \ (-0.685073) - f \ (0)} = -1.252076$$

The Method of False Position

The only difference is

if
$$(f(p_2) * f(p_1) < 0) p_0 = p_1$$
;

Otherwise p_0 stays same

$$p_1 = p_2$$

$$f(p_2) = f(-0.685073) = -0.452850 f(p_1) = f(0) = -1$$

then
$$p_3 = -0.685073 - \frac{f\left(-0.685073\right)\left(-0.685073 - (-1)\right)}{f\left(-0.685073\right) - f\left(-1\right)} = -0.841355$$