# **Credibility Dynamics and Disinflation Plans**

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The views expressed herein are those of the authors and should not be attributed to the IMF, its Executive Board, or its management.

### Motivation

- · Macro models: expectations of future policy determine current outcomes
- · Policy typically set assuming commitment or discretion
- · Governments actively attempt to influence beliefs about future policy
  - · Forward guidance, inflation targets, fiscal rules
- This paper: rational-expectations theory of government credibility
- Application in a (modern) Barro-Gordon setup

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- · Governments actively attempt to influence beliefs about future policy
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- · This paper: rational-expectations theory of government credibility
  - · Insights from reputation literature



· Application in a (modern) Barro-Gordon setup

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- · What is reputation?
  - · Private sector posterior belief that the government is committed to a particular plan
- Given a plan [Continuation equilibrium]
  - Larger departures are easier to detect
    - Crucial feature: noise partially masks government's current choice
  - $\cdot$  'More time-inconsistent' plans have a more negative average drift of reputation
- Planner anticipates credibility dynamics of plans [Equilibrium
- Consider the limit when initial reputation vanishes to zero

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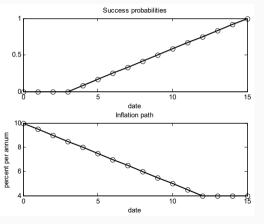
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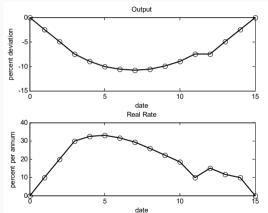
	Main result
Planner chooses a back-loaded plan	<ul><li>In application, gradual disinflation</li><li>No real inertia, but good for incentives</li></ul>

· Consider the limit when initial reputation vanishes to zero

# Our want operator

· Goodfriend and King (2005) describe the Volcker disinflation





### Literature

## Sustainable plans – anything goes

from Kydland and Prescott (1977), Chari and Kehoe (1990), Abreu, Pearce, and Stacchetti (1990), Phelan and Stacchetti (2001)

### Reputation without noise – zero inflation at onset

Milgrom and Roberts (1982), Kreps and Wilson (1982), Barro (1986), Backus and Driffill (1985), Barro and Gordon (1986), Sleet and Yeltekin (2007)

Dovis and Kirpalani (2019) – constant but more than zero

## · Reputation with noise

Commitment: Lu (2013), Lu, King, and Pastén (2008, 2016)

Static plans: Faingold and Sannikov (2011)

### · Preference uncertainty with noise - announcements irrelevant

Cukierman and Meltzer (1986), Faust and Svensson (2001), Phelan (2006), etc

# Roadmap

- · Model
- · Continuation equilibria conditional on a plan
- · Plans
- Discussion
- · Conclusion

# Model

### Framework

· A government dislikes inflation and output away from a target  $y^* > 0$ 

$$L_{t} = \mathbb{E}_{t} \left[ \sum_{s=0}^{\infty} \beta^{s} \left( (\mathbf{y}^{\star} - \mathbf{y}_{t+s})^{2} + \gamma \pi_{t+s}^{2} \right) \right]$$

· A Phillips curve relates output to current and expected future inflation

$$\pi_t = \kappa \mathbf{y}_t + \beta \mathbb{E}_t \left[ \pi_{t+1} \right]$$

- The government controls inflation only imperfectly (through  $g_t$ )

$$\pi_t = \mathbf{g}_t + \epsilon_t$$

with  $\epsilon_t \stackrel{\textit{iid}}{\sim} F_{\epsilon}$ 

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## Reputation

- The government can be rational or one of many 'behavioral' types
  - Behavioral types  $c \in \mathcal{C}$
  - Type c is committed to an inflation plan  $\{a_t\}_{t=0}^{\infty}$
  - · For simplicity let all plans have  $a_{t+1} = \phi_c(a_t)$

[Finding the state is an art]

- Behavioral types have (total) probability z
  - · Conditional on behavioral, probability  $\nu$  over  $\mathcal C$
- Private sector knows z and  $\nu$ 
  - Does inference over the government's type
  - Uses announcement and inflation choices

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# Behavioral types

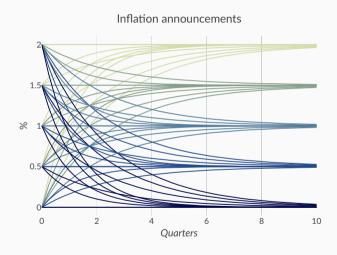
- What is the set C?
  - $\cdots$  and associated possible  $\phi_c$  functions
- Consider  $\{a_t\}_t$  paths characterized by
  - Starting point a<sub>0</sub>
  - Decay rate  $\omega$
  - · Asymptote  $\chi$

$$a_t = \chi + (a_0 - \chi)e^{-\omega t}$$
$$\phi(a) = \chi + e^{-\omega}(a - \chi)$$

# Behavioral types

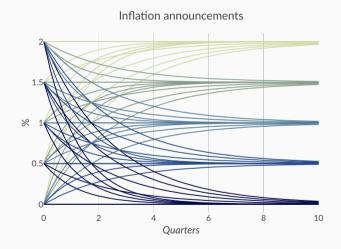
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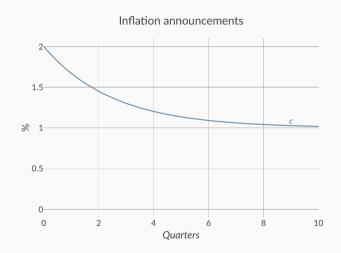
# Gameplay

- At t = 0, inflation targets are announced
  - Type  $\mathbf{c} \in \mathcal{C}$  says  $\mathbf{c}$
  - Rational type strategizes announces r possibly  $\in C$
- At time  $t \ge 0$ , the government sets inflation
  - Behavioral type  $c \in C$ implements  $g_t = a_t^c$
  - Rational type acts strategically chooses q<sub>t</sub> ≤ q<sub>t</sub><sup>c</sup>



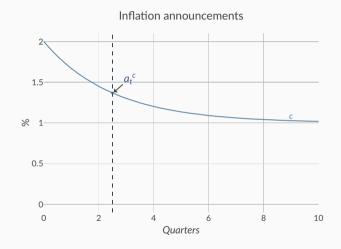
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# Continuation equilibria conditional on a plan

# **Reputation and Outcomes**

· Output is determined by beliefs  $\mathbb{E}_t\left[\pi_{t+1}\right]$  and actual inflation  $\pi_t = g_t + \epsilon_t$ 

$$\pi_{t} = \kappa y_{t} + \beta \mathbb{E}_{t} \left[ \pi_{t+1} \right] = \kappa y_{t} + \beta \mathbb{E}_{t} \left[ \mathbb{1}_{c} a_{t+1}^{c} + (1 - \mathbb{1}_{c}) g_{t+1}^{\star} \right]$$

Private sector solves a signal extraction problem to update beliefs

$$\mathbb{P}\left(c \mid \pi_{t}, \mathcal{F}_{t-1}\right) = \frac{\mathbb{P}\left(c \mid \mathcal{F}_{t-1}\right) \cdot f_{\epsilon}(\epsilon_{t} | c)}{\mathbb{P}\left(c \mid \mathcal{F}_{t-1}\right) \cdot f_{\epsilon}(\epsilon_{t} | c) + (1 - \mathbb{P}\left(c \mid \mathcal{F}_{t-1}\right)\right) \cdot f_{\epsilon}(\epsilon_{t} | r)}$$

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### Given an announcement c,

· The problem of the rational type is, given expectations  $g_c^{\star}$ 

$$\mathcal{L}^{c}(p,a) = \min_{g} \mathbb{E}\left[ (\mathbf{y}^{\star} - \mathbf{y})^{2} + \gamma \pi^{2} + \beta \mathcal{L}^{c}(p',\phi_{c}(a)) \right]$$
 subject to  $\pi = g + \epsilon$  
$$\pi = \kappa \mathbf{y} + \beta \left[ p'\phi_{c}(a) + (1 - p')g_{c}^{\star}(p',\phi_{c}(a)) \right]$$
 
$$p' = p + p(1 - p) \frac{f_{\epsilon}(\pi - a) - f_{\epsilon}(\pi - g_{c}^{\star}(p,a))}{pf_{\epsilon}(\pi - a) + (1 - p)f_{\epsilon}(\pi - g_{c}^{\star}(p,a))}$$

· Rational expectations requires  $g_c^{\star}$  to be the policy associated with  $\mathcal{L}^c$ 

# **Continuation Equilibrium**

## Definition

Given an announcement c, a continuation equilibrium is a pair  $(\mathcal{L}^c, g_c^*)$  such that

- ·  $\mathcal{L}^c$  is the rational type's value function at expectations  $g_c^\star$
- $\cdot g_c^{\star}$  is the policy function associated with  $\mathcal{L}^c$

## A First Look at Different Plans

### Observation

• Plans  $c \in \mathcal{C}$  are

$$c=(a_0,\chi,\omega)$$

• For  $a, b \in \mathbb{R}$ 

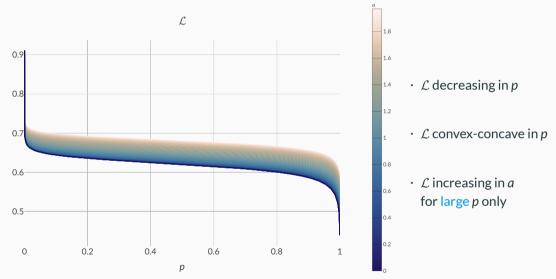
$$(\mathcal{L}, g^*)$$
 is a continuation equilibrium for  $(a, \chi, \omega)$ 

$$\iff$$

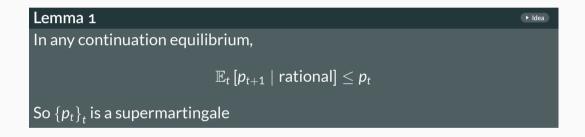
 $(\mathcal{L}, g^*)$  is a continuation equilibrium for  $(b, \chi, \omega)$ 

· Means  $a\mapsto \mathcal{L}^c(p,a)$  compares the same plan at different times and different plans

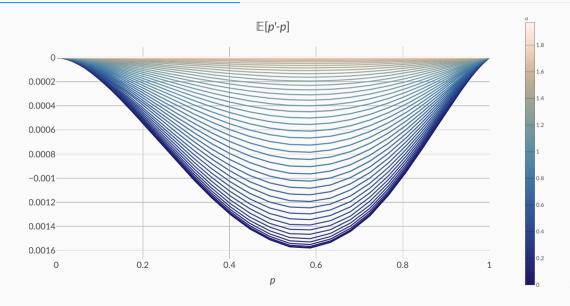
## The Value Function



# **Reputation Dynamics**



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$$rac{\partial \mathsf{y}}{\partial \pi} = rac{1}{\kappa} \left[ 1 - eta rac{\partial \mathsf{p}'}{\partial \pi} \left( \phi_{\mathsf{c}}(\mathsf{a}) - \mathsf{g}^{\star}(\mathsf{p}', \phi_{\mathsf{c}}(\mathsf{a})) + (1 - \mathsf{p}') rac{\partial \mathsf{g}^{\star}(\mathsf{p}', \phi_{\mathsf{c}}(\mathsf{a}))}{\partial \mathsf{p}'} 
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ight]$$

- · More inflation
  - 1. Increases output by  $\frac{1}{\kappa}$
  - 2. Shifts inflation expectations from  $\phi_c(a)$  towards  $g^*(p', \phi_c(a))$ 
    - ... p' decreases with higher  $\pi$  when  $g^*(p, a) > a$
  - 3. Shifts expectations of the rational type's future choice

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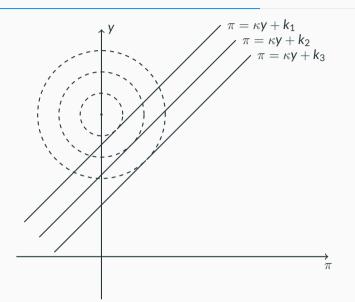
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# Phillips curves

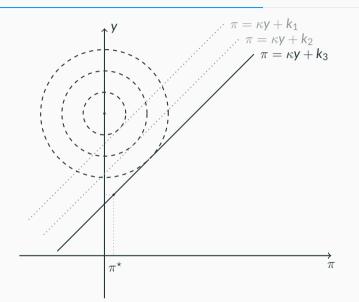




- Without reputation: if  $\beta \mathbb{E} [\pi'] = k_j$  choose point on *j*th PC
- If announced aand in eq'm  $g^*(p,a) = a$  $\implies$  get flat PC
- If  $g^*(p,a) > a$   $\implies \frac{\partial p'}{\partial \pi}$  matters

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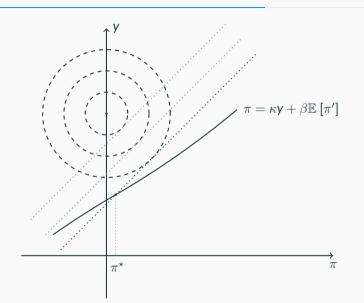




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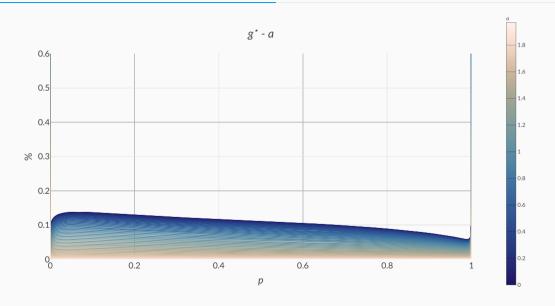
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- · If  $g^{\star}(p, a) > a$   $\implies \frac{\partial p'}{\partial \pi}$  matters

# **Equilibrium Deviations**



#### Conjecture

· Let  $\pi^N$  be the Nash equilibrium inflation of the stage game. Then

$$\forall c \in C: \qquad g_c^{\star}(p,a) \leq \pi^N$$

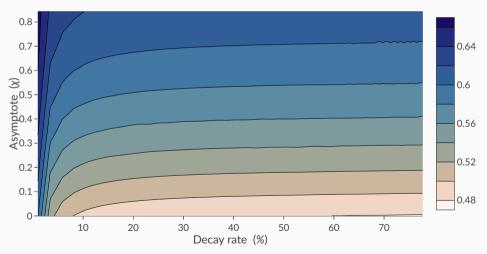
· Define the remaining credibility of a plan as

$$C_c(p,a) = (1-\beta)\frac{\pi^N - g_c^{\star}(p,a)}{\pi^N - a} + \beta \mathbb{E}\left[C_c(p_c'(p,a), \phi_c(a))\right]$$

# Plans

### Credibility



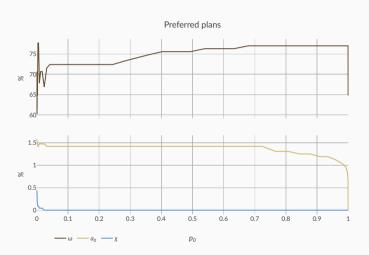


#### **Plans**

- For each  $c \in C$ , find  $\mathcal{L}^c(p,a), g_c^{\star}(p,a)$ .
- Generates big matrix  $\mathcal{L}(p, a; \omega, \chi)$
- First pass: preferred plan at each p

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#### What plan to choose?

#### Back to the initial announcement: two notions

• If in equilibrium gov't announces type c with density  $\mu(c)$ ,

$$p_0(c; z, \mu) = \frac{z\nu(c)}{z\nu(c) + (1-z)\mu(c)}$$

· So study

$$\lim_{z\to 0} \min_{\mu} \int \mathcal{L}(p_0(a_0,\omega,\chi;z,\mu),a_0,\omega,\chi) d\mu$$

- Kambe (1999): gov't announces type c and becomes committed to c with exogenous p<sub>0</sub> probability
- · Tractable:  $p_0$  independent of c
- So the limit we consider is

$$\lim_{p_0\to 0} \min_{a_0,\omega,\chi} \mathcal{L}(p_0,a_0,\omega,\chi)$$

- Not entirely arbitrary
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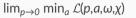
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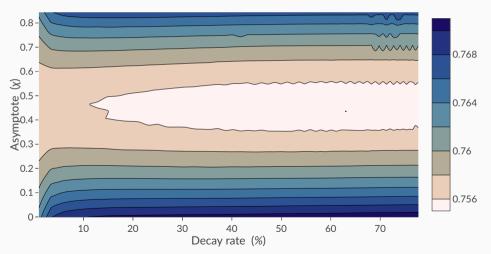
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### Equilibrium for given z

• We want k and  $\mu$  such that

$$\begin{split} \int_{\mathcal{C}} \mu(c) &= 1 \\ p_0(c) &= \frac{z\nu(c)}{z\nu(c) + (1-z)\mu(c)} \\ \mathcal{L}(p_0(c),c) &= k \quad \text{if } \mu(c) > 0 \\ \mathcal{L}(p_0(c),c) &\geq k \quad \text{if } \mu(c) = 0 \end{split}$$

- · We do
  - Start with  $k_0 \leq \mathcal{L}(0,c) = \mathcal{L}^N$
  - · Partition states

$$\mathcal{L}(\mathbf{1},c) \geq k \quad \rightarrow \quad \mu(c) = 0$$
  
 $\mathcal{L}(\mathbf{1},c) < k$ 

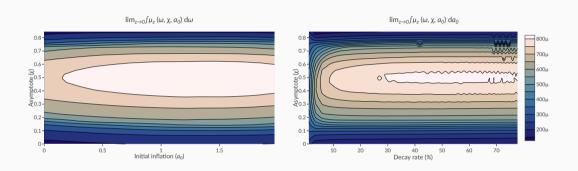
· In second case find  $\mu(c)$  such that

$$\mathcal{L}(p_0(c),c)=k$$

This is possible if  $k \le \text{value}$  in static Nash

- Set  $\mu(c) = \mathcal{B}^{-1}(p_0(c); \nu, z)$  if unset
- · Check whether  $\int_{\mathcal{C}} \mu(c) = 1$

#### Equilibrium distribution of announcements



- Gradualism:  $\mathbb{P}(a_0 > \chi) = 81.3\%$ .  $\mathbb{P}(a_0 > 5\chi) = 52.6\%$ .
- Imperfect credibility:  $\mathbb{P}(\chi = 0) = 9.62\%$ .

# Discussion

#### Other Models

#### We dissect our gradualism result by linking to sustainable-plans literature

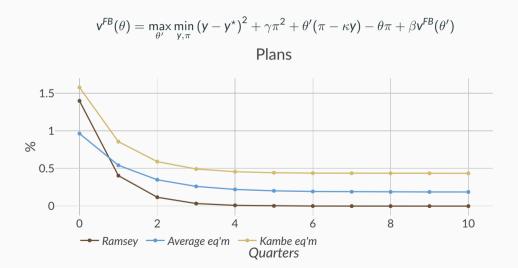
- Four models
  - 1. Ramsey plan
  - 2. Sustainable plans
    - · Threat of high inflation expectations
  - 3. Sustainable plans with a control shock
    - · Threat of inflation threshold that triggers punishment regime
  - 4. Recursive plans with reputation
    - $\cdot\;$  Sustained with promise of anchoring of favorable expectations

#### A Planning Problem

$$\mathbf{v}^{\mathsf{FB}}(\theta) = \max_{\theta'} \min_{\mathbf{y},\pi} \left( \mathbf{y} - \mathbf{y}^{\star} \right)^{2} + \gamma \pi^{2} + \theta'(\pi - \kappa \mathbf{y}) - \theta \pi + \beta \mathbf{v}^{\mathsf{FB}}(\theta')$$

- · Recursive version of Ramsey plan
  - · Initial  $\theta = 0$
  - · Time inconsistency:  $\theta'(0) \neq 0$
- · FOC for  $\theta'$ :  $\pi \kappa \mathbf{y} + \beta \frac{\partial \mathbf{v}^{\mathsf{FB}}(\theta')}{\partial \theta'} = \mathbf{0} \longrightarrow \pi = \kappa \mathbf{y} + \beta \pi'$
- · Simulate by iterating on  $\pi_t = \pi(\theta)$ ,  $\theta_{t+1} = \theta'(\theta)$
- $\cdot \ \, \text{Imperfect control irrelevant} \quad \longrightarrow \quad \text{only adds } \sigma_{\epsilon}^2 \left( \gamma + \frac{1}{\kappa^2} \right)$

# A Planning Problem





#### Descentralization

- · Perfect control of inflation
- Private sector 'threatens' to expect  $\xi$  after deviations

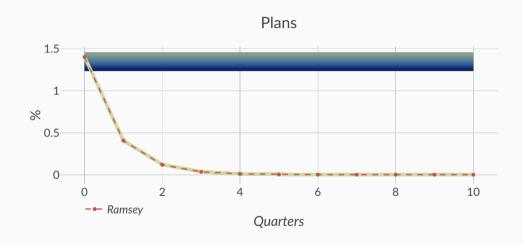
$$v^{\xi}(p,a) = \min_{\mathbf{y},\pi,a'} (\mathbf{y} - \mathbf{y}^{\star})^{2} + \gamma \pi^{2} + \beta v^{\xi}(p',a')$$
subject to 
$$\pi = \kappa \mathbf{y} + \beta \left( p' \mathbf{g}_{\pi}^{\xi} (\mathbf{1},a') + (\mathbf{1} - p') \xi \right)$$

$$p' = \begin{cases} 1 & \text{if } \pi = a \\ 0 & \text{otherwise} \end{cases}$$

 $\cdot$  Use p to denote whether the government has deviated

▶ Is this Reputation?

# Sustainable plans with expectations as threats



# Sustainable plans with reverting triggers



• Trigger 'punishment regime' if deviation large enough (as in Green & Porter, 1984)

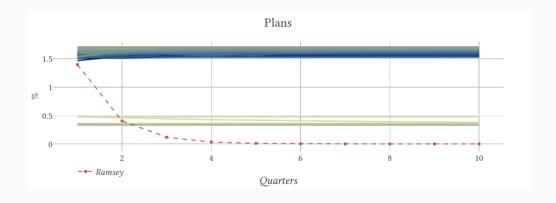
$$\begin{aligned} \mathbf{v}^{\mathsf{G}}(a) &= \min_{\mathbf{g}, a'} \mathbb{E}\left[ (\mathbf{y} - \mathbf{y}^{\star})^2 + \gamma \pi^2 + \beta \left( p' \mathbf{v}^{\mathsf{G}}(a) + (\mathbf{1} - p') \mathbf{v}^{\mathsf{P}} \right) \right] \\ \text{subject to} \quad \pi &= \mathbf{g} + \epsilon \\ \pi &= \kappa \mathbf{y} + \beta \left( p' \mathbf{g}^{\mathsf{G}}(a') + (\mathbf{1} - p') \xi \right) \\ p' &= \begin{cases} \mathbf{1} & \text{if } \frac{|\pi - a|}{a} < D \\ 0 & \text{otherwise} \end{cases} \end{aligned}$$

$$\mathbf{v}^{\mathsf{P}} = \min_{\pi, a'} (\mathbf{y} - \mathbf{y}^{\star})^{2} + \gamma \pi^{2} + \beta \left( \theta \mathbf{v}^{\mathsf{G}}(a) + (1 - \theta) \mathbf{v}^{\mathsf{P}} \right) + \sigma_{\epsilon}^{2} \left( \gamma + \frac{1}{\kappa^{2}} \right)$$
subject to  $\pi = \kappa \mathbf{y} + \beta \xi$ 

# Sustainable plans with reverting triggers (cont'd)

$$\begin{aligned} \mathbf{v}^{\mathsf{GP}}(p,a) &= \min_{g,a'} \mathbb{E}\left[ (\mathbf{y} - \mathbf{y}^\star)^2 + \gamma \pi^2 + \beta \left( \mathbf{v}^{\mathsf{GP}}(p',a') \right) \right] \\ \mathsf{subject} \ \mathsf{to} &\quad \pi = g + \epsilon \\ &\quad \pi = \kappa \mathbf{y} + \beta \left( p' g^{\mathsf{GP}}(p',a') + (\mathbf{1} - p') \xi \right) \\ &\quad b' = \begin{cases} 1 & \text{if } \frac{|\pi - a|}{a} < \mathsf{D} \\ 0 & \text{otherwise} \end{cases} & \text{if } p = 1 \\ 1 & \text{with prob } \theta \\ 0 & \text{with prob } 1 - \theta \end{cases} \end{aligned}$$

# Sustainable plans with reverting triggers

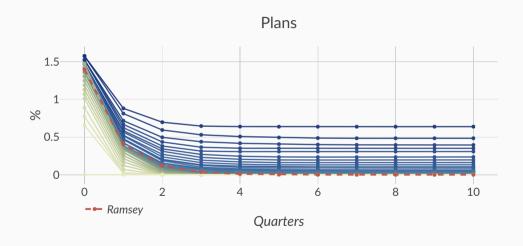


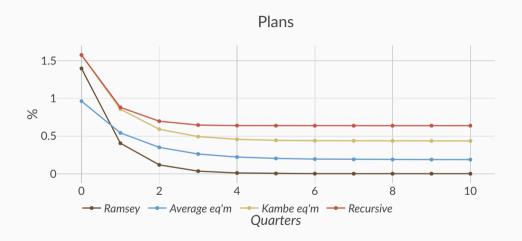


· Planner + policy maker structure (as in Dovis & Kirpalani, 2019)

$$\begin{split} \mathbf{v}^{\mathsf{R}}(p,a) &= \min_{g,a'} \, \mathbb{E}\left[ (\mathbf{y} - \mathbf{y}^{\star})^2 + \gamma \pi^2 + \beta \mathbf{v}^{\mathsf{R}}(p',a') \right] \\ \text{subject to} \quad \pi &= g + \epsilon \\ \quad \pi &= \kappa \mathbf{y} + \beta \left( p'a' + (1-p')g^{\mathsf{R}}(p',a') \right) \\ \quad p' &= p + p(1-p) \frac{f_{\epsilon}(\pi-a) - f_{\epsilon}(\pi-g^{\mathsf{R}}(p,a))}{pf_{\epsilon}(\pi-a) + (1-p)f_{\epsilon}(\pi-g^{\mathsf{R}}(p,a))} \end{split}$$

# Recursive plans with reputation





Model	Ramsey	Kambe eq'm	'Average' rec plan	Recursive plan
Initial inflation	1.40%	1.63%	1.58%	1.58%
Long-run inflation	0%	0.44%	0.65%	0.65%
Value function	0.3364	0.7552	0.7589	0.7554

Table 1: Inflation plans

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Table 1: Inflation plans

 $\cdot\,$  Kambe gains from pre-announcing: lower asymptote, more credibility esp. early on

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Table 1: Inflation plans

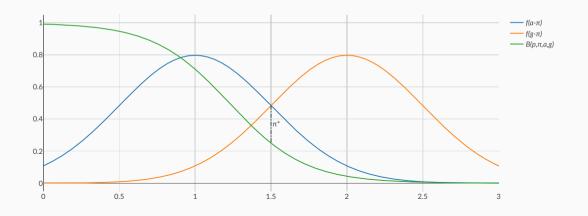
 $\cdot$  Recursive gains from flexibility: modulates a' to developments in p



#### **Concluding Remarks**

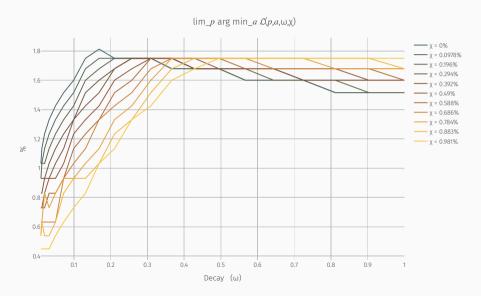
- Model of reputational dynamics and policy
  - · Simple environment
  - · Focus on low reputation limit
- · Credibility-dynamics concerns influence choice of policy
  - · Tradeoff between literal promises and incentives
  - · Gradual plans boost reputation-building incentives for future decision-makers
- · Structure of reputation maps into the incentive constraint of a planner's problem
  - ... creating large option values of complying
  - ... which are larger when the plan is backloaded

$$\mathcal{B}(p,\pi,a,g) = p + p(1-p) \frac{f_{\epsilon}(\pi-a) - f_{\epsilon}(\pi-g)}{pf_{\epsilon}(\pi-a) + (1-p)f_{\epsilon}(\pi-g)}$$



#### Results





#### Reputation (Kreps and Wilson, 1982; Milgrom and Roberts, 1982)



#### Imagine an incumbent facing a sequence of potential entrants

- · Each period, entrant decides entry, incumbent fights or accomodates
  - · Incumbent prefers entrant to stay out but prefers to accomodate if entry
- Fighting the first entrant doesn't affect the decision of following entrants
- Reputation as incomplete information
  - $\cdot$  What if the incumbent could be behavioral and always produce q upon entry?
- Incentive for the rational incumbent to pretend to be behaviora
- Independent of the 'objective' probability of behavioral

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