
MODULE *cache*

EXTENDS *TLC*, *Integers*

CONSTANTS

ResourceCap,
MaxConsumerCap,
Actors

ASSUME *ResourceCap* > 0
ASSUME *MaxConsumerCap* ∈ 1 .. *ResourceCap*

Time \triangleq {“t1”}
Processes \triangleq *Actors* ∪ *Time*

VARIABLES

resources_left,
resources_needed,
reserved,
pc

vars \triangleq ⟨*resources_left*, *resources_needed*, *pc*, *reserved*⟩

Init \triangleq

∧ *resources_left* = *ResourceCap*
∧ *reserved* = 0
∧ *resources_needed* ∈ [*Actors* → 1 .. *MaxConsumerCap*]
∧ *pc* ∈ [*Processes* → {“init”}]

CheckConsume(*actor*) \triangleq

Check if there are enough resources to consume. If so reserve them and set up as ready for consumption

∧ *pc*[*actor*] = “init”
∧ *resources_left* − *reserved* ≥ *resources_needed*[*actor*]
∧ *reserved*' = *reserved* + *resources_needed*[*actor*]
∧ *pc*' = [*pc* EXCEPT ![*actor*] = “ready”]
∧ UNCHANGED ⟨*resources_left*, *resources_needed*⟩

Consume(*actor*) \triangleq

Given that there are enough reserved resources, consume them one at a time

∧ *pc*[*actor*] = “ready”
∧ IF *resources_needed*[*actor*] > 0
THEN ∧ *resources_left*' = *resources_left* − 1
∧ *resources_needed*' = [*resources_needed* EXCEPT ![*actor*] = *resources_needed*[*actor*] − 1]
∧ *reserved*' = *reserved* − 1

$$\begin{aligned}
& \wedge \text{UNCHANGED } \langle pc \rangle \\
\text{ELSE } & \wedge \exists x \in 1 \dots \text{MaxConsumerCap} : \text{resources_needed}' = [\text{resources_needed} \text{ EXCEPT } ![actor] = \\
& \wedge pc' = [pc \text{ EXCEPT } ![actor] = \text{"init"}] \\
& \wedge \text{UNCHANGED } \langle \text{resources_left}, \text{reserved} \rangle
\end{aligned}$$

$$\begin{aligned}
\text{Refill}(time) & \triangleq \\
& \text{Refill resources at any time} \\
& \wedge pc[time] = \text{"init"} \\
& \wedge \text{resources_left}' = \text{ResourceCap} \\
& \wedge \text{UNCHANGED } \langle pc, \text{resources_needed}, \text{reserved} \rangle
\end{aligned}$$

$$\begin{aligned}
\text{Next} & \triangleq \\
& \vee \exists actor \in \text{Actors} : \text{Consume}(actor) \vee \text{CheckConsume}(actor) \\
& \vee \exists timer \in \text{Time} : \text{Refill}(timer)
\end{aligned}$$

$$\begin{aligned}
\text{Spec} & \triangleq \\
& \wedge \text{Init} \\
& \wedge \Box [Next]_{vars} \\
& \wedge \exists actor \in \text{Actors} : \text{WF}_{vars}(\text{Consume}(actor)) \\
& \wedge \exists actor \in \text{Actors} : \text{WF}_{vars}(\text{CheckConsume}(actor))
\end{aligned}$$

$$\text{NoZeroResources} \triangleq \text{resources_left} \geq 0$$

$$\text{EventuallyRefills} \triangleq \exists n \in 1 \dots \text{ResourceCap} : (\text{reserved} = n) \rightsquigarrow (\text{reserved} > n)$$
