

Lab 04 Digital 1

I

13

1.

A	B	C	Y
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	0
1	1	1	1

C \ AB	00	01	11	10
	0	1	0	1
0	1	1	0	1
1	0	0	1	1

$$Y = \bar{A}\bar{C} + A\bar{B} + AC$$

2.

A	B	C	Y
0	0	0	1
0	0	1	X
0	1	0	0
0	1	1	0
1	0	0	X
1	0	1	1
1	1	0	0
1	1	1	0

C \ AB	00	01	11	10
	0	1	0	0
0	1	0	0	X
1	X	0	0	1

$$Y = \bar{A}\bar{B} + A\bar{B}$$

$$Y = \bar{B}$$

GT

3. A B C D Y

0	0	0	0	1	-
0	0	0	1	0	
0	0	1	0	0	
0	0	1	1	1	-
0	1	0	0	0	
0	1	0	1	1	✓
0	1	1	0	1	✓
0	1	1	1	0	
1	0	0	0	0	
1	0	0	1	1	✓
1	0	1	0	1	-
1	0	1	1	0	
1	1	0	0	1	✓
1	1	0	1	0	
1	1	1	0	0	
1	1	1	1	1	

CD \ AB	00 01 11 10			
	00	01	11	10
00	1	0	1	0
01	0	1	0	1
11	1	0	1	0
10	0	1	0	1

$$Y = \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}CD + \bar{A}B\bar{C}\bar{D} + \bar{A}BC\bar{D}$$

$$+ AB\bar{C}\bar{D} + ABCD + A\bar{B}\bar{C}\bar{D} + A\bar{B}C\bar{D}$$

4.

A	B	C	D	Y
0	0	0	0	X
0	0	0	1	X
0	0	1	0	X
0	0	1	1	0 ✓
0	1	0	0	0 ✓
0	1	0	1	X
0	1	1	0	0 ✓
0	1	1	1	X
1	0	0	0	1 ✓
1	0	0	1	0 ✓
1	0	1	0	X
1	0	1	1	1 ✓
1	1	0	0	1 ✓
1	1	0	1	1 ✓
1	1	1	0	X
1	1	1	1	1 ✓

	00	01	11	10
00	X	0	1	1
01	X	X	1	0
11	0	X	1	1
10	X	0	X	X

$$Y = AB + AC + A\bar{D}$$

14. II.

$$1. Y = A \cdot B \cdot C \cdot \bar{D} + A \cdot B \cdot C \cdot D + (A + B + C + D)$$

A	B	C	D	Y
0	0	0	0	1 ✓
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1 ✓
1	0	0	1	1 ✓
1	0	1	0	1 ✓
1	0	1	1	1 ✓
1	1	0	0	1 ✓
1	1	0	1	1 ✓
1	1	1	0	1 ✓
1	1	1	1	0

AB	00	01	11	10
00	1	0	1	1
01	0	0	1	1
11	0	0	0	1
10	0	0	1	1

$$Y = A\bar{B} + A\bar{C} + A\bar{D} + \bar{B}\bar{C}\bar{D}$$

$$(0,0,0,0) = 0 \cdot 0 \cdot 0 \cdot 1 + 0 \cdot (0 \cdot 0 \cdot 0) + (0 + 0 + 0 + 0) = 1$$

$$(0,0,0,1) = 0 \cdot 0 \cdot 0 \cdot 0 + 0 \cdot (0 \cdot 0 \cdot 1) + (0 + 0 + 0 + 1) = 0$$

$$(0,0,1,0) = 0 \cdot 0 \cdot 1 \cdot 1 + 0 \cdot (0 \cdot 1 \cdot 0) + (0 + 0 + 1 + 0) = 0$$

$$(0,0,1,1) = 0 \cdot 0 \cdot 1 \cdot 0 + 0 \cdot (0 \cdot 1 \cdot 1) + (0 + 0 + 1 + 1) = 0$$

$$(0,1,0,0) = 0 \cdot 1 \cdot 0 \cdot 1 + 0 \cdot (1 \cdot 0 \cdot 0) + (0 + 1 + 0 + 0) = 0$$

$$(0,1,0,1) = 0 \cdot 1 \cdot 0 \cdot 0 + 0 \cdot (1 \cdot 0 \cdot 1) + (0 + 1 + 0 + 1) = 0$$

$$(0,1,1,0) = 0 \cdot 1 \cdot 1 \cdot 1 + 0(\overline{1 \cdot 1 \cdot 0}) + (\overline{0 \cdot 1 + 1 + 0}) = 0$$

$$(0,1,1,1) = 0 \cdot 1 \cdot 1 \cdot 0 + 0(\overline{1 \cdot 1 \cdot 1}) + (\overline{0 \cdot 1 + 1 + 1}) = 0$$

$$(1,0,0,0) = 1 \cdot 0 \cdot 0 \cdot 1 + 1(\overline{0 \cdot 0 \cdot 0}) + (\overline{1 + 0 + 0 + 0}) = 1$$

$$(1,0,0,1) = 1 \cdot 0 \cdot 0 \cdot 0 + 1(\overline{0 \cdot 0 \cdot 1}) + (\overline{1 + 0 + 0 + 1}) = 1$$

$$(1,0,1,0) = 1 \cdot 0 \cdot 1 \cdot 1 + 1(\overline{0 \cdot 1 \cdot 0}) + (\overline{1 + 0 + 1 + 0}) = 1$$

$$(1,0,1,1) = 1 \cdot 0 \cdot 1 \cdot 0 + 1(\overline{0 \cdot 1 \cdot 1}) + (\overline{1 + 0 + 1 + 1}) = 1$$

$$(1,1,0,0) = 1 \cdot 1 \cdot 0 \cdot 1 + 1(\overline{1 \cdot 0 \cdot 0}) + (\overline{1 + 1 + 0 + 0}) = 1$$

$$(1,1,0,1) = 1 \cdot 1 \cdot 0 \cdot 0 + 1(\overline{1 \cdot 0 \cdot 1}) + (\overline{1 + 1 + 0 + 1}) = 1$$

$$(1,1,1,0) = 1 \cdot 1 \cdot 1 \cdot 1 + 1(\overline{1 \cdot 1 \cdot 0}) + (\overline{1 + 1 + 1 + 0}) = 1$$

$$(1,1,1,1) = 1 \cdot 1 \cdot 1 \cdot 0 + 1(\overline{1 \cdot 1 \cdot 1}) + (\overline{1 + 1 + 1 + 1}) = 0$$

A	B	C	D	Y
1	0	x	x	1
1	x	0	x	1
1	x	x	0	1
x	0	0	0	1

$$2. Y = \bar{A} \cdot B \cdot C + \overline{B \cdot \bar{C}} + B \cdot C$$

A	B	C	Y
0	0	0	1
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	0
1	1	1	1

AB				
	00	01	11	10
0	1	0	0	1
1	1	1	1	1

$$Y = \bar{B} + C$$

$$Y = \underbrace{\bar{A} \cdot B \cdot C}_{0-1 \cdot 1} + \underbrace{\overline{B \cdot \bar{C}}}_{0-1} + \underbrace{B \cdot C}_{1-1}$$

A	B	C	Y
x	0	x	1
x	x	1	1

3

A	B	C	D	Y
0	0	0	0	0 ✓
0	0	0	1	1
0	0	1	0	0 ✓
0	0	1	1	0 ✓
0	1	0	0	1
0	1	0	1	1
0	1	1	0	1
0	1	1	1	1

CD \ AB	00	01	11	10
00	0	1	1	0
01	1	1	1	1
11	0	1	1	1
10	0	1	1	0

1	0	0	0	0 ✓
1	0	0	1	1
1	0	1	0	0 ✓
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

$$Y = B + \bar{C}D + AD$$

$$Y = \underbrace{(A+B+C)}_{0+0+0} \cdot D + A \cdot D + B$$

$$0+0+0 = 1 + 1 \cdot 1 + 1$$

A	B	C	D	Y
x	1	x	x	1
x	x	0	1	1
1	x	x	1	1

4.

A	B	C	Y
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

	AB			
C	00	01	11	10
0	1	1	1	0
1	0	1	1	0

$$Y = \bar{A}\bar{C} + B$$

$$y = \underbrace{B \cdot C}_{1 \cdot 1} + \underbrace{\bar{A} \cdot \bar{B} \cdot \bar{C}}_{0 \cdot 0 \cdot 0} + \underbrace{B \cdot \bar{C}}_{1 \cdot 0}$$

A	B	C	Y
0	x	0	1
x	1	x	1

V

- Y Alarma y luces encendidas \rightarrow Salida 1 = encendido
 A sensor ventana/porta \rightarrow Entrada 1 = ok
 B sensor de movimiento \rightarrow Entrada 0 = no mov
 C Alarma armada \rightarrow Entrada 1 = armado

A	B	C	Y
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

SOP =

$$Y = \bar{A}\bar{B}C + \bar{A}BC + ABC$$

POS =

$$Y = (A+B+\bar{C}) \cdot (A+\bar{B}+C) \cdot (\bar{A}+B+C) \cdot (\bar{A}+B+\bar{C}) \cdot (\bar{A}+\bar{B}+C)$$

c \ AB	00	01	11	10
0	0	0	0	0
1	1	1	1	0

$$Y = \bar{A}C + BC$$