$$O(k) \hookrightarrow \operatorname{St}(k, \mathbb{R}^n)$$

$$\downarrow$$

$$\operatorname{Gr}(k, \mathbb{R}^n)$$