

$$\begin{array}{ccc}
 U(k) & \hookrightarrow & \text{St}(k, \mathbb{C}^n) \\
 & & \downarrow \\
 & & \text{Gr}(k, \mathbb{C}^n)
 \end{array}$$