

# Cluster Analysis: Identifying Parkinson's Disease Subtypes

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## 1 Preprocessing

### 1.1 Dataset Description

951 subjects, 145 metrics, collected 15-4-2012. From Pablo Martinez Martín. 170 subjects with missing values (brought down to 781); these were removed automatically, even if the missing values were not included in the selected features below. This will need to be changed later on, by keeping those removed that still have all selected features and perhaps with some compensation for missing values.

### 1.2 Selected Features

Combination of non-motor scale (NMS) symptoms and standard motor symptoms.

Name	Type	Format	Description
nms_d1	byte	%8.0g	cardiovascular
nms_d2	byte	%8.0g	sleep/fatigue
nms_d3	byte	%8.0g	mood/cognition
nms_d4	byte	%8.0g	percep/hallucinations
nms_d5	byte	%8.0g	attention/memory
nms_d6	byte	%8.0g	gastrointestinal
nms_d7	byte	%8.0g	urinary
nms_d8	byte	%8.0g	sexual function
nms_d9	byte	%8.0g	miscellaneous
tremor	float	%9.0g	tremor
bradykin	float	%9.0g	bradykinesia <sup>1</sup>
rigidity	float	%9.0g	rigidity
axial	float	%9.0g	axial <sup>2</sup>
pigd	float	%9.0g	postural instability and gait difficulty

Table 1: Selected Features and Details

Name	$\mu$	$\sigma$	min-max
nms_d1	1.76	3.32	0-24
nms_d2	8.71	8.76	0-48
nms_d3	8.70	11.83	0-60
nms_d4	1.65	3.94	0-33
nms_d5	5.22	7.44	0-36
nms_d6	5.67	6.92	0-36
nms_d7	8.02	9.09	0-36
nms_d8	3.57	5.97	0-24
nms_d9	6.99	7.74	0-48
tremor	2.59	2.63	0-12
bradykin	2.49	1.39	0-6
rigidity	2.34	1.36	0-6
axial	3.28	2.75	0-12
pigd	3.36	2.77	0-12

Table 2: Descriptive Statistics

### 1.3 Dimensionality Reduction: PCA

May not be useful? If we're trying to identify *clinically* relevant features, merging them may not be a good idea.

Figure 1 shows scree test elbow occurs around 2 or 3. Also, eigenvalues 1 and 2  $> 1$ , while 3 is around .9

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<sup>1</sup>Impaired ability to adjust the body's position.

<sup>2</sup>Issues affecting the middle of the body.

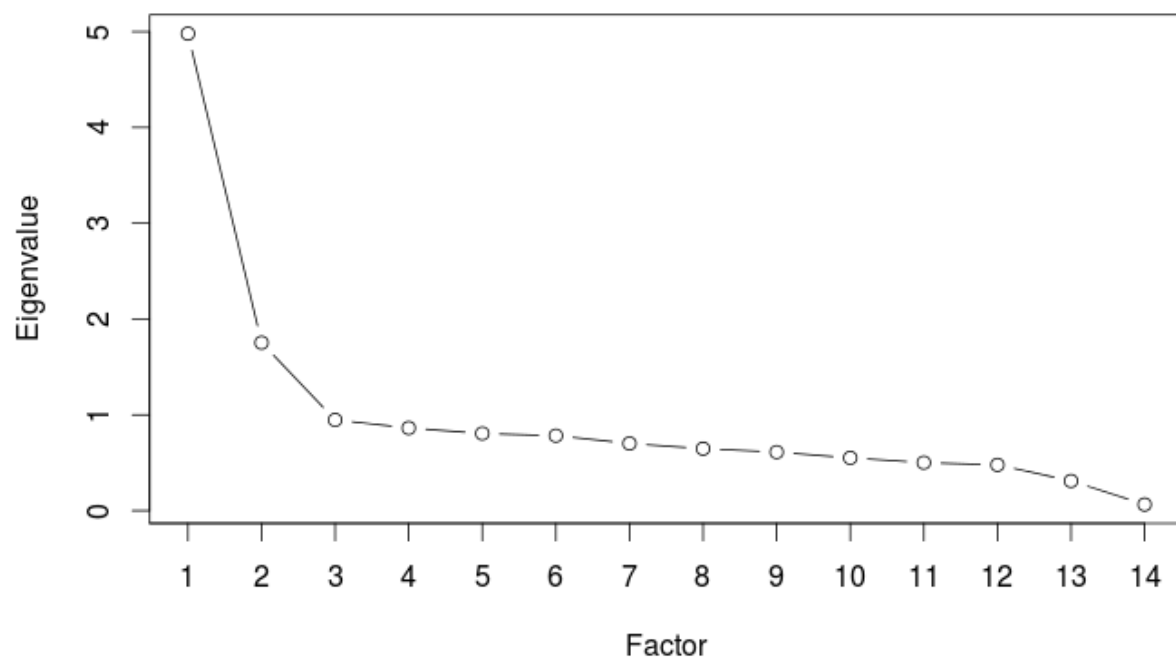


Figure 1: Scree test: eigenvalues by factor

## 2 $k$ -means

### 2.1 Identifying optimal number of clusters

#### 2.1.1 WSS Error Scree Test

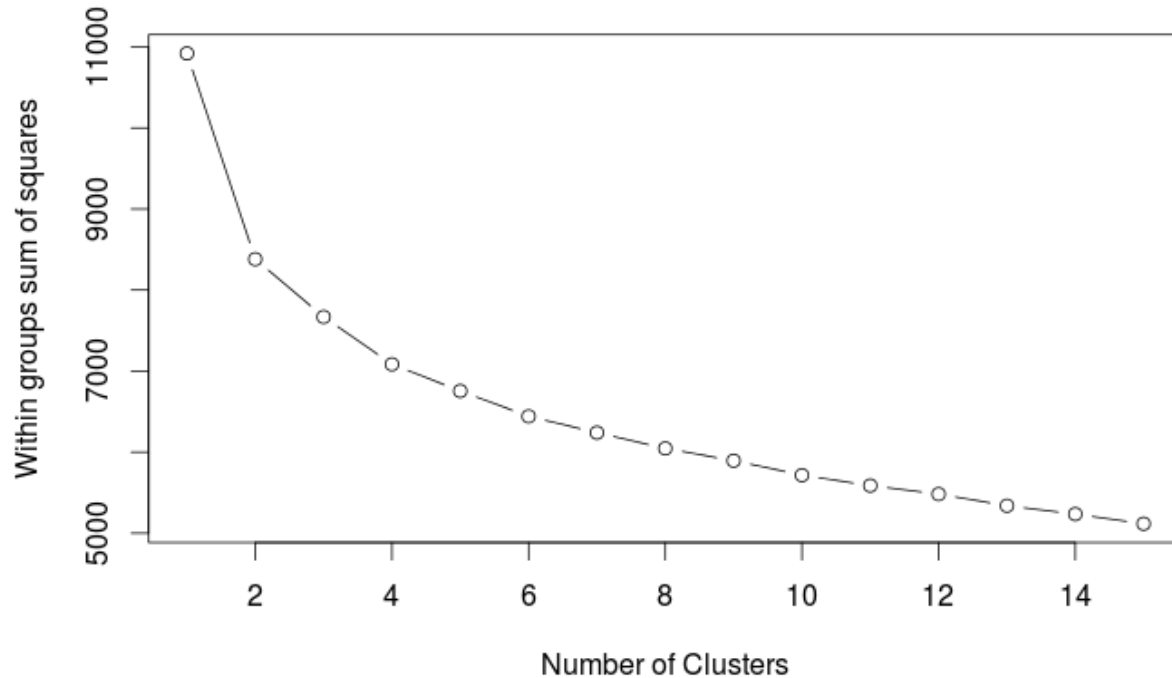


Figure 2: Scree test: WSS error by cluster size

Figure 2 shows no optimal elbow in scree test! Maybe 2-3?

#### 2.1.2 Gap Statistic

Optimal cluster is the local maximum of the gap statistic, but it appears to be consistently increasing in Figure 3.

#### 2.1.3 Average Silhouette Width

Figure 4 shows average silhouette width as being consistently under 0.25 for all clusters, implying the data is not well structured.

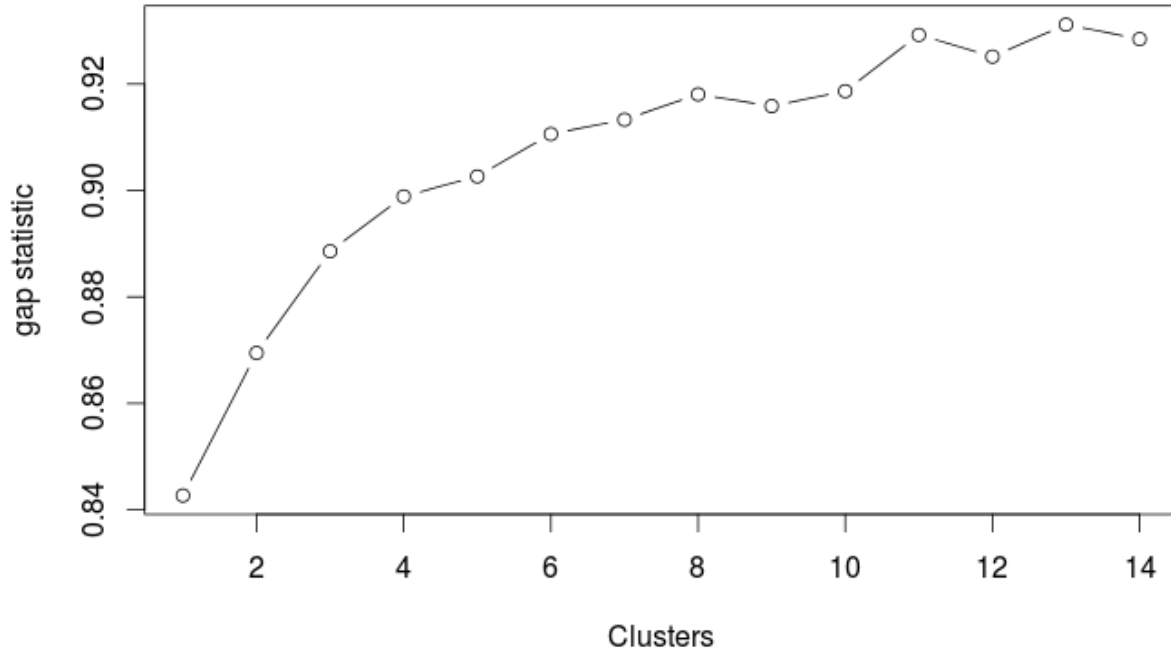


Figure 3: Gap statistic by cluster size

$k$	$n$	Within SS	sum(Within SS)
2	201/580	4248.585/4132.434	8381.019
3	420/231/130	2618.368/1973.82/3076.542	7668.73
4	61/372/145/203	1481.25/1845.389/2147.988/1609.555	7084.183

Table 3: Cluster statistics

## 2.2 Cluster statistics

## 2.3 Silhouette plots

Available in Figures 5, 6, and 7. Note: constructed with standardized  $z$ -score data.

## 2.4 Decision trees based on clusters

## 2.5 Interpretation of Clusters

### 2.5.1 Cluster summaries

Available in Figures 11, 12, and 13. Error bar is standard error.

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<sup>3</sup>Complexity Parameter

<sup>4</sup>10-fold cross validation

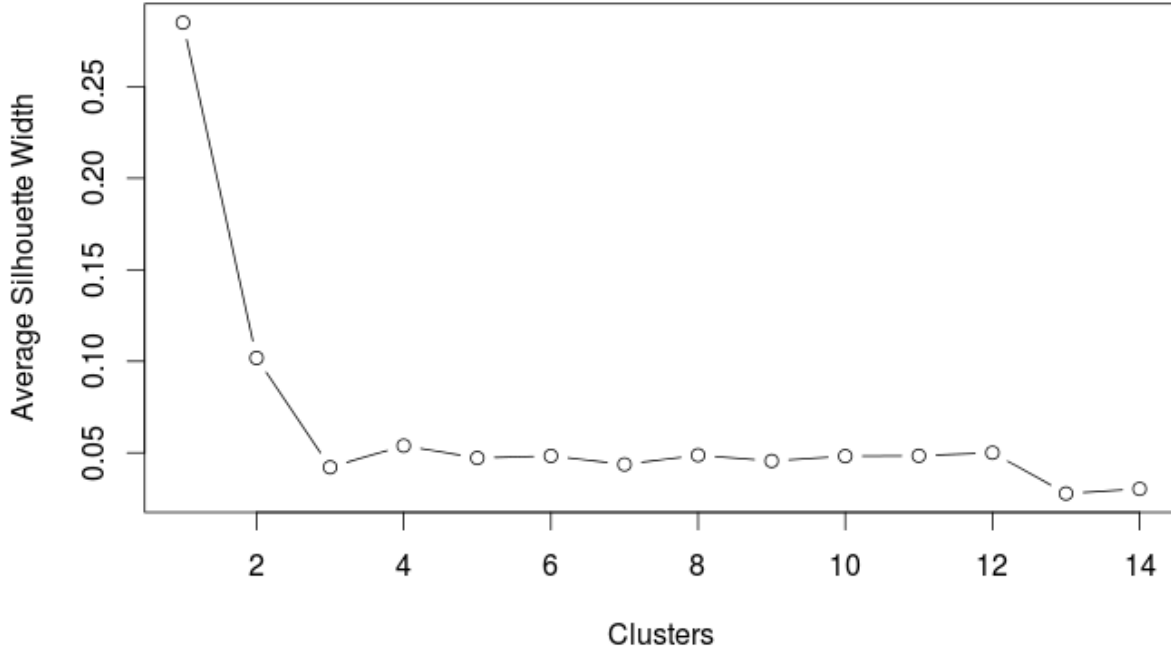


Figure 4: Average silhouette width by cluster size

$k$	CP <sup>3</sup>	CV Xerror <sup>4</sup>	Root Feature	Root Error	Figure
2	0.0348	0.134	axial $\geq 0.44$	0.257	Figure 8
3	0.0100	0.194	bradykin $< 0.0041$	0.462	Figure 9
4	0.0100	0.248	bradykin $< 0.0041$	0.523	Figure 10

Table 4:  $k$ -kmeans decision trees statistics

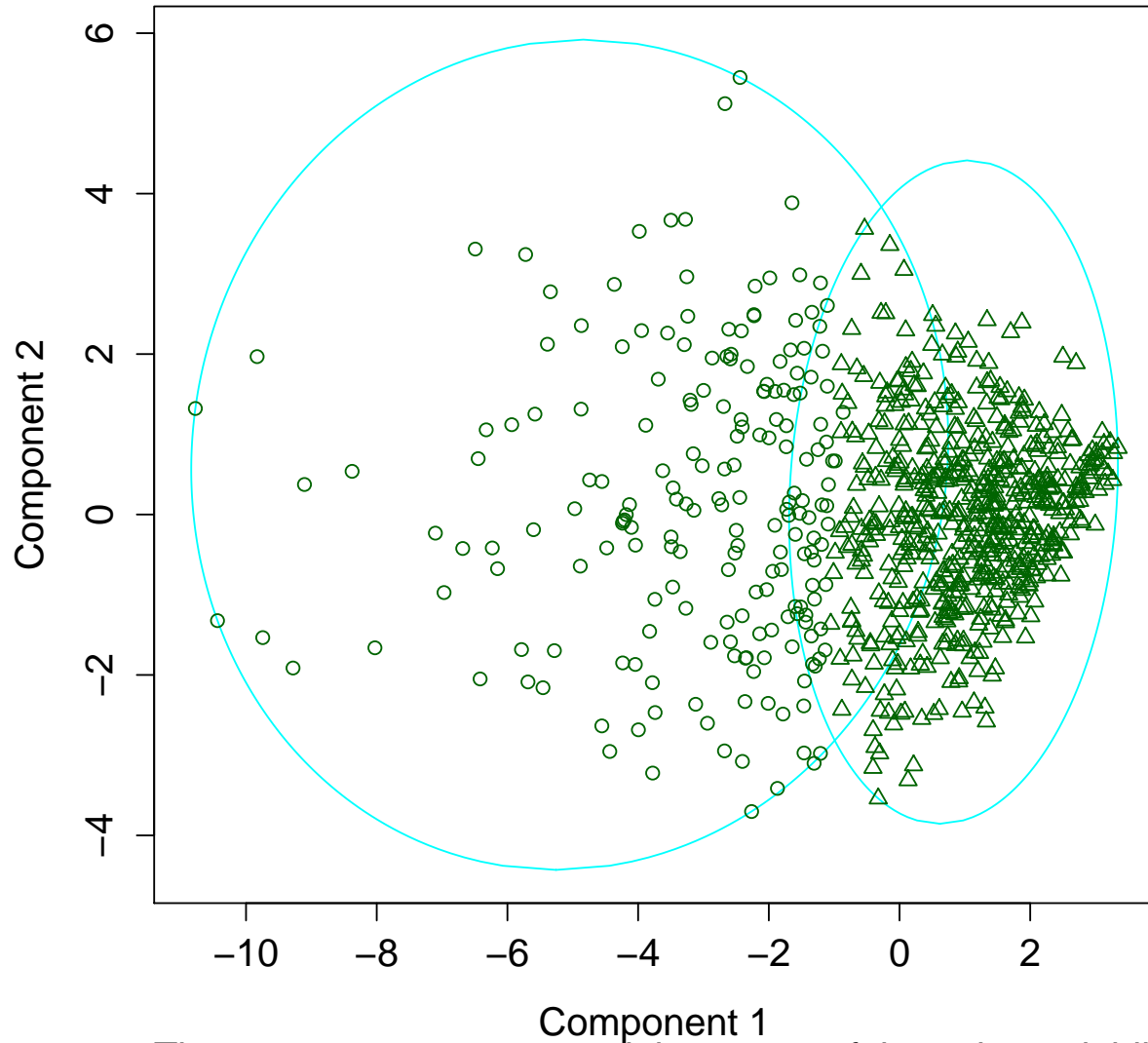
### 2.5.2 Interpretation

$k = 2$  seems too basic. Cluster is organized solely by severity - all symptoms, including motor and nonmotor, are higher in severity in cluster 1, and lower in cluster 2. Quite consistently, groups in cluster 1 are generally of slightly higher age and pd duration.

$k = 3$  seems like a further development of  $k = 2$ , where clusters are simply organized by linearly increasing severity.

$k = 4$  is where it gets interesting.

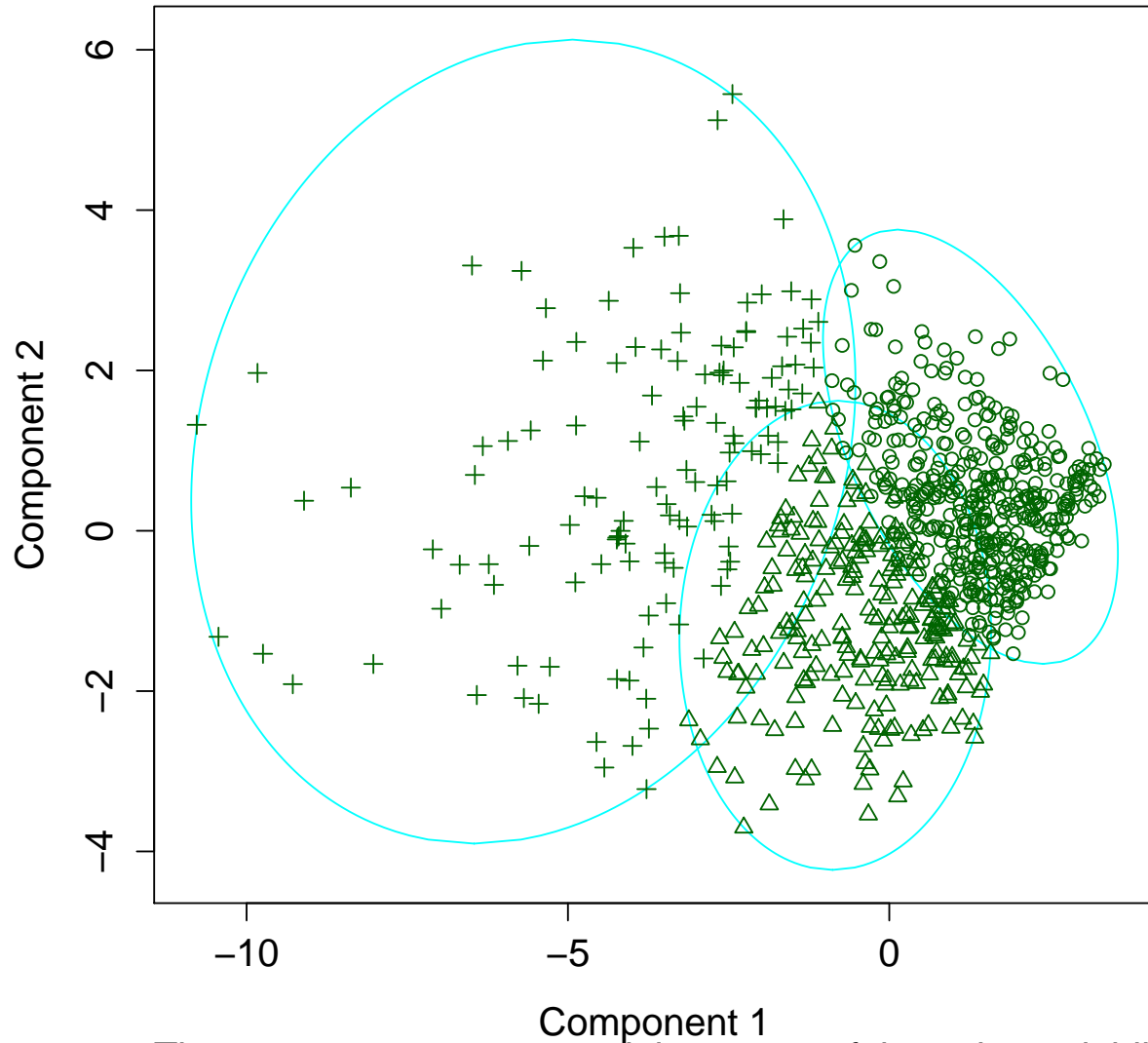
## Silhouette plot $k = 4$



Component 1  
These two components explain 48.1 % of the point variability.

Figure 5:  $k$ -means cluster silhouette plot,  $k = 2$

### Silhouette plot $k = 4$

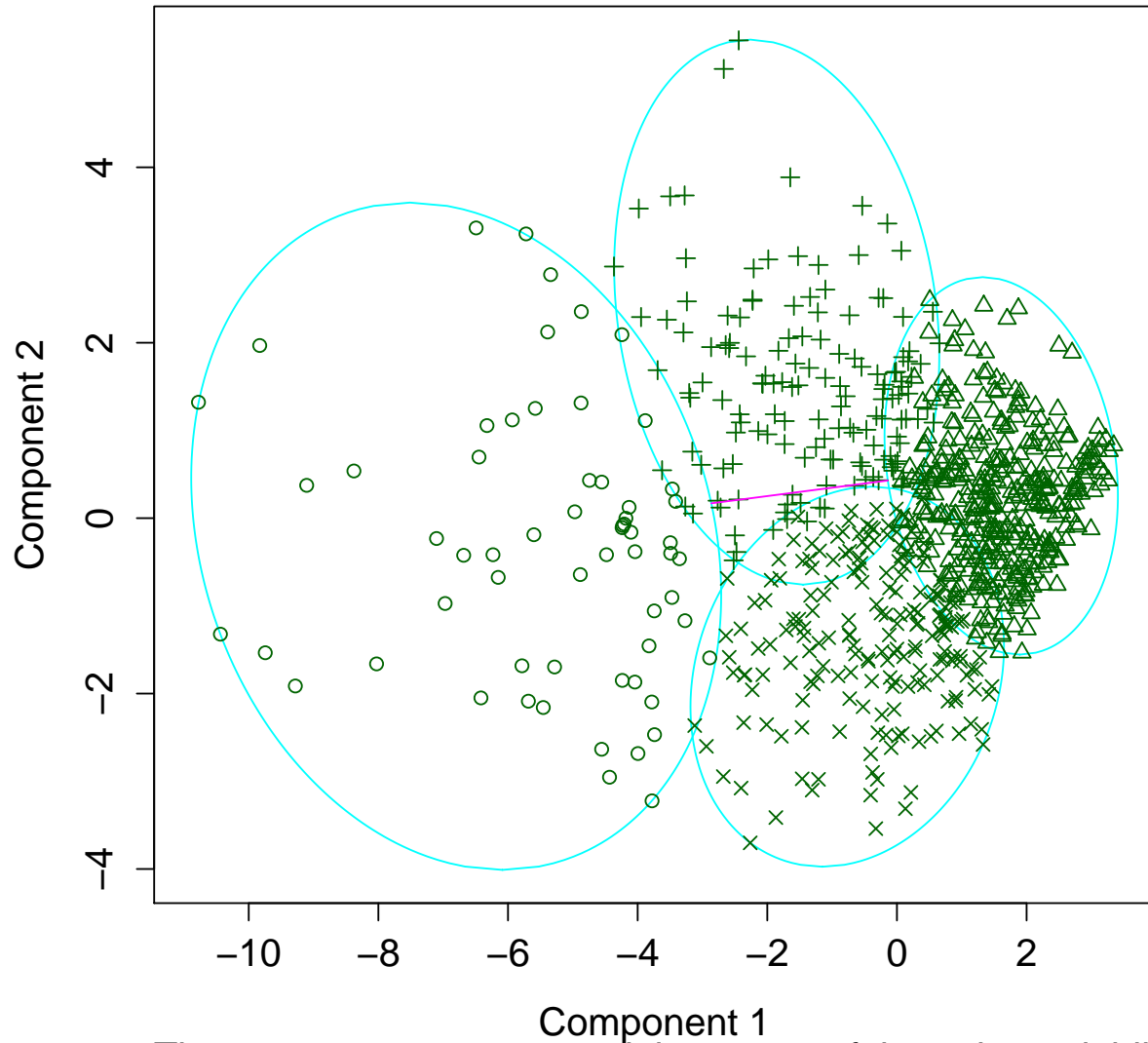


Component 1  
These two components explain 48.1 % of the point variability.

Figure 6:  $k$ -means cluster silhouette plot,  $k = 3$



## Silhouette plot $k = 4$



Component 1  
These two components explain 48.1 % of the point variability.

Figure 7:  $k$ -means cluster silhouette plot,  $k = 4$

## UNSCALED Pruned Tree, 2 clusters

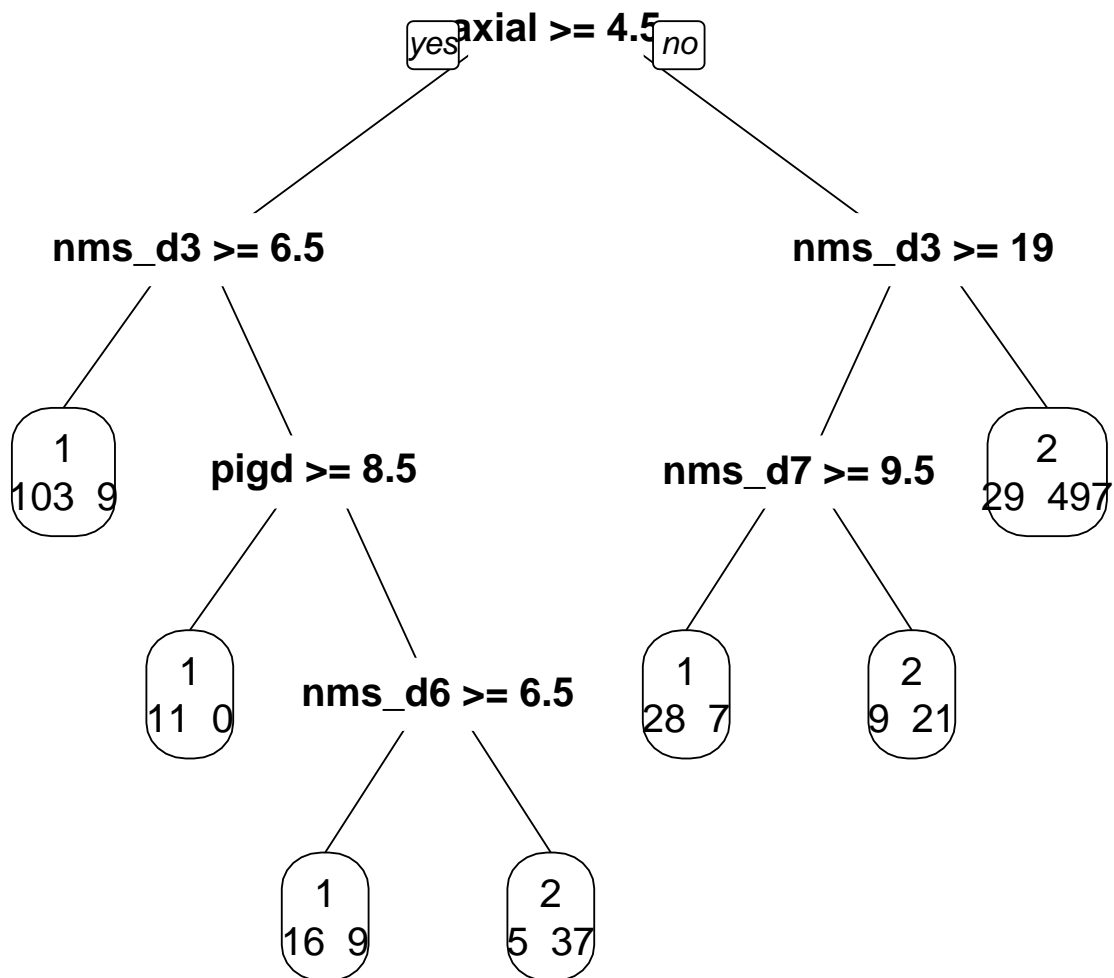


Figure 8: Decision Tree from  $k$ -means clustering, 2 clusters

## UNSCALED Pruned Tree, 3 clusters

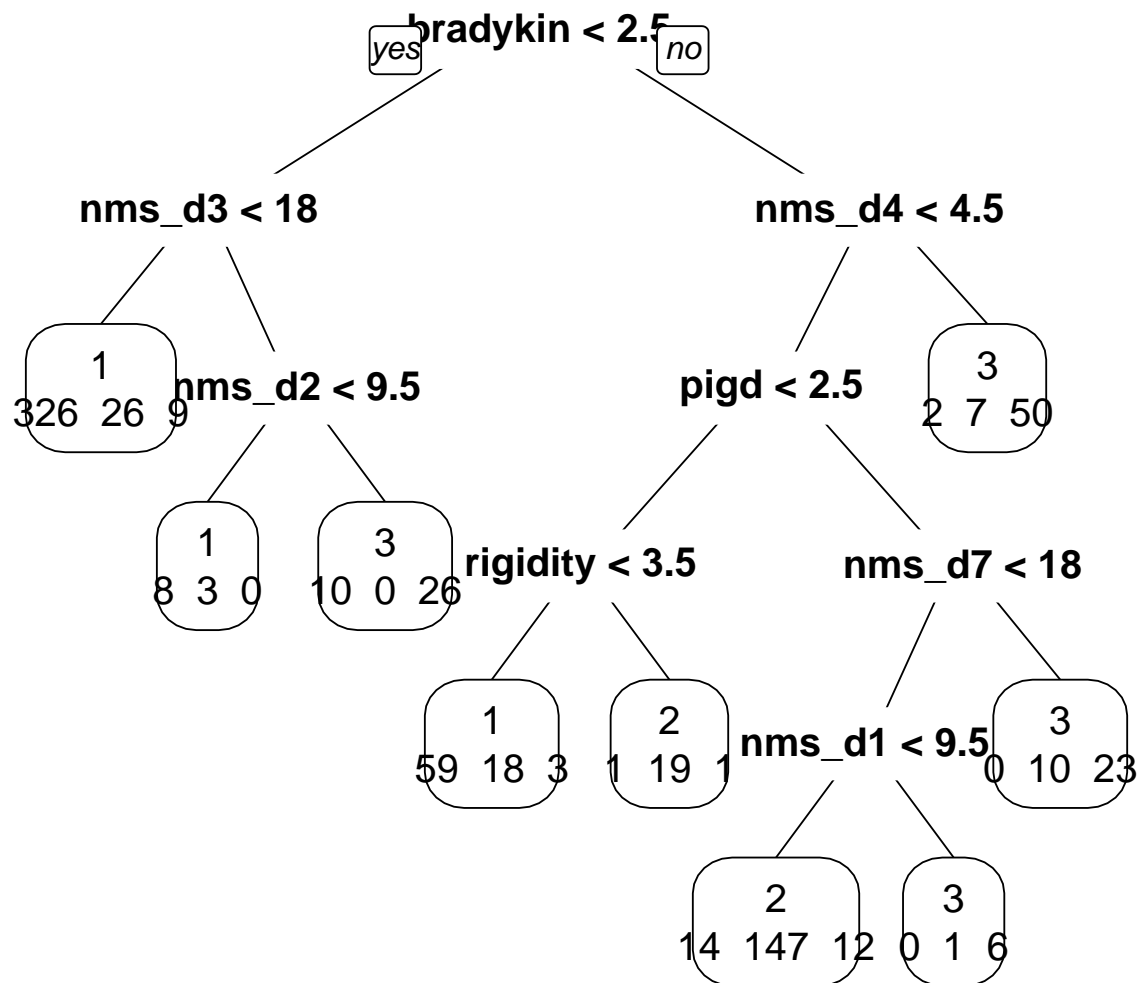


Figure 9: Decision Tree from  $k$ -means clustering, 3 clusters

## UNSCALED Pruned Tree, 4 clusters

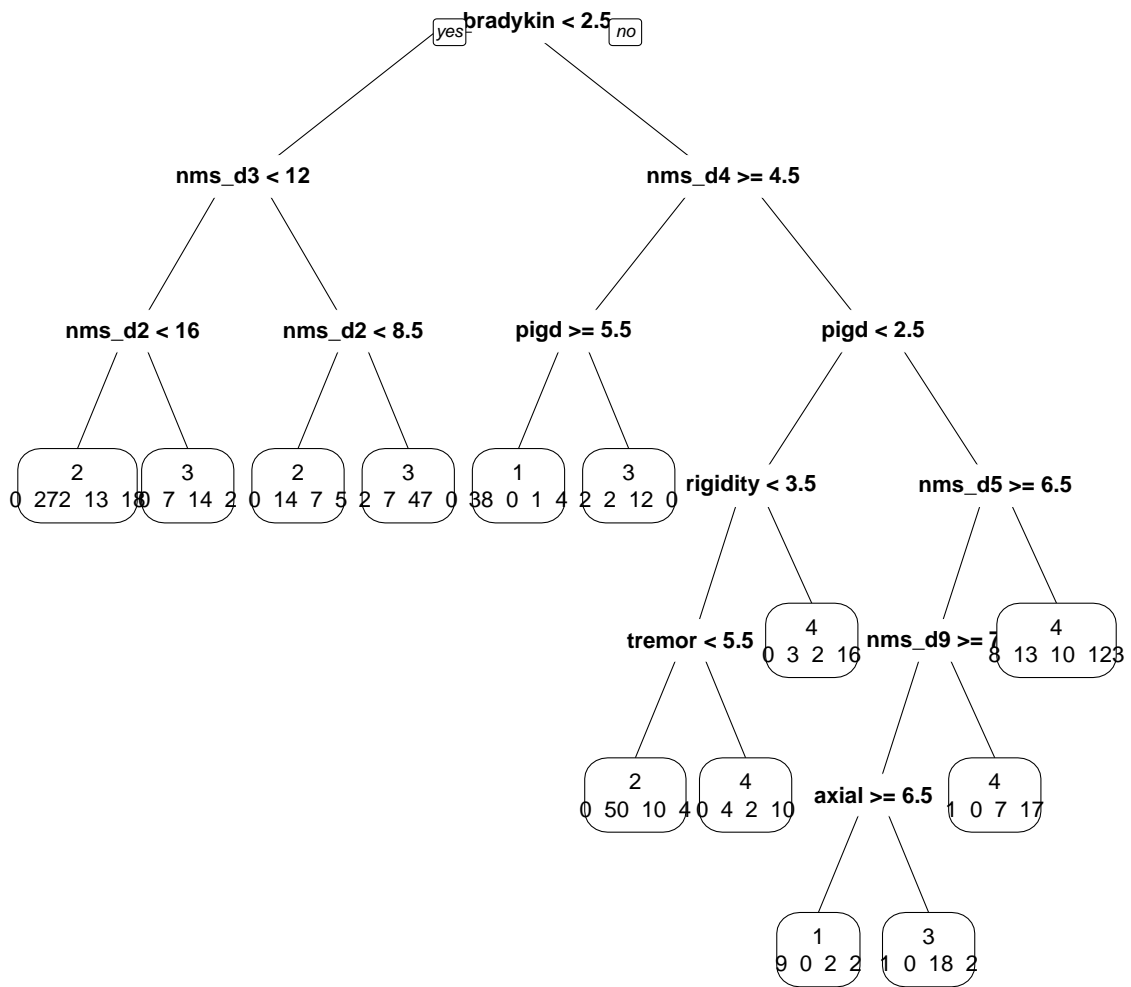


Figure 10: Decision Tree from  $k$ -means clustering, 4 clusters

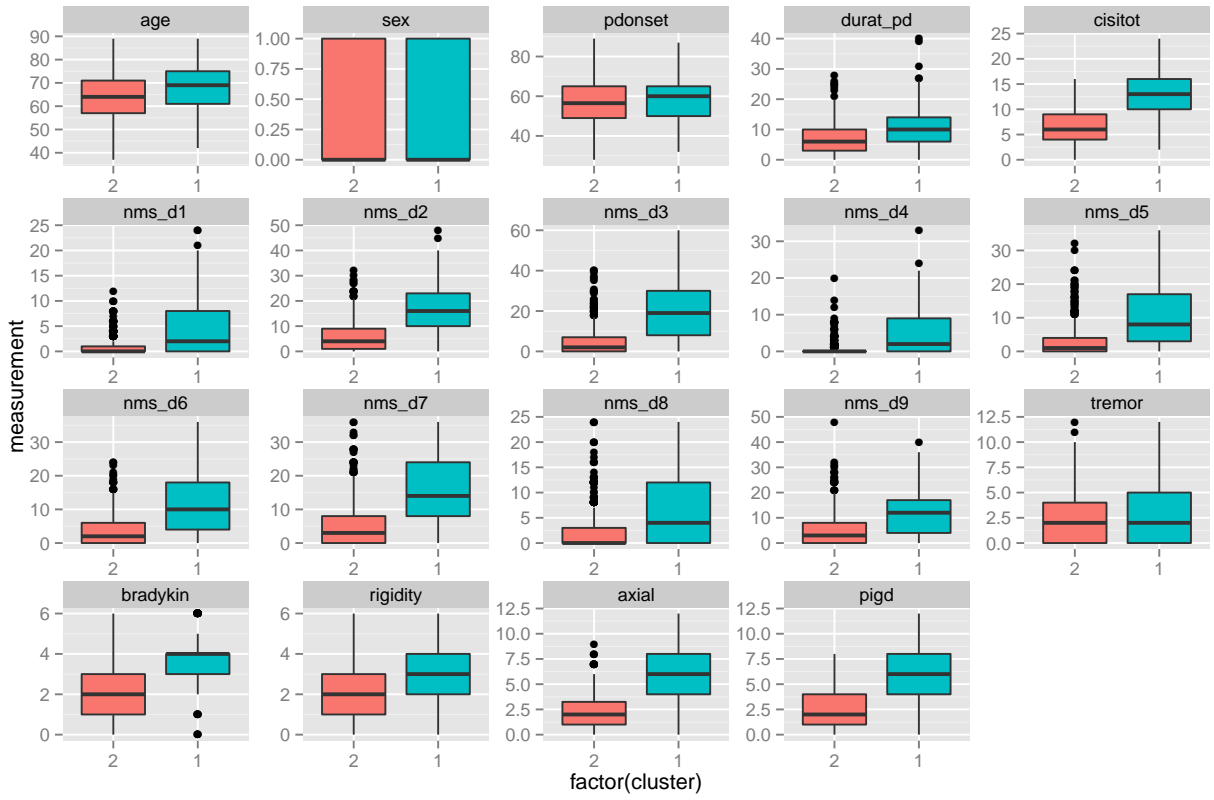


Figure 11: Cluster Summaries,  $k = 2$

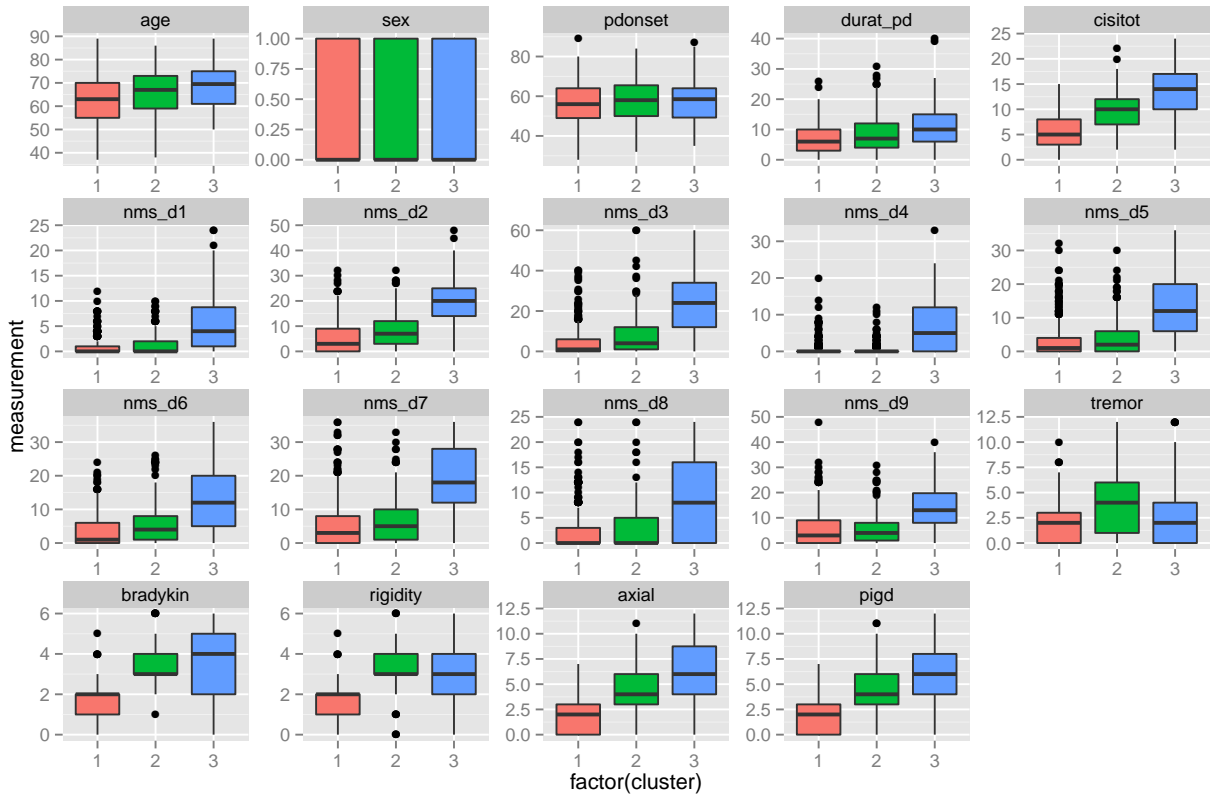


Figure 12: Cluster Summaries,  $k = 3$

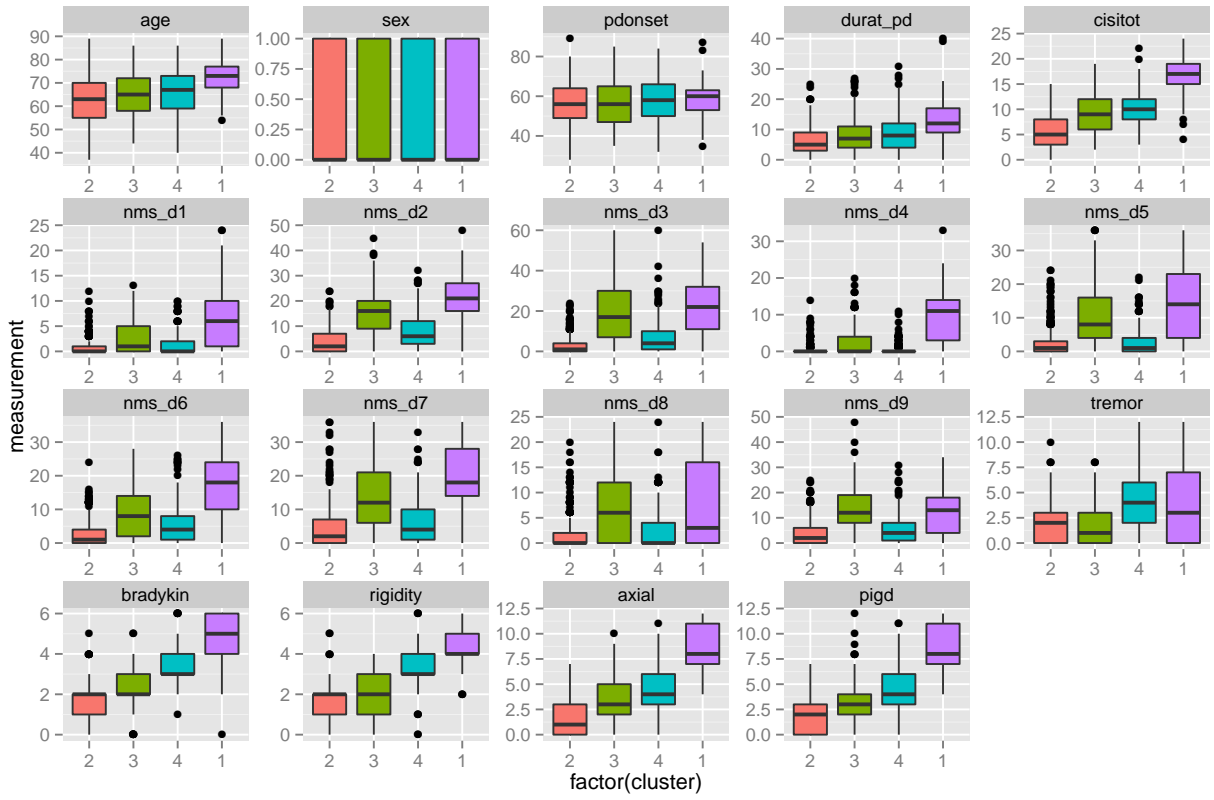


Figure 13: Cluster Summaries,  $k = 4$

## 3 Affinity Propagation

### 3.1 Clustering

Package `apcluster` was used. Distance matrix was the negative euclidean squared distance ( $r = 2$ ).

AP with input preferences minimized ( $q = 0$ ) resulted in 8 clusters. With the standard median input preferences ( $q = 0.5$ ), algorithm failed to converge with default parameters. Even setting damping factor to 0.98, maximum iterations to 10000, and convergence iterations to 1000 failed to converge. Might need to try a longer run.

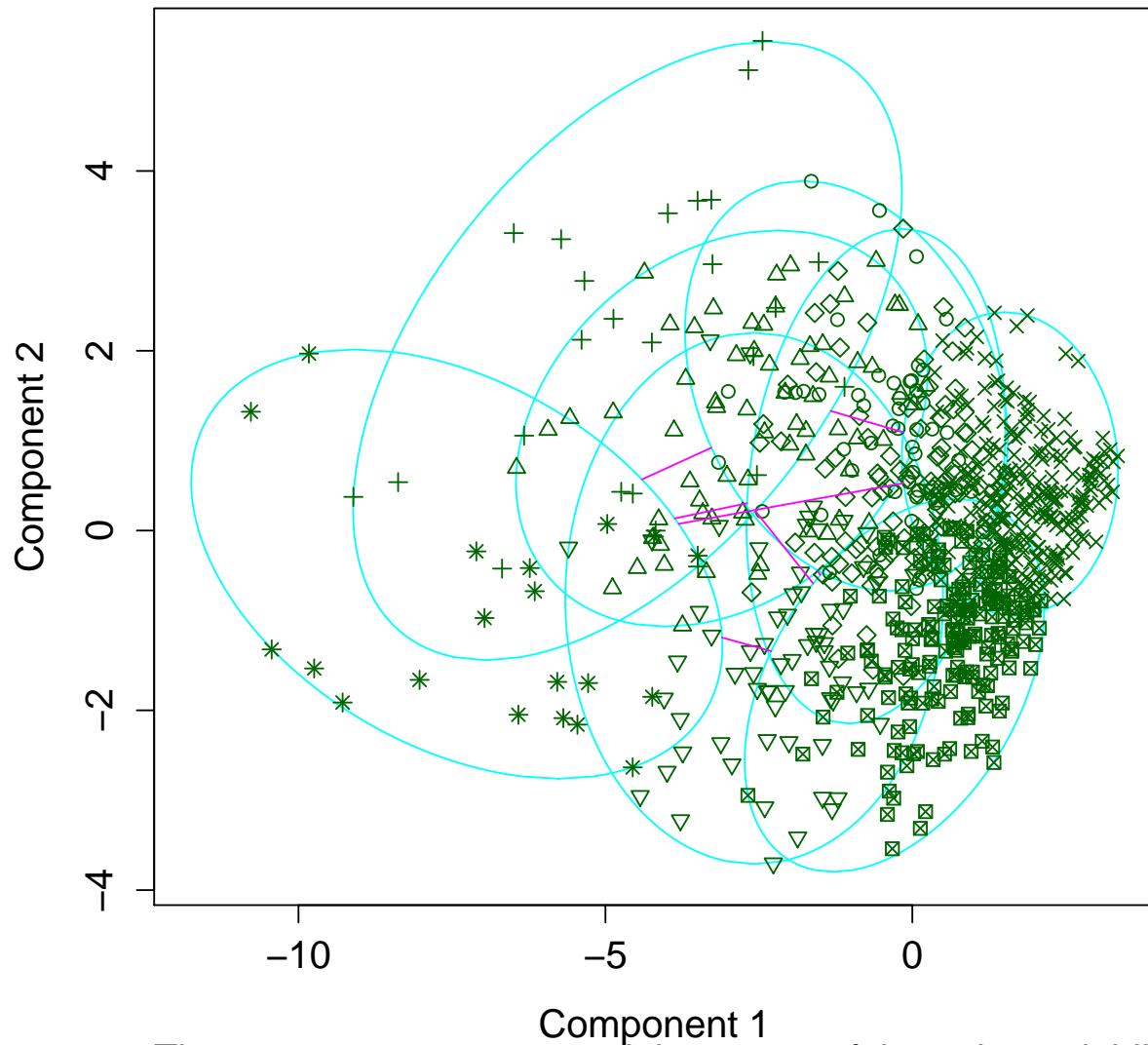
*However*, given that input preferences control how many clusters are found, I don't think it's very useful to have some dozen clusters running around.

#### 3.1.1 Silhouette Plots

Silhouette plot in Figure 14 looks pretty weak, really. Tons of overlap between the clusters.



## AP Silhouette Plot $k = 8$



These two components explain 48.1 % of the point variability.

Figure 14: AP silhouette plot,  $k = 8$

## 4 Hierarchical Clustering

### 4.1 Clustering

Four dissimilarity methods were used with a euclidean distance matrix. Dendrograms available in Figure 15

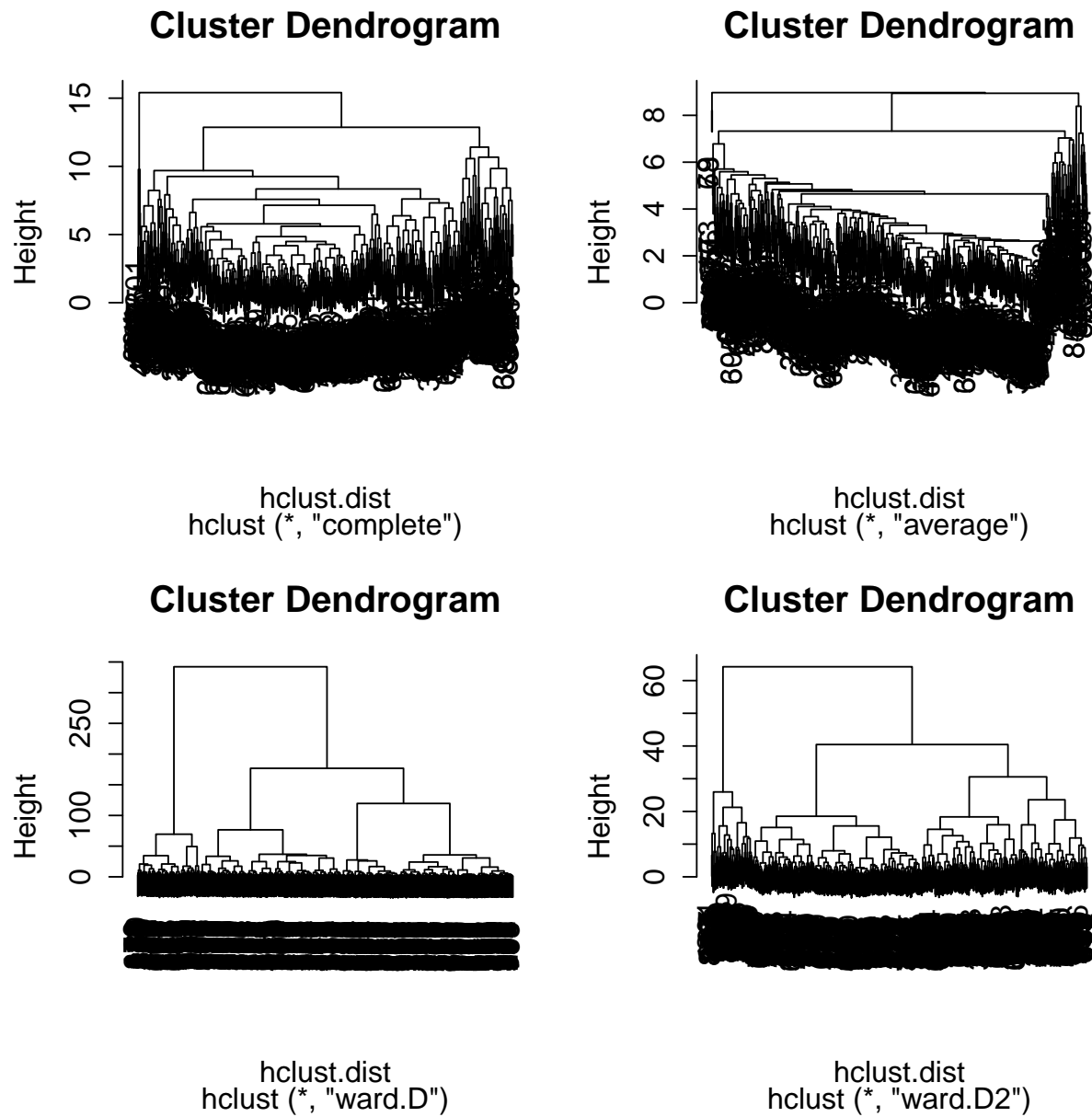


Figure 15: Dendrograms

Method	Condition	n	Figure
Complete	$k = 4$	4 (665/74/35/7)	16
Complete	<code>dynamicTreeCut</code> <sup>5</sup>	11 (7/270/138/83/79/49/46/39/35/35)	17
Ward	$k = 4$	4 (294/236/120/131)	18
Ward	$h = 60$	6 (97/236/120/197/91/40)	19

Table 5: Clusters from Tree Cutting

## 4.2 Cutting Trees

## 4.3 Interpretation

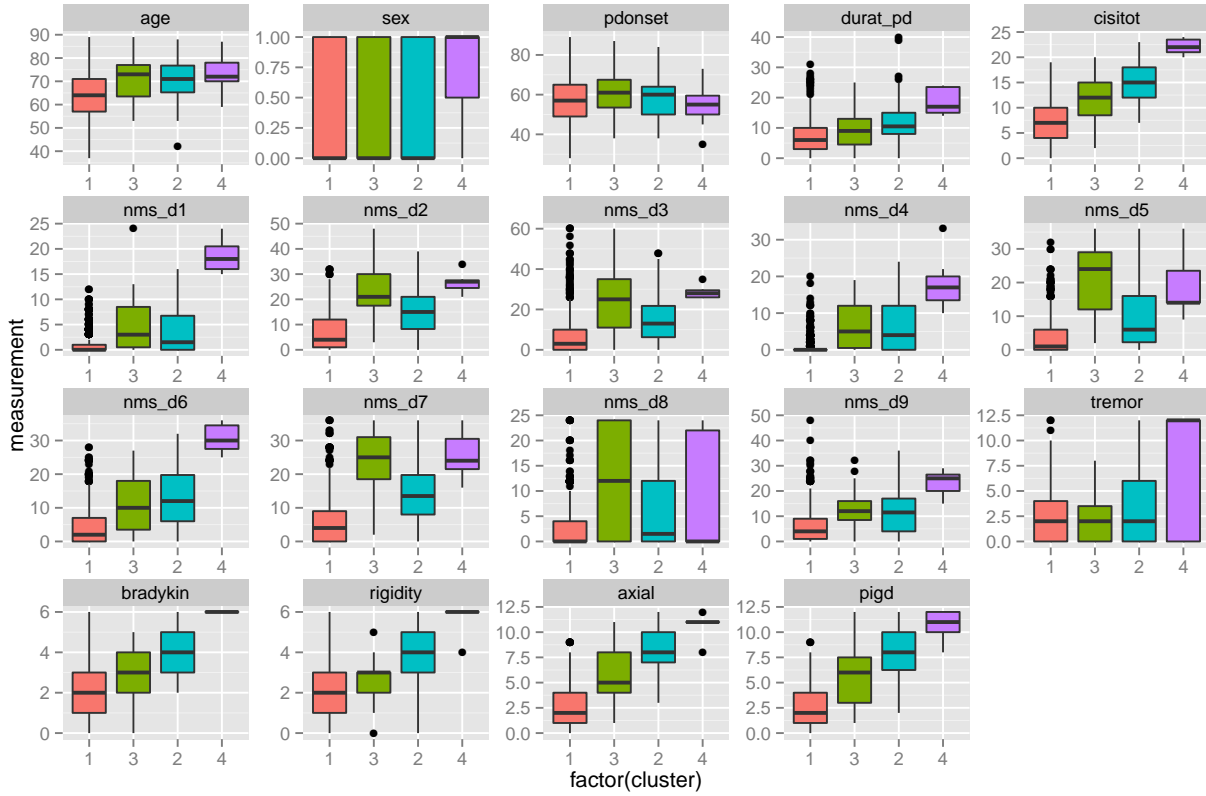


Figure 16: Using maximum (complete linkage) dissimilarity, cutting tree for  $k = 4$

## 4.4 Interpretation

Cluster sizes are available in Table 6

Boxplot summary of clusters available in Figure 20. **Discussion forthcoming.**

<sup>5</sup>Package `dynamicTreeCut` in R (Langfelder P, Zhang B, Horvath S (2007)). Hybrid method, minimum cluster selection parameters

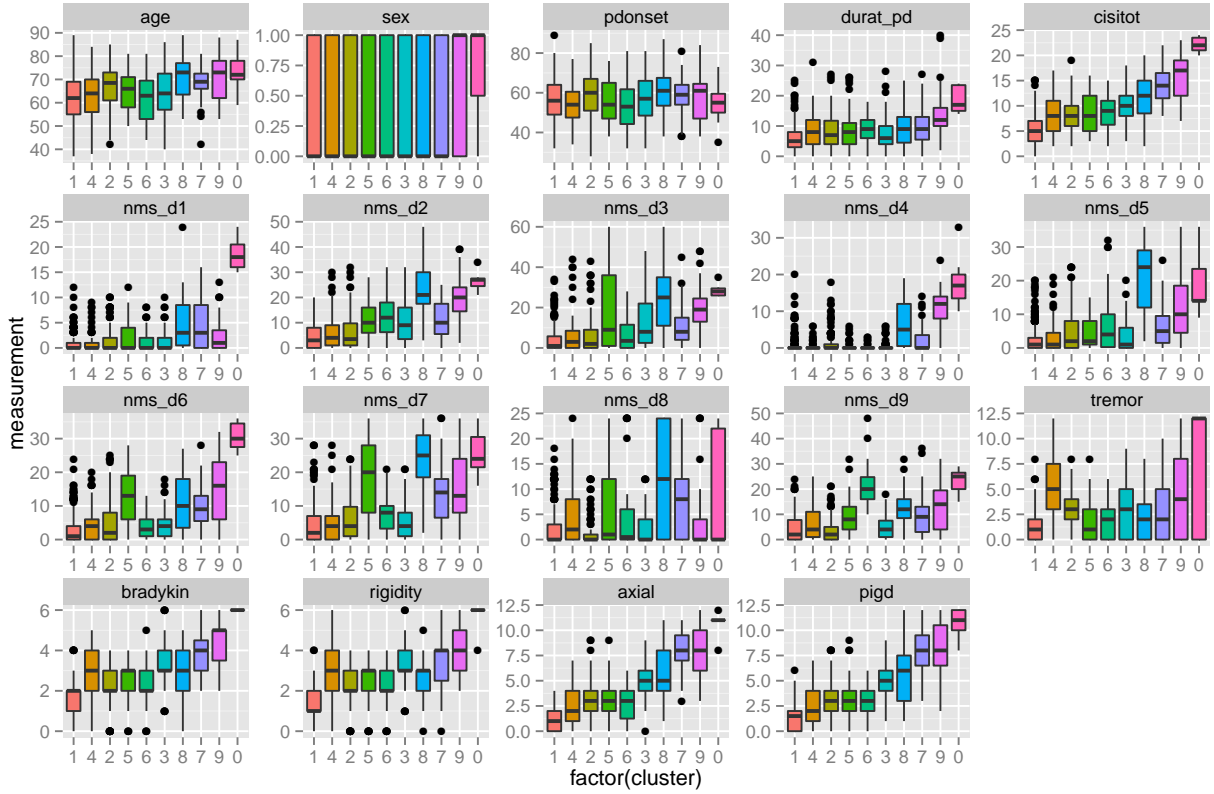


Figure 17: Using maximum (complete linkage) dissimilarity, cutting tree dynamically

## 5 Biclustering

Used BCBimax clustering algorithm. Clusters seem quite sparse.

## 6 Subspace clustering

## 7 Bayesian Networks

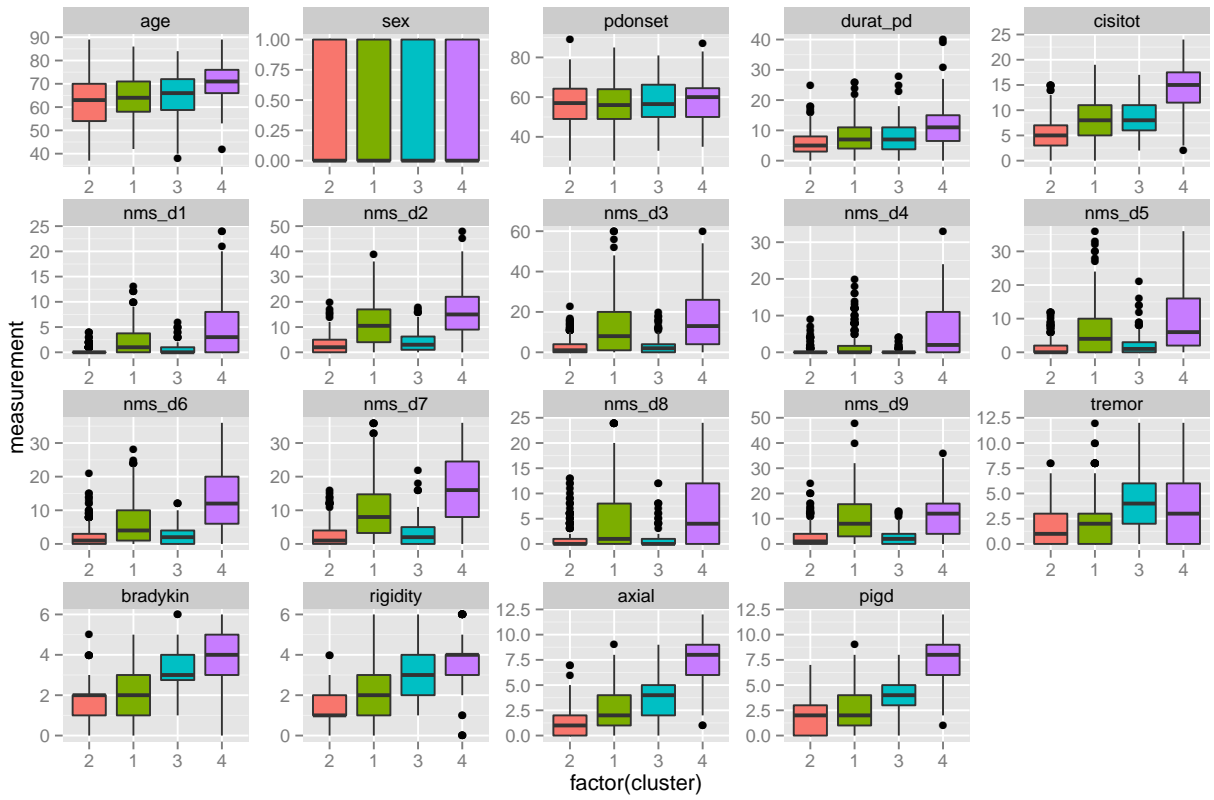


Figure 18: Using Ward (1963) dissimilarity, cutting tree for  $k = 4$

Cluster	Size
1	54
2	68
3	25
4	259
5	102
6	68
7	185
8	20

Table 6: AP Cluster Sizes

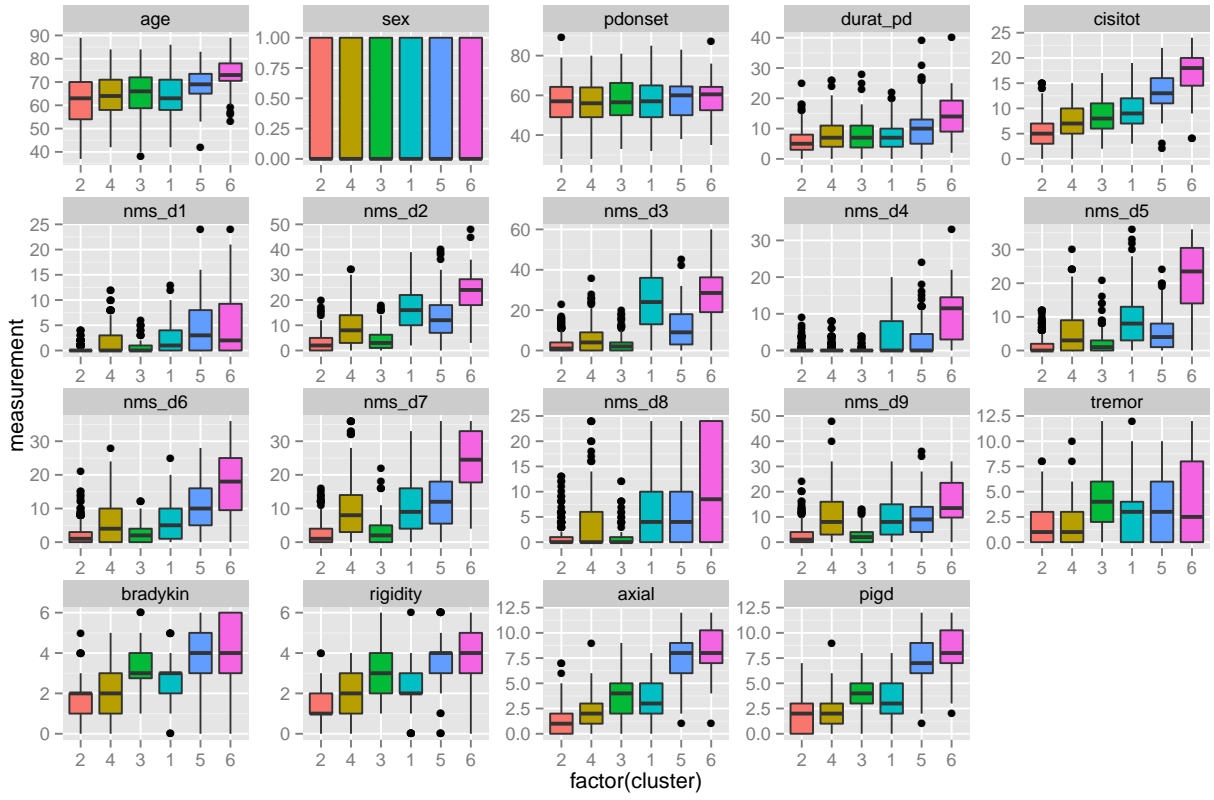


Figure 19: Using Ward (1963) dissimilarity, cutting tree at  $h = 60$

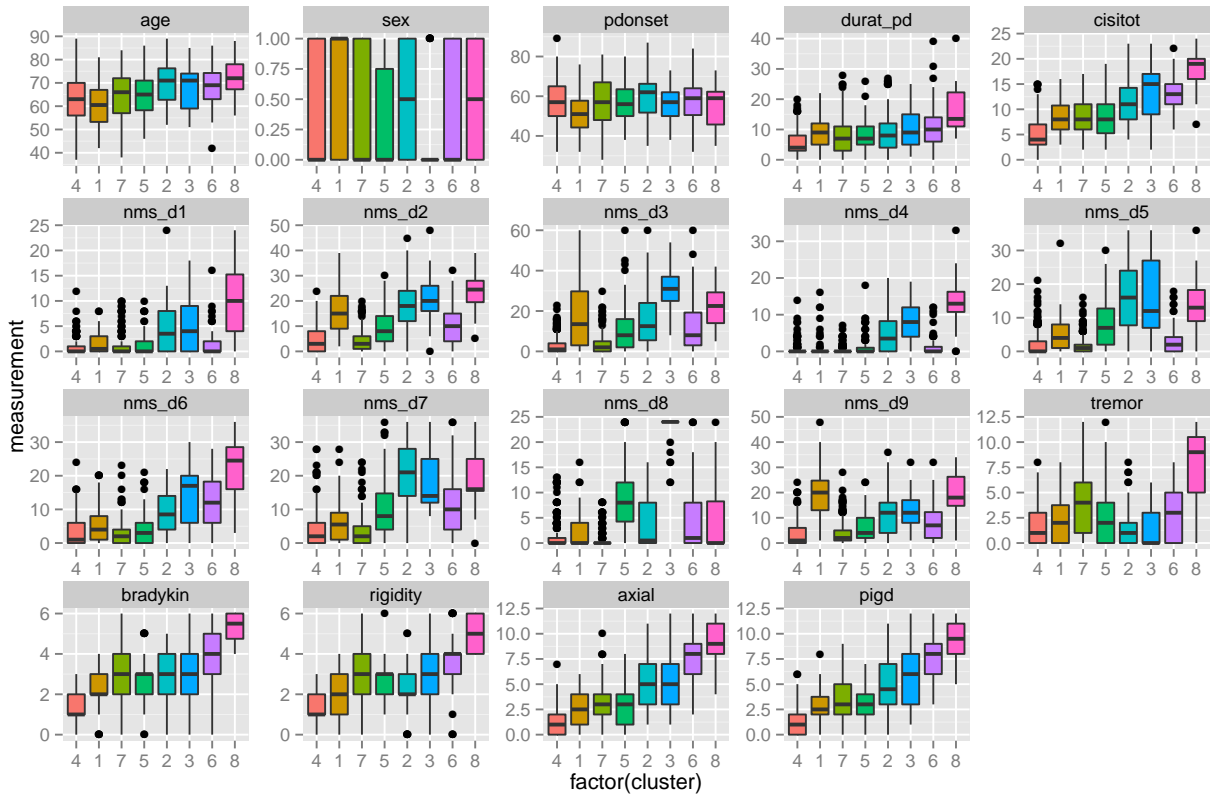


Figure 20: AP Boxplot Summaries

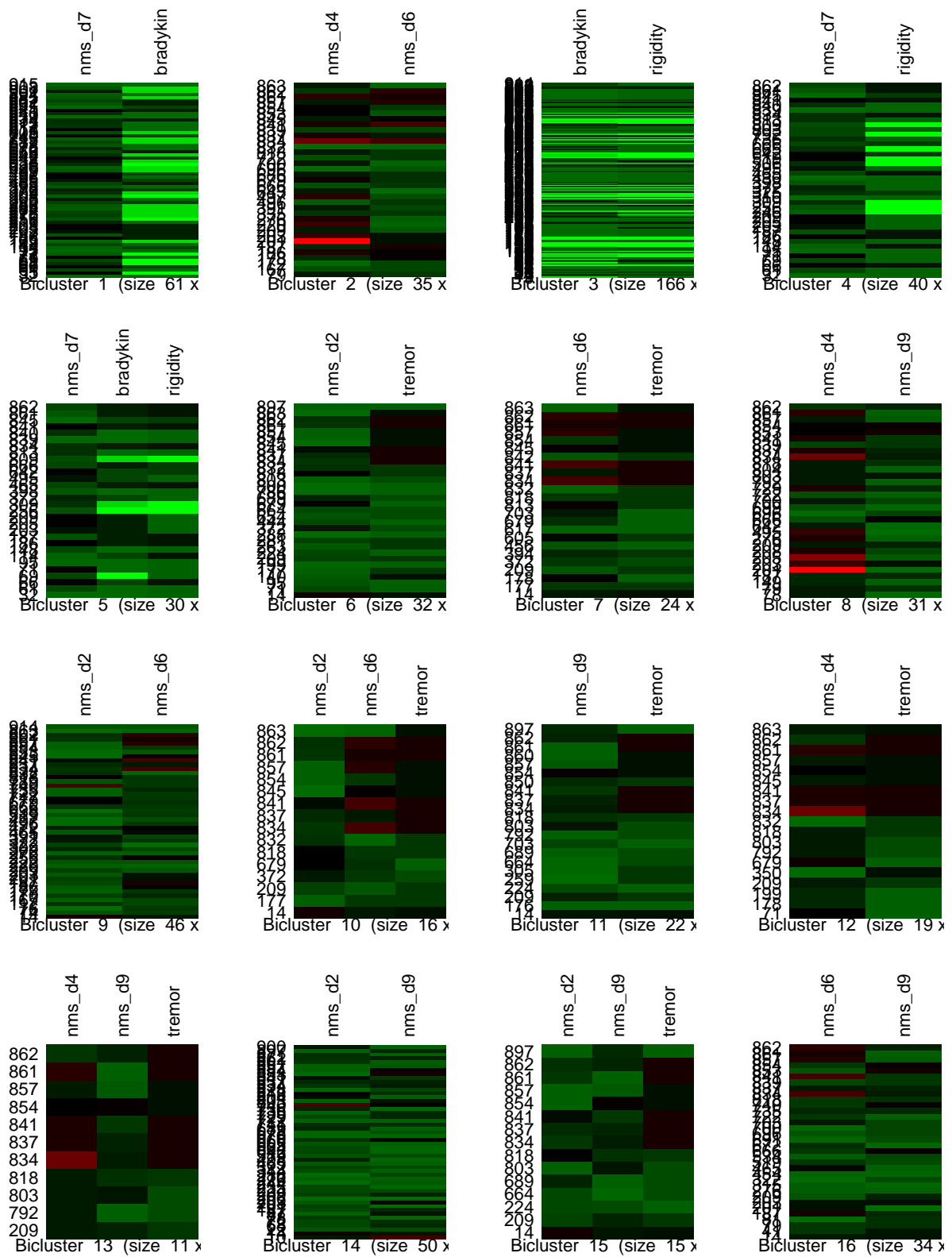


Figure 21: Biclustering  $N = 16$





Figure 22: Bubbleplot  $N = 16$