

Cluster Analysis: Identifying Parkinson's Disease Subtypes

Jesse Mu

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1 Preprocessing

1.1 Dataset Description

951 subjects, 145 metrics, collected 15-4-2012 from Pablo Martinez ín. Only 19 features used for clustering and/or interpretation. 50 subjects with missing values of the features to be used in clustering (brought down to 901). Imputation may be a good idea later on.

1.2 Selected Features

Combination of non-motor scale (NMS) symptoms and standard motor symptoms.

| Name | Type | Format | Description |
|----------|-------|--------|--|
| nms_d1 | byte | %8.0g | cardiovascular |
| nms_d2 | byte | %8.0g | sleep/fatigue |
| nms_d3 | byte | %8.0g | mood/cognition |
| nms_d4 | byte | %8.0g | percep/hallucinations |
| nms_d5 | byte | %8.0g | attention/memory |
| nms_d6 | byte | %8.0g | gastrointestinal |
| nms_d7 | byte | %8.0g | urinary |
| nms_d8 | byte | %8.0g | sexual function |
| nms_d9 | byte | %8.0g | miscellaneous |
| tremor | float | %9.0g | tremor |
| bradykin | float | %9.0g | bradykinesia ¹ |
| rigidity | float | %9.0g | rigidity |
| axial | float | %9.0g | axial ² |
| pigd | float | %9.0g | postural instability and gait difficulty |

Table 1: Selected Features and Details

¹Impaired ability to adjust the body's position.

²Issues affecting the middle of the body.

| Name | μ | σ | min-max |
|----------|-------|----------|---------|
| nms_d1 | 1.73 | 3.35 | 0-24 |
| nms_d2 | 8.75 | 8.70 | 0-48 |
| nms_d3 | 8.68 | 11.55 | 0-60 |
| nms_d4 | 1.64 | 3.86 | 0-33 |
| nms_d5 | 5.42 | 7.43 | 0-36 |
| nms_d6 | 5.53 | 6.79 | 0-36 |
| nms_d7 | 8.08 | 8.94 | 0-36 |
| nms_d8 | 3.52 | 5.97 | 0-24 |
| nms_d9 | 7.13 | 7.79 | 0-48 |
| tremor | 2.59 | 2.58 | 0-12 |
| bradykin | 2.40 | 1.41 | 0-6 |
| rigidity | 2.24 | 1.36 | 0-6 |
| axial | 3.25 | 2.68 | 0-12 |
| pigd | 3.31 | 2.71 | 0-12 |

Table 2: Descriptive Statistics

1.3 Dimensionality Reduction: PCA

May not be useful? If we're trying to identify *clinically* relevant features, merging them may not be a good idea. Regardless, Figure 1 shows results of preliminary PCA.

Figure 2 shows scree test elbow occurs around 2 or 2 or .4 Also, eigenvalues $1 - 5 > 1$.

Individuals factor map (PC1)

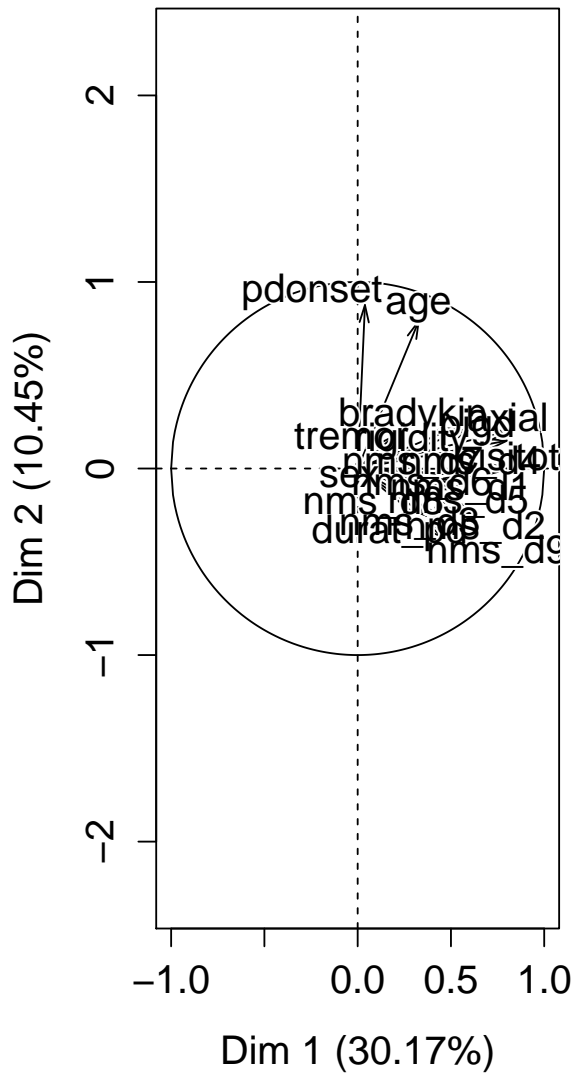
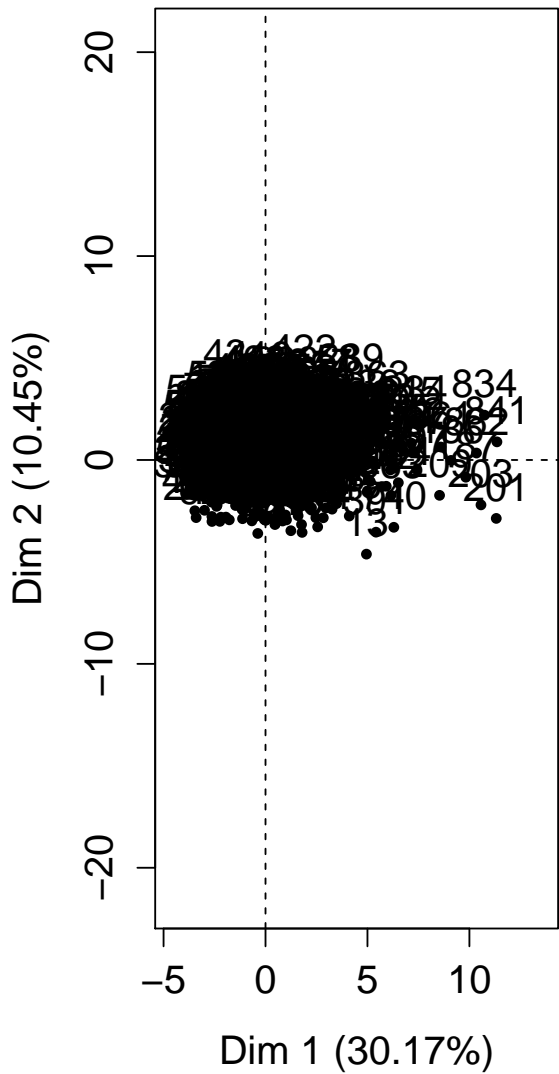


Figure 1: PCA Analysis

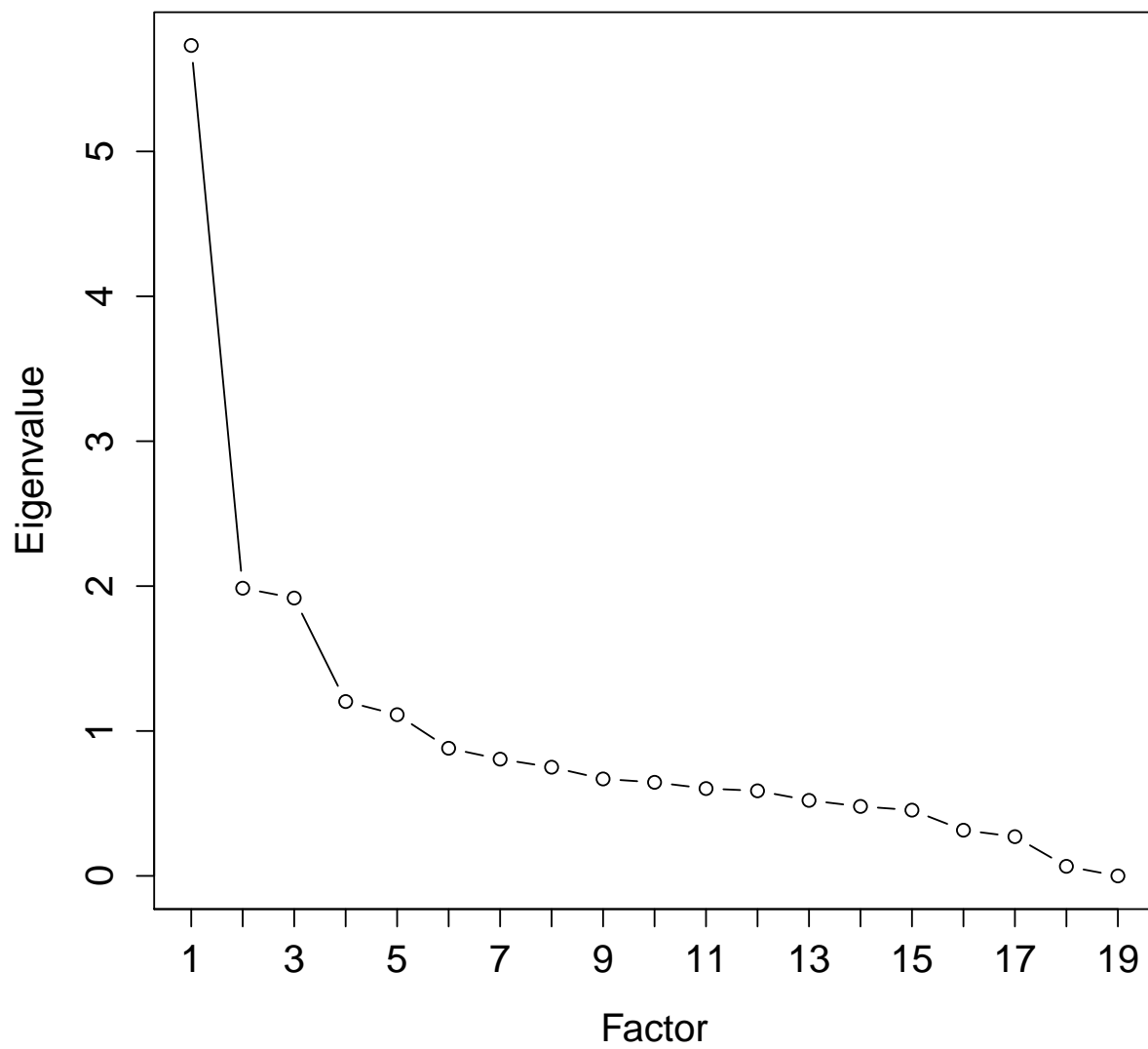


Figure 2: Scree test: eigenvalues by factor

2 k -means

2.1 Identifying optimal number of clusters

2.1.1 WSS Error Scree Test

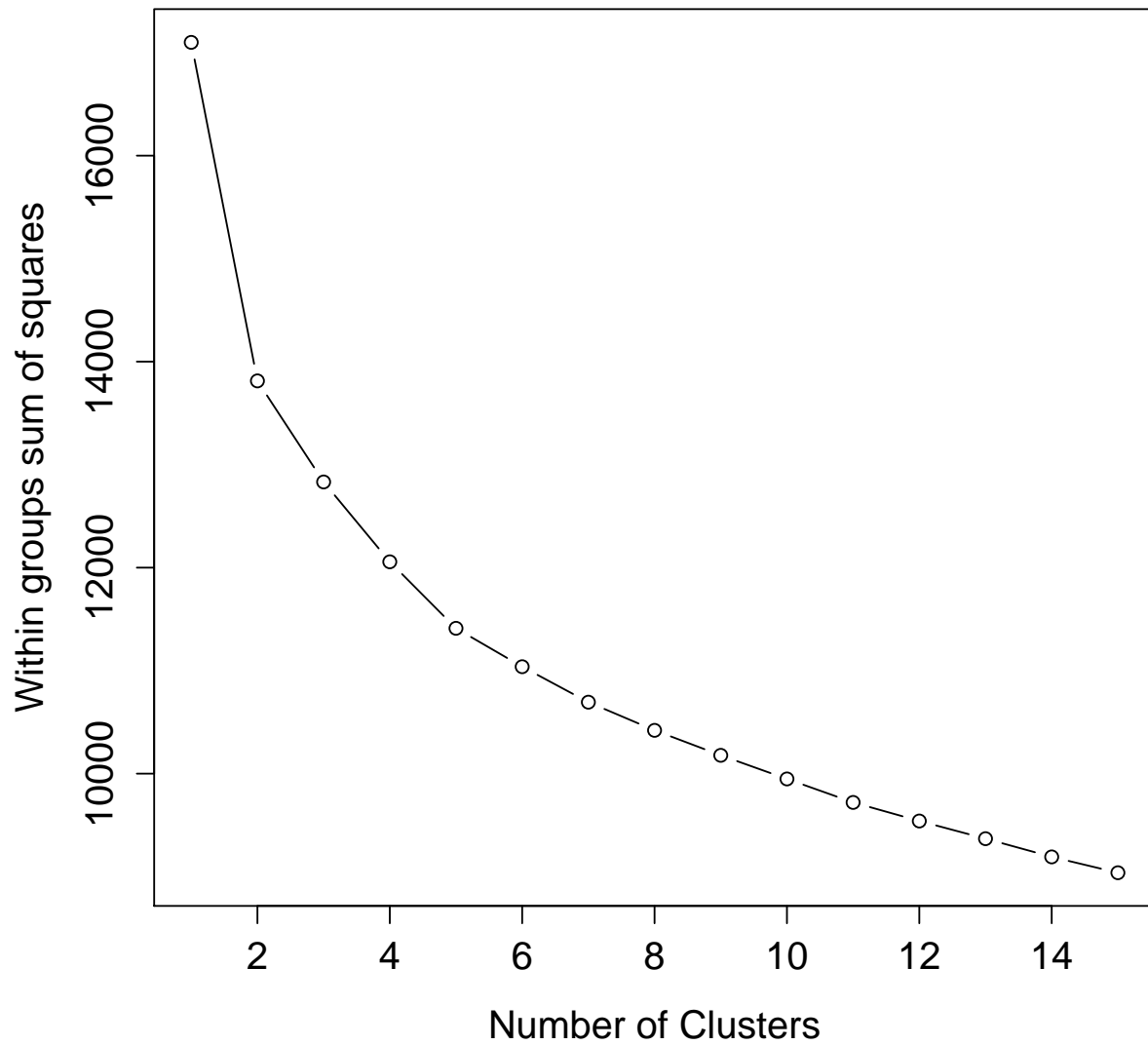


Figure 3: Scree test: WSS error by cluster size

Figure 3 shows no optimal elbow in scree test! Maybe 2-3?

2.1.2 Gap Statistic

Optimal cluster is the local maximum of the gap statistic, but it appears to be consistently increasing in Figure 4.

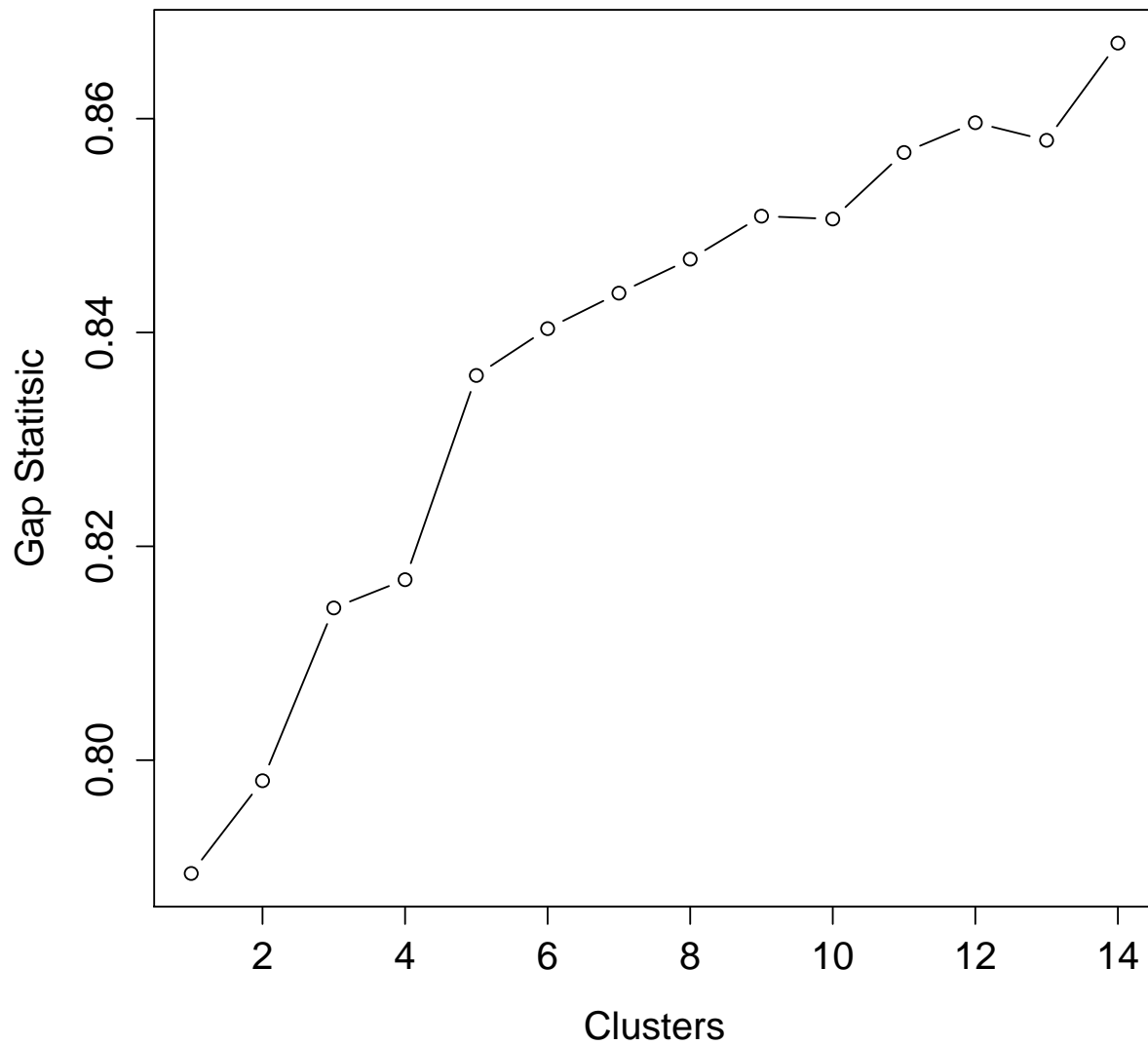


Figure 4: Gap statistic by cluster size

2.1.3 Average Silhouette Width

Figure 5 shows average silhouette width as being consistently under 0.25 for all clusters, implying the data is not well structured.

2.2 Cluster statistics

| k | n | Within SS | sum(Within SS) |
|-----|----------------|---------------------|----------------|
| 2 | 229/672 | 6118/7695 | 13813 |
| 3 | 333/134/434 | 4669/40009/4154 | 12832 |
| 4 | 79/394/275/153 | 2367/3357/3454/2880 | 12057 |

Table 3: Cluster statistics

2.3 Silhouette plots

Available in Figures 6, 7, and 8. Note: constructed with standardized z -score data.

2.4 Decision trees based on clusters

| k | CP ³ | CV Xerror ⁴ | Root Feature | Root Error | Figure |
|-----|-----------------|------------------------|------------------|------------|-----------|
| 2 | 0.0218 | 0.113 | axial ≥ 4.5 | 0.254 | Figure 9 |
| 3 | 0.0107 | 0.191 | pigd ≥ 2.5 | 0.518 | Figure 10 |
| 4 | 0.0100 | 0.255 | pigd < 2.5 | 0.563 | Figure 11 |

Table 4: k -kmeans decision trees statistics

2.5 Interpretation of Clusters

2.5.1 Cluster summaries

Available in Figures 12, 13, and 14. Error bar is standard error.

2.5.2 Interpretation

$k = 2$ seems too basic. Cluster is organized solely by severity - all symptoms, including motor and nonmotor, are higher in severity in cluster 1, and lower in cluster 2. Quite consistently, groups in cluster 1 are generally of slightly higher age and pd duration.

$k = 3$ seems like a further development of $k = 2$, where clusters are simply organized by linearly increasing severity.

$k = 4$ is where it gets interesting.

³Complexity Parameter

⁴10-fold cross validation

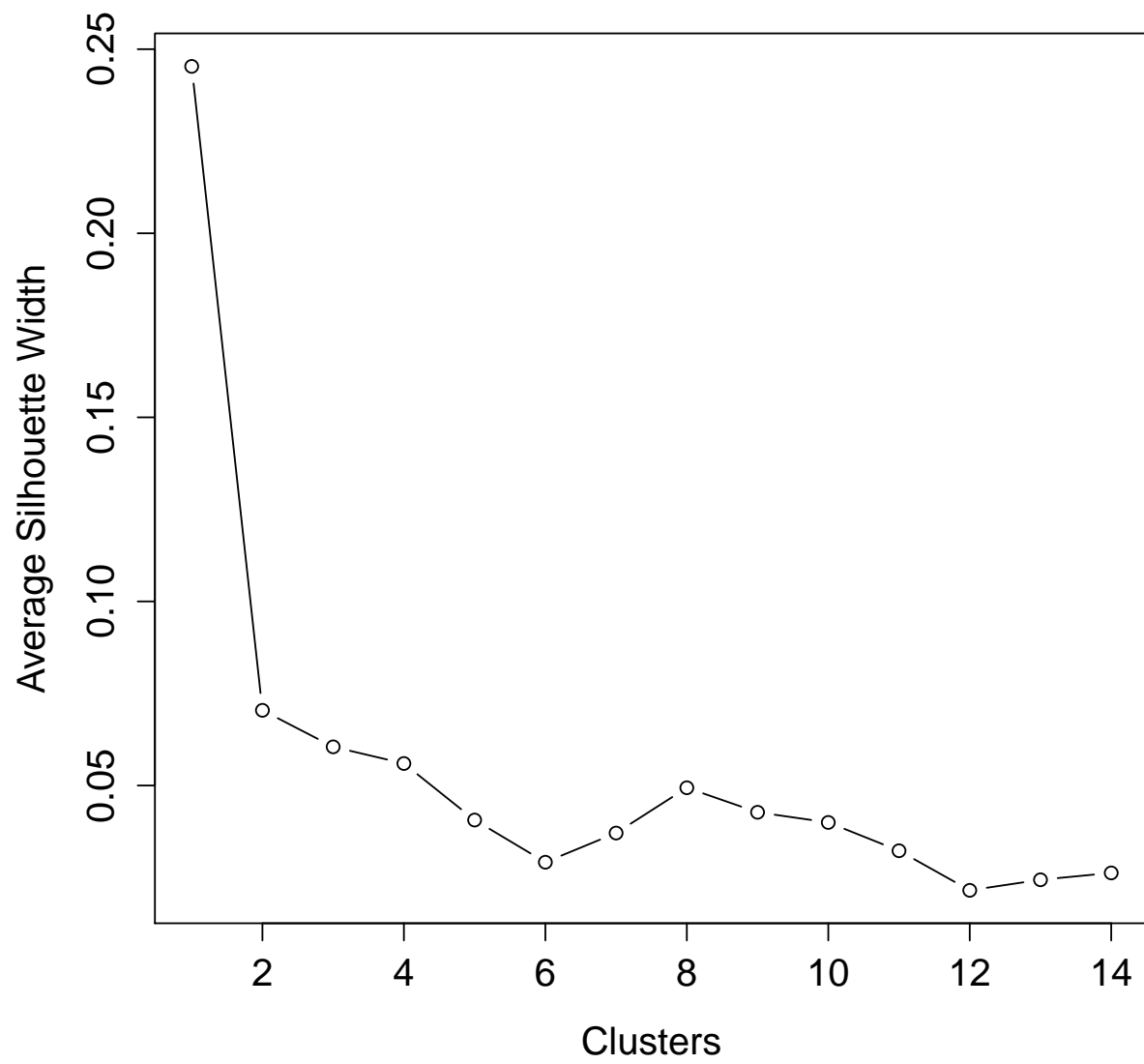


Figure 5: Average silhouette width by cluster size

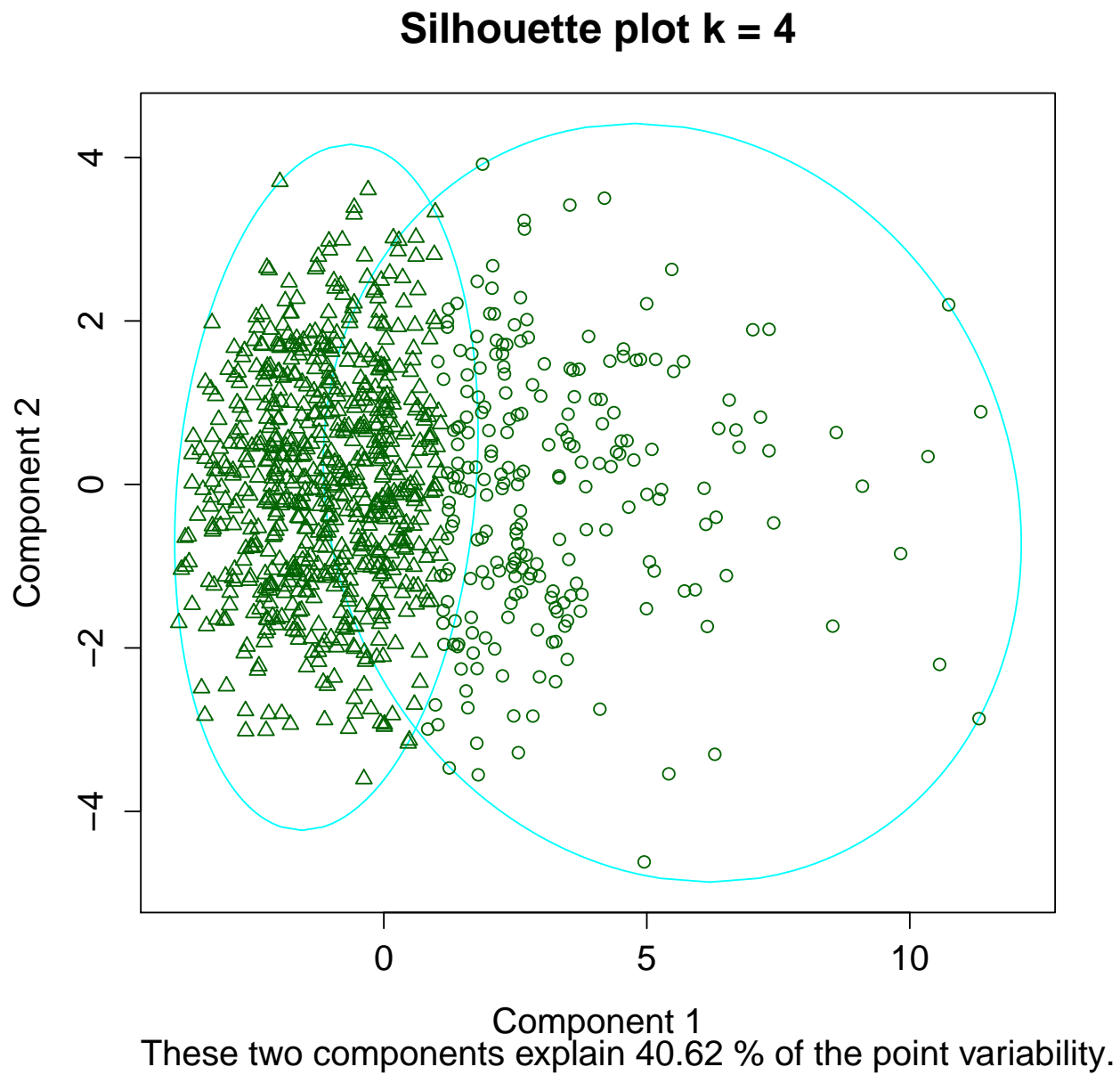


Figure 6: k -means cluster silhouette plot, $k = 2$

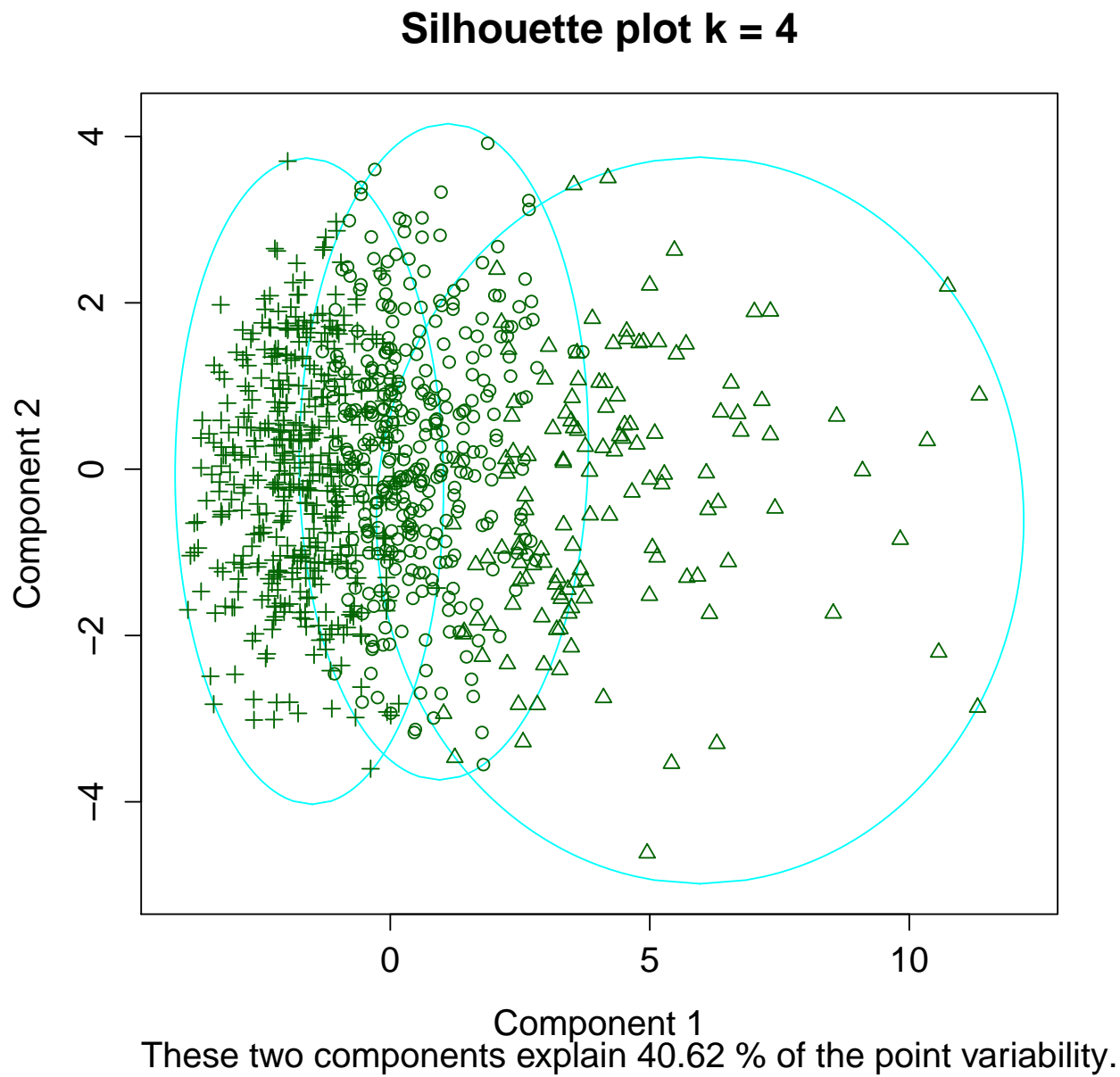
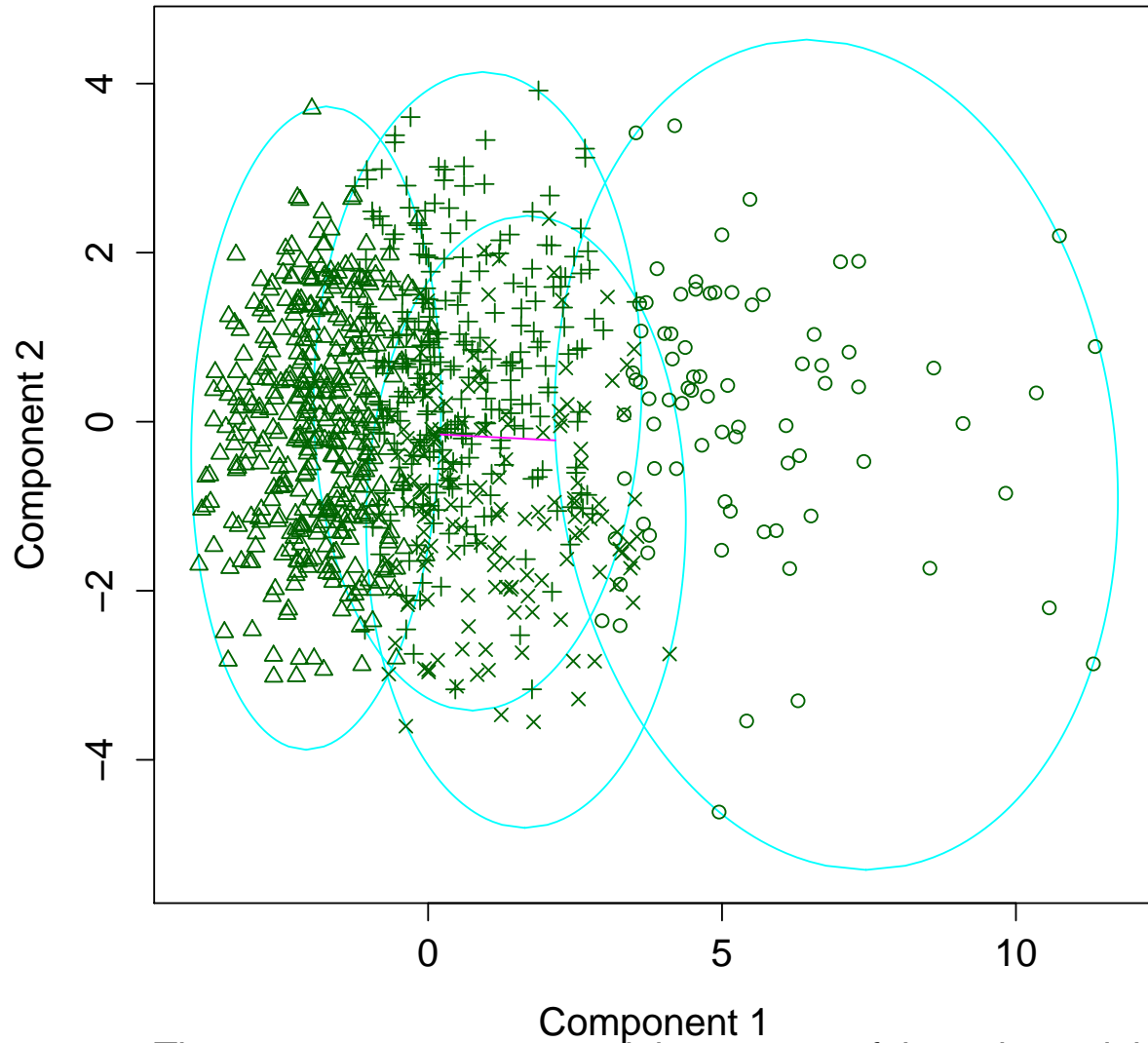


Figure 7: k -means cluster silhouette plot, $k = 3$

Silhouette plot $k = 4$



These two components explain 40.62 % of the point variability.

Figure 8: k -means cluster silhouette plot, $k = 4$

UNSCALED Pruned Tree, 2 clusters

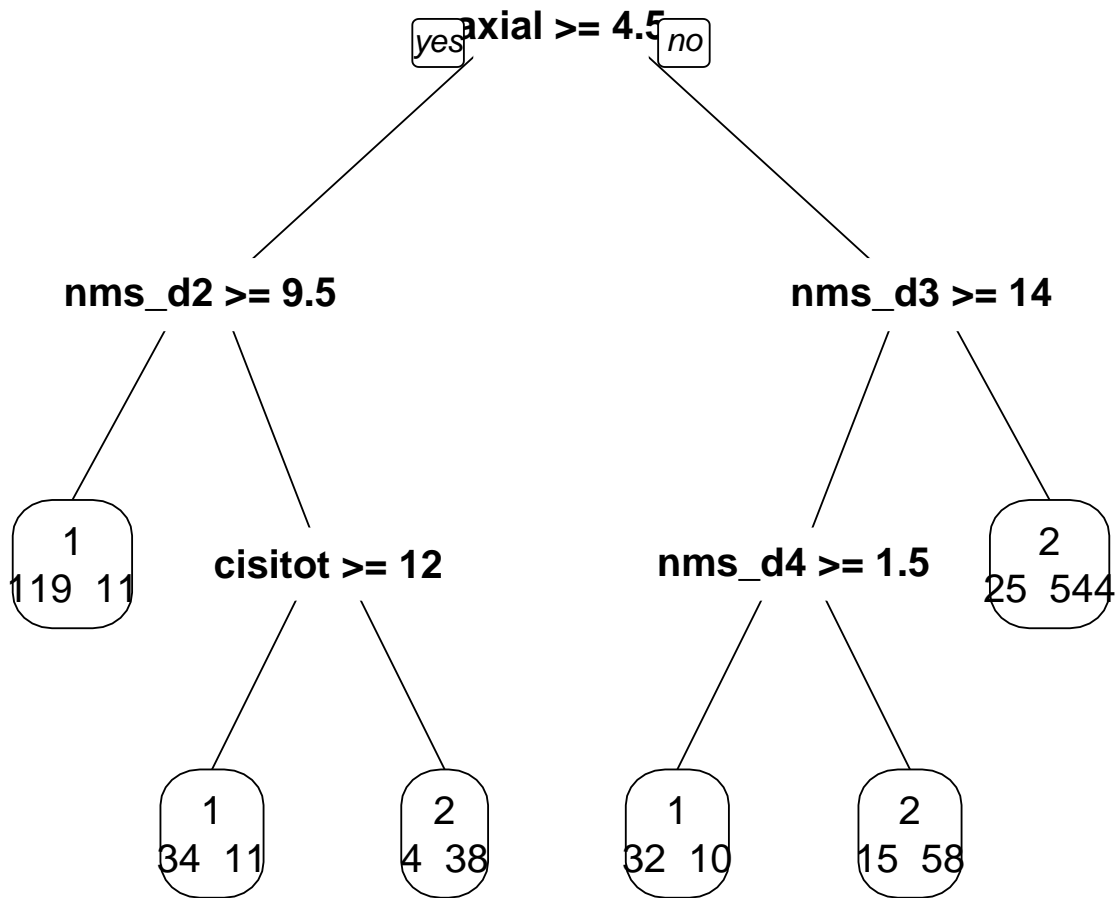


Figure 9: Decision Tree from k -means clustering, 2 clusters

UNSCALED Pruned Tree, 3 clusters

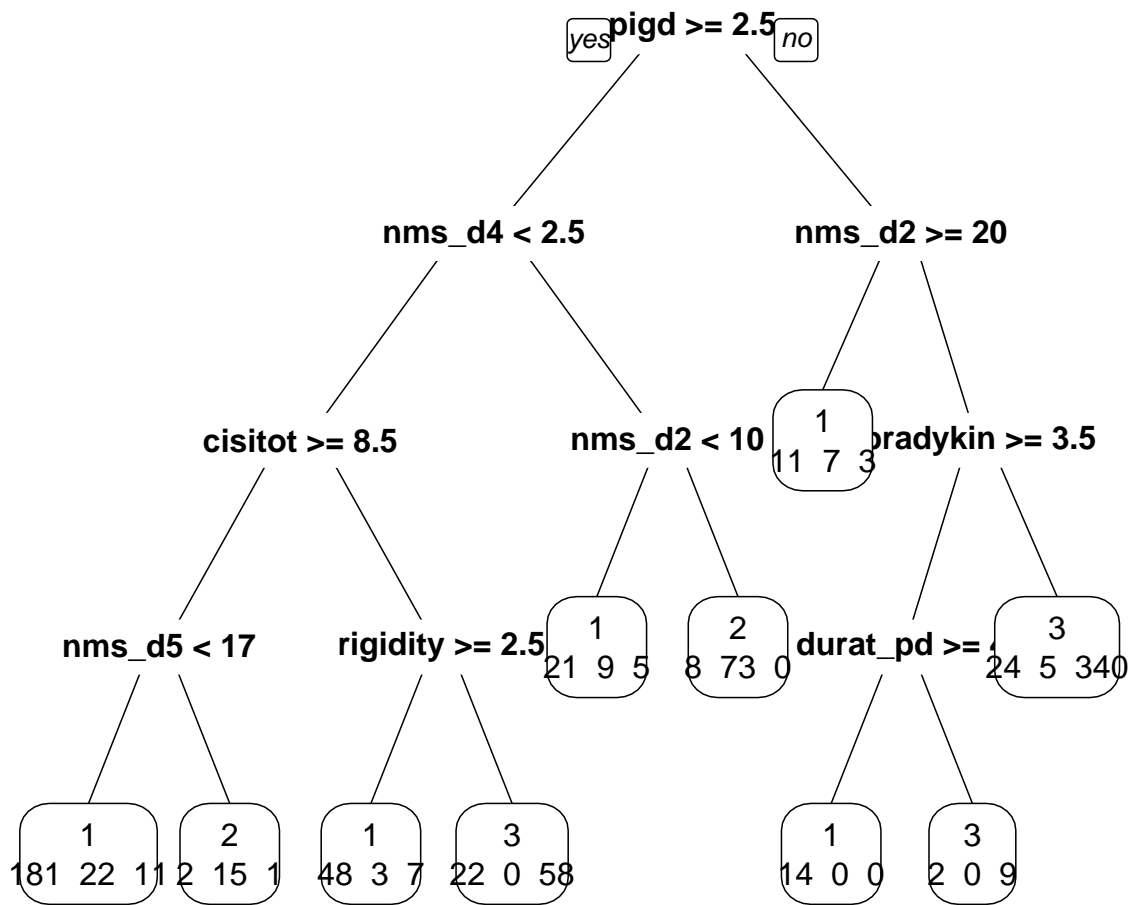


Figure 10: Decision Tree from *k*-means clustering, 3 clusters

UNSCALED Pruned Tree, 4 clusters

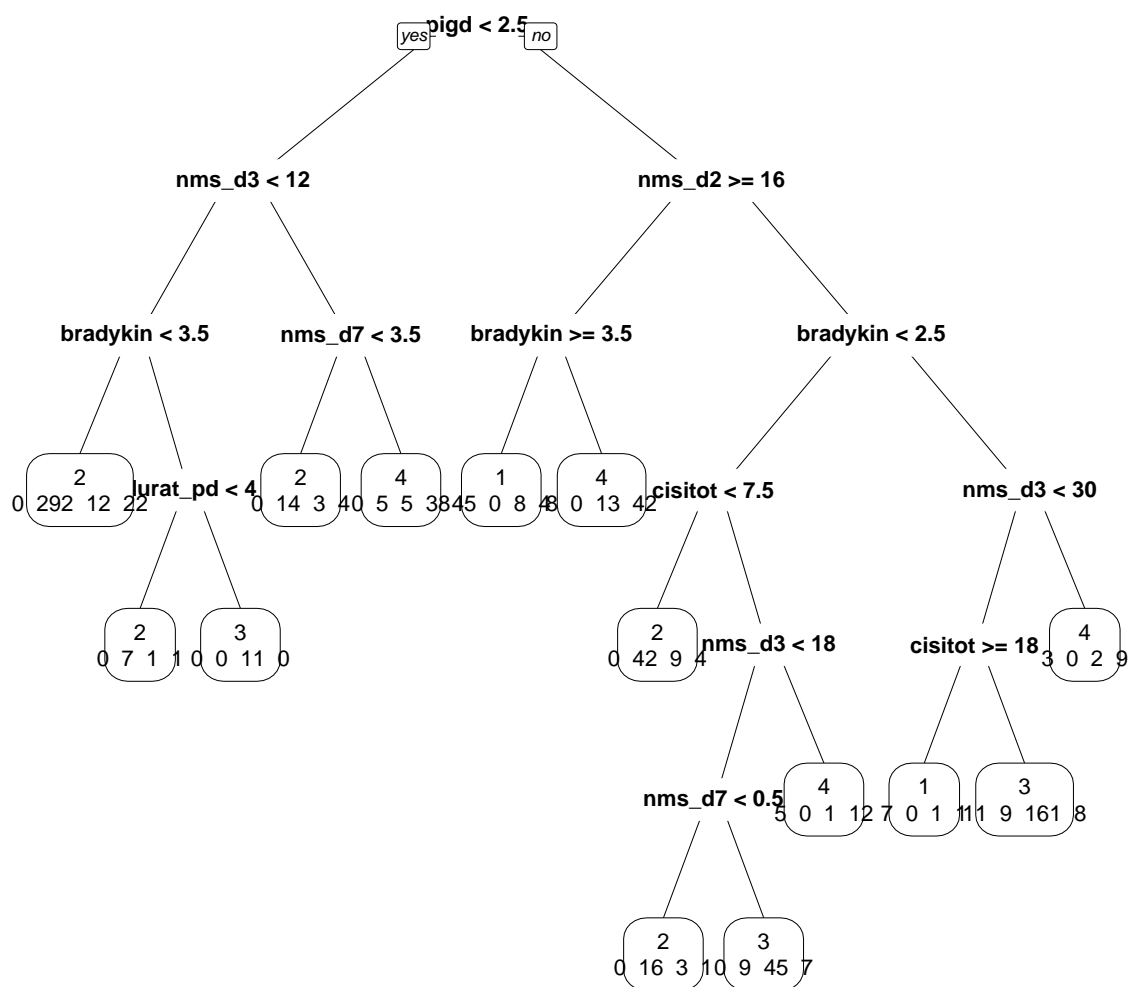


Figure 11: Decision Tree from *k*-means clustering, 4 clusters

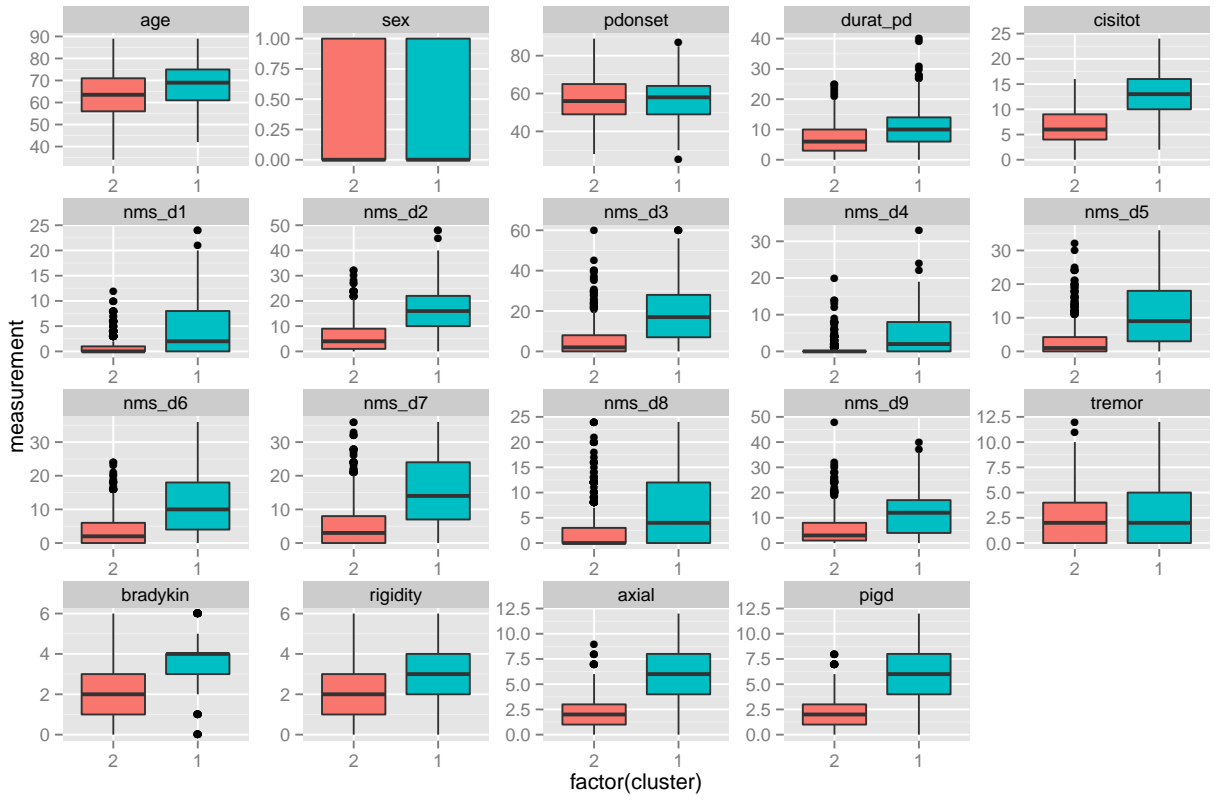


Figure 12: Cluster Summaries, $k = 2$

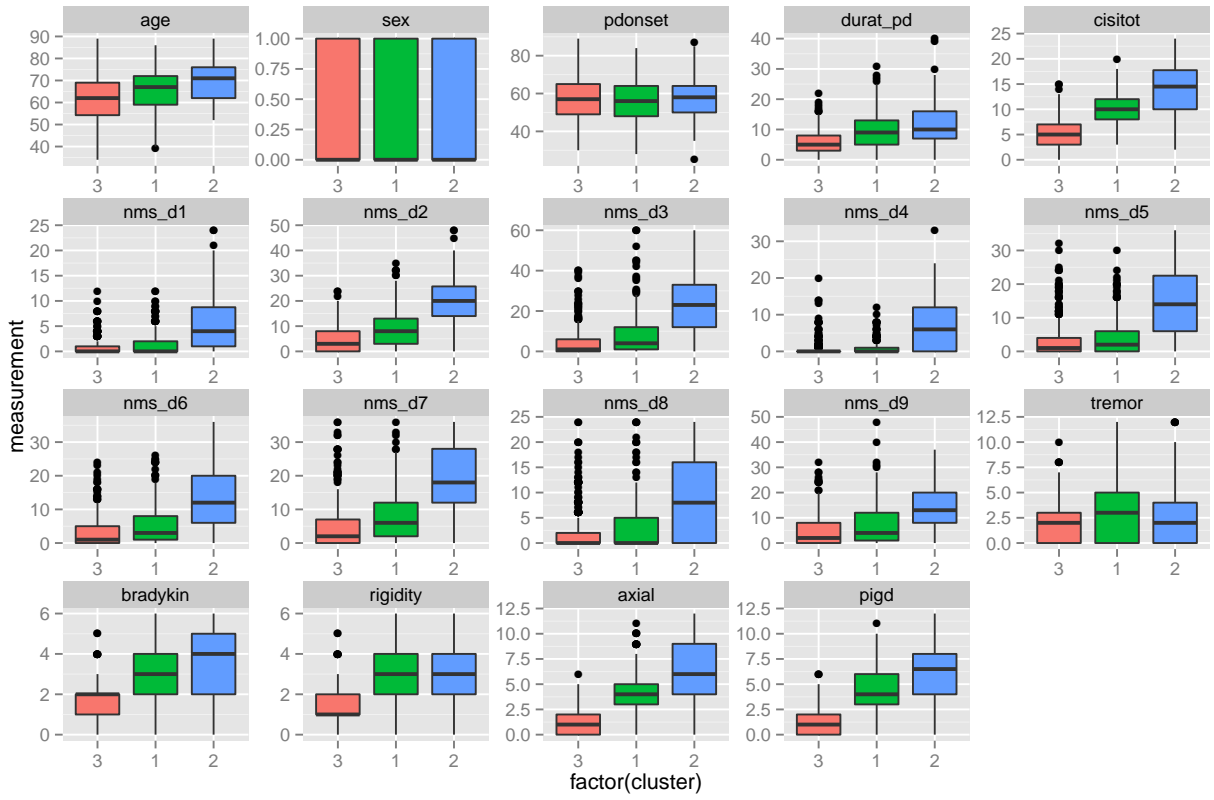


Figure 13: Cluster Summaries, $k = 3$

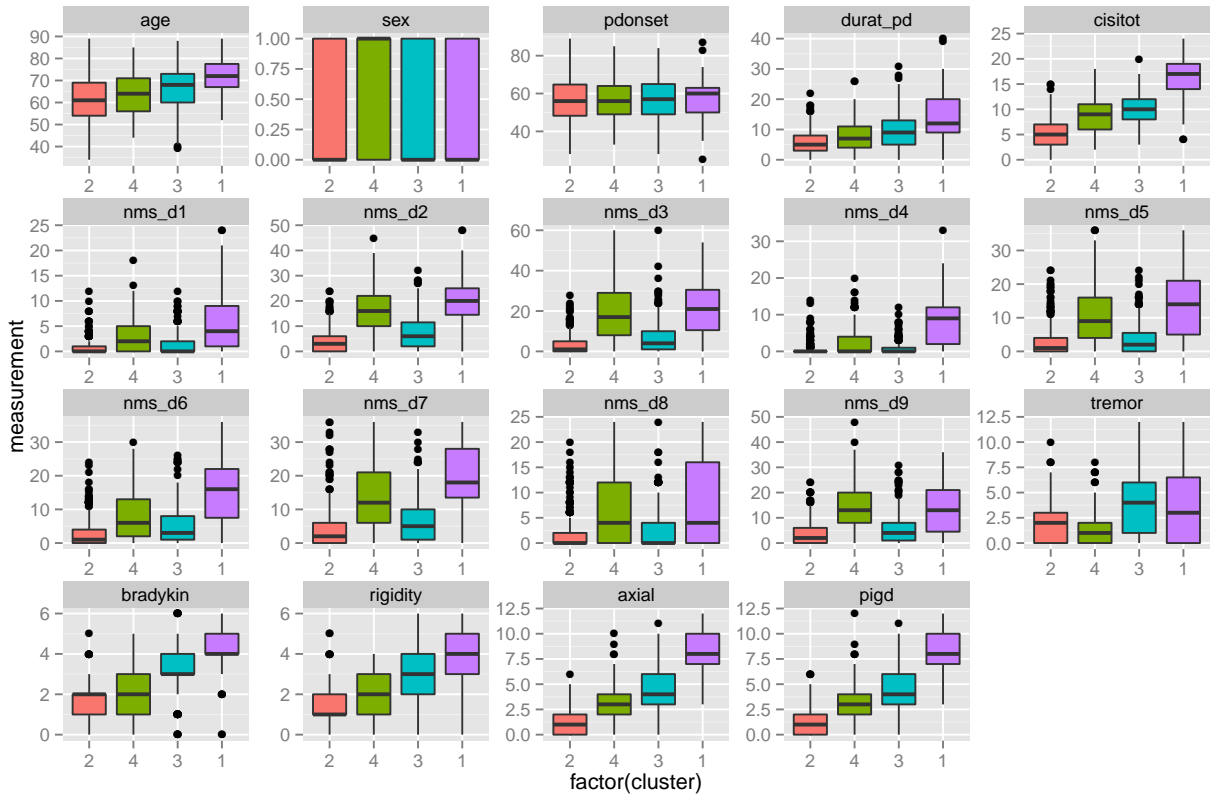


Figure 14: Cluster Summaries, $k = 4$

3 Affinity Propagation

3.1 Clustering

Package `apcluster` was used. Distance matrix was the negative euclidean squared distance ($r = 2$).

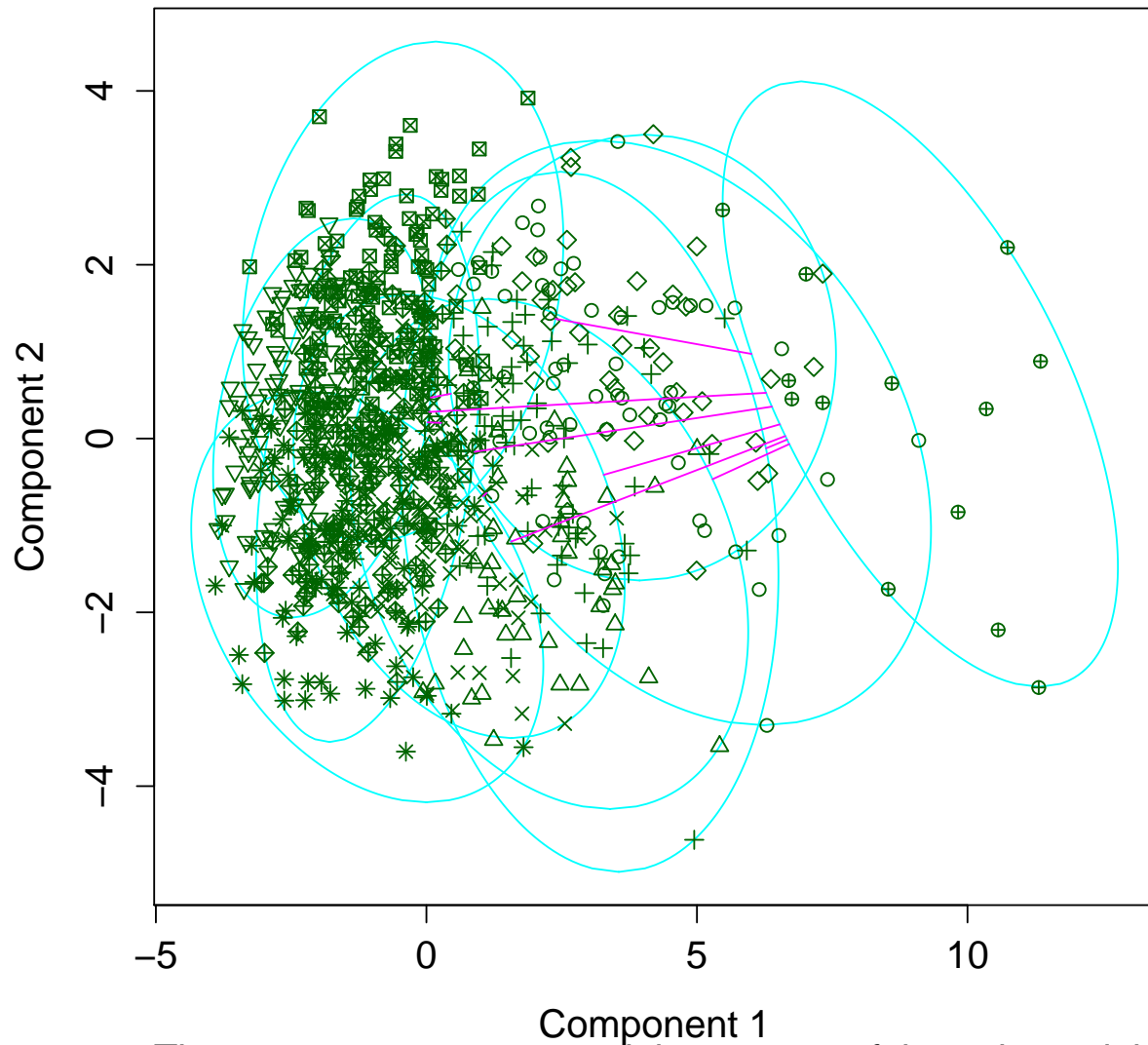
AP with input preferences minimized ($q = 0$) resulted in 8 clusters. With the standard median input preferences ($q = 0.5$), algorithm failed to converge with default parameters. Even setting damping factor to 0.98, maximum iterations to 10000, and convergence iterations to 1000 failed to converge. Might need to try a longer run.

However, given that input preferences control how many clusters are found, I don't think it's very useful to have some dozen clusters running around.

3.1.1 Silhouette Plots

Silhouette plot in Figure 15 looks pretty weak, really. Tons of overlap between the clusters.

AP Silhouette Plot k = 10



These two components explain 40.62 % of the point variability.

Figure 15: AP silhouette plot, $k = 8$

4 Hierarchical Clustering

4.1 Clustering

Four dissimilarity methods were used with a euclidean distance matrix. Dendrograms available in Figure 16

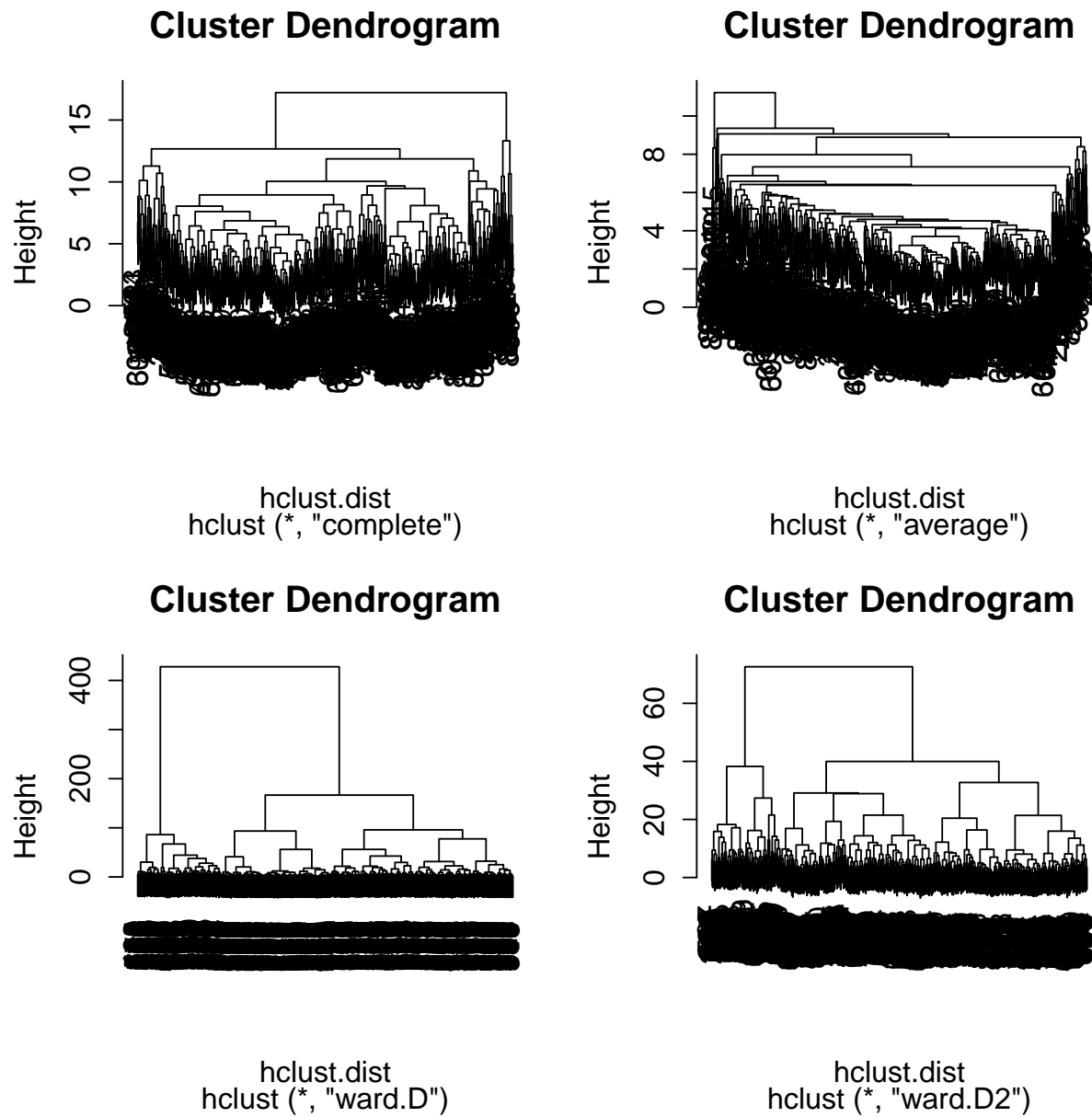


Figure 16: Dendrograms

| Method | Condition | n | Figure |
|----------|-----------------------------|--|--------|
| Complete | $k = 4$ | 4 (790/81/18/12) | 17 |
| Complete | dynamicTreeCut ⁵ | 13 (255/99/77/64/62/58/56/46/44/41/37/32/30) | 18 |
| Ward | $k = 4$ | 4 (200/237/263/201) | 19 |
| Ward | $h = 100$ | 3 (437/263/201) | 20 |

Table 5: Clusters from Tree Cutting

4.2 Cutting Trees

4.3 Interpretation

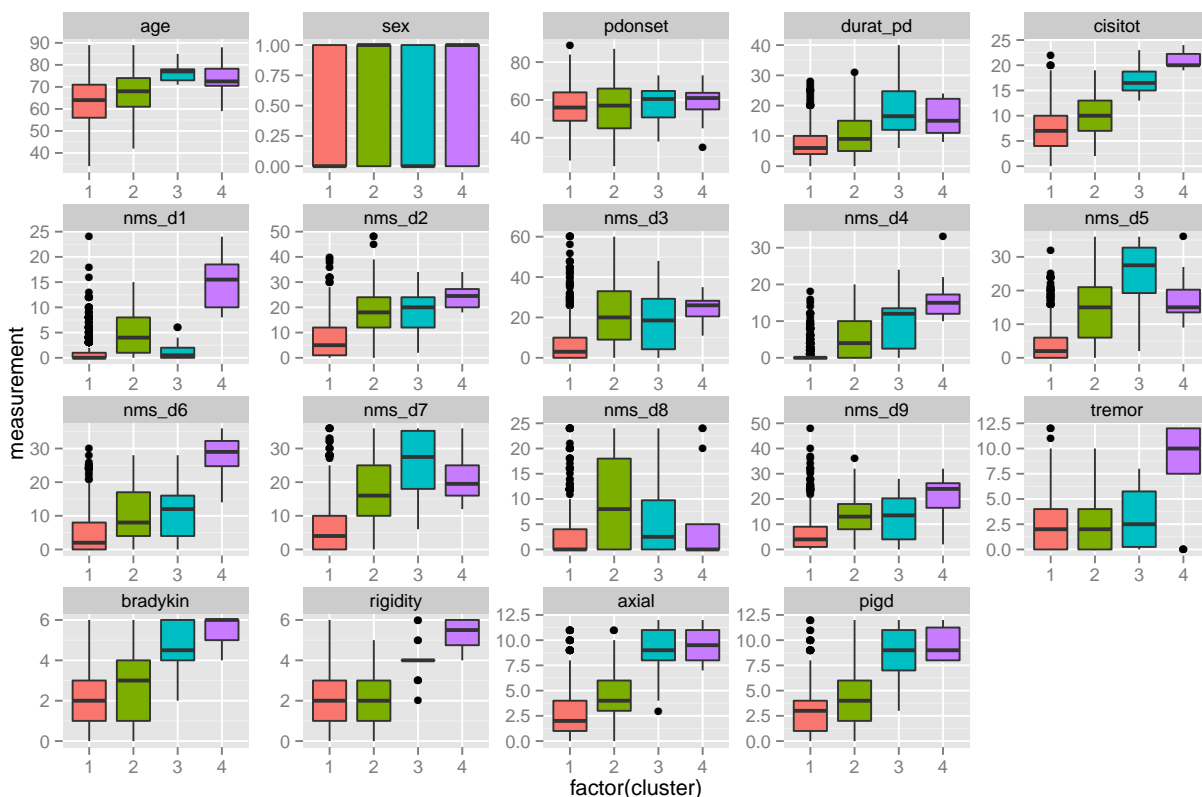


Figure 17: Using maximum (complete linkage) dissimilarity, cutting tree for $k = 4$

4.4 Interpretation

Cluster sizes are available in Table 6

Boxplot summary of clusters available in Figure 21. **Discussion forthcoming.**

⁵Package dynamicTreeCut in R (Langfelder P, Zhang B, Horvath S (2007)). Hybrid method, minimum cluster selection parameters

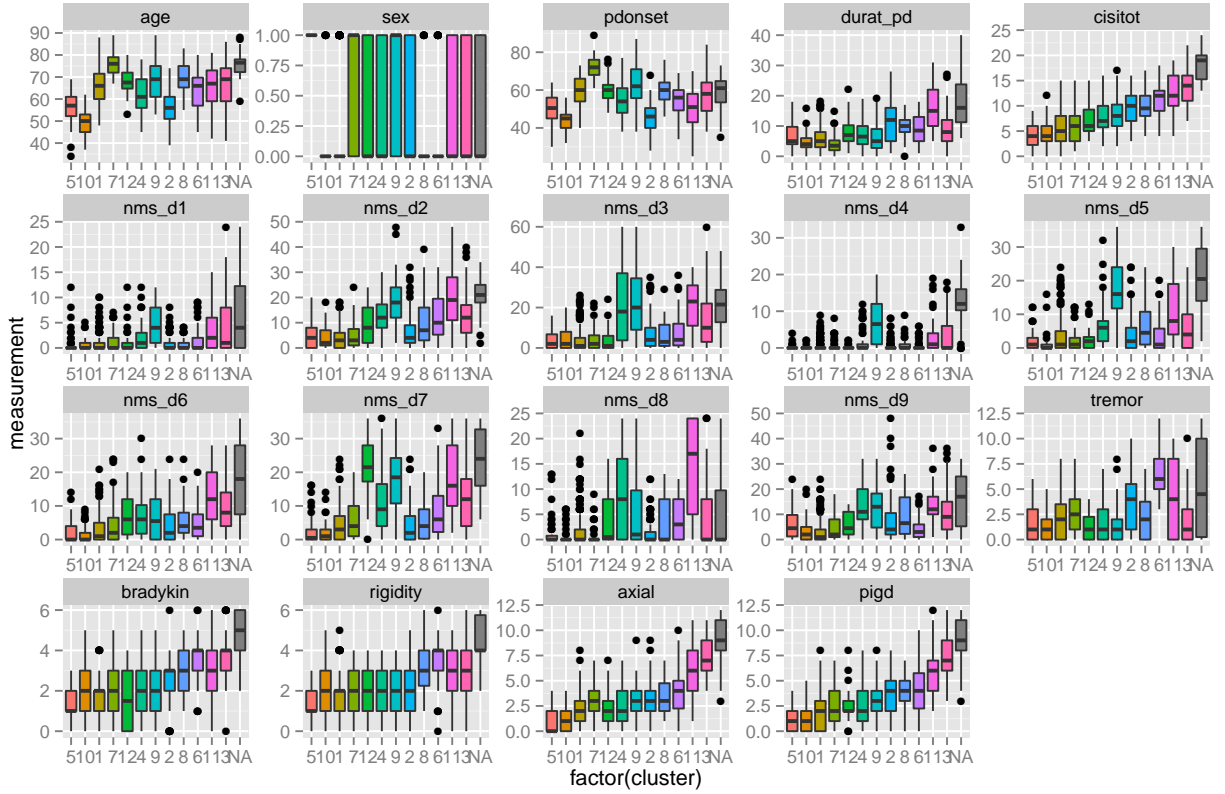


Figure 18: Using maximum (complete linkage) dissimilarity, cutting tree dynamically

5 Biclustering

Used BCBimax clustering algorithm. Clusters seem quite sparse.

6 Subspace clustering

7 Bayesian Networks

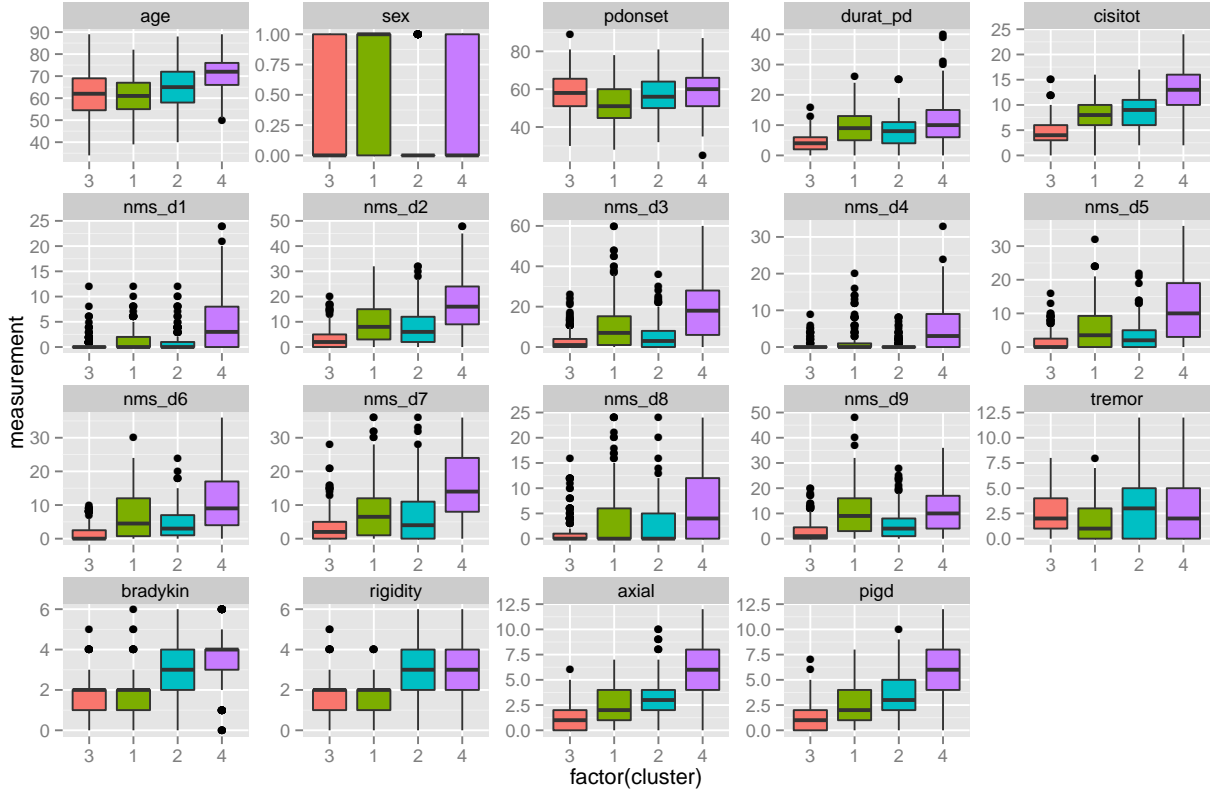


Figure 19: Using Ward (1963) dissimilarity, cutting tree for $k = 4$

| Cluster | Size |
|---------|------|
| 1 | 63 |
| 2 | 53 |
| 3 | 85 |
| 4 | 122 |
| 5 | 48 |
| 6 | 126 |
| 7 | 123 |
| 8 | 102 |
| 9 | 166 |
| 10 | 13 |

Table 6: AP Cluster Sizes

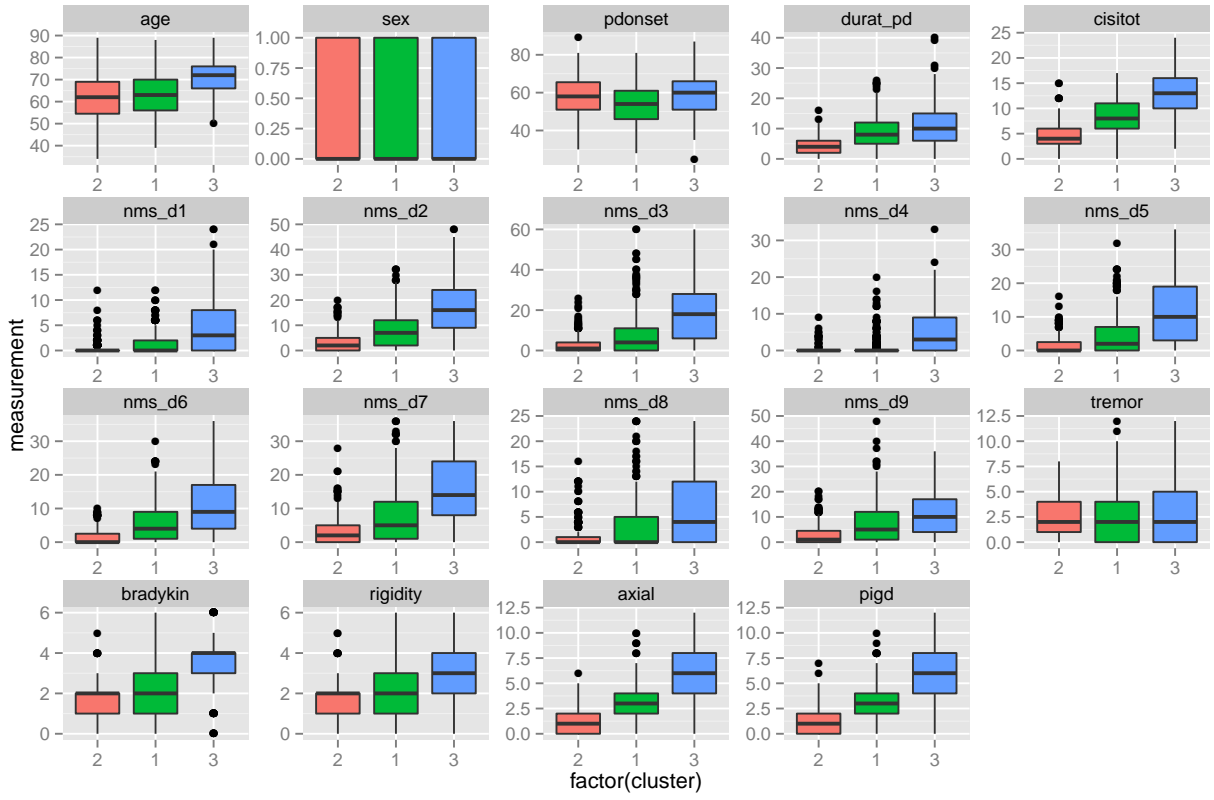


Figure 20: Using Ward (1963) dissimilarity, cutting tree at $h = 100$

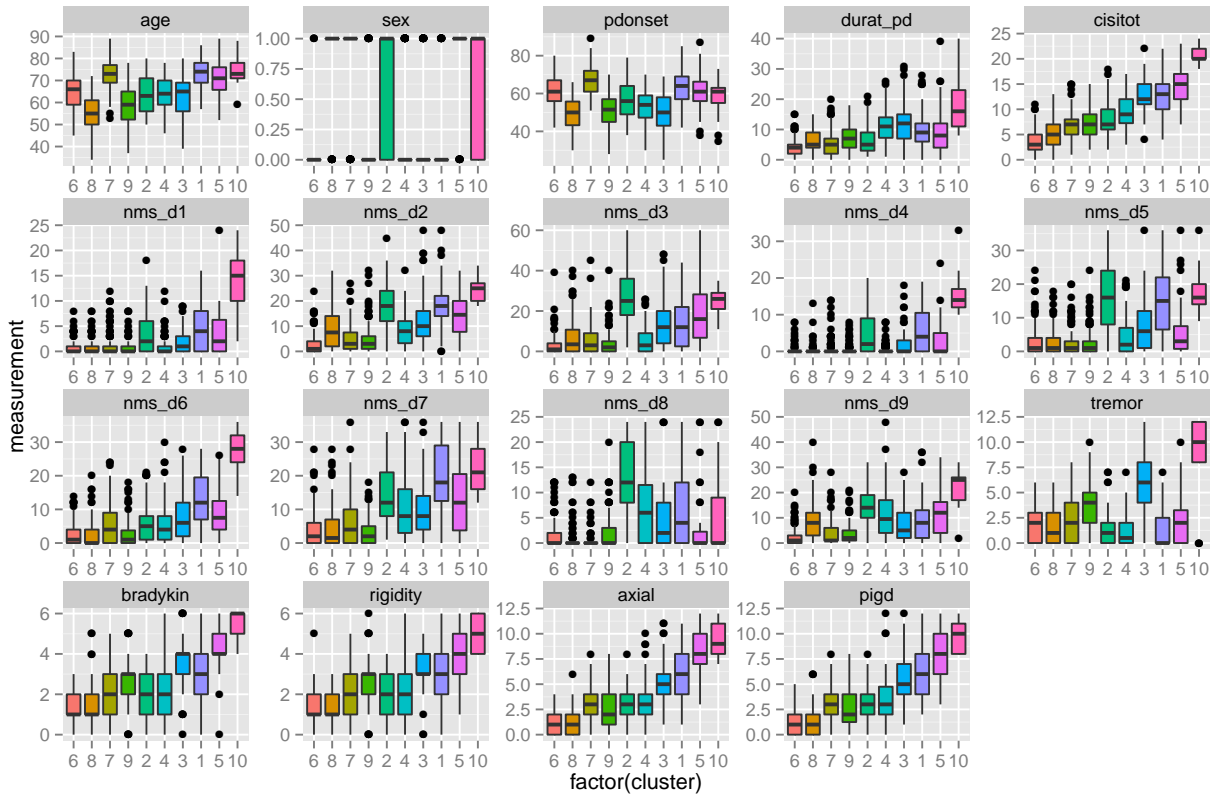


Figure 21: AP Boxplot Summaries

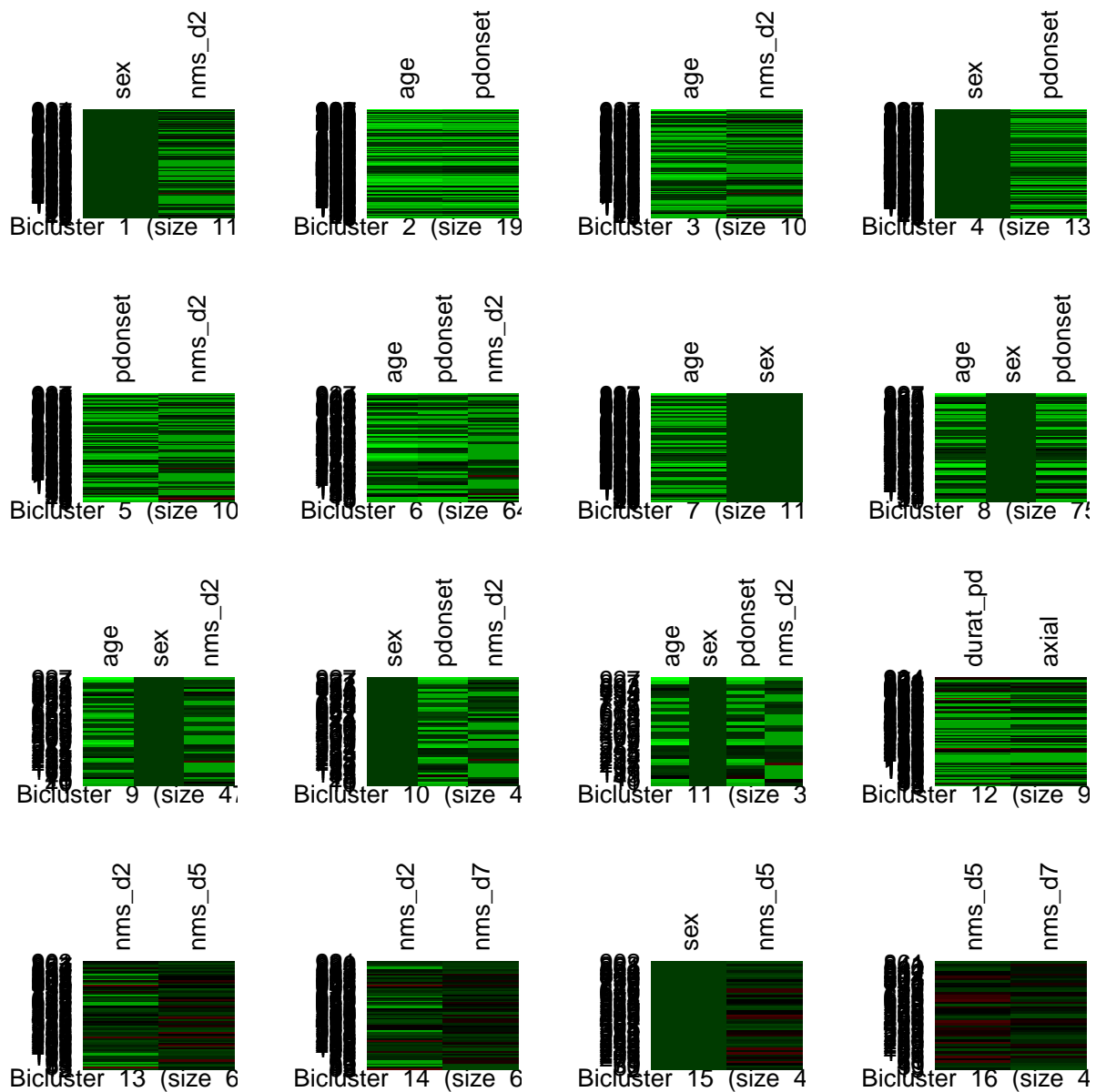


Figure 22: Biclustering heatmaps $N = 16$

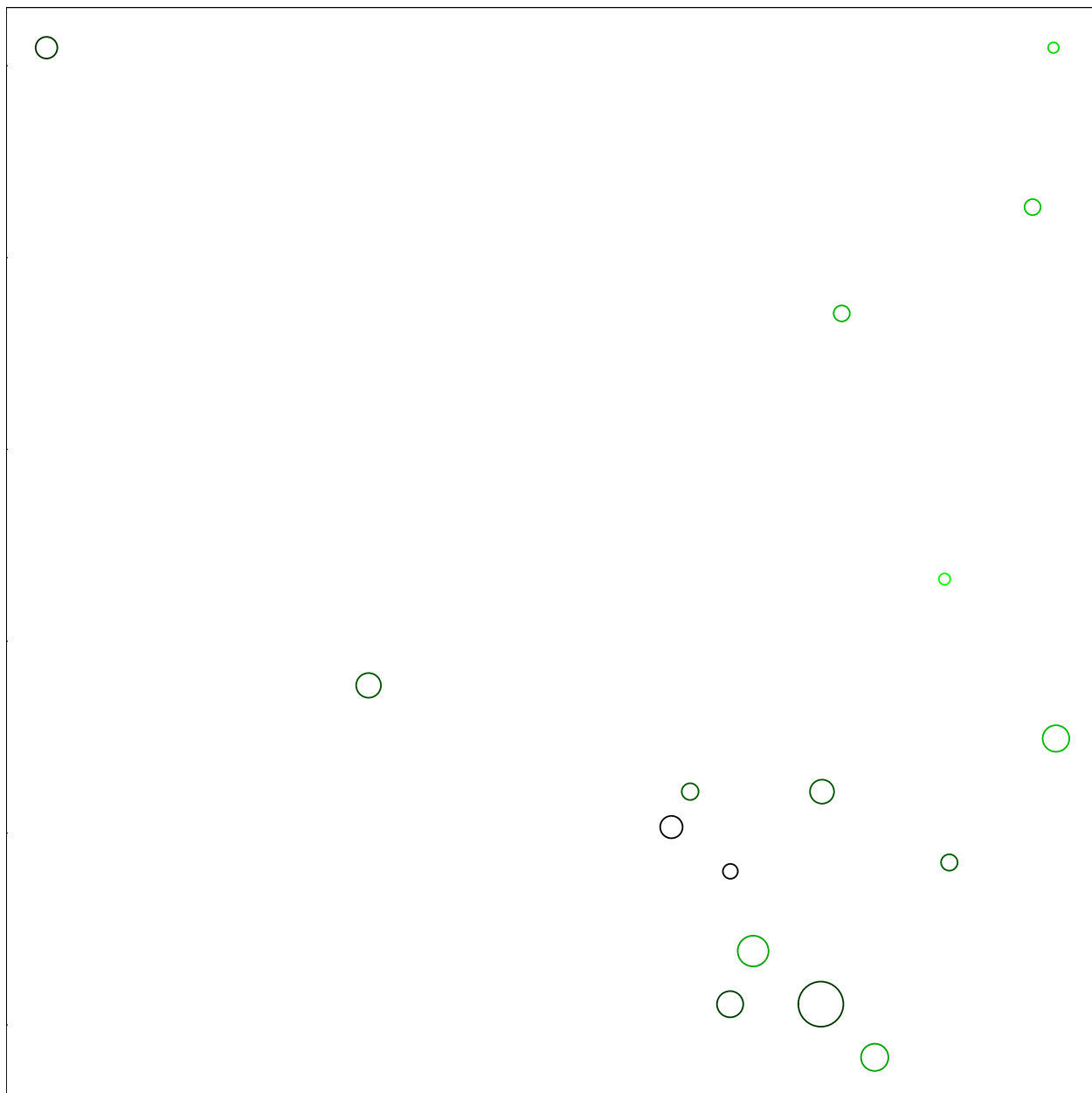


Figure 23: Bubbleplot $N = 16$