

# Learning Fair Representations

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# Content

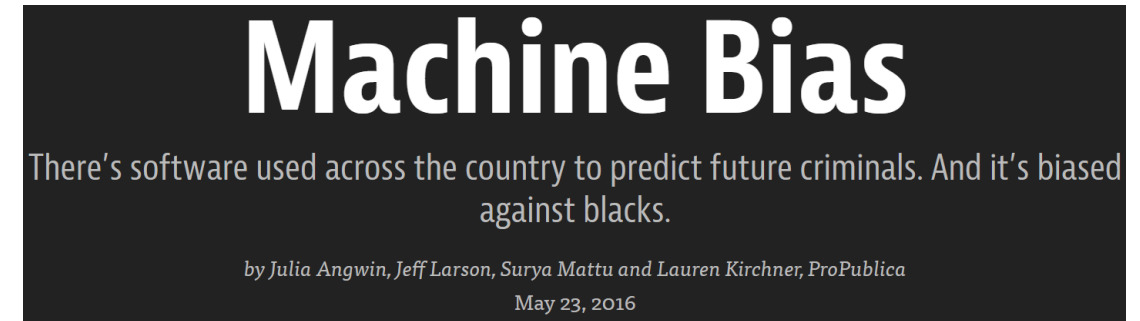
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# Motivation

## Fairness in Machine Learning Systems

Further Examples:

- Mortgage discrimination
- Screening candidates to hire



Examples of legally recognized protected groups: Race, Color, Sex, Religion, National origin, Citizenship, Age, Familial status, Disability status, ...

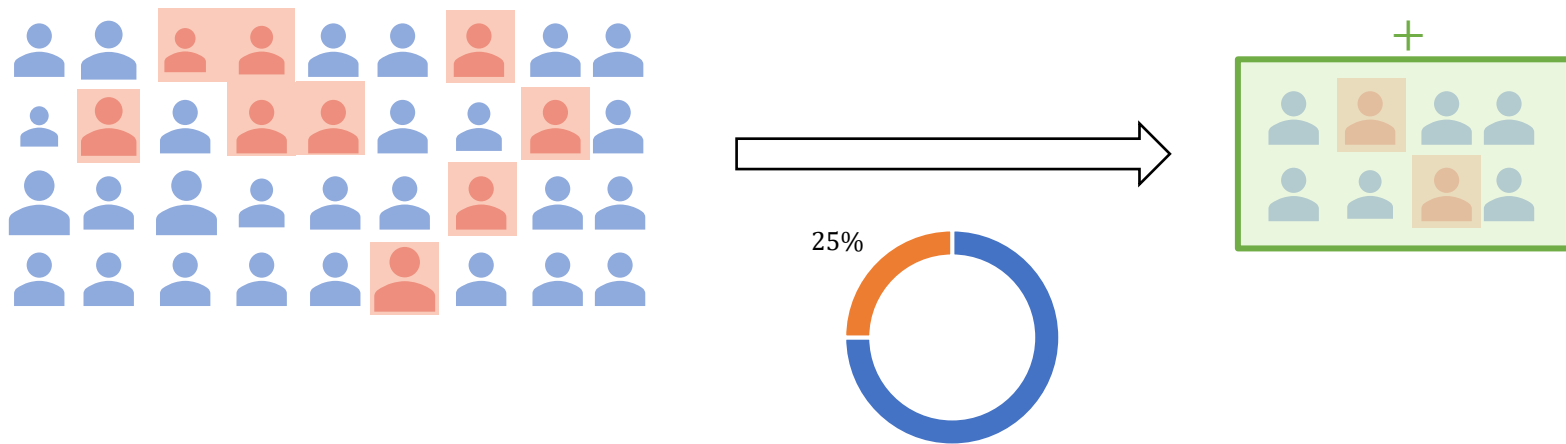
What is the actual problem?  
How can we combat this?

# Theoretical Background

## Group Fairness and Individual Fairness

### Group Fairness (= Statistical Parity)

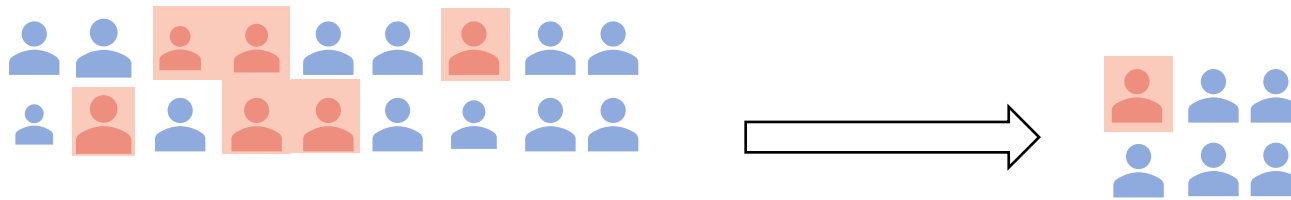
- Proportion of members of a protected group receiving positive/negative classification are identical to the proportion of the protected group in the population.



# Theoretical Background

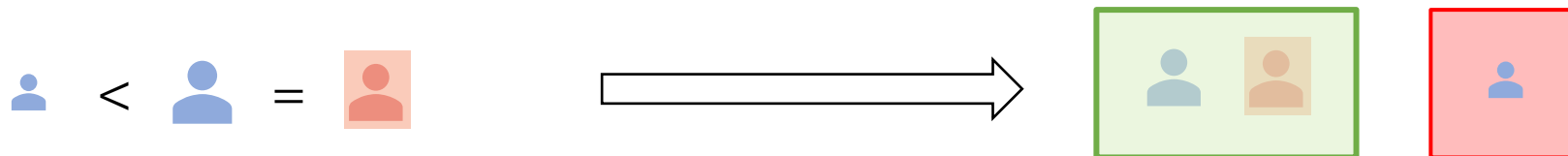
## Group Fairness and Individual Fairness

What does group fairness miss?



## Individual Fairness

- Ensures, that any two individuals who are **similar** should be classified similarly



# Theoretical Background

## Prior Work

Fairness Through Awareness – Dwork et al. (2011)

- Introduces the concept of a **hypothetical** measure of similarity between individuals with respect to the classification task at hand.
- Method: Define probabilistic mapping from individuals to an intermediate representation, which achieves the above goals.

# Theoretical Background

Prior Work - Dwork et al. (2011) - Shortcomings

- 1) A fair similarity measure between individuals is assumed to be given. Finding a fair similarity measure is challenging!
- 2) The mapping to intermediate representations are only defined for the given set of individuals → Lacks generalization for unseen data.

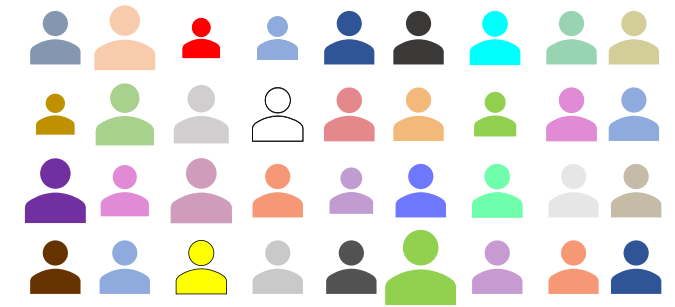


# The LFR Model

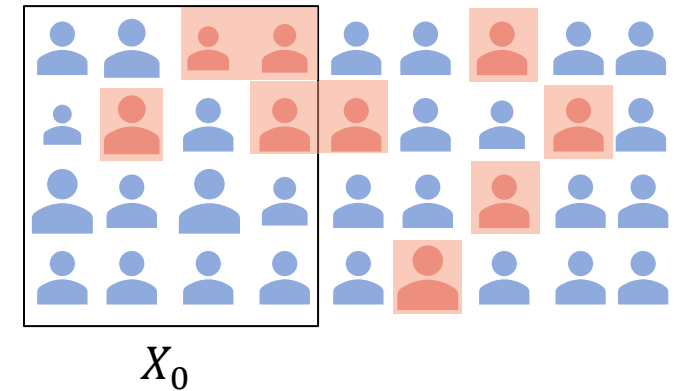
# LFR Model

## Notation

- Dataset  $X$  of individuals  $x \in X \in \mathbb{R}^D$ 
  - Qualitative or numerical
- $S$ : is  $x$  a member of the **protected group**?
  - Subset of individuals in the protected group:  $X^+ \subset X$
  - Subset of individuals not in the protected group:  $X^- \subset X$
- Training set  $X_0 \subset X$ 
  - Subset of individuals in the protected group:  $X_0^+ \subset X$
  - Subset of individuals not in the protected group:  $X_0^- \subset X$
- $Y$  is the binary random variable (classification for each individual)



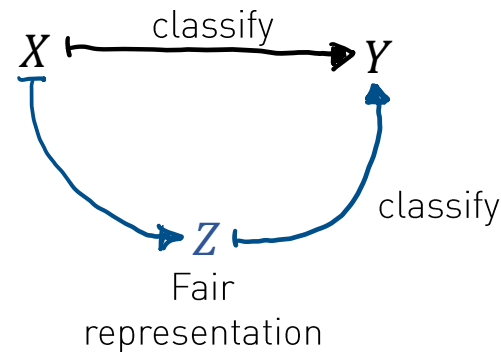
$S = 1$   
 $S = 0$



# LFR Model

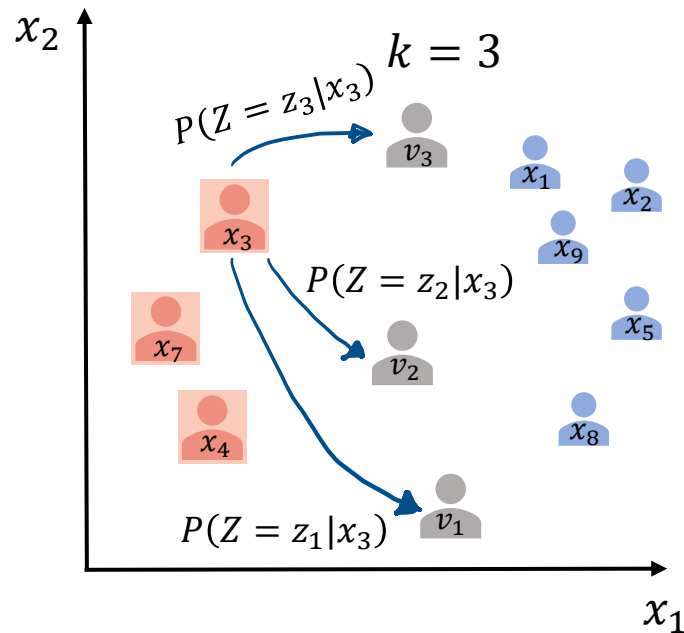
## The Basic Idea

- Two-step model via a **fair**, intermediate representation
- Probabilistic mapping:  $X \rightarrow Z$  to a set of prototypes.
  - Mapping should **hide the membership** of an individual in the protected group
  - Mapping should **retain** as much **information** about the individual as possible
- Mapping from prototypes to classification decision:  $Z \rightarrow Y$



# The LFR Model

## Clustering: Prototypes



- $Z = [z_1, \dots, z_K]$ : set of prototypes. “Centroid” vector  $\mathbf{v}_k \in \mathbb{R}^D$  for each  $z_k$

$$P(Z = k | \mathbf{x}_n) = \text{softmax}(-d(\mathbf{x}_n, \mathbf{v}_k, \alpha)) \\ = \frac{\exp(-d(\mathbf{x}_n, \mathbf{v}_k, \alpha))}{\sum_{j=1}^K \exp(-d(\mathbf{x}_n, \mathbf{v}_j, \alpha))}$$

# LFR Model

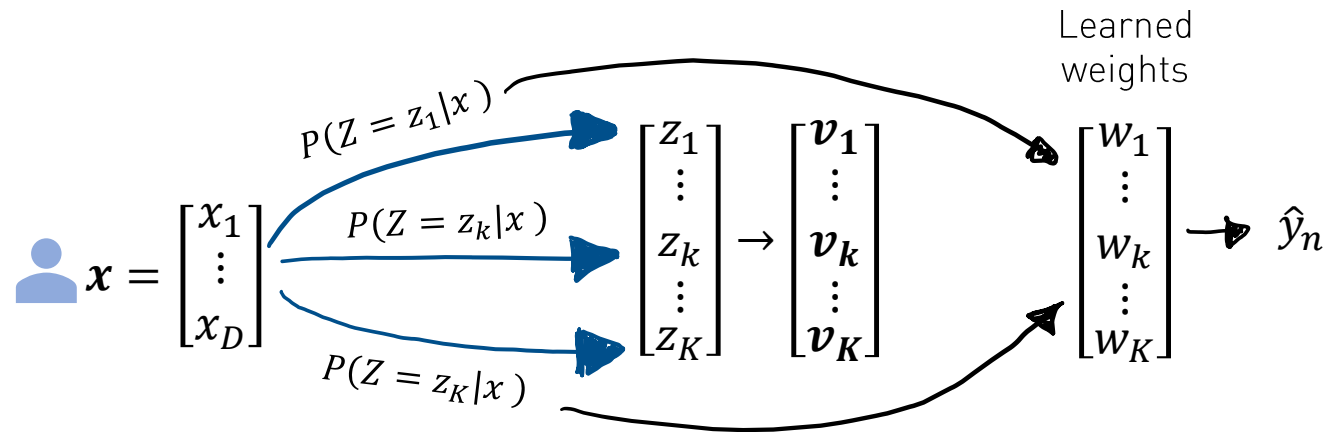
## The Model Specifics

- Probabilistic mapping:  $X \rightarrow Z$  (between individuals and set of prototypes)

$$P(Z = k | \mathbf{x}_n) = \text{softmax}(-d(\mathbf{x}_n, \mathbf{v}_k, \alpha)) = \frac{\exp(-d(\mathbf{x}_n, \mathbf{v}_k, \alpha))}{\sum_{j=1}^K \exp(-d(\mathbf{x}_n, \mathbf{v}_j, \alpha))}$$

- Mapping from prototypes to classification decision:  $Z \rightarrow Y$

$$\hat{y}_n = \sum_{k=1}^K P(Z = k | \mathbf{x}_n) \cdot w_k$$



# LFR Model

## Objectives

- 1) We want an accurate prediction  $\hat{y}_n$
- 2) Intermediate representation should be accurate:  $\hat{\mathbf{x}}_n = \sum_{k=1}^K P(Z = k | \mathbf{x}_n) \cdot \mathbf{v}_k$
- 3) Obfuscate membership in protected group:  $P(Z = k | \mathbf{x} \in X^+) = P(Z = k | \mathbf{x} \in X^-)$

Estimated on the training data:

$$\mathbb{E}_{\mathbf{x} \in X^+} P(Z = k | \mathbf{x}) = \mathbb{E}_{\mathbf{x} \in X^-} P(Z = k | \mathbf{x}) \leftrightarrow M_k^+ = M_k^-, \quad \forall k$$

Optimize:  $\alpha_i, \{\mathbf{v}_k\}_{k=1}^K, \mathbf{w}$

Objective Function:

$$L = A_z \cdot \sum_{k=1}^K |M_k^+ - M_k^-| + A_x \cdot \sum_{n=1}^N (\mathbf{x}_n - \hat{\mathbf{x}}_n)^2 + A_y \cdot \sum_{n=1}^N -y_n \log \hat{y}_n - (1 - y_n) \log(1 - \hat{y}_n)$$

# Experiments

# Experiments

## Evaluation

How do we quantify the quality of a fair model?

- Accuracy:  $1 - \frac{1}{N} \sum_{n=1}^N |y_n - \hat{y}_n|$
- Discrimination:  $\left| \frac{\sum_{n:s_n=1} \hat{y}_n}{\sum_{n:s_n=1} 1} - \frac{\sum_{n:s_n=0} \hat{y}_n}{\sum_{n:s_n=0} 1} \right|$
- Consistency: comparison to  $kNN(\mathbf{x})$ :  $1 - \frac{1}{Nk} \sum_n \left| \hat{y}_n - \sum_{j \in kNN(x_n)} \hat{y}_j \right|$

Model Selection?

- Min discrimination
- Max. Delta (between accuracy and discrimination)



# Experiments

## Compared Models and Datasets

- German credit dataset (1000 samples)
  - Each individual is represented by **20 attributes**
  - Classify bank account holders into a “Good” or “Bad”
  - Considered attribute = **Age**
- Adult income dataset (45'222 samples)
  - Each individual is represented by **14 attributes**
  - Classify whether the income is larger than 50'000 dollars
  - Considered attribute = **Gender**
- Health Heritage Dataset (147'473 samples)
  - Each individual is represented by **139 attributes**
  - Classify whether a person will be in the hospital in a particular year
  - Considered attribute = **Age**

### Models:

- LR = Logistic Regression
- FNB = Fair Naïve Bayes
- RLR = Regularized Logistic Regression
- LFR = Learned Fair Representation

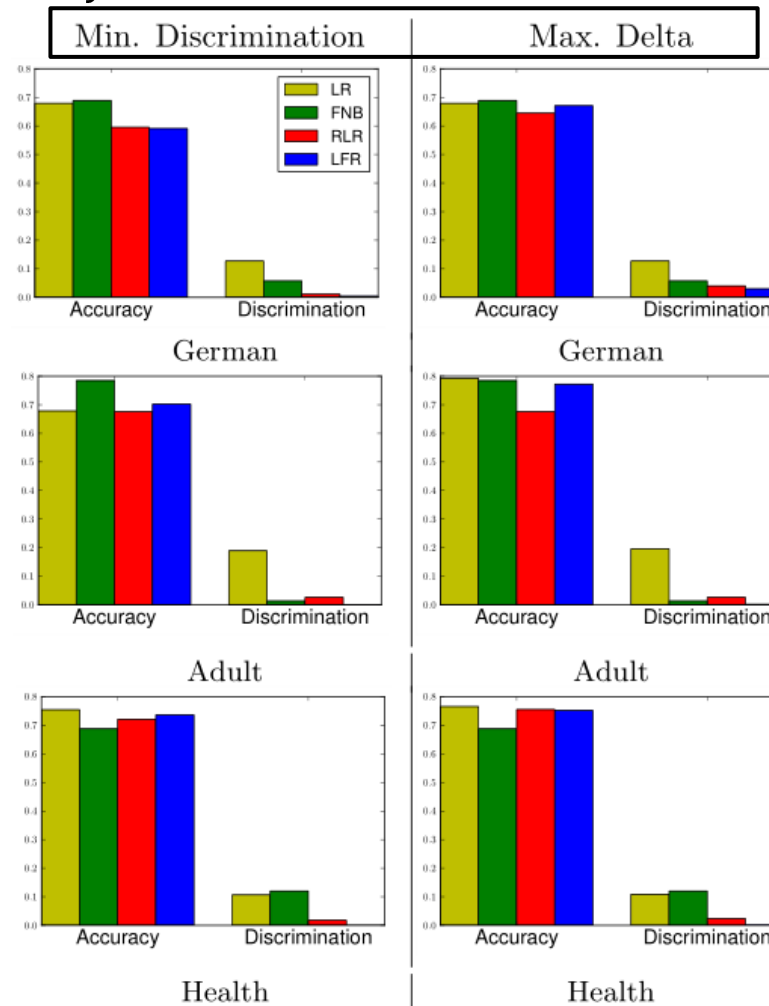
# Experiments

Results + Discussion: Accuracy and Discrimination

Model selection criteria

Models (Legend):

- LR = Logistic Regression
- FNB = Fair Naïve Bayes
- RLR = Regularized Logistic Regression
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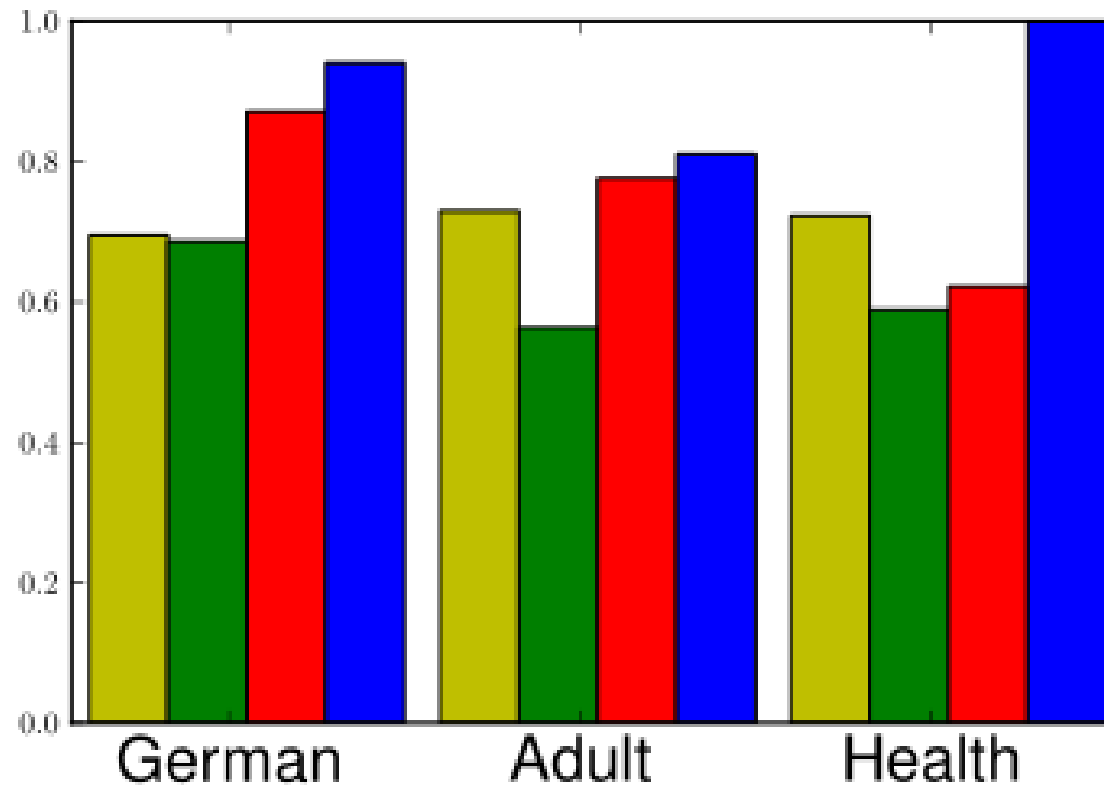


# Experiments

## Results + Discussion 2: Consistency (Measure of individual fairness)

Models (Legend):

- LR = Logistic Regression
- FNB = Fair Naïve Bayes
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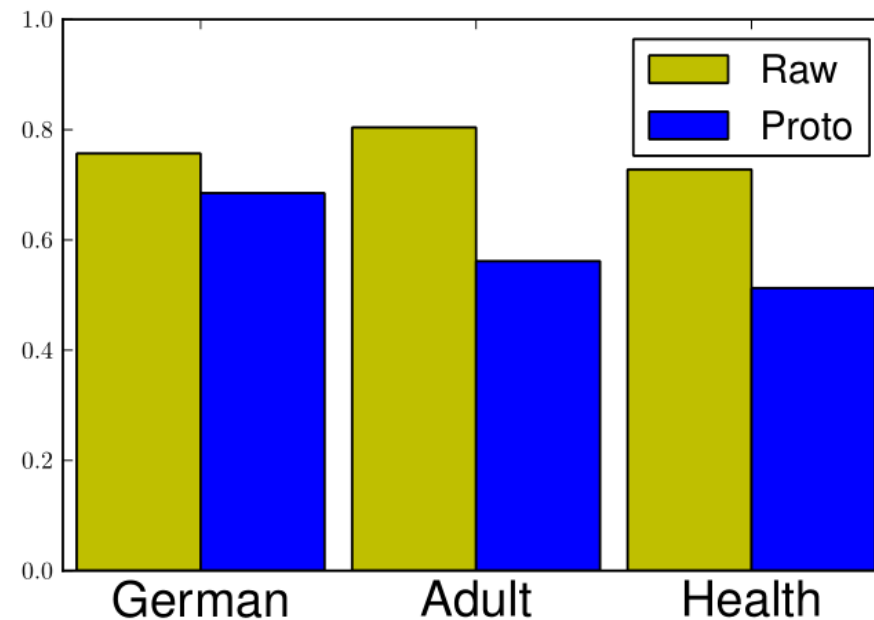


# Experiments

Results + Discussion 3: How well is information about  $S$  obfuscated?

Create a predictor which learns  $S$  from  $Z$ :  $\hat{s}_n = \sum_{k=1}^K P(Z = k | \mathbf{x}_n) u_k$

What are desirable values?  $\rightarrow$  lower bound: 0.5



# Big Picture Contributions

## Technical Contributions

- Framework achieves both **group** and **individual** fairness
- **Learning** framework: learn the weights of the distance function, as well as a fair intermediate representation with good properties.
- Mapping  $X \rightarrow Z$  can be generalized to samples not in the training set!

# Critic of the Paper

- + very **simple**, intuitively understandable framework
- + novel formulation of fairness as optimization
- Achieving individual fairness is either way very hard to achieve. Is individual fairness truly achieved here?
- LFR is currently only considered for binary classification.

End.