

LAB4. Flow Control Optimizations

Loop unrolling and Inlining

a)

i)

```
lab4_session/matriu4x4> ../../scripts/autopca -e ./matriu4x4.opt.g2 -g ./matriu4x4.g2 -n 10
[i] Comparant els outputs dels executables...
[i] Accounting de ./matriu4x4.g2, numero de repeticions: 10

    Max. elapsed:   .52 seconds
    Min. elapsed:   .51 seconds
    Avg. elapsed:   .5110 seconds

    Max. CPU time:  .51 seconds
    Min. CPU time:  .51 seconds
    Avg. CPU time:  .5100 seconds

    Max. CPU:       100%
    Min. CPU:       99%
    Avg. CPU:       99.30%

[i] Accounting de ./matriu4x4.opt.g2, numero de repeticions: 10

    Max. elapsed:   .46 seconds
    Min. elapsed:   .46 seconds
    Avg. elapsed:   .4600 seconds

    Max. CPU time:  .46 seconds
    Min. CPU time:  .45 seconds
    Avg. CPU time:  .4590 seconds

    Max. CPU:       100%
    Min. CPU:       99%
    Avg. CPU:       99.10%

[i] Calcul del Speedup
    Speedup elapsed: 1.1108
    Speedup CPU: 1.1111
```

ii)

```
Samples: 1K of event 'branches', Event count (approx.): 844111092
Overhead Command Shared Object Symbol
 100.00% matriu4x4.opt.g2 matriu4x4.opt.g2 [.] main
   0.00% perf [kernel.kallsyms] [k] perf_event_exec
```

844M de branches

		nop
0.43	88:	mov %rsp,%r11
		mov %rdi,%rbp
	8e:	lea 0x40(%rsp),%r8
		mov %rbp,%r10
0.33	96:	mov (%r10),%esi
4.61		lea 0x40(%r8),%r9
6.52		mov %r8,%rax
		mov %r11,%rcx
8.36	a3:	mov (%rcx),%edx
9.99		add \$0x10,%rax
11.23		add \$0x4,%rcx
10.97		imul -0x10(%rax),%edx
13.57		add %edx,%esi
15.96		cmp %r9,%rax
	↑	jne a3
0.04		add \$0x4,%r8
3.53		mov %esi,(%r10)
12.44		add \$0x4,%r10
		cmp %rbx,%r8
	↑	jne 96
		add \$0x10,%r11
0.05		add \$0x10,%rbp
1.95		cmp %r12,%r11
	↑	jne 8e
		add \$0x1,%r13d
		cmp %r13d,%r14d
		ja 88
	de: →	callq print_matriu

iii)

multiplica: $((6 \cdot n_iter) \cdot (7 \cdot 4) \cdot (7 \cdot 4) \cdot (8 \cdot 4)) = 150528 \cdot n_iter$

for_ITER: // 6 ins * niter

mov -0x8(%rsp),%r11

mov %r15,%r12

mov %rdi,%rbp

for_I: // 7 ins * 4

lea -0x10(%r12),%r10

mov %rsi,%rbx

for_J: // 7 ins * 4

mov (%r10),%r9d

mov %rbx,%r8

mov %rbp,%rax

for_K: // 8 ins * 4

mov (%rax),%edx

add \$0x4,%rax

add \$0x10,%r8

imul -0x10(%r8),%edx

add %edx,%r9d

cmp %rax,%r11

mov %r9d,(%r10)

jne for_K

add \$0x4,%r10

add \$0x4,%rbx

cmp %r10,%r12

jne for_J

add \$0x10,%rbp

add \$0x10,%r12

add \$0x10,%r11

cmp %r13,%rbp

jne for_I

add \$0x1,%r14d

cmp %ecx,%r14d

jne for_ITER

- b)
- i)

Timing de inlining - unrolling amb només inlining

```
lab4_session/matriu4x4> ../../scripts/autopca -e ./matriu4x4.optk.g2 -g ./matriu4x4.opt.g2 -n 10
[i] Comparant els outputs dels executables...
[i] Accounting de ./matriu4x4.opt.g2, numero de repeticions: 10

    Max. elapsed:  .46 seconds
    Min. elapsed:  .46 seconds
    Avg. elapsed:  .4600 seconds

    Max. CPU time:  .46 seconds
    Min. CPU time:  .45 seconds
    Avg. CPU time:  .4590 seconds

    Max. CPU:      100%
    Min. CPU:      99%
    Avg. CPU:      99.30%

[i] Accounting de ./matriu4x4.optk.g2, numero de repeticions: 10

    Max. elapsed:  .22 seconds
    Min. elapsed:  .21 seconds
    Avg. elapsed:  .2110 seconds

    Max. CPU time:  .21 seconds
    Min. CPU time:  .21 seconds
    Avg. CPU time:  .2100 seconds

    Max. CPU:      100%
    Min. CPU:      99%
    Avg. CPU:      99.10%

[i] Calcul del Speedup
    Speedup elapsed: 2.1800
    Speedup CPU: 2.1857
```

Timing amb la versió original.

```

lab4_session/matriu4x4> ../../scripts/autopca -e ./matriu4x4.optk.g2 -g ./matriu4x4.g2 -n 10
[i] Comparant els outputs dels executables...
[i] Accounting de ./matriu4x4.g2, numero de repeticions: 10

    Max. elapsed: .53 seconds
    Min. elapsed: .51 seconds
    Avg. elapsed: .5150 seconds

    Max. CPU time: .53 seconds
    Min. CPU time: .51 seconds
    Avg. CPU time: .5130 seconds

    Max. CPU:      100%
    Min. CPU:      99%
    Avg. CPU:      99.40%

[i] Accounting de ./matriu4x4.optk.g2, numero de repeticions: 10

    Max. elapsed: .22 seconds
    Min. elapsed: .21 seconds
    Avg. elapsed: .2180 seconds

    Max. CPU time: .22 seconds
    Min. CPU time: .21 seconds
    Avg. CPU time: .2110 seconds

    Max. CPU:      100%
    Min. CPU:      99%
    Avg. CPU:      99.30%

[i] Calcul del Speedup
    Speedup elapsed: 2.3623
    Speedup CPU: 2.4312

```

um

ii)

Samples: 874 of event 'cycles', 4000 Hz, Event count (approx.): 746435319			
main /home2/users/alumnes/1227356/PCA/PCA-FIB/LAB4/lab4_session/matriu4x4/matriu4x4.optk.g2			
Percent	unsigned int n_iter=N_ITER, i,j;		
	xor %r13d,%r13d		
	lea 0x10(%r12),%rbx		
	nop		
0.11	88:	mov %rsp,%rsi	
0.11		mov %rdi,%rbp	
	n_iter = atoi(argv[1]);		
	}		
	MULTIPLICA(A, B, C, n_iter);		
1.25	8e:	mov (%rsi),%r11d	
1.48		mov 0x4(%rsi),%r10d	
1.87		lea 0x40(%rsp),%rdx	
0.79		mov 0x8(%rsi),%r9d	
1.25		mov 0xc(%rsi),%r8d	
1.25		mov %rbp,%rcx	
5.35	a5:	mov (%rdx),%eax	
4.30		mov 0x10(%rdx),%r15d	
5.68		add \$0x4,%rdx	
5.33		add \$0x4,%rcx	
3.68		imul %r11d,%eax	
5.68		add -0x4(%rcx),%eax	
4.99		imul %r10d,%r15d	
5.65		add %r15d,%eax	
4.20		mov 0x1c(%rdx),%r15d	
6.48		imul %r9d,%r15d	
4.99		add %r15d,%eax	
6.04		mov 0x2c(%rdx),%r15d	
5.80		imul %r8d,%r15d	
5.69		add %r15d,%eax	
7.76		mov %eax,-0x4(%rcx)	
1.36		cmp %rdx,%rbx	
4.24	↑	jne a5	
0.79		add \$0x10,%rsi	
0.91		add \$0x10,%rbp	
		cmp %rsi,%r12	
2.16	↑	jne 8e	
0.68		add \$0x1,%r13d	
		cmp %r13d,%r14d	
0.11	↑	ja 88	

Samples: 878 of event 'branches', Event count (approx.): 210320059

Overhead	Command	Shared Object	Symbol
99.96%	matriu4x4.optk.	matriu4x4.optk.g2	[.] main
0.04%	matriu4x4.optk.	[kernel.kallsyms]	[k] unmap_page_range
0.00%	matriu4x4.optk.	[kernel.kallsyms]	[k] prepend_name
0.00%	matriu4x4.optk.	[kernel.kallsyms]	[k] __vma_adjust
0.00%	matriu4x4.optk.	[kernel.kallsyms]	[k] rcu_irq_exit
0.00%	perf	[kernel.kallsyms]	[k] perf_event_exec

210M branches → s'han reduït considerablement.

iii)

	88:	mov	%rsp,%rsi	
		mov	%rdi,%rbp	
		n_iter = atoi(argv[1]);		
		}		
		MULTIPLICA(A, B, C, n_iter);		
0.91	8e:	mov	(%rsi),%r11d	
		mov	0x4(%rsi),%r10d	
		lea	0x40(%rsp),%rdx	
		mov	0x8(%rsi),%r9d	
		mov	0xc(%rsi),%r8d	
		mov	%rbp,%rcx	
7.51	a5:	mov	(%rdx),%eax	
9.20		mov	0x10(%rdx),%r15d	
8.38		add	\$0x4,%rdx	
7.41		add	\$0x4,%rcx	
0.81		imul	%r11d,%eax	
0.23		add	-0x4(%rcx),%eax	
8.22		imul	%r10d,%r15d	
5.12		add	%r15d,%eax	
4.11		mov	0x1c(%rdx),%r15d	
5.13		imul	%r9d,%r15d	
4.83		add	%r15d,%eax	
1.18		mov	0x2c(%rdx),%r15d	
6.80		imul	%r8d,%r15d	
4.84		add	%r15d,%eax	
1.25		mov	%eax,-0x4(%rcx)	
10.52		cmp	%rdx,%rbx	
	↑	jne	a5	
4.56		add	\$0x10,%rsi	
4.67		add	\$0x10,%rbp	
3.87		cmp	%rsi,%r12	
	↑	jne	8e	
0.46		add	\$0x1,%r13d	
		cmp	%r13d,%r14d	
	↑	ja	88	

$17 \cdot 4 \cdot 10 \cdot 4 \cdot 5 \cdot N_iter = 13600 \cdot N_iter$

c)

i)

```

lab4_session/matriu4x4> ../../../../scripts/autopca -e ./matriu4x4.optj.g2 -g ./matriu4x4.g2 -n 10
[i] Comparant els outputs dels executables...
[i] Accounting de ./matriu4x4.g2, numero de repeticions: 10

    Max. elapsed:    .51 seconds
    Min. elapsed:    .51 seconds
    Avg. elapsed:    .5100 seconds

    Max. CPU time:   .51 seconds
    Min. CPU time:   .51 seconds
    Avg. CPU time:   .5100 seconds

    Max. CPU:        100%
    Min. CPU:         99%
    Avg. CPU:         99.40%

[i] Accounting de ./matriu4x4.optj.g2, numero de repeticions: 10

    Max. elapsed:    .19 seconds
    Min. elapsed:    .19 seconds
    Avg. elapsed:    .1900 seconds

    Max. CPU time:   .18 seconds
    Min. CPU time:   .18 seconds
    Avg. CPU time:   .1800 seconds

    Max. CPU:         99%
    Min. CPU:         98%
    Avg. CPU:         98.90%

[i] Calcul del Speedup
    Speedup elapsed: 2.6842
    Speedup CPU: 2.8333

lab4_session/matriu4x4> ../../../../scripts/autopca -e ./matriu4x4.optj.g2 -g ./matriu4x4.optk.g2 -n 10
[i] Comparant els outputs dels executables...
[i] Accounting de ./matriu4x4.optk.g2, numero de repeticions: 10

    Max. elapsed:    .22 seconds
    Min. elapsed:    .21 seconds
    Avg. elapsed:    .2110 seconds

    Max. CPU time:   .21 seconds
    Min. CPU time:   .21 seconds
    Avg. CPU time:   .2100 seconds

    Max. CPU:         99%
    Min. CPU:         99%
    Avg. CPU:         99.00%

[i] Accounting de ./matriu4x4.optj.g2, numero de repeticions: 10

    Max. elapsed:    .19 seconds
    Min. elapsed:    .19 seconds
    Avg. elapsed:    .1900 seconds

    Max. CPU time:   .18 seconds
    Min. CPU time:   .18 seconds
    Avg. CPU time:   .1800 seconds

    Max. CPU:         99%
    Min. CPU:         98%
    Avg. CPU:         98.90%

[i] Calcul del Speedup
    Speedup elapsed: 1.1105
    Speedup CPU: 1.1666

```

ii)
Cicles:

Samples: 753 of event 'cycles', 4000 Hz, Event count (approx.): 645840077	
main /home2/users/alumnes/1227356/PCA/PCA-FIB/LAB4/lab4_session/matriu4x4/matriu4x4.optj.g2 [Percent	
Percent	
	MULTIPLICA(A, B, C, n_iter);
75:	mov 0x94(%rsp),%eax
	mov 0x80(%rsp),%r15d
	lea 0x100(%rsp),%r11
	mov 0x90(%rsp),%r14d
	mov 0xa0(%rsp),%r13d
	mov 0xb0(%rsp),%r12d
	mov 0x84(%rsp),%ebp
	mov %eax,0x8(%rsp)
	mov 0xa4(%rsp),%eax
	mov 0xbc(%rsp),%ebx
	movl \$0x0,0x38(%rsp)
	mov %eax,0xc(%rsp)
	mov 0xb4(%rsp),%eax
	mov %eax,0x10(%rsp)
	mov 0x88(%rsp),%eax
	mov %eax,0x14(%rsp)
	mov 0x98(%rsp),%eax
	mov %eax,0x18(%rsp)
	mov 0xa8(%rsp),%eax
	mov %eax,0x1c(%rsp)
	mov 0xb8(%rsp),%eax
	mov %eax,0x20(%rsp)
	mov 0x8c(%rsp),%eax
	mov %eax,0x24(%rsp)
	mov 0x9c(%rsp),%eax
	mov %eax,0x28(%rsp)
	mov 0xac(%rsp),%eax
	mov %eax,0x2c(%rsp)
	lea 0xc0(%rsp),%rax
	mov %rax,0x30(%rsp)
	xchg %ax,%ax
130:	mov 0x30(%rsp),%r9
1.31	lea 0x40(%rsp),%r10
0.26	13a: mov (%r10),%ecx
4.11	mov 0x4(%r10),%edx
0.39	mov 0x8(%r10),%eax
1.31	mov 0xc(%r10),%esi
	mov %ecx,%r8d
4.13	mov %edx,%edi
0.26	imul %r15d,%r8d
2.83	add (%r9),%r8d
0.26	imul %r14d,%edi
5.10	add %edi,%r8d
0.39	mov %eax,%edi
1.05	imul %r13d,%edi
0.26	add %r8d,%edi
3.80	mov %esi,%r8d
0.13	imul %r12d,%r8d
1.99	add %r8d,%edi
	mov %ecx,%r8d
5.13	mov %edi,(%r9)
0.13	mov 0x8(%rsp),%edi
1.56	imul %ebp,%r8d
0.26	add 0x4(%r9),%r8d
3.93	imul %edx,%edi
	add %edi,%r8d
2.63	mov 0xc(%rsp),%edi

Branches:

Samples: 760 of event 'branches', Event count (approx.): 50208700			
Overhead	Command	Shared Object	Symbol
99.87%	matriu4x4.optj.	matriu4x4.optj.g2	[.] main
0.13%	matriu4x4.optj.	libc-2.26.so	[.] _dl_addr
0.00%	perf	[kernel.kallsyms]	[k] perf_event_exec

50M de branches

iii)

33 (tots els moves de l'inici) + $57 \cdot 4 \cdot 6 \cdot N_{\text{iter}} = 33 + 1368 \cdot N_{\text{iter}}$

d)

i) No s'ha pogut fer el timing amb el GNU time ja que aquest només permet precisió fins a les centèsimes de segon. Hem usat el time de bash que té precisió fins als mil·lisegons per a poder calcular el speedup.

Speedup respecte la versió anterior:

```
dhap0@kali:~/UNI/pca/PCA-FIB/LAB4/lab4_session/matriu4x4$ time ./matriu4x4.opti.g2
1400780143 -768217222 804885694 1856772449
197236110 1678700198 -487200378 1332173696
1284348296 -1124999449 1954104691 -232562345
-1547499970 -879578979 1049980953 -877687785

real    0m0.004s
user    0m0.003s
sys     0m0.002s

dhap0@kali:~/UNI/pca/PCA-FIB/LAB4/lab4_session/matriu4x4$ time ./matriu4x4.optj.g2
1400780143 -768217222 804885694 1856772449
197236110 1678700198 -487200378 1332173696
1284348296 -1124999449 1954104691 -232562345
-1547499970 -879578979 1049980953 -877687785

real    0m0.313s
user    0m0.309s
sys     0m0.005s

dhap0@kali:~/UNI/pca/PCA-FIB/LAB4/lab4_session/matriu4x4$ python -c "print(0.313/0.004)"
78.25
```

Speedup respecte la versió original:

```
dhap0@kali:~/UNI/pca/PCA-FIB/LAB4/lab4_session/matriu4x4$ time ./matriu4x4.opti.g2
1400780143 -768217222 804885694 1856772449
197236110 1678700198 -487200378 1332173696
1284348296 -1124999449 1954104691 -232562345
-1547499970 -879578979 1049980953 -877687785

real    0m0.002s
user    0m0.001s
sys     0m0.000s

dhap0@kali:~/UNI/pca/PCA-FIB/LAB4/lab4_session/matriu4x4$ time ./matriu4x4.opt.g2
1400780143 -768217222 804885694 1856772449
197236110 1678700198 -487200378 1332173696
1284348296 -1124999449 1954104691 -232562345
-1547499970 -879578979 1049980953 -877687785

real    0m0.636s
user    0m0.636s
sys     0m0.001s

dhap0@kali:~/UNI/pca/PCA-FIB/LAB4/lab4_session/matriu4x4$ python -c "print(0.636/0.002)"
318.0
```

ii)

Hem reduït considerablement el nombre de branches de 50 milions a 36.237.

quinnod@mx: ~/UPC/PCA/PCA-FIB/LAB4/lab4_session/matriu4x4

Samples: 27 of event 'branches:u', Event count (approx.): 36237			
Overhead	Command	Shared Object	Symbol
25,99%	matriu4x4.opti.	ld-2.33.so	[.] __GI___tunables_init
24,06%	matriu4x4.opti.	ld-2.33.so	[.] _dl_relocate_object
14,21%	matriu4x4.opti.	ld-2.33.so	[.] _dl_map_object_from_fd
13,56%	matriu4x4.opti.	ld-2.33.so	[.] intel_check_word.constprop.0
11,02%	matriu4x4.opti.	ld-2.33.so	[.] _dl_lookup_symbol_x

iii)

gracies a:

<https://stackoverflow.com/questions/13313510/quick-way-to-count-number-of-instructions-executed-in-a-c-program>

```

36     if (argc > 1) {
35         n_iter = atoi(argv[1]);
34     }
33 ///////////////////////////////////////////////////////////////////
32 // baines rares per contar instruccions
31 ///////////////////////////////////////////////////////////////////
30     struct perf_event_attr pe;
29     long long count;
28     int fd;
27     memset(&pe, 0, sizeof(struct perf_event_attr));
26     pe.type = PERF_TYPE_HARDWARE;
25     pe.size = sizeof(struct perf_event_attr);
24     pe.config = PERF_COUNT_HW_INSTRUCTIONS;
23     pe.disabled = 1;
22     pe.exclude_kernel = 1;
21     // Don't count hypervisor events.
20     pe.exclude_hv = 1;
19
18     fd = perf_event_open(&pe, 0, -1, -1, 0);
17     if (fd == -1) {
16         fprintf(stderr, "Error opening leader %llx\n", pe.config);
15         exit(EXIT_FAILURE);
14     }
13
12     ioctl(fd, PERF_EVENT_IOC_RESET, 0);
11     ioctl(fd, PERF_EVENT_IOC_ENABLE, 0);
10
9 // macro que ens interessa
8
7     MULTIPLICA(A, B, C, n_iter);
6
5     ioctl(fd, PERF_EVENT_IOC_DISABLE, 0);
4 // lectura de instruccions
3     ioctl(fd, PERF_EVENT_IOC_DISABLE, 0);
2     read(fd, &count, sizeof(long long));
1
146 printf("Used %lld instructions\n", count);

```

```
dhap0@kali:~/UNI/pca/PCA-FIB/LAB4/lab4_session/matriu4x4$ sudo !!
sudo ./matriu4x4.opti.g2
Used 430 instructions
1400780143 -768217222 804885694 1856772449
197236110 1678700198 -487200378 1332173696
1284348296 -1124999449 1954104691 -232562345
-1547499970 -879578979 1049980953 -877687785
```

hem passat de les $(33 + 1368 * N_iter)$ instruccions a només 430

(e)

La versió més ràpida amb diferència és la del full-unroll, ja que obte un speedup de 318 respecte l'original i passa dels 844 milions de salts que tenia la primera versió del codi a només 36.237 salts.

(f)

```

34
33 void multiplica(int A[4][4], int B[4][4], int C[4][4], unsigned int n_iter)
32 {
31     int iter;
30     int i,j,k;
29
28     for (iter=0; iter<n_iter; iter++)
27     {
26         C[0][0] = C[0][0] + A[0][0] * B[0][0];
25 C[0][0] = C[0][0] + A[0][1] * B[1][0];
24 C[0][0] = C[0][0] + A[0][2] * B[2][0];
23 C[0][0] = C[0][0] + A[0][3] * B[3][0];
22 C[0][1] = C[0][1] + A[0][0] * B[0][1];
21 C[0][1] = C[0][1] + A[0][1] * B[1][1];
20 C[0][1] = C[0][1] + A[0][2] * B[2][1];
19 C[0][1] = C[0][1] + A[0][3] * B[3][1];
18 C[0][2] = C[0][2] + A[0][0] * B[0][2];
17 C[0][2] = C[0][2] + A[0][1] * B[1][2];
16 C[0][2] = C[0][2] + A[0][2] * B[2][2];
15 C[0][2] = C[0][2] + A[0][3] * B[3][2];
14 C[0][3] = C[0][3] + A[0][0] * B[0][3];
13 C[0][3] = C[0][3] + A[0][1] * B[1][3];
12 C[0][3] = C[0][3] + A[0][2] * B[2][3];
11 C[0][3] = C[0][3] + A[0][3] * B[3][3];
10 C[1][0] = C[1][0] + A[1][0] * B[0][0];
9 C[1][0] = C[1][0] + A[1][1] * B[1][0];
8 C[1][0] = C[1][0] + A[1][2] * B[2][0];
7 C[1][0] = C[1][0] + A[1][3] * B[3][0];
6 C[1][1] = C[1][1] + A[1][0] * B[0][1];
5 C[1][1] = C[1][1] + A[1][1] * B[1][1];
4 C[1][1] = C[1][1] + A[1][2] * B[2][1];
3 C[1][1] = C[1][1] + A[1][3] * B[3][1];
2 C[1][2] = C[1][2] + A[1][0] * B[0][2];
1 C[1][2] = C[1][2] + A[1][1] * B[1][2];
0 C[1][2] = C[1][2] + A[1][2] * B[2][2];
/UPC/PCA/PCA-FIB/LAB4/lab4_session/matriu4x4/matriu4x4.unroll_no_inline.c 36%

```

Com podem veure a la captura següent hi ha un canvi considerable entre els 0,004s que triga la versió amb inlining i els 0,291 que es triguen sense inlining:

```

16:40 quim: ~/UPC/PCA/PCA-FIB/LAB4/lab4_session/matriu4x4 [main]$ time ./matriu4x4.opti.g2
1400780143 -768217222 804885694 1856772449
197236110 1678700198 -487200378 1332173696
1284348296 -1124999449 1954104691 -232562345
-1547499970 -879578979 1049980953 -877687785

real    0m0,004s
user    0m0,001s
sys      0m0,004s
16:41 quim: ~/UPC/PCA/PCA-FIB/LAB4/lab4_session/matriu4x4 [main]$ time ./matriu4x4.unroll_no_inline
1400780143 -768217222 804885694 1856772449
197236110 1678700198 -487200378 1332173696
1284348296 -1124999449 1954104691 -232562345
-1547499970 -879578979 1049980953 -877687785

real    0m0,291s
user    0m0,289s
sys      0m0,001s

```

Això és degut a que el compilador no pot preveure els paràmetres que es passen a la funció quan no es fa inlining i per tant no pot aplicar certes optimitzacions en el codi de la funció que si que podria fer en el cas de que es fes inlining.

Optimizacions de Pi.c

Unrolling

Fent profiling de la nostra millor versió de la pràctica anterior veiem que hi ha molts salts a les funcions calculate (que executa els divides) i LONGDIV.

Overhead	Command	Shared Object	Symbol
79.72%	pi.opt3.g3	pi.opt3.g3	[.] calculate
18.32%	pi.opt3.g3	pi.opt3.g3	[.] LONGDIV
0.11%	pi.opt3.g3	[kernel.kallsyms]	[k] psi_group_change

887,3 M de branches.

Per a començar apliquem un unroll de 2:

```

#define BODY_FOR_CALCULATE(j) {\
    SET( c, 1 );\
    LONGDIV( c, j );\
\
    SUBTRACT( a, c, a );\
    DIVIDE_25( a );\
\
    SUBTRACT( b, c, b );\
    DIVIDE_239( b );\
    DIVIDE_239( b );\
\
    progress();\
}

#define BODY_FOR_DIVIDE(k) {\
    u = r * 10 + x[k];\
    q = u/n;\
    r = u - q * n; \
    x[k] = q;}
#define BODY_FOR_DIVIDE239(k) {\
    u = r * 10 + x[k]; \
    x[k] = memo_q239[u];\
    r = memo_r239[u];}
#define BODY_FOR_DIVIDE25(k) {\
    u = r * 10 + x[k];\
    x[k] = memo_q25[u];\
    r = memo_r25[u];}
#define BODY_FOR_DIVIDE5(k) {\
    u = r * 10 + x[k];\
    x[k] = memo_q5[u];\
    r = memo_r5[u];}

```

```

void DIVIDE( signed char *x, int n )
{
    int j, k;
    unsigned q, r, u;
    long v;

    r = 0;
    for( k = 0; k+1 <= N4; k+=2 )
    {
        BODY_FOR_DIVIDE(k)
        BODY_FOR_DIVIDE(k+1)
    }
    for(;k <= N4; k++) BODY_FOR_DIVIDE(k);
}

void DIVIDE_239( signed char *x)
{
    int j, k;
    unsigned q, r, u;
    long v;

    r = 0;
    for( k = 0; k+1 <= N4; k+=2 )
    {
        BODY_FOR_DIVIDE239(k);
        BODY_FOR_DIVIDE239(k+1);
    }
    for(;k <= N4; k++) BODY_FOR_DIVIDE239(k);
}

```

```

void DIVIDE_25( signed char *x)
{
    int j, k;
    unsigned q, r, u;
    long v;

    r = 0;
    for( k = 0; k+1 <= N4; k+=2 )
    {
        BODY_FOR_DIVIDE25(k);
        BODY_FOR_DIVIDE25(k+1);
    }
    for(;k <= N4; k++) BODY_FOR_DIVIDE25(k);
}
//Dividir entre 25 es dividir entre 5 dos cops
void DIVIDE_5( signed char *x)
{
    int j, k;
    unsigned q, r, u;
    long v;

    r = 0;
    for( k = 0; k+1 <= N4; k+=2 )
    {
        BODY_FOR_DIVIDE5(k);
        BODY_FOR_DIVIDE5(k+1);
    }
    for(;k <= N4; k++) BODY_FOR_DIVIDE5(k);
}

```

Timing d'aquesta versió anomenada **pi.opt6.c** que obté un speedup respecte el laboratori anterior de **1.0031**:

```
dhap0@kali:~/UNI/pca/PCA-FIB/LAB4/lab4_session/pi$ ../../../../scripts/autopca -e ./pi.opt6.g3 -g ./pi.opt3.g3 -n 5
[i] Comparant els outputs dels executables ...
[i] Accounting de ./pi.opt3.g3, numero de repeticions: 5
Max. elapsed: 3.89 seconds
Min. elapsed: 3.88 seconds
Avg. elapsed: 3.8820 seconds

Max. CPU time: 3.88 seconds
Min. CPU time: 3.87 seconds
Avg. CPU time: 3.8780 seconds

Max. CPU: 100%
Min. CPU: 99%
Avg. CPU: 99.20%

[i] Accounting de ./pi.opt6.g3, numero de repeticions: 5
Max. elapsed: 3.87 seconds
Min. elapsed: 3.87 seconds
Avg. elapsed: 3.8700 seconds

Max. CPU time: 3.87 seconds
Min. CPU time: 3.86 seconds
Avg. CPU time: 3.8640 seconds

Max. CPU: 100%
Min. CPU: 99%
Avg. CPU: 99.20%

[i] Calcul del Speedup
Speedup elapsed: 1.0031
Speedup CPU: 1.0036
```

I al profiling veiem que hem reduït el nombre de branches:

```
Samples: 15K of event 'branches', Event count (approx.): 738298132
Overhead Command Shared Object Symbol
75.27% pi.opt6.g3 pi.opt6.g3 [.] calculate
22.25% pi.opt6.g3 pi.opt6.g3x Format[.] LONGDIV implements Ajuda
0.14% pi.opt6.g3 [kernel.kallsyms] [k] psi_group_change
0.13% pi.opt6.g3 [kernel.kallsyms] [k] select_task_rq_fair
```

Si apliquem un unroll de 4 perdem tot l'speedup:

```
dhap0@kali:~/UNI/pca/PCA-FIB/LAB4/lab4_session/pi$ ../../../../scripts/autopca -e ./pi.opt4.g3 -g ./pi.opt3.g3 -n 5
[i] Comparant els outputs dels executables ...
[i] Accounting de ./pi.opt3.g3, numero de repeticions: 5
Max. elapsed: 3.88 seconds
Min. elapsed: 3.88 seconds
Avg. elapsed: 3.8800 seconds

Max. CPU time: 3.88 seconds
Min. CPU time: 3.87 seconds
Avg. CPU time: 3.8720 seconds

Max. CPU: 99%
Min. CPU: 99%
Avg. CPU: 99.00%

[i] Accounting de ./pi.opt4.g3, numero de repeticions: 5
Max. elapsed: 3.91 seconds
Min. elapsed: 3.90 seconds
Avg. elapsed: 3.9040 seconds

Max. CPU time: 3.90 seconds
Min. CPU time: 3.90 seconds
Avg. CPU time: 3.9000 seconds

Max. CPU: 100%
Min. CPU: 99%
Avg. CPU: 99.20%

[i] Calcul del Speedup
Speedup elapsed: .9938
Speedup CPU: .9928
```

unroll de 4:

Analitzant el codi i valorant les possibilitats d'unrolling, fem unrolling 4 a les funcions calculate i als diferents DIVIDES especialitzats que havíem fet a la pràctica anterior.

Samples: 15K of event 'branches', Event count (approx.): 661963693			
Overhead	Command	Shared Object	Symbol
60.48%	pi.opt4.g3	pi.opt4.g3	[.] calculate
24.56%	pi.opt4.g3	pi.opt4.g3	[.] LONGDIV implements Ajuda
8.07%	pi.opt4.g3	pi.opt4.g3	[.] DIVIDE_239
4.05%	pi.opt4.g3	pi.opt4.g3	[.] DIVIDE_25
0.18%	pi.opt4.g3	[kernel.kallsyms]	[k] psi_group_change
0.11%	pi.opt4.g3	[kernel.kallsyms]	[k] try_to_wake_up

Doncs la versió definitiva d'aquesta secció de la pràctica és **pi.opt6.c** que ens dona un speedup respecte el pi.c original de **1.0945**.

```
dhap0@kali:~/UNI/pca/PCA-FIB/LAB4/lab4_session/pi$ ../../scripts/autopca -e ./pi.opt6.g3 -g ./pi.g3 -n 10
[i] Comparant els outputs dels executables ...
[i] Accounting de ./pi.g3, numero de repeticions: 10

Max. elapsed: 4.25 seconds
Min. elapsed: 4.23 seconds
Avg. elapsed: 4.2360 seconds

Max. CPU time: 4.24 seconds
Min. CPU time: 4.22 seconds
Avg. CPU time: 4.2280 seconds

Max. CPU: 100%
Min. CPU: 99%
Avg. CPU: 99.10%

[i] Accounting de ./pi.opt6.g3, numero de repeticions: 10

Max. elapsed: 3.87 seconds
Min. elapsed: 3.87 seconds
Avg. elapsed: 3.8700 seconds

Max. CPU time: 3.87 seconds
Min. CPU time: 3.86 seconds
Avg. CPU time: 3.8650 seconds

Max. CPU: 100%
Min. CPU: 99%
Avg. CPU: 99.10%

[i] Calcul del Speedup
Speedup elapsed: 1.0945
Speedup CPU: 1.0939
```

LoopFusion

Fusionem els DIVIDE_239 i els SUBTRACT(a,c,a) i SUBTRACT (b,c,b) de la següent fracció de codi:

```
#define BODY_FOR_CALCULATE(j) {\
    SET( c, 1 );\
    LONGDIV( c, j );\
\
    SUBTRACT( a, c, a );\
    DIVIDE_25( a );\
\
    SUBTRACT( b, c, b );\
    DIVIDE_239( b );\
    DIVIDE_239( b );\
\
    progress();\
}
```

De tal manera que la macro BODY_FOR_CALCULATE quedarà de la següent manera:


```

#define BODY_FOR_CALCULATE(j) {\
    SET( c, 1 );\
    LONGDIV( c, j );\
\
    SUBTRACT_FUSION_A_B(a,b,c,a,b);\
    DIVIDE_25( a );\
\
\
\
    DIVIDE_57121(b);\
\
    progress();\
}

```

i les noves funcions:

```

void SUBTRACT_FUSION_A_B( signed char *x, signed char *x2, signed char *y, signed char *z, signed char *z2)
{
    int j, k;
    unsigned q, r, u;
    long v;
    for( k = N4; k >= 1; k-- )
    {
        if( (x[k] = y[k] - z[k]) < 0 )
        {
            x[k] += 10;
            z[k-1]++;
        }

        if( (x2[k] = y[k] - z2[k]) < 0 )
        {
            x2[k] += 10;
            z2[k-1]++;
        }
    }
    if( (x[k] = y[k] - z[k]) < 0 )
    {
        x[k] += 10;
    }

    if( (x2[k] = y[k] - z2[k]) < 0 )
    {
        x2[k] += 10;
    }
}

```

```

void DIVIDE_57121( signed char *x)
{
    int j, k;
    unsigned q, r, u, r2;
    long v;

    r = 0;
    r2 = 0;
    for( k = 0; k+1 <= N4; k+=2 )
    {
        BODY_FOR_DIVIDE57121(k);
        BODY_FOR_DIVIDE57121(k+1);
    }
    for(; k <= N4; k++) BODY_FOR_DIVIDE57121(k);
}

```

```

#define BODY_FOR_DIVIDE57121(k) {\
    u = r * 10 + x[k]; \
    x[k] = memo_q239[u];\
    r = memo_r239[u];\
\
    u = r2 * 10 + x[k];\
    x[k] = memo_q239[u];\
    r2 = memo_r239[u];\
}

```

Aquesta nova versió que anomenem **pi.loopf.c** aconsegueix un speedup respecte el programa original de **1.2514**.

```
dhap00@kali:~/UNI/pca/PCA-FIB/LAB4/lab4_session/pi$ ../../scripts/autopca -e ./pi.loopf.g3 -g ./pi.g3 -n 3
[i] Comparant els outputs dels executables...
[i] Accounting de ./pi.g3, numero de repeticions: 3
    Max. elapsed: 4.23 seconds
    Min. elapsed: 4.23 seconds
    Avg. elapsed: 4.2300 seconds
    Max. CPU time: 4.23 seconds
    Min. CPU time: 4.22 seconds
    Avg. CPU time: 4.2233 seconds
    Max. CPU: 99%
    Min. CPU: 99%
    Avg. CPU: 99.00%
[i] Accounting de ./pi.loopf.g3, numero de repeticions: 3
    Max. elapsed: 3.39 seconds
    Min. elapsed: 3.37 seconds
    Avg. elapsed: 3.3800 seconds
    Max. CPU time: 3.38 seconds
    Min. CPU time: 3.36 seconds
    Avg. CPU time: 3.3700 seconds
    Max. CPU: 99%
    Min. CPU: 99%
    Avg. CPU: 99.00%
[i] Calcul del Speedup
    Speedup elapsed: 1.2514
    Speedup CPU: 1.2532
```

Removing Conditional Branches

En aquesta part de la pràctica es treballa en una versió que anomenarem **pi.loopf.opt2.c**. Aquest nou codi incorporerà la millora de les funcions SUBTRACT i LONGDIV per tal d'eliminar els salts condicionals per mitjà de bithacks. També s'ha afegit unroll a les funcions SUBTRACT que no s'havia incorporat anteriorment. La funció LONGDIV ha sigut canviada per la funció DIVIDE optimitzada amb unrolling.

Canvis a la funció SUBTRACT:

```
void SUBTRACT_OPT( signed char *x, signed char *y, signed char *z )
{
    int j, k;
    unsigned q, r, u;
    long v;
    signed char t;
    for( k = N4; k-1 >= 1; k-=2 )
    {
        BODY_SUBTRACT(k);
        BODY_SUBTRACT(k-1);
    }
    for ( ; k >= 1; k--) BODY_SUBTRACT(k);
    t = y[k] - z[k];
    x[k] = t;
    x[k] += (10 & (t>>7));
}
```



```

void DIVIDE( signed char *x, int n )
{
    int j, k;
    unsigned q, r, u;
    long v;

    r = 0;
    for( k = 0; k+1 <= N4; k+=2 )
    {
        BODY_FOR_DIVIDE(k)
        BODY_FOR_DIVIDE(k+1)
    }
    for(;k <= N4; k++) BODY_FOR_DIVIDE(k);
}

```

```

#define BODY_FOR_DIVIDE(k) {\
    u = r * 10 + x[k];\
    q = u/n;\
    r = u - q * n; \
    x[k] = q;}

```

Aquesta versió del codi és la definitiva. Entregada per l'usuari **pca06**, anomenat **pi.loopf.opt2.c** amb un speedup respecte l'original de **1.8851**.

```

|00:14:40|dhap0@bunker:[pi]$ ../../scripts/autopca -e ./pi.loopf.opt2.g3 -g ./pi.g3 -n 10
[i] Comparant els outputs dels executables...
[i] Acounting de ./pi.g3, numero de repeticions: 10

Max. elapsed: 2.30 seconds
Min. elapsed: 2.26 seconds
Avg. elapsed: 2.2810 seconds

Max. CPU time: 2.29 seconds
Min. CPU time: 2.26 seconds
Avg. CPU time: 2.2710 seconds

Max. CPU: 99%
Min. CPU: 99%
Avg. CPU: 99.00%

[i] Acounting de ./pi.loopf.opt2.g3, numero de repeticions: 10

Max. elapsed: 1.23 seconds
Min. elapsed: 1.19 seconds
Avg. elapsed: 1.2100 seconds

Max. CPU time: 1.22 seconds
Min. CPU time: 1.19 seconds
Avg. CPU time: 1.2020 seconds

Max. CPU: 99%
Min. CPU: 99%
Avg. CPU: 99.00%

[i] Calcul del Speedup
Speedup elapsed: 1.8851
Speedup CPU: 1.8893

```

La taula següent mostra els diferents speedups que s'han anat aconseguint en les diferents versions del codi pi.c.

