

# Leveraging Hardware Construction Languages for Flexible Design Space Exploration on FPGA

Bruno FERRES

Director: Frédéric ROUSSEAU, Prof. at Univ. Grenoble Alpes

Advisor: Olivier MULLER, Associate Prof. at Grenoble INP - Ensimag

System Level Synthesis - TIMA  
Université Grenoble Alpes



March 23, 2022







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VCU128 board from Xilinx

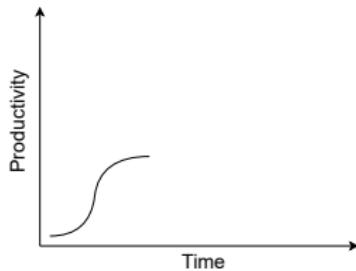


How to program this big circuit?

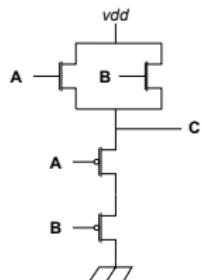
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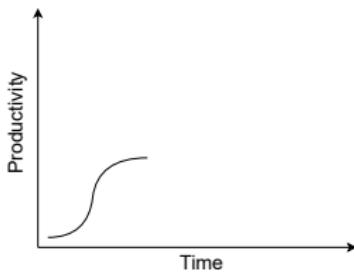
# Design Methodologies and Productivity



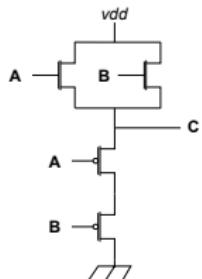
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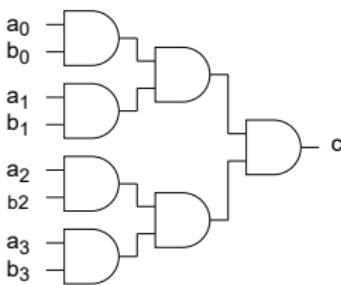
Circuit level



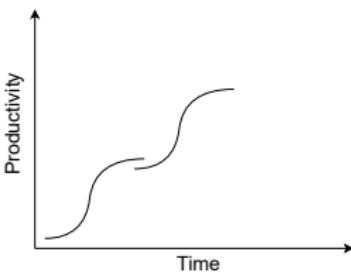
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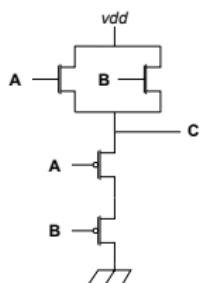
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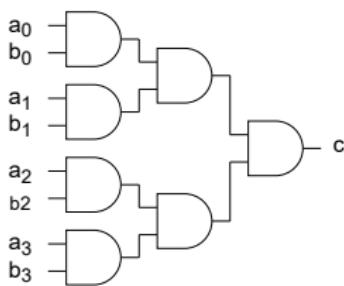
Logical level



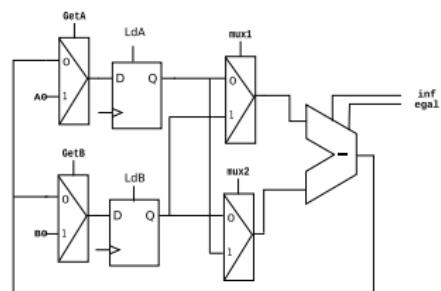
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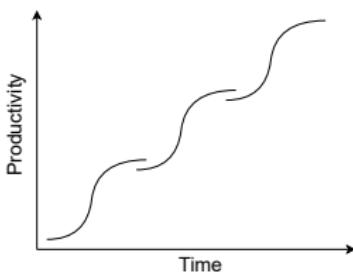
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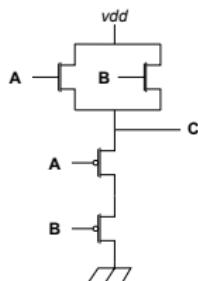
Logical level



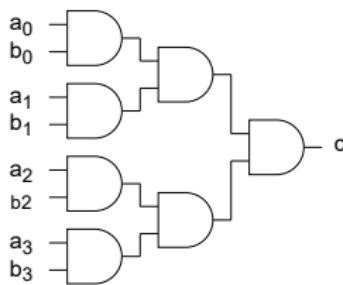
Register Transfer level



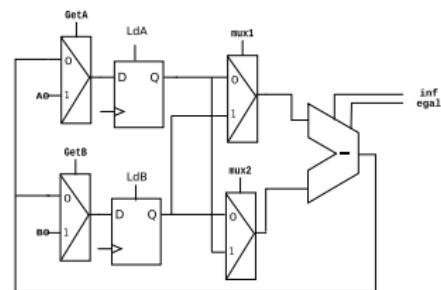
# Design Methodologies and Productivity



Circuit level



Logical level

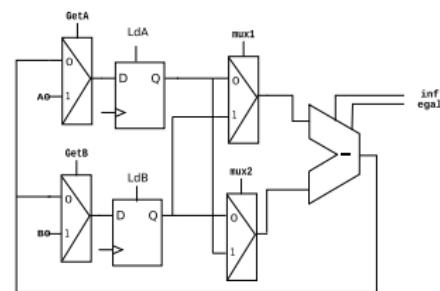
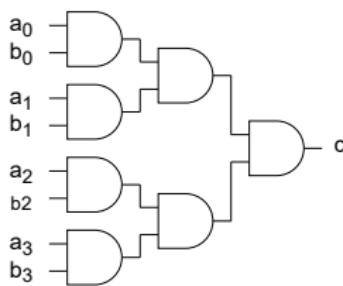
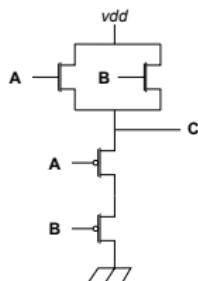


Register Transfer level

## Improving hardware designers productivity

- which **innovations** do we rely on?

# Design Methodologies and Productivity



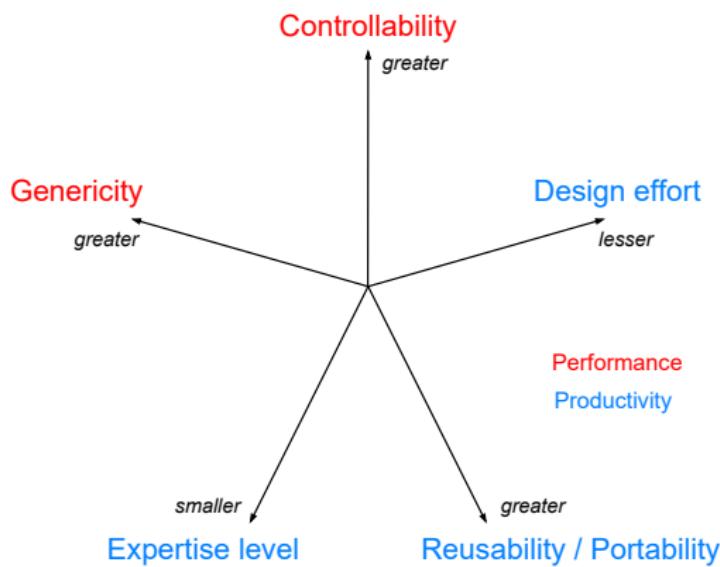
## Improving hardware designers productivity

- which **innovations** do we rely on?
- what is **productivity** when it comes to **hardware design**?

# Plan

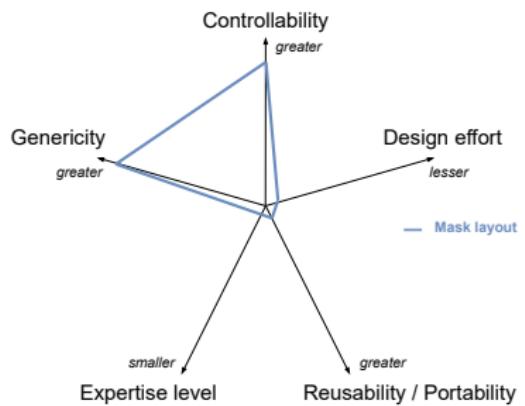
- 1** Context and Motivations
- 2** Proposed Methodologies
- 3** Quick Exploration using Chisel Estimators
- 4** Experiments and Results
- 5** Conclusion and Perspectives

# Characteristics of Design Methodologies



**Productivity** and **performance** criteria for hardware design

# Digital Design Methodologies

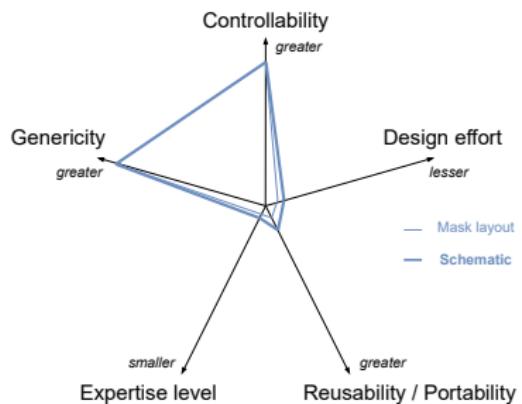


## A small history on digital design

■ IC mask layout

(circuit level)

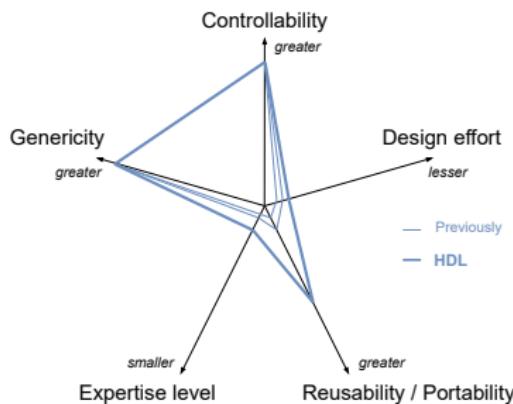
# Digital Design Methodologies



## A small history on digital design

- IC mask layout (circuit level)
- standard cells (logical level)

# Digital Design Methodologies



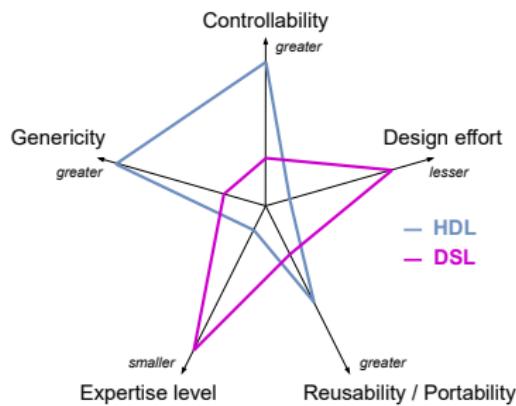
## A small history on digital design

- IC mask layout (circuit level)
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## Democratization of the HDLs

- Hardware Description Languages (Register Transfer Level)

# Digital Design Methodologies



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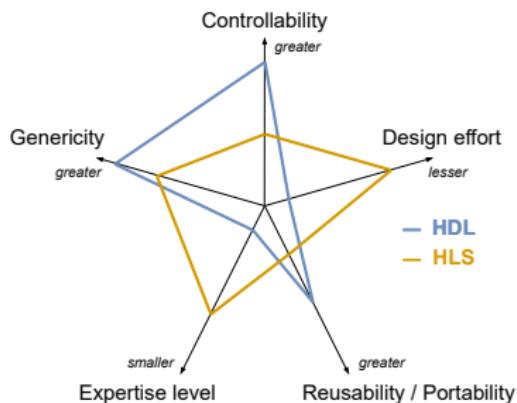
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## Existing alternatives (algorithmic level)

- Domain Specific Languages (DSL)

# Digital Design Methodologies



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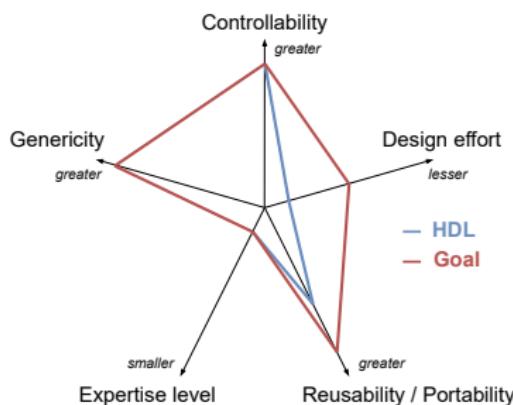
## Democratization of the HDLs

- **Hardware Description Languages (Register Transfer Level)**

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- **Domain Specific Languages (DSL)**
- **High Level Synthesis (HLS)**

# Digital Design Methodologies



## A small history on digital design

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## Democratization of the HDLs

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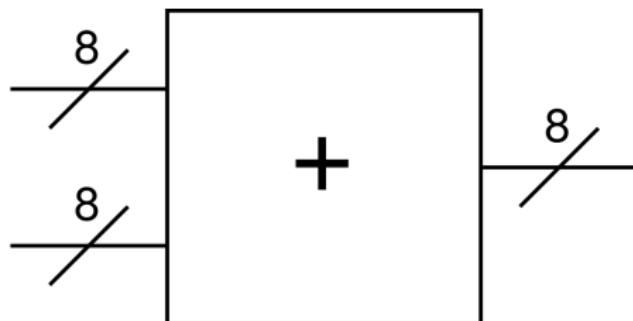
## Existing alternatives (algorithmic level)

- Domain Specific Languages (DSL)
- High Level Synthesis (HLS)

What now?

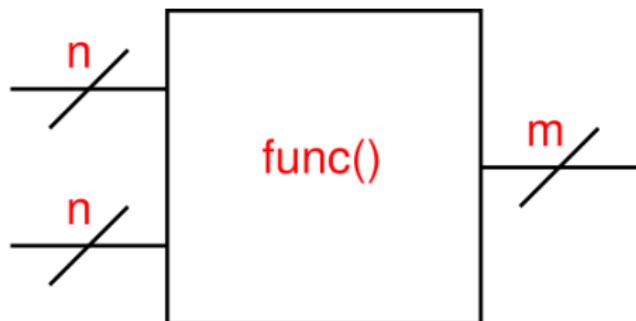
How to improve **productivity** while maintaining **performance**?

# Improving Reusability through Hardware Construction



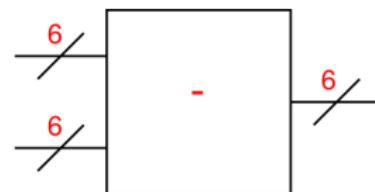
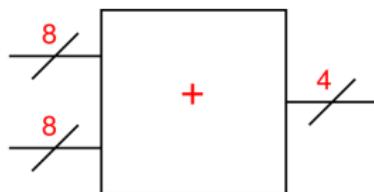
Simple 8 bit adder

# Improving Reusability through Hardware Construction

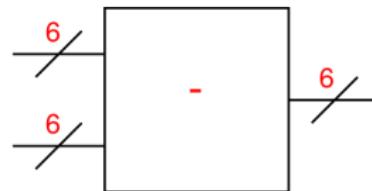
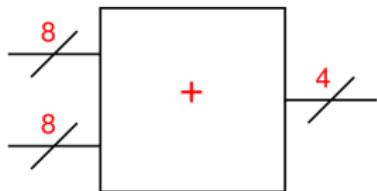


Parametrized functional block

# Improving Reusability through Hardware Construction



# Improving Reusability through Hardware Construction



---

```
module adder (
    input [7:0] op1,
    input [7:0] op2,
    output [3:0] out
);
    wire [8:0] tmp;
    tmp = op1 + op2
    out = tmp > 15 ?
        15 : tmp[3:0] ;
end module
```

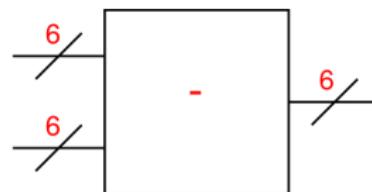
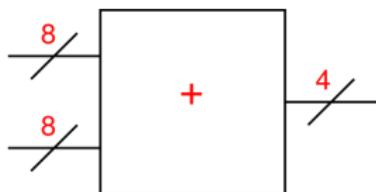
---

---

```
module sub (
    input [5:0] op1,
    input [5:0] op2,
    output [5:0] out
);
    out = op1 - op2;
end module
```

---

# Improving Reusability through Hardware Construction



---

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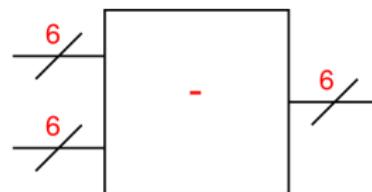
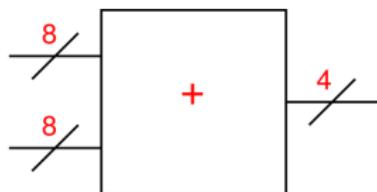
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end module
```

---

## Hardware Description Languages features

**Generic parameters** could be used ... but not for everything!

# Improving Reusability through Hardware Construction



## Hardware Description limits

Same functionality, but limited sharing possible...

... low reusability!

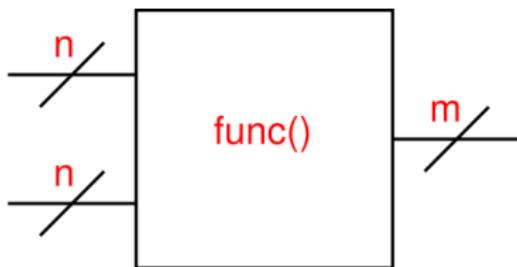
## Interests of reusability

- **Reusable code = productivity increase**
- **Less code = less error = less debug!**

# Improving Reusability through Hardware Construction

## Hardware Construction Languages

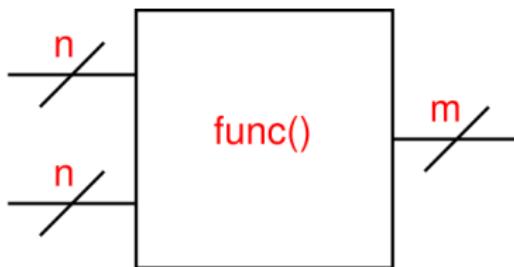
Designing **hardware generators** instead of *hardware accelerators*



# Improving Reusability through Hardware Construction

## Hardware Construction Languages

Designing **hardware generators** instead of *hardware accelerators*



---

```
class CustomBlock[T <: Data] (                                | Chisel syntax
    inputBitwidth: Int,
    outputBitwidth: Int,
    func:          (T, T) => T
) extends Module { ... }
```

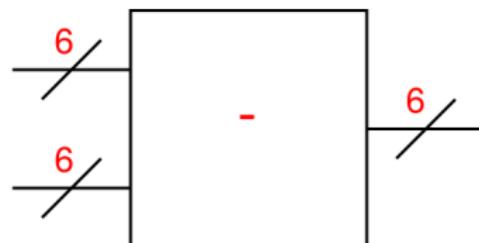
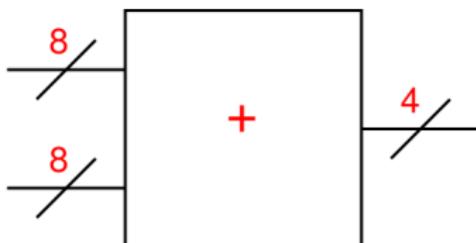
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# Improving Reusability through Hardware Construction

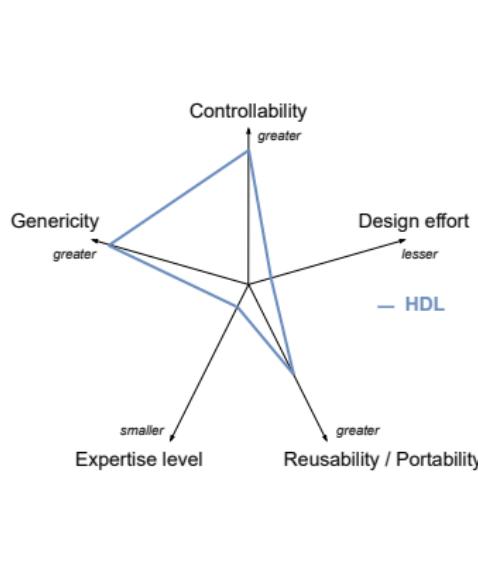
---

```
class CustomBlock[T <: Data] {  
    inputBitwidth: Int,  
    outputBitwidth: Int,  
    func: (T, T) => T  
} extends Module { ... }  
  
val adder = new CustomBlock[UInt](8, 4, _ + _)  
val sub = new CustomBlock[UInt](6, 6, _ - _)
```

---

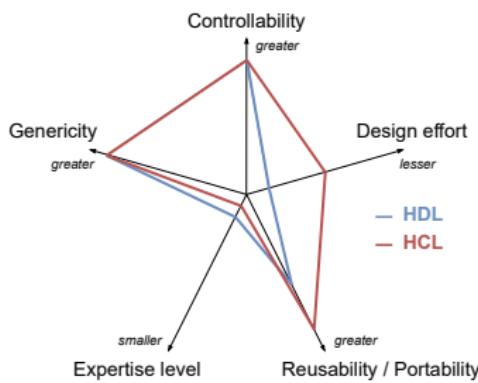


# Hardware Construction Languages



**HDL/HCL:** Hardware Description / Construction Language

# Hardware Construction Languages

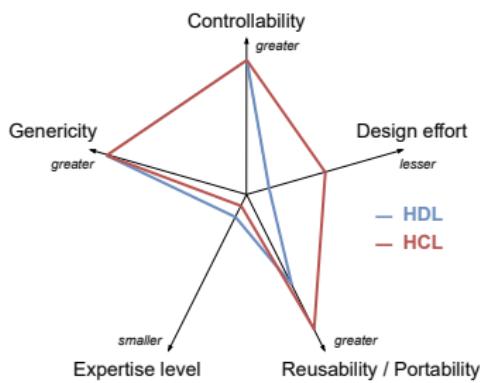


## Hardware Construction Languages

- high reusability with **high level parameters**
- **controlled variations** of architectures
- **high level features**
  - ▶ *object oriented programming*

**HDL/HCL:** Hardware Description / Construction Language

# Hardware Construction Languages



## Hardware Construction Languages

- high reusability with **high level parameters**
- **controlled variations** of architectures
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  - ▶ *object oriented programming*

## Chisel

- based on **Scala**
  - ▶ *functional programming*
- **open-source** framework
- **active community!**

**HDL/HCL:** Hardware Description / Construction Language

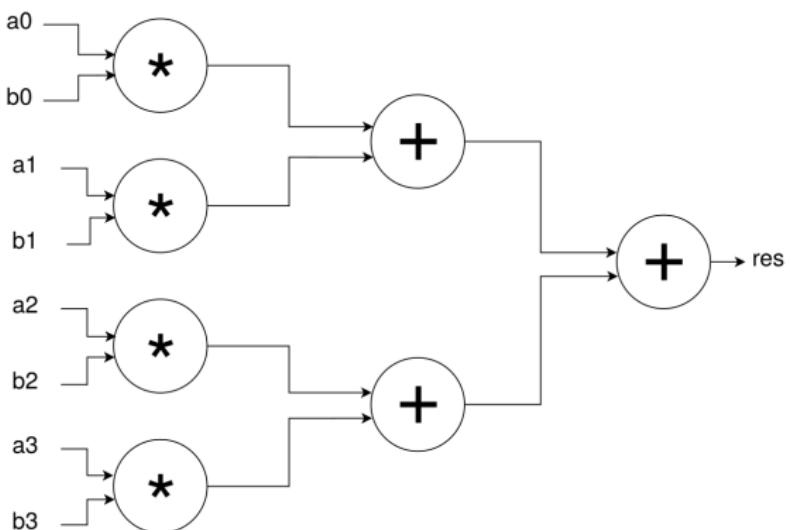
# The Importance of Reusability: a Simple Usecase

$$\begin{pmatrix} a_0 \\ a_1 \\ a_2 \\ a_3 \end{pmatrix} \cdot \begin{pmatrix} b_0 \\ b_1 \\ b_2 \\ b_3 \end{pmatrix} = a_0b_0 + a_1b_1 + a_2b_2 + a_3b_3$$

Dot Product computation

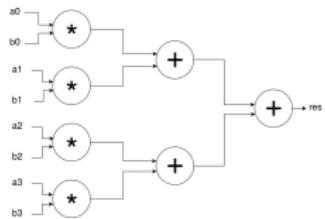
# The Importance of Reusability: a Simple Usecase

$a_0 b_0 +$   
 $a_1 b_1 +$   
 $a_2 b_2 +$   
 $a_3 b_3$



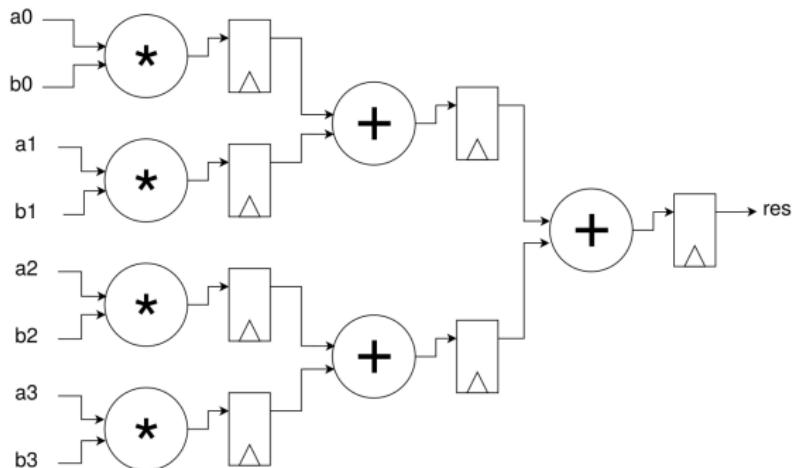
Architecture A

# The Importance of Reusability: a Simple Usecase



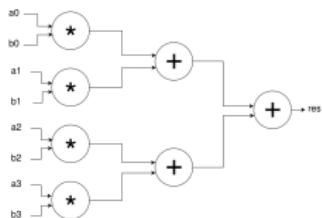
Architecture A

$$\begin{aligned} &a_0 b_0 + \\ &a_1 b_1 + \\ &a_2 b_2 + \\ &a_3 b_3 \end{aligned}$$

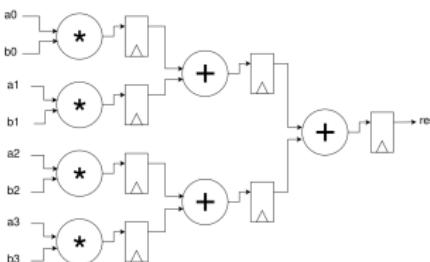


Architecture B

# The Importance of Reusability: a Simple Usecase

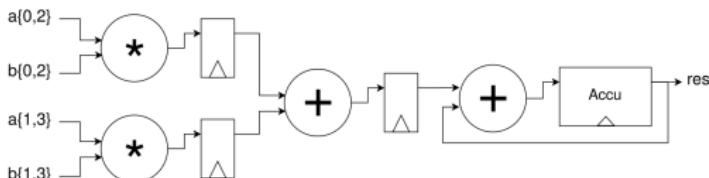


Architecture A



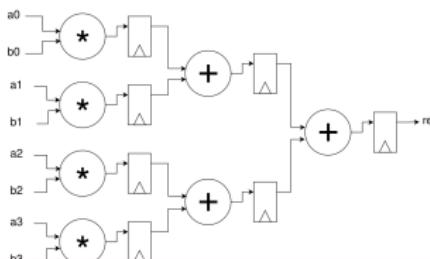
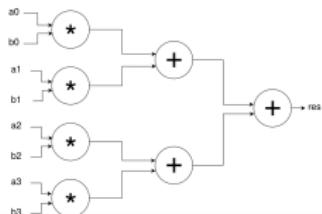
Architecture B

$$\begin{aligned} & a_0 b_0 + \\ & a_1 b_1 + \\ & a_2 b_2 + \\ & a_3 b_3 \end{aligned}$$



Architecture C

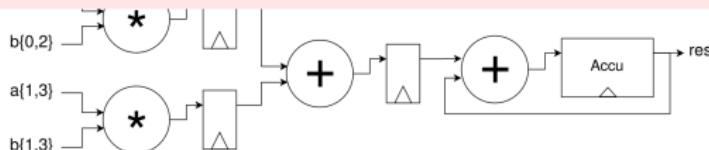
# The Importance of Reusability: a Simple Usecase



**Problematic**

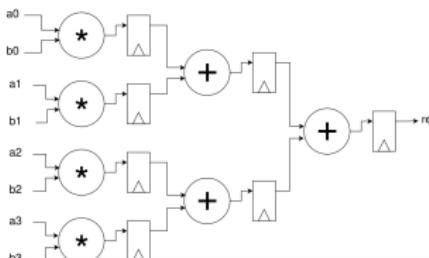
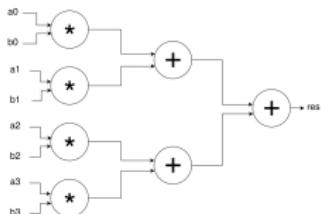
- which **architecture** is the best for the usecase?
- how many **different descriptions** do we need?

$$\begin{aligned} &a_0 b_0 + \\ &a_1 b_1 + \\ &a_2 b_2 + \\ &a_3 b_3 \end{aligned}$$



Architecture C

# The Importance of Reusability: a Simple Usecase



## Problematic

- which **architecture** is the best for the usecase?
- how many **different descriptions** do we need?

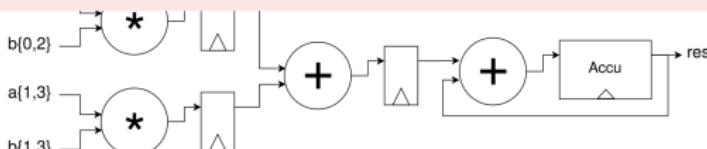
⇒ how to perform **Design Space Exploration**?

$a_0 a_1 +$

$a_1 b_1 +$

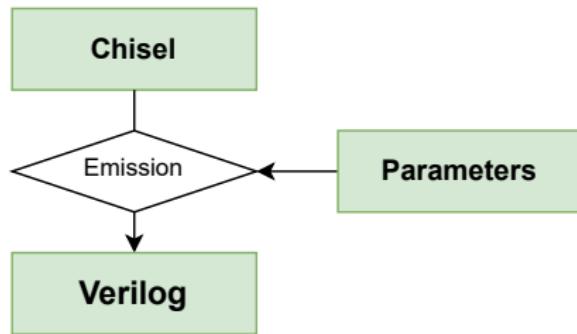
$a_2 b_2 +$

$a_3 b_3$



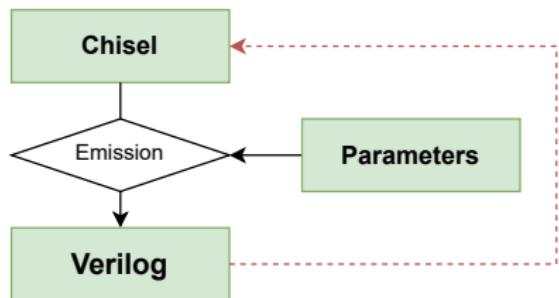
Architecture C

# Hardware Construction Languages for Design Space Exploration



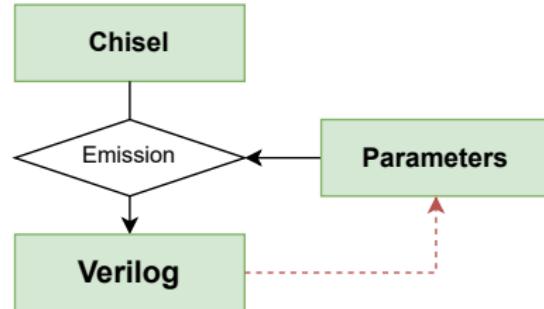
Standard Chisel emission flow

# Hardware Construction Languages for Design Space Exploration



Iterating on the Chisel description

VS



Iterating on the emission parameters

## Chisel for Design Space Exploration

Two **possible approaches**:

- iterate on the **Chisel description** itself
- exhibit **controlled variations of architecture through high level parameters**

# Hardware Construction Languages for Design Space Exploration

## Exploring the Dot Product Implementations

### Identified parameters:

- use registers for pipelining?
- how many multipliers should be used in parallel?

# Hardware Construction Languages for Design Space Exploration

## Exploring the Dot Product Implementations

### Identified parameters:

- use registers for pipelining?
- how many multipliers should be used in parallel?

---

```
class DotProduct(                                | Chisel syntax
    useRegisters: Boolean,
    parallelism: Int
) extends Module { ... }
```

---

# Motivations

## Problem Statement

- What can HCLs bring to hardware developers?
- How can HCLs help building efficient DSE processes?

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## Problem Statement

- What can HCLs bring to hardware developers?
- How can HCLs help building efficient DSE processes?

## Positioning

- **Public:** hardware developers / design experts
- **Target:** *Field-Programmable Gate Array* devices
- **Goal:** increase **reusability** of designs and provide features to build **expertise-based** design processes
- **Approach:** provide a **flexible design space exploration framework** based on the usage of **Chisel**

# Plan

- 1** Context and Motivations
- 2** Proposed Methodologies
- 3** Quick Exploration using Chisel Estimators
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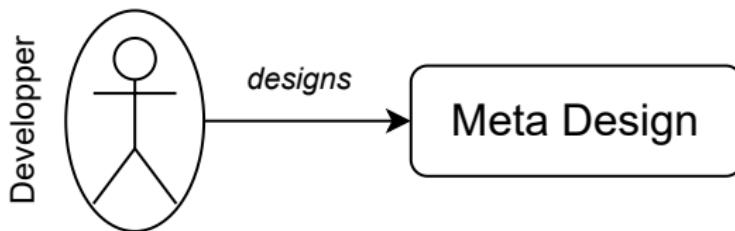
# Contributions

Dual-methodology for efficient HCL-based DSE:

# Contributions

## Dual-methodology for efficient HCL-based DSE:

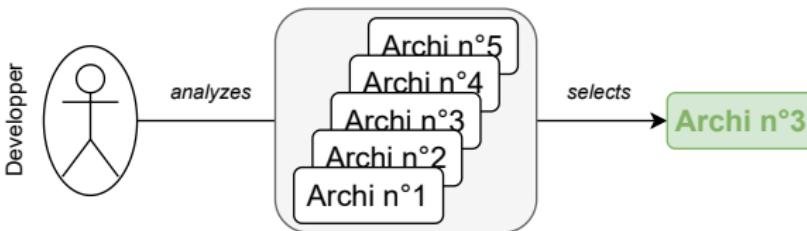
- **meta design** — how to build explorable generators?
  - ▶ how to define the useful parameters?
  - ▶ how to use them to build a generator?



# Contributions

## Dual-methodology for efficient HCL-based DSE:

- **meta design** — how to build explorable generators?
  - ▶ how to define the useful parameters?
  - ▶ how to use them to build a generator?
- **meta exploration** — how to efficiently explore them?
  - ▶ how to expose the design space?
  - ▶ how to estimate the quality of an implementation?
  - ▶ how to scan and compare multiple implementations?



# Meta Design

Generator design process based on **prior analysis** of algorithm and target.



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Generator design process based on **prior analysis** of algorithm and target.



## Algorithm Analysis

Study the implemented algorithm, and its interactions with the target.

# Meta Design

Generator design process based on **prior analysis** of algorithm and target.



## Architecture Schemes

Define the **hierarchy of components** to be used in the built generator.

# Meta Design

Generator design process based on **prior analysis** of algorithm and target.



## Parameter Definition

Exhibit **high level parameters** to build meaningful generators.

# Meta Design

Generator design process based on **prior analysis** of algorithm and target.



## Generator Description

Describe an **accelerator generator** based on the defined parameters.

# Meta Design

Generator design process based on **prior analysis** of algorithm and target.



## Design Validation

**Validate the behaviour** of (some of) the generated accelerators.

# Simple Usecase

## Algorithm: GEMM (General Matrix Multiply)

$$\begin{aligned}f: \mathbb{N} \times \mathbb{N} \times \mathcal{M}_n \times \mathcal{M}_n \times \mathcal{M}_n &\rightarrow \mathcal{M}_n \\(\alpha, \beta, A, B, C) &\mapsto \alpha \cdot A \times B + \beta \cdot C\end{aligned}$$

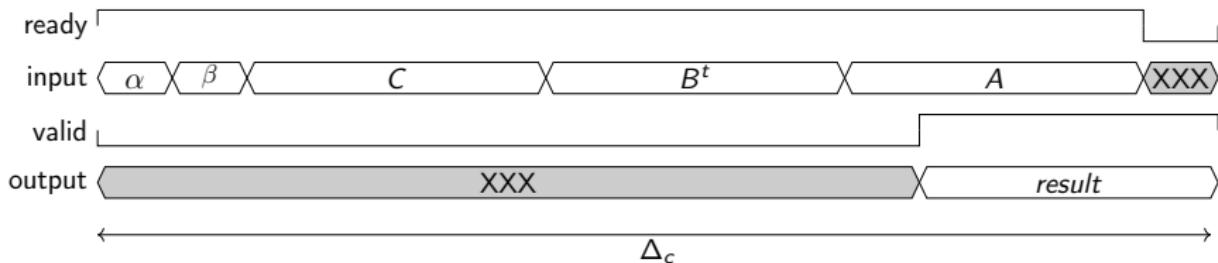
# Simple Usecase

## Algorithm: GEMM

$$\alpha \cdot A \times B + \beta \cdot C$$



## Targeted temporal behaviour:



Using users expertise for algorithm analysis

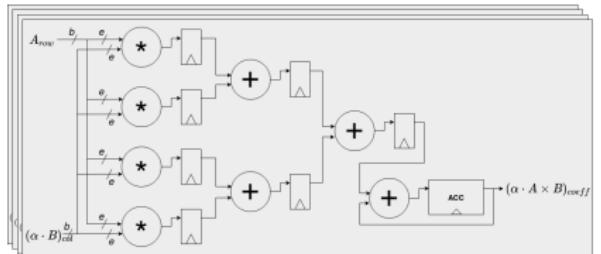
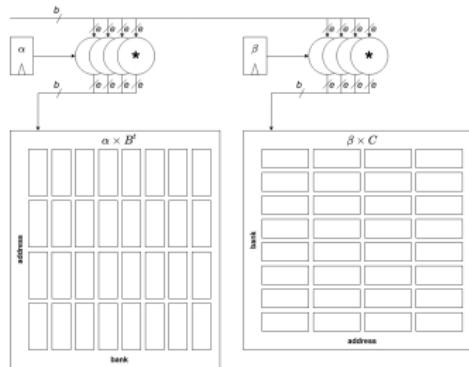
# Simple Usecase

## Algorithm: GEMM

$$\alpha \cdot A \times B + \beta \cdot C$$



## Architecture choices:

 $\times n$

# Simple Usecase

Three parameters identified:

- **architectural** parameters
  - ▶ capacity of the bus
  - ▶ width of the elements
- **applicative** parameters
  - ▶ matrix dimension



# Simple Usecase

Three parameters identified:

- **architectural** parameters
  - ▶ capacity of the bus
  - ▶ width of the elements
- **applicative** parameters
  - ▶ matrix dimension



---

```
class GemmModule(
    busWidth:      Int ,
    elementWidth:  Int ,
    dimension:     Int
) extends Module {...}
```

---

# Simple Usecase

Three parameters identified:

- **architectural** parameters
  - ▶ capacity of the bus
  - ▶ width of the elements
- **applicative** parameters
  - ▶ matrix dimension



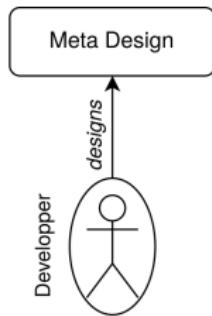
---

```
class GemmModule(
    busWidth:      Int ,
    elementWidth:  Int ,
    dimension:     Int
) extends Module {...}
```

---

Design validation is not much changed with respect to HDL flows

# Meta Exploration

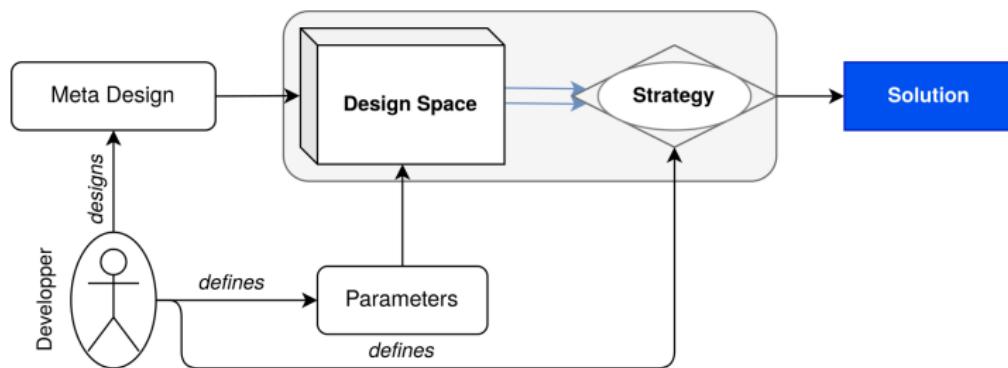


From Meta Design to Meta Exploration

How to efficiently use the built generators for **exploration**?

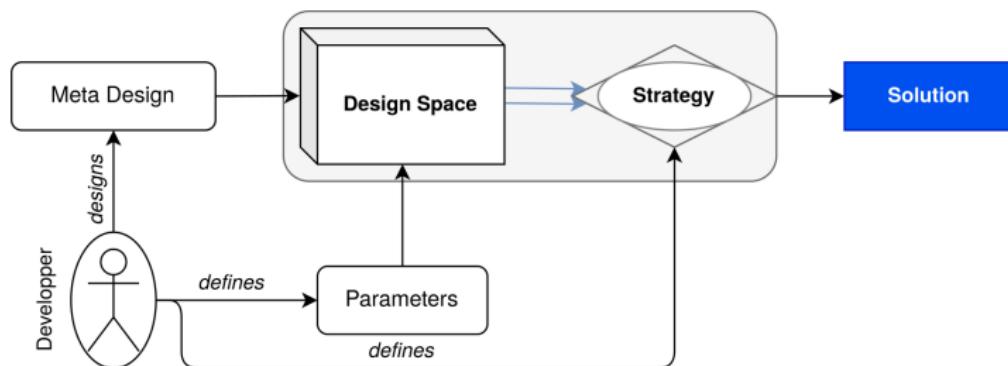
# Meta Exploration

Exploration process exploiting both **exposed design space** and **user knowledge**.



# Meta Exploration

Exploration process exploiting both **exposed design space** and **user knowledge**.



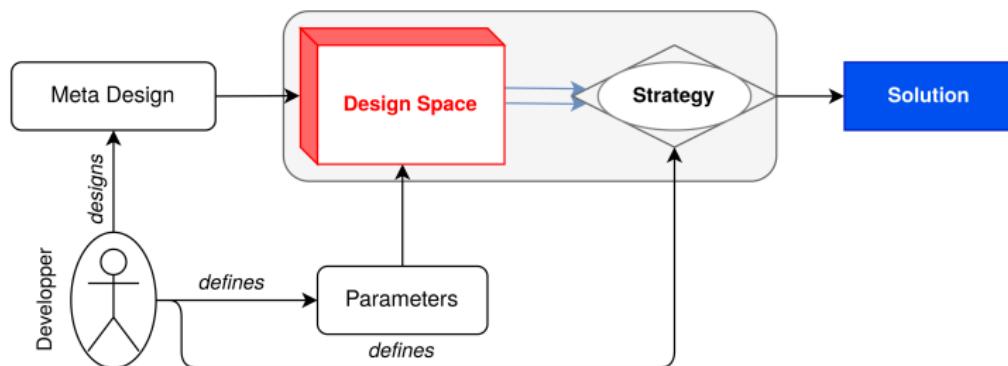
## Two step approach

- expose the design space to explore
- define how to explore it for a particular use case

# Meta Exploration — Design Space Exposition

## Designer-based approach

Expose an **interesting design space** to be explored.



# Simple Usecase

## Exposing the meta design space:

---

```
class GemmModule(  
    @pow2(5, 10) busWidth:      Int,  
    @enum(32)     elementWidth:  Int,  
    @pow2(4, 10) dimension:     Int  
) extends Module with Explorable
```

---

# Simple Usecase

## Exposing the meta design space:

```
class GemmModule(  
    @pow2(5, 10) busWidth: Int,  
    @enum(32)     elementWidth: Int,  
    @pow2(4, 10)   dimension: Int  
) extends Module with Explorable
```

- busWidth  $\in \{2^5, 2^6, 2^7, 2^8, 2^9, 2^{10}\}$  (6 values)
- elementWidth  $\in \{32\}$  (1 value)
- dimension  $\in \{2^4, 2^5, 2^6, 2^7, 2^8, 2^9, 2^{10}\}$  (7 values)

# Simple Usecase

## Exposing the meta design space:

```
class GemmModule(  
    @pow2(5, 10) busWidth: Int,  
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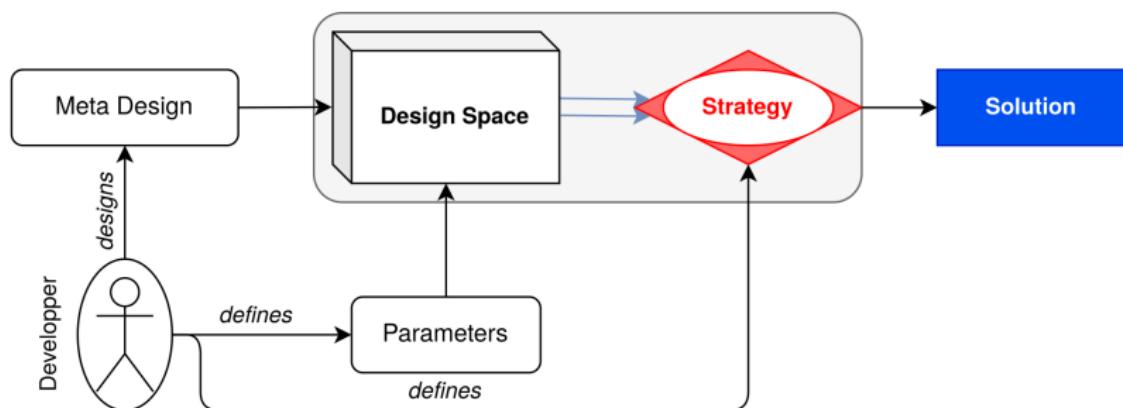
- busWidth  $\in \{2^5, 2^6, 2^7, 2^8, 2^9, 2^{10}\}$  (6 values)
- elementWidth  $\in \{32\}$  (1 value)
- dimension  $\in \{2^4, 2^5, 2^6, 2^7, 2^8, 2^9, 2^{10}\}$  (7 values)

A  $6 \times 7 = 42$  implementations wide design space is exposed

# Meta Exploration — Strategy Definition

## Functional approach

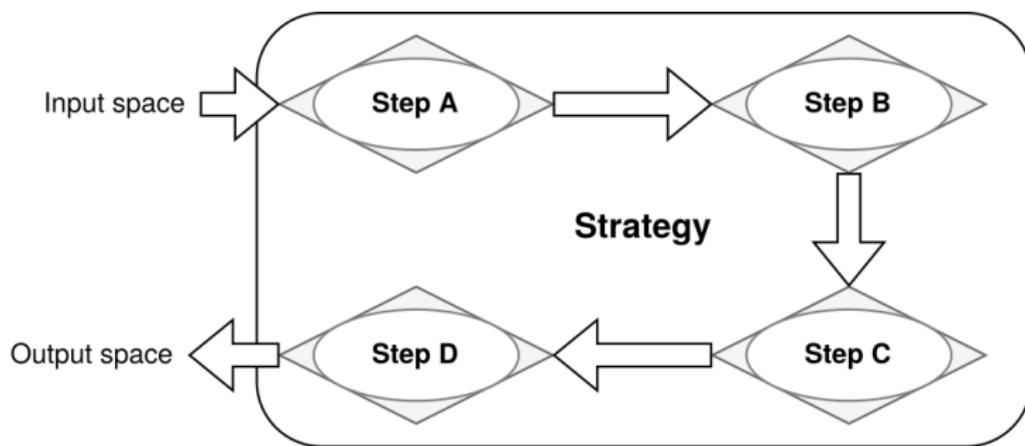
Describe an **exploration strategy** as a composition of **basic steps**



# Meta Exploration — Strategy Definition

## Functional approach

Describe an **exploration strategy** as a composition of **basic steps**



# Meta Exploration — Strategy Definition

## Functional approach

Describe an **exploration strategy** as a composition of **basic steps**

Each step relies on **two main notions**:

- the **metrics of interest** and their **estimators**
- the algorithm to **scan** the design space and produce a new one

# Simple Usecase

## Algorithm analysis:

Matrix multiply algorithm is computation intensive.

# Simple Usecase

## Algorithm analysis:

Matrix multiply algorithm is computation intensive.

### Designer expertise

- **FPGA target & limited memory model**



### Impact on the Strategy

- usage of LUT/DSP over FF/BRAM

# Simple Usecase

## Algorithm analysis:

Matrix multiply algorithm is computation intensive.

### Designer expertise

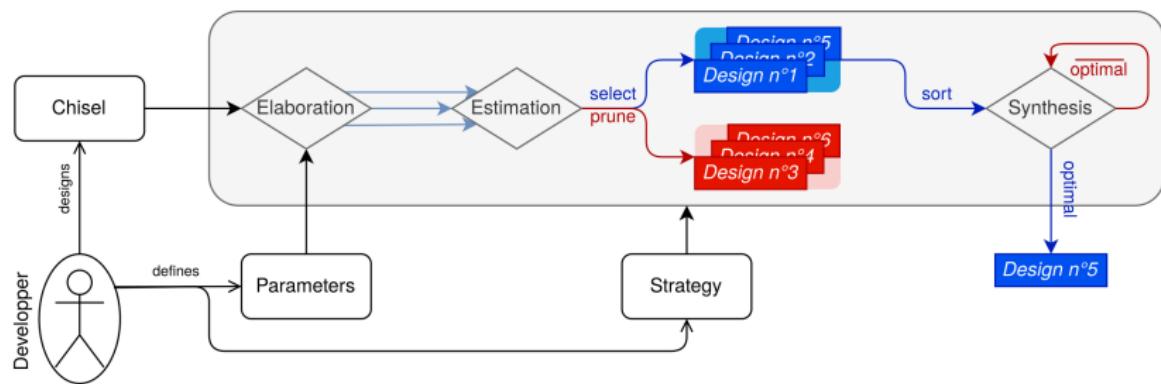
- **FPGA target & limited memory model**
- **32 bits elements**



### Impact on the Strategy

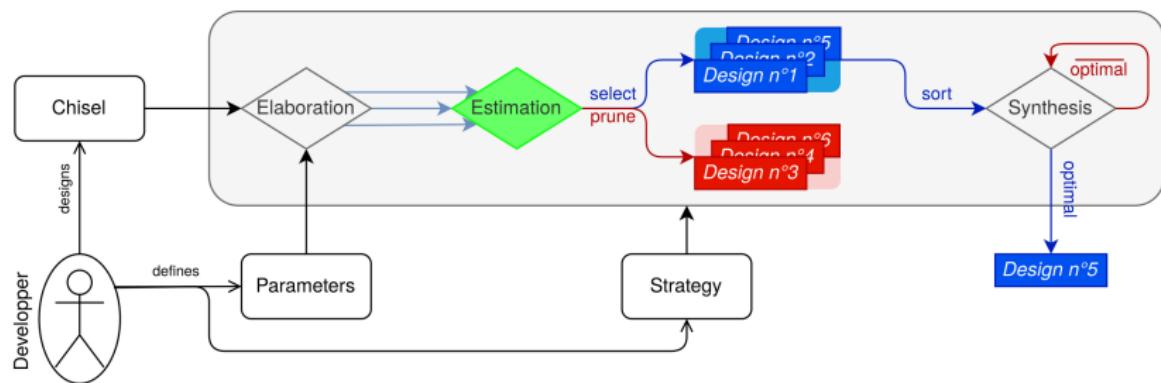
- usage of LUT/DSP over FF/BRAM
- usage of DSP over LUT

# Simple Usecase



Example of meta exploration strategy

# Simple Usecase

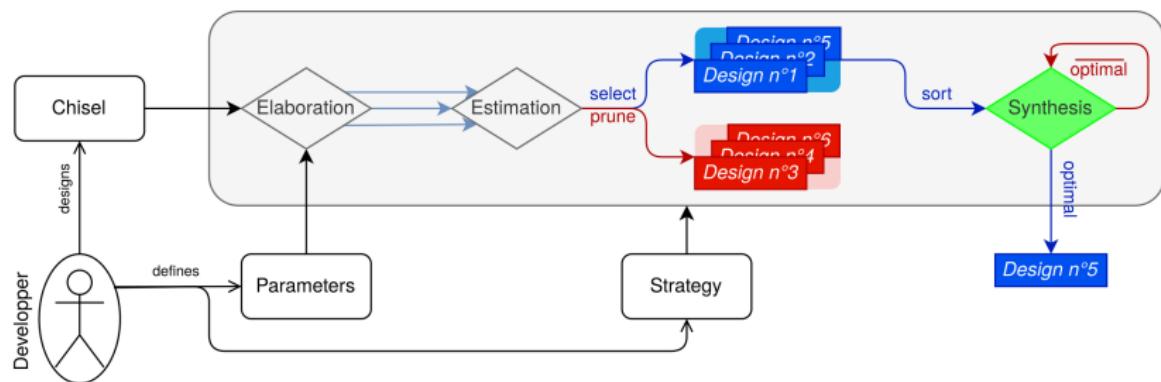


Example of meta exploration strategy

## Step 1

Estimate the DSP usage at high level for efficient pruning

# Simple Usecase

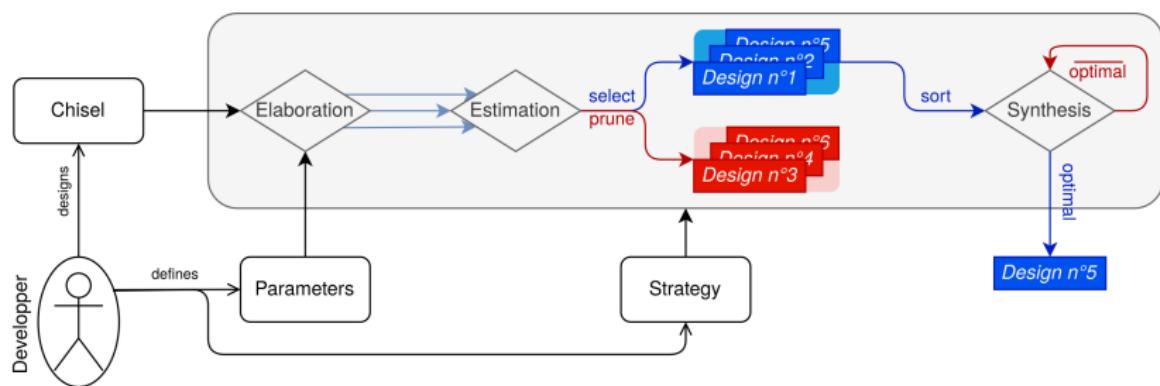


Example of meta exploration strategy

## Step 2

Gradient approach and syntheses to find a realistic solution

# Proposed Methodologies



Example of meta exploration strategy

## Synthesis

**Dual-methodology** for efficient **HCL-based DSE**...

... but how to demonstrate its **usability**?

# Plan

- 1** Context and Motivations
- 2** Proposed Methodologies
- 3** Quick Exploration using Chisel Estimators
- 4** Experiments and Results
- 5** Conclusion and Perspectives

# Building a Demonstrator

## Technical contribution

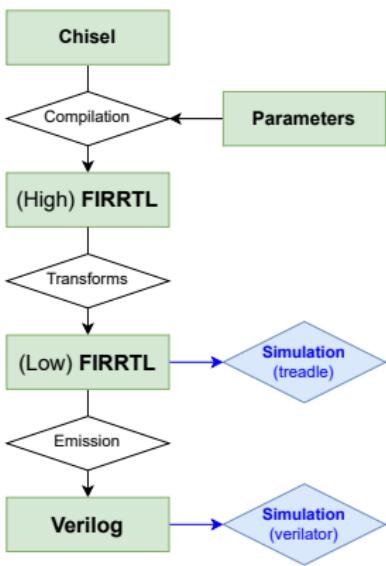
- build a **demonstrator** for the **proposed methodology**
- leverage **Scala features** for expertise-based DSE
- provide a **functional API** for concise definition of design processes
  - ▶ focus on providing a **flexible API**
- **open-source** code!

# Proposed Framework

## QECE (*Quick Exploration using Chisel Estimators*)

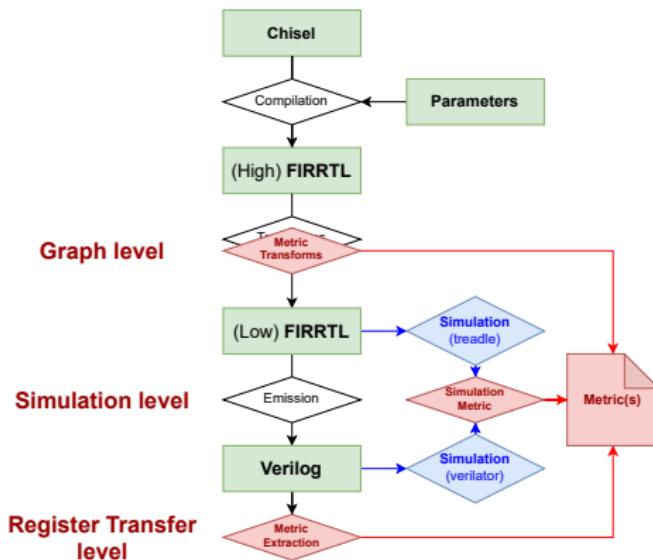
- allows estimations at different **abstraction levels**
- provides a **functional exploration API**
- **built-in libraries** of estimators and strategies
- provided as an **open-source Scala package**
  - ▶ can be imported in any **Chisel-based project**
  - ▶ provided with an **applicative benchmark**

# QECE Structure and API



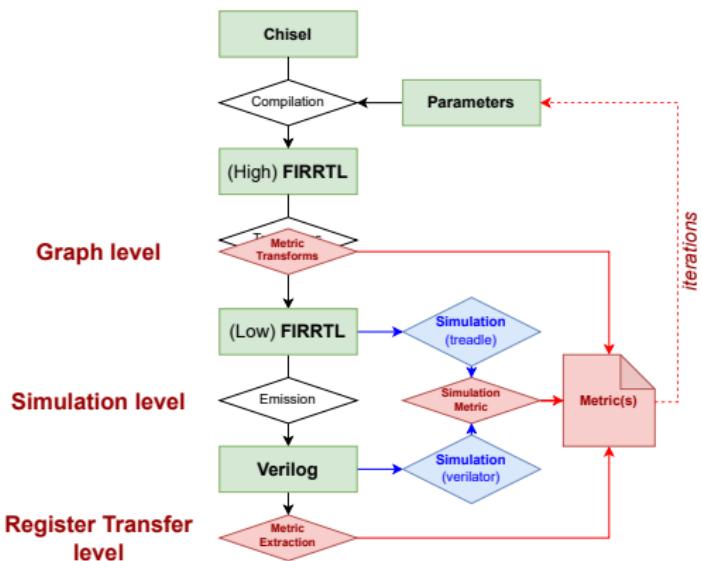
Standard Chisel design flow

# QECE Structure and API



Integrating estimators in Chisel

# QECE Structure and API



Proposed HCL-based DSE approach

# Built-in Estimators

## Metrics of interest

- resource usage *LUT, FF, DSP, BRAM*
- operating frequency *MHz, ns*
- quality of service *error rate*
- custom metrics *latency, throughput, ...*

# Built-in Estimators

## Metrics of interest

- resource usage *LUT, FF, DSP, BRAM*
- operating frequency *MHz, ns*
- quality of service *error rate*
- custom metrics *latency, throughput, ...*

## Estimation methodologies

- **Graph level**
  - ▶ resource usage
  - ▶ custom metrics*characterized library  
analytical formulas*
- **Simulation level**
  - ▶ quality of service*empirical approach*
- **Register Transfer Level**
  - ▶ resource usage & operating frequency*synthesis results*

# Built-in Strategies

## Functional exploration

Strategies can be built by composing **basic exploration steps**

# Built-in Strategies

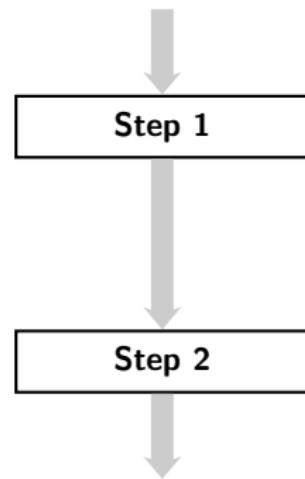
## Functional exploration

Strategies can be built by composing **basic exploration steps**

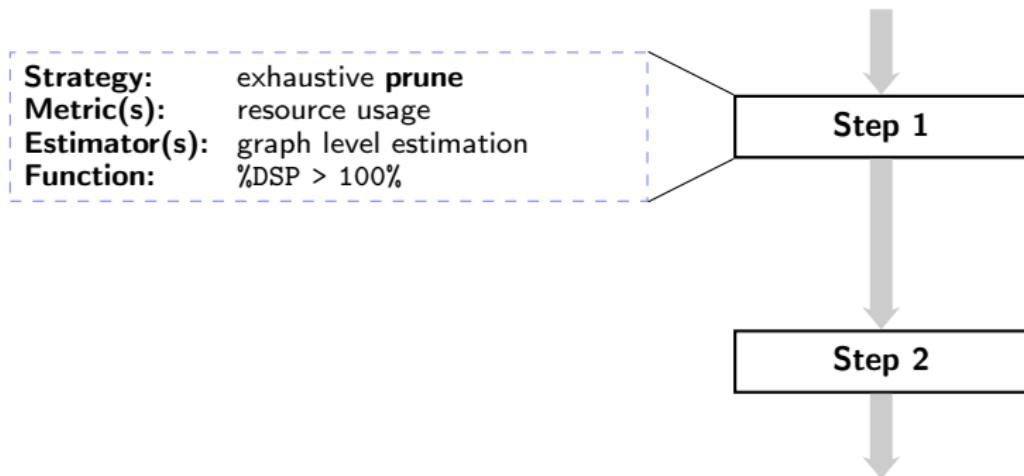
### Library of basic steps:

- exhaustive function **map**
- exhaustive **sort**
- exhaustive **prune**
- **gradient**-based sort
- **quick pruning**

# Simple Usecase: Demonstrating QECE Expressivity



# Simple Usecase: Demonstrating QECE Expressivity



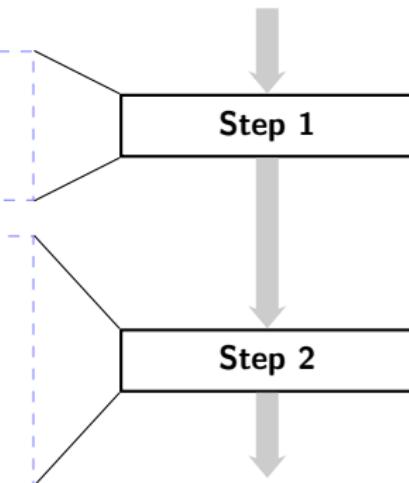
# Simple Usecase: Demonstrating QECE Expressivity

**Strategy:** exhaustive **prune**  
**Metric(s):** resource usage  
**Estimator(s):** graph level estimation  
**Function:**  $\%DSP > 100\%$

**Strategy:** gradient-based sort  
**Metric(s):**

- resource usage
- operating frequency
- throughput
- synthesis tool
- analytical formula

**Estimator(s):**  
**Function:**  $\max(\text{throughput})$

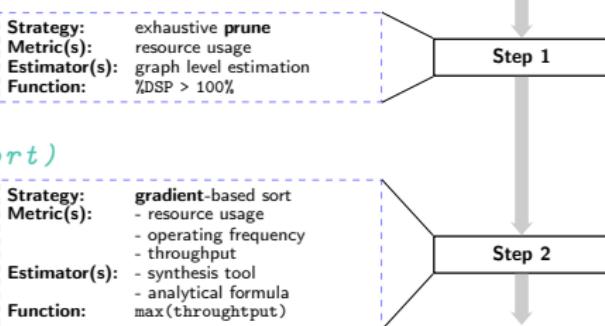


# Simple Usecase: Demonstrating QECE Expressivity

```

0 val builder = StrategyBuilder()
1 val strategy = builder.buildStrategy(
2   builder.compose(
3     // first step (prune)
4     builder.prune[GemmModule]{
5       tfs = TransformSeq.resources,
6       func = m => m("%dsp") > 1.0
7     },
8     // second step (gradient sort)
9     builder.gradient[GemmModule]{
10       tfs = TransformSeq.synthesis ++
11         throughputFormula,
12       func = (_ > _),
13       cmp = (_ > _),
14       numThread = 4
15     }
16   )
17 )

```



## Implementing an exploration strategy with QECE

- only a few lines of code
- each step can be tuned finely

# Proposed Framework

## Technical contributions

- **QECE** is proposed as an operational **open source** library<sup>1</sup>
  - ▶ embedded **libraries** to build **estimation** and **exploration** processes
  - ▶ **complex processes** can be described in a **concise way**
  - ▶ article to be submitted to **ACM TODAES** to demonstrate usability
- an **applicative benchmark** has been developed for demonstrations

---

<sup>1</sup><https://gricad-gitlab.univ-grenoble-alpes.fr/tima/sls/projects/>

# Plan

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# Applicative Benchmark

Custom benchmark of significant FPGA kernel generators, including:

- GEMM (General Matrix Multiply) *Image processing*
- Black Scholes computation unit *Finance*

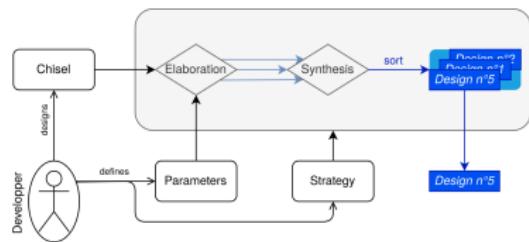
# Simple Usecase — Exploring GEMM meta design

## Demonstration goal

Compare different **exploration strategies** for a **GEMM-based usecase**:

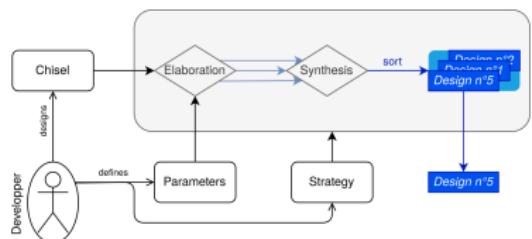
- **FPGA** target board: **Xilinx VC709**
- maximize the **throughput** on the given board

# Simple Usecase — Exploring GEMM meta design

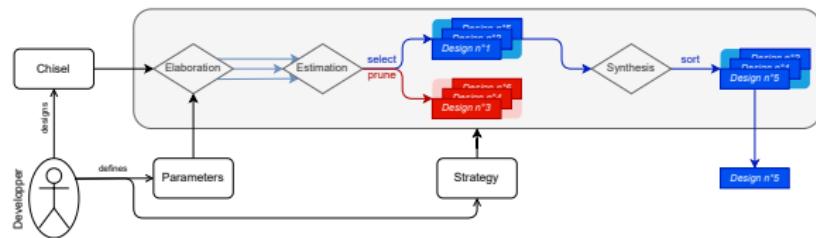


Exhaustive strategy

# Simple Usecase — Exploring GEMM meta design

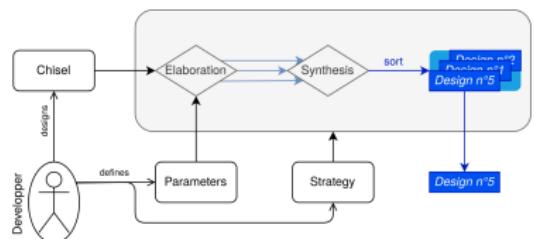


Exhaustive strategy

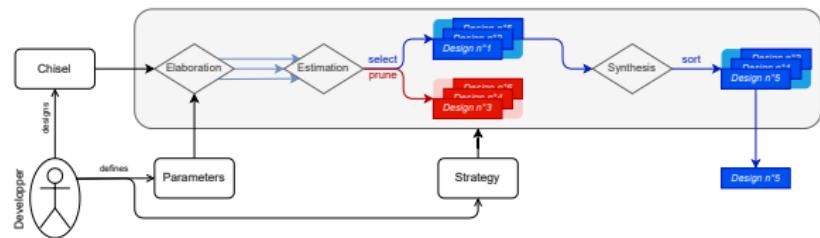


Pruning strategy

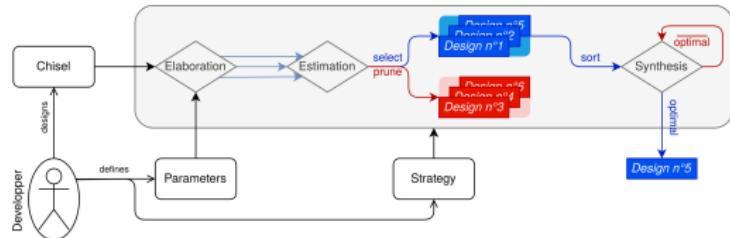
# Simple Usecase — Exploring GEMM meta design



Exhaustive strategy



Pruning strategy



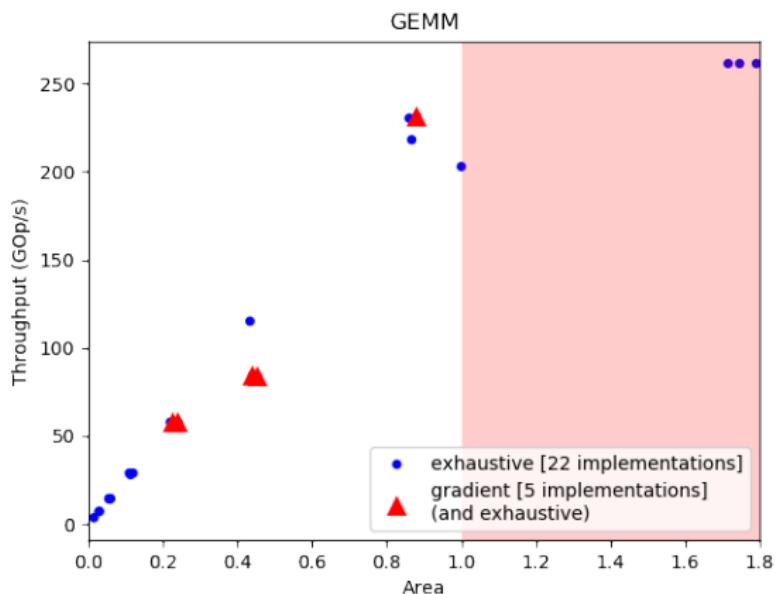
Gradient strategy

# Simple Usecase — Exploring GEMM meta design

Strategy	Best throughput	#(space)	#synth (#timeout)	Time	Speed-up
Exhaustive	231.334 GOp/s		41 (19)	13h51m56s	-
Pruning	231.334 GOp/s		26 (7)	08h52m00s	$\times 1.5$
Gradient	231.334 GOp/s	41	6 (1)	03h21m06s	$\times 4.1$

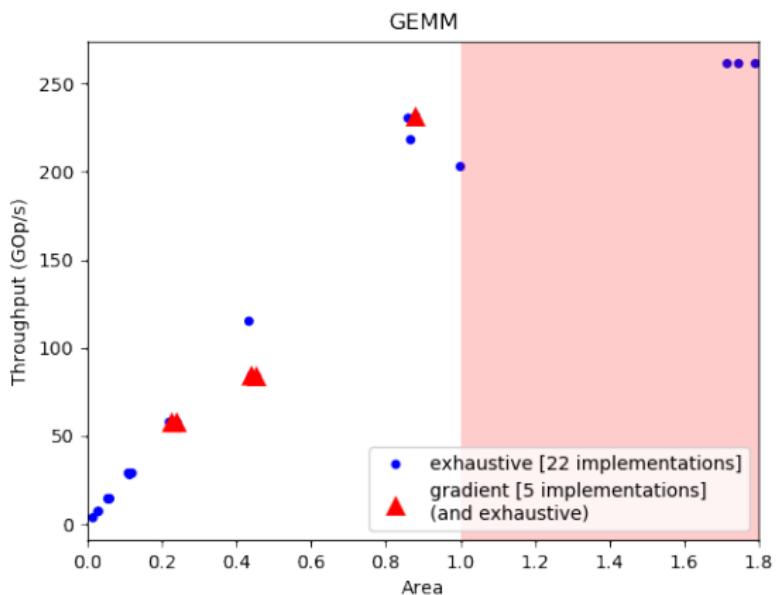
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## Results

- reduced the **number of syntheses**
- found the **same optimum**

# Exploring Black Scholes Implementations

## Black Scholes Model

**Black Scholes model** is used to estimate the **price of an option**:

- based on the **Monte Carlo** method
- **accuracy** depends on the **number of samples**
- **latency** depends on the **number of parallel cores**
- need for an **applicative model** to define the **quality of service**

```
class BlackScholes(  
    @resource @qos @linear(8, 32) dynamic: Int,  
    @resource @qos @linear(8, 32) precision: Int,  
    @qos @pow2(5, 10) nbIteration: Int,  
    @qos @pow2(1, 6) nbEuler: Int,  
    @resource @pow2(2, 10) nbCore: Int  
) extends Module with Explorable {...}
```

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## Application Specific Exploration

**Two concerns** for the exploration:

- respect an **error rate** threshold — *i.e.* < 5%
- select the implementation with the **best throughput**

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## Application Specific Exploration

**Two concerns** for the exploration:

- respect an **error rate** threshold — *i.e.* < 5%
- select the implementation with the **best throughput**

**5 generation parameters** ⇒ **202,500 implementations**

→ need for an **intelligent strategy** to explore them

# Exploring Black Scholes Implementations

## Implemented Exploration Strategy

Based on **5 sequential steps**, including:

# Exploring Black Scholes Implementations

## Implemented Exploration Strategy

Based on **5 sequential steps**, including:

- quality of service based **pruning**       $\simeq 37\text{h}$  ( $\approx 22,500$  simulations)
- synthesis based sorting       $\simeq 30\text{ min}$  (only **27 actual syntheses**)

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- quality of service based **pruning**       $\simeq 37\text{h}$  ( $\approx 22,500$  simulations)
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Rank	Parameters	Error	Throughput (est. $s^{-1}$ )	Area		Frequency
				Max %	Resource	
1	[12, 21, 64, 2, 64]	5.34%	125.06	25%	DSP	250.13 MHz
2	[12, 20, 64, 2, 64]	4.6%	125.06	25%	DSP	250.13 MHz
3	[12, 22, 64, 2, 64]	6.54%	125.03	25%	DSP	250.06 MHz
4	[13, 21, 64, 2, 64]	6.06%	125.03	25%	DSP	250.06 MHz
5	[12, 22, 64, 2, 32]	5.34%	62.53	12.5%	DSP	250.13 MHz

# Synthesis on the Experiments

## Synthesis

**QECE** usability has been demonstrated on **multiple usecases**:

# Synthesis on the Experiments

## Synthesis

QECE usability has been demonstrated on **multiple usecases**:

- different **exploration strategies** have been compared

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# Synthesis on the Experiments

## Synthesis

QECE usability has been demonstrated on **multiple usecases**:

- different **exploration strategies** have been compared
- various **concerns** and **objectives** have been considered
- the sources for the experiments can be **found online**

# Synthesis on the Experiments

## Synthesis

QECE usability has been demonstrated on **multiple usecases**:

- different **exploration strategies** have been compared
- various **concerns** and **objectives** have been considered
- the sources for the experiments can be **found online**

Doing so, we also demonstrated the **conciseness** of the approach

# Plan

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# Contributions

## Conceptual contributions

- HCL-based design flow based on a **dual-methodology**
- **Functional approach** for design space exploration
- **Productivity** increases thanks to:
  - ▶ HCLs, which improve **reusability**
  - ▶ QECE, with **concise and powerful DSE processes**

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- **Productivity** increases thanks to:
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  - ▶ QECE, with **concise and powerful DSE processes**

## Technical contributions

- PoC framework: **QECE** (*Quick Exploration using Chisel Estimators*)
  - ▶ **built-in libraries** of estimators and exploration strategies
  - ▶ allows defining **complex strategies** in a **concise way**
- Demonstration benchmark: set of **FPGA kernel generators**
- Both projects are **open-sourced** in TIMA/SLS gitlab<sup>1</sup>

---

<sup>1</sup><https://gricad-gitlab.univ-grenoble-alpes.fr/tima/sls/projects/>

# Perspectives

## Estimation features

- improve the provided **estimators**
  - ▶ better timing estimators
  - ▶ machine learning approaches
- introduce **other metrics & estimation methodologies**
  - ▶ routability, memory usage and other technological concerns
  - ▶ provide multiple ways to estimate the metrics
- provide direct **feedback and hints** to the users
  - ▶ quick feedback on routability and resource usage
  - ▶ estimate of the critical areas of a design

# Perspectives

## Exploration features

- improve the **library of exploration strategies**  
(e.g. reinforcement learning, genetic algorithms, ...)
- provide **visualization models** for the users
- allow **hierarchical explorations**
  - ▶ could be used to build **Systems on Chip**
  - ▶ would cope with our **flexible approach**
- demonstrate on a **more realistic usecase**
  - ▶ could consider an industrial usecase
  - ▶ explore our custom **MultiLayer Perceptron** generator

# Publications

## International Conferences and Workshops:

- Chisel UseCase: Designing General Matrix Multiply for FPGA

Bruno Ferres, Olivier Muller, Frédéric Rousseau. In *Proc. of the 16<sup>th</sup> International Symposium on Applied Reconfigurable Computing (ARC2020)*, Toledo, Spain, 2020.

- Integrating Quick Resource Estimators in Hardware Construction Framework for Design Space Exploration

Bruno Ferres, Olivier Muller, Frédéric Rousseau. In *Proc. of the 32<sup>nd</sup> International Workshop on Rapid System Prototyping (RSP'21)*.

## Journal Articles (to be submitted):

- Chisel Framework for Flexible Design Space Exploration through a Functional Approach

Bruno Ferres, Olivier Muller, Frédéric Rousseau. In *ACM Transactions on Design and Automation of Electronic Systems (TODAES)*, 2022.

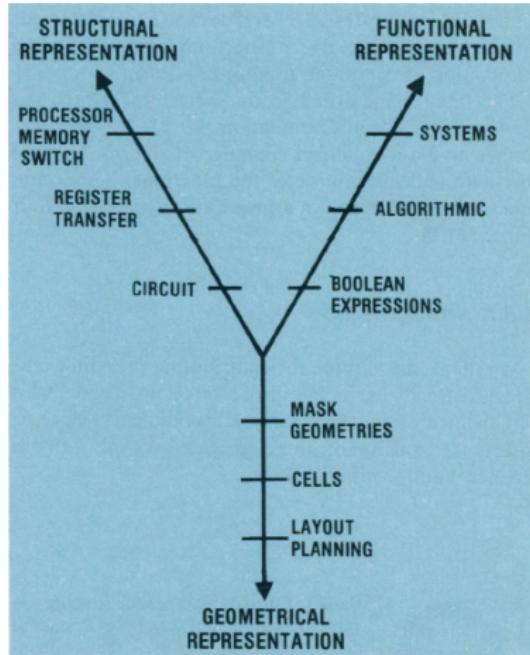
Thank you for your attention...

Thank you for your attention...

...now it's **question time!**

# APPENDICES

# Abstraction Levels for Digital Design



Gajski-Kuhn chart [GK83]<sup>1</sup>

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<sup>1</sup>Gajski and Kuhn, "New VLSI Tools", in *Computer*, 1983

# State of the Art: DSE Approaches and Tools

- No other approach proposing a **flexible** and **functional approach** for defining **design space exploration strategies**
- Many approaches for HLS-based DSE (e.g. [PBMR14]<sup>1</sup>) and DSL-based DSE (e.g. [NKO19]<sup>2</sup>)
- **Dovado** leverages HDL parameters for exploration ([PCS21]<sup>3</sup>)

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<sup>1</sup> Prost-Boucle *et al.*: "Fast and standalone Design Space Exploration for High-Level Synthesis under resource constraints.", in *Journal of Systems Architecture*, 2014

<sup>2</sup> Nardi *et al.*: "Practical Design Space Exploration.", in *International Symposium on Modeling, Analysis, and Simulation of Computer and Telecommunication Systems*, 2019

<sup>3</sup> Paletti *et al.*: "Dovado: An Open-Source Design Space Exploration Framework.", in *International Parallel and Distributed Processing Symposium Workshops*, 2021

# State of the Art: Estimation and Exploration

- a lot of research on **estimation methodologies** (e.g. [SJ08]<sup>1</sup>)
- we only consider **sequential strategies** at the moment ([SR18]<sup>2</sup>)
- different types of strategies considered ([SW20]<sup>3</sup>)
  - ▶ **meta heuristics, dedicated heuristics and supervised learning**
  - ▶ **graph analysis** — cannot be applied directly with HCLs

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<sup>1</sup>Schumacher *et al.*: "Fast and accurate resource estimation of RTL-based designs targeting FPGAs.", in *International Conference on Field Programmable Logic and Applications*, 2008

<sup>2</sup>Shatanaa *et al.*: "Design Space Exploration for Architectural Synthesis — A Survey.", in *Recent Finding in Intelligent Computing Techniques*, 2018

<sup>3</sup>Schaffer *et al.*: "High-Level Synthesis Design Space Exploration: Past, Present, and Future.", in *IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems*, 2020

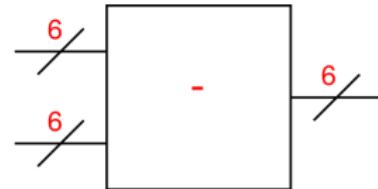
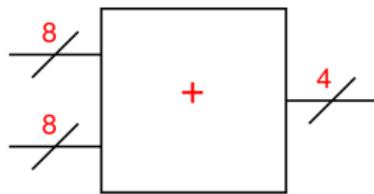
# What about SystemVerilog?

- a lot of interesting features (*POO*, *UVM*, ...) for **simulation purposes**
- some interesting features for **circuit description**:
  - ▶ more complex **data types**  
(enum and struct, multidimensional arrays, logic registers, ...)
  - ▶ **behavioral indications**:  
always\_comb, always\_ff and always\_latch  
⇒ useful for **readability** and **warnings**
  - ▶ **advanced interface definition** with custom bundles
  - ▶ verilog is a **subset of SystemVerilog**  
⇒ both are **Hardware Description Languages**  
⇒ a lot of features are actually from SystemVerilog  
(custom types, 2D arrays, ...)
- ...but no powerful features such as **POO** or **functional programming** for **circuit description**

# What about SystemC?

- based on a **C++ library**
- used at **system level** to model the **behaviour** of **complex systems**
  - ▶ a lot **simulation features** at different **levels**  
*(register transfer level, transaction level, platform level)*
  - ▶ useful for **co-design** and **virtual prototyping**
- **HLS tools** can generate components from **algorithmic descriptions**
- power features (*POO, templates, ...*) for **simulation** and **prototyping**
  - ▶ but limited performances on **circuit descriptions**
  - ▶ semantic and approach are **tightly coupled to simulation**

# Generic Implementation with Verilog



---

```
module adder
  #(parameter IN_WIDTH=8,
    parameter OUT_WIDTH=8)
  (input [IN_WIDTH-1:0] op1,
   input [IN_WIDTH-1:0] op2,
   output [OUT_WIDTH:0] out);
  localparam MAX = 1 << OUT_WIDTH - 1;
  wire [IN_WIDTH:0] tmp;
  tmp = op1 + op2;
  out = tmp > MAX ?
        MAX : tmp[OUT_WIDTH-1:0];
end module
```

---

---

```
module sub
  #(parameter IN_WIDTH=8,
    parameter OUT_WIDTH=8)
  (input [IN_WIDTH-1:0] op1,
   input [IN_WIDTH-1:0] op2,
   output [OUT_WIDTH-1:0] out);
  out = op1 - op2;
end module
```

---

# Some Chisel-Based Projects<sup>1</sup>

- Rocket Chip Generator *RISC-V in-order generator*
- BOOM<sup>2</sup> *RISC-V out-of-order generator*
- Edge TPU (from Google) *AI Inference Accelerator*
- DANA *Multilayer Perceptron Accelerator for Rocket*
- Gemmini *Systolic-array Accelerator Generator*
- ...

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<sup>1</sup>From <https://www.chisel-lang.org/community.html>

<sup>2</sup>Berkeley Out-of-order Machine

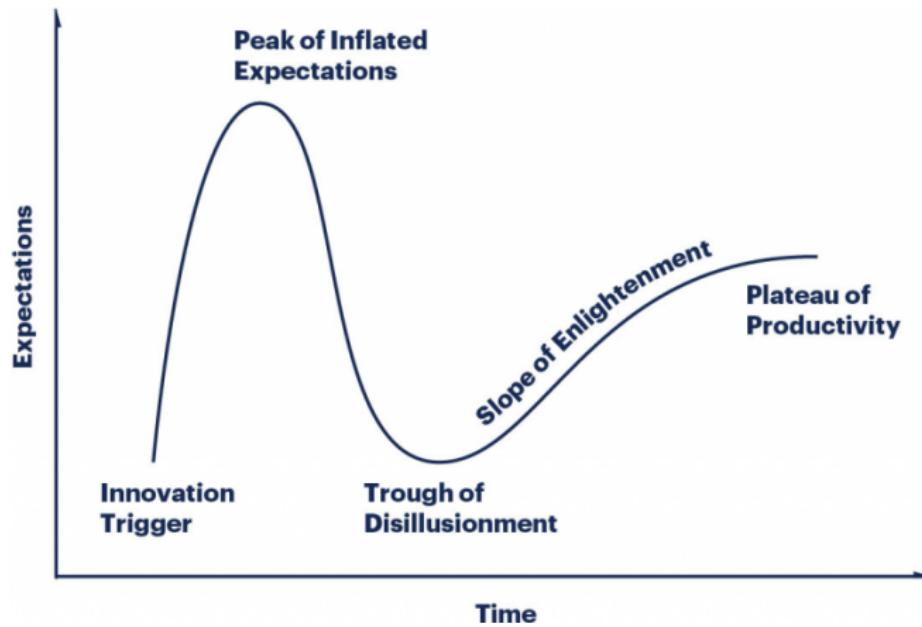
# Building a Functional Block in Chisel

---

```
class CustomBlock[T <: Data](gen: T)(  
    inputBitwidth: Int,  
    outputBitwidth: Int,  
    func: (T, T) => T  
) extends Module {  
    val io = IO(new Bundle {  
        val op1 = Input(UInt(inputBitwidth.W))  
        val op2 = Input(UInt(inputBitwidth.W))  
        val out = Input(UInt(outputBitwidth.W))  
    })  
    io.out := func(  
        io.op1.asTypeOf(gen),  
        io.op2.asTypeOf(gen)  
    ).asTypeOf(io.out)  
}  
  
val adder     = new CustomBlock(SInt(8.W))(8, 4, _ + _)  
val sub       = new CustomBlock(UInt(6.W))(6, 6, _ - _)
```

---

# Hardware Construction Languages and Productivity



<sup>1</sup>From <https://www.gartner.com>

# Hardware Construction Languages and Productivity

Rough approximation of productivity gain, based on our personal experiences

Criterion	Methodology		
	HDL	HLS	HCL
Learning	weeks	days	weeks (days)
Mastering	months	months	months (months)
Design	days	hours	days
Optimization	days	days	days
Debug	days	days	days
Reuse	days	days	hours

## Feedback on the use of Hardware Construction Languages

3 years expertise on Chisel usage, with:

- two PhD students
- four engineer interns

## Exploring an accelerator generator

Standard DSE methodologies not applicable for HCLs:

- HLS-based methodologies use **inferences**
- HDL-based methodologies does not consider **high level parameters**

# HCL-based DSE: Motivations

## Exploring an accelerator generator

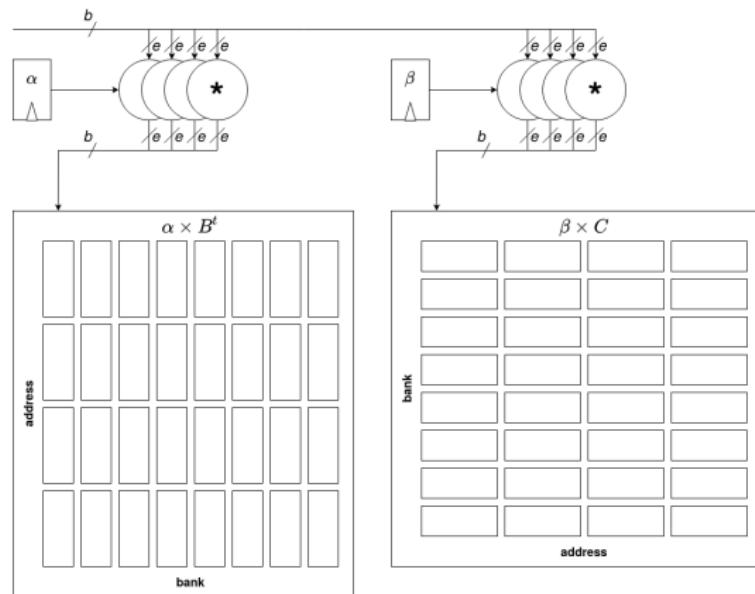
Standard DSE methodologies not applicable for HCLs:

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## Purpose of an HCL-based DSE methodology

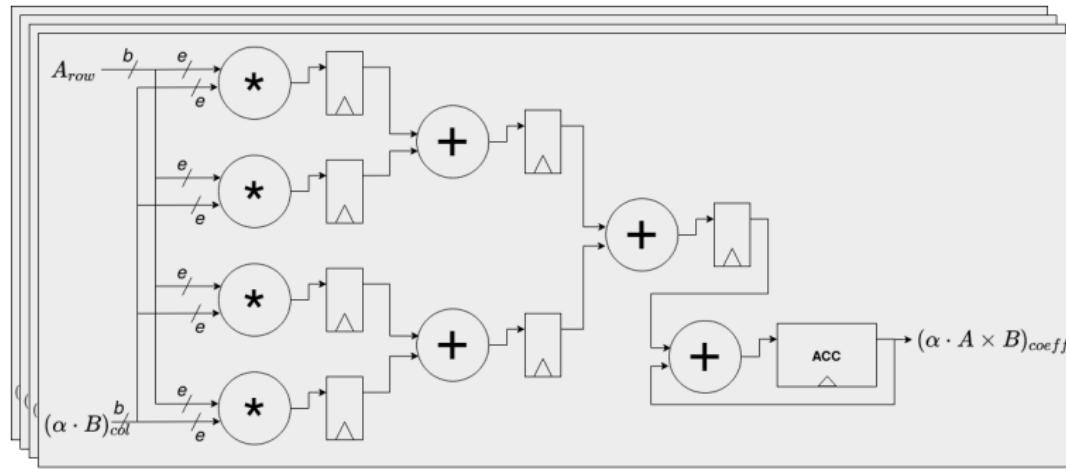
- shall take advantage of the **HCL features**
  - ▶ module **generation**
  - ▶ **high-level** programming features
- **expertise-based** approach

# GEMM Architecture



Chosen memory architecture

# GEMM Architecture



Chosen computation unit architecture

# Application: Fast Fourier Transform

---

```
class FftModule(
    @pow2(1, 10) parallelism: Int,
    @enum(32)      elementWidth: Int,
    @enum(SIZE)    size:           Int
) extends Module { ... }
```

---

Exposing **Fast Fourier Transform** design space

# Application: Fast Fourier Transform

Size	Strategy	Best throughput	#(space)	#synth (#timeout)	Time	Speed-up
128	Exhaustive	1.767 Tb/s	7	7 (0)	00h22m45s	-
	Pruning	1.767 Tb/s		7 (0)	00h24m14s	$\times 0.94$
	Gradient	1.767 Tb/s		3 (0)	00h19m51s	$\times 1.15$
512	Exhaustive	5.479 Tb/s	9	9 (0)	02h11m51s	-
	Pruning	5.479 Tb/s		9 (0)	03h17m52s	$\times 0.66$
	Gradient	5.479 Tb/s		3 (0)	02h18m29s	$\times 0.95$

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## Results

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- but only consider a **small design space**
  - ▶ only **one meaningful parameter** (*parallelism*)
  - ▶ hence **complex strategies** are slower

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## Results

- found the **same optimum**
- but only consider a **small design space**
  - ▶ only **one meaningful parameter** (*parallelism*)
  - ▶ hence **complex strategies** are slower
- need to compare different *element widths* and *problem sizes*
  - ▶ need an **applicative model** to do so!

# Meta Exploration Strategy for Black Scholes

---

```
class BlackScholes(
    @resource @qos @linear(8, 32) dynamic: Int,
    @resource @qos @linear(8, 32) precision: Int,
    @qos @pow2(5, 10)           nbIteration: Int,
    @qos @pow2(1, 6)            nbEuler: Int,
    @resource @pow2(2, 10)       nbCore: Int
) extends Module with Explorable {...}
```

---

Exposed design space

# Meta Exploration Strategy for Black Scholes

---

```
val builder = StrategyBuilder()
val strategy = builder.buildStrategy(
    context.quickPrune[BlackScholes](
        QualityOfService.simulation,
        _.error > 0.05,
        metric = Some(new qos)
    ),
    context.reduceDimension[BlackScholes](new resource, true),
    context.map[BlackScholes](Transforms.latency),
    context.sort[BlackScholes](<@TransformSeq.empty,
        m => m("dynamic") + m("precision") + m("nbCore"),
        (_ < _)
    ),
    context.gradient[BlackScholes](
        TransformSeq.synthesis ++ Transforms.throughput
        func = _("throughput"),
        cmp = (_ > _)
    )
)
```

---

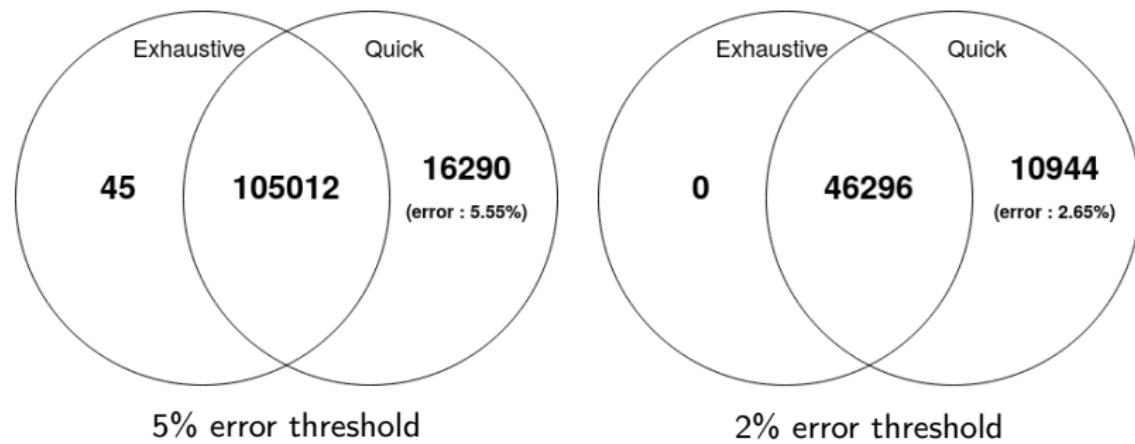
Expertise-based exploration strategy

# Meta Exploration Strategy for Black Scholes

Error threshold	Number of impl.	Strategy	Exploration time	Speed-up
5%	202500	Exhaustive pruning	46h29m19s	-
		Quick pruning	32h59m29s	×1.40
2%	202500	Exhaustive pruning	46h21m42s	-
		Quick pruning	48h46m53s	×0.95

Comparing the pruning strategies over Black Scholes kernels

# Meta Exploration Strategy for Black Scholes



Comparing the accuracy of the pruning strategies on Black Scholes