Scenegraphs

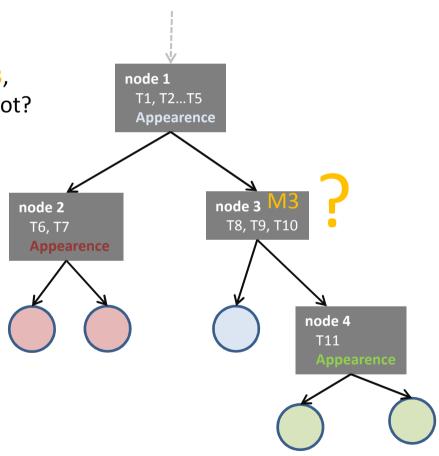
- Scenegraph nodes:
 - Compound node
 - Leaf node

- Node properties
 - Geometric transformations and propagation

Questions

What is the transformation matrix M3, to apply to sub-tree with node 3 as root?

How to store M3?



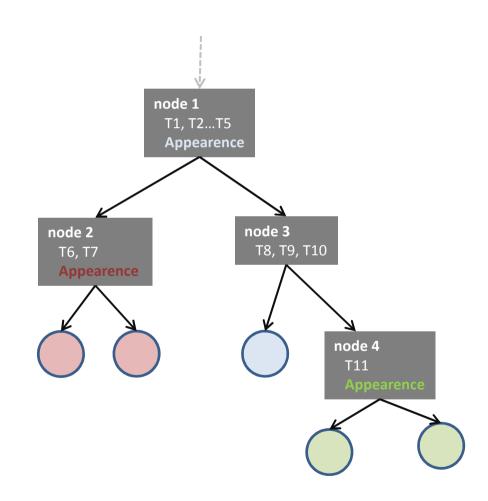
Solution 1: transformation list

Keep a transformation list, accumulating transformations for parent nodes.

For node 3: T1, T2,...,T5, T8, T9, T10

In rendering time traverse the list and apply transformations.

Drawback: not efficient!



Solution 2: calculate and keep a transformation matrix for each node

Use OpenGL to perform the calculation of a transformation matrix for each compound node in the scenegraph!

Requires a function to retrieve the current MODEL_VIEW matrix. Ex 1:

```
float m1[4][4];
      glGetFloatv(GL MODELVIEW MATRIX, &m1[0][0]);
Ex 2:
      float m1[4][4];
      float m2[4][4];
                                                               //M = I
      glLoadIdentity();
      glRotated(20.0,1,0,0);
                                                               // M = M.Rx(20)
      glRotated(-45,0,1,0);
                                                               // M = M.Ry(-45)
      glTranslated(0.0,0.0,-25);
                                                              // M = M.Tz(-25)
      glGetFloatv(GL MODELVIEW MATRIX, &m1[0][0]);
                                                              // m1 = M
      glTranslated(0.0,15.0,0.0);
                                                              // M = M.Ty(15)
      glGetFloatv(GL MODELVIEW MATRIX, &m2[0][0]);
                                                              // m2 = M
```

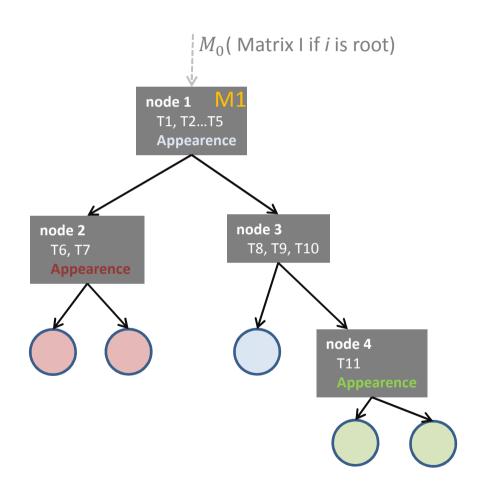
Solution 2: calculate transformation matrix for node 1

Calculate:

$$M_1 = I \times M_0 \times (I \cdot T_1 \cdot T_2 \cdot ... \cdot T_5)$$

Store M1 in node 1

Important: / is the identity matrix



Transformation Matrix for nodes 2 and 3

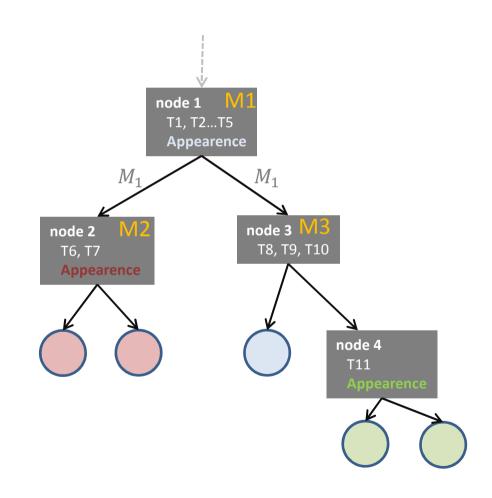
Calculate M_2

$$M_2 = I \times M_1 \times (I \cdot T_1 \cdot T_2)$$

Calculate M_3

$$M_3 = I \times M_1 \times (I \cdot T_1 \cdot T_2 \cdot T_3)$$

Store M2 in node 2 and M3 in node 3



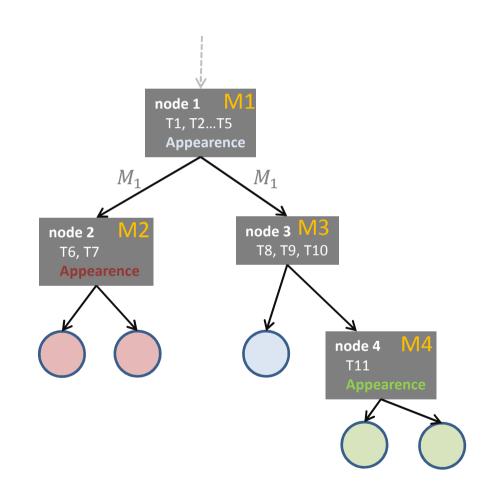
OpenGL transformation Matrix for node 3

```
M_3 = I \times M_1 \times (I \cdot T_1 \cdot T_2 \cdot T_3)
// calculate m = (I.T1.T2.T3). In this example assume:
// T1 = Rx(50)
// T2 = Sy(1.5)
// T3 = Tz(10)
float m[4][4];
glLoadIdentity();
                                                            //M = I
glRotated(50.0,1,0,0);
                                                            // M = M.Rx(50.0)
glScaled(1.5,0,1,0);
                                                            // M = M.Sy(1.5)
glTranslated(0,0,10.0);
                                                            // M = M.Tz(10.0)
glGetFloatv(GL MODELVIEW MATRIX, &m[0][0]);
                                                            // m = M
// now calculate I x M1 x m
// assumed M1 is passed from parent node
float M3[4][4];
                                                            //M = I
glLoadIdentity();
                                                            // M = M \times M1
glMultMatrixf(&M1);
glMultMatrixf(&m);
                                                            // M = M \times m
glGetFloatv(GL MODELVIEW MATRIX, &M3[0][0]);
                                                            // M3 = M
// we now got M3 calculated!
```

Transformation Matrix for node 4

Calculate M_4 $M_4 = I \times M_3 \times (I \cdot T_1)$

Store M4 in node 4



Geometric transformations

From parser to a transformation matrix **m**

```
<transformations>
         <rotate axis="x" angle="40" />
         <rotate axis="y" angle="20" />
         <scale factor="1.0 5.0 2.0" />
         <translate to="10.0 5.0 3.0" />
</transformations>
Rx(40.0); Ry(20.0); Sy(5.0); Sy(2.0); T(10,5,3)
// now calculate I x M1 x m
// assumed M1 is passed from parent node
float m[4][4];
glLoadIdentity();
glRotated(40.0,1,0,0);
glRotated(20.0,0,1,0);
glScaled(5,0,1,0);
glScaled(2,0,0,1);
glTranslated(10.0,5.0.3.0);
```

glGetFloatv(GL MODELVIEW MATRIX, &m[0][0]);

Whatever the number of geometric transformations defined for a node, a single matrix **m** is required to represent the set.