Star Battle

Resolução de Problema de Decisão usando Programação em Lógica com Restrições

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Resumo Este artigo complementa o segundo projecto da Unidade Curricular de Programação em Lógica, do Mestrado Integrado em Engenharia Informática e de Computação. O projecto consiste num programa, escrito em Prolog, capaz de resolver qualquer tabuleiro do jogo Star Battle, que é um problema de decisão.

Keywords: star battle, sicstus, prolog, feup

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asdasdad
asdads

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Código fonte

starBattle.pl

```
%=============================================%
%=                                           =%
%=           ..:: STAR BATTLE ::..           =%
%=                                           =%
%=        Type 'starBattle.' to start        =%
%=                                           =%
%=============================================%
%=                                           =%
%=             ..:: Authors ::..             =%
%=                                           =%
%=     Henrique Ferrolho && Joao Pereira     =%
%=                FEUP - 2014                =%
%=                                           =%
%=============================================%

%===============%
%= @@ includes =%
%===============%
:- use_module(library(clpfd)).
:- include('containers.pl').
:- include('printer.pl').
:- include('solver.pl').
:- include('starBattleTestBoards.pl').
:- include('utilities.pl').

%====================%
%= @@ game launcher =%
%====================%
starBattle:-
    clearConsole,
    write('To run the program type:'), nl,
    nl,
    write('\tstarBattle(NumBoard, NumStars).'),nl,
    nl,
    write('- NumBoard'), nl,
    write('number of the board you wish to test.'), nl,
    nl,
    write('- NumStars'), nl,
    write('number of stars you wish to place on each row, column and region.'), nl,
    nl.

starBattle(BoardNumber, NumStars):-
    clearConsole,
    write('==============='), nl,
```

```
    write('= Star Battle ='), nl,
    write('==============='), nl,
    nl,
    format('Trying to place ~d stars on board no. ~d:', [NumStars, BoardNumber]), nl,

    getBoard(BoardNumber, Board),
    printBoard(Board), !,

    solveBoard(Board, NumStars, Result), !,
    pressEnterToContinue,

    %getBoardSize(Board, BoardSize),
    %printResult(Result, BoardSize, NumStars),
    printResultBoard(Board, Result, NumStars), !.
```

solver.pl

```
solveBoard(Board, S, Result):-
    getBoardSize(Board, N),

    % a board NxN can not have more than N/2 stars
    S #=< (N - 1) // 2 + 1,

    ResultLength #= N * S,

    length(Result, ResultLength),
    length(ResultRegions, ResultLength),

    domain(Result, 1, N),
    domain(ResultRegions, 1, N),

    % 1st restriction
    validateNumOfOccurrencesForEachElem(Result, S, N),

    % 2nd restriction
    fetchResultRegions(Board, Result, N, S, ResultRegions),
    validateNumOfOccurrencesForEachElem(ResultRegions, S, N),

    % 3rd restriction
    noAdjacentStars(Result, S, N),

    statistics(walltime, _),
    labeling([bisect], Result),
    statistics(walltime, [_, ElapsedTime | _]),
```

```
    format('An answer has been found!~nElapsed time: ~3d seconds', ElapsedTime), nl,
    fd_statistics,
    nl.


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getBoardSize([Head|_], N):-
    length(Head, N).


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validateNumOfOccurrencesForEachElem(Elements, NumOfOccurrences, N):-
    validateNumOfOccurrencesForEachElem(Elements, NumOfOccurrences, N, 1).

validateNumOfOccurrencesForEachElem(Result, S, N, N):-
    exactly(N, Result, S).
validateNumOfOccurrencesForEachElem(Result, S, N, I):-
    exactly(I, Result, S),
    I1 #= I + 1,
    validateNumOfOccurrencesForEachElem(Result, S, N, I1).


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fetchResultRegions(Board, Result, ResRows, ResCols, ResultRegions):-
    fetchResultRegions(Board, Result, ResRows, ResCols, [], 1, ResultRegions).

fetchResultRegions(_, _, ResRows, ResCols, ResultRegions, Pos, ResultRegions):-
    Pos #= ResRows * ResCols + 1.
fetchResultRegions(Board, Result, ResRows, ResCols, ResultRegionsSoFar, Pos, ResultRegions):-
    % calculating row and col of result to access
    Row #= (Pos - 1) // ResCols + 1,
    Col #= ((Pos - 1) mod ResCols) + 1,

    % get the value of result[Row][Col], which is the column where a star is placed
    getMatrixOfListElemAt(Result, ResRows, ResCols, Row, Col, StarCol),

    % get line Row of the board
    getListElemAt(Board, Row, Line),

    % get the region of that position - board[Row][StarCol]
    element(StarCol, Line, Region),
```

```
    % push value to ResultRegionsSoFar
    listPushBack(ResultRegionsSoFar, Region, NewResultRegionsSoFar),

    % fetch next element
    Pos1 #= Pos + 1,
    fetchResultRegions(Board, Result, ResRows, ResCols, NewResultRegionsSoFar, Pos1, ResultRegions).


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noAdjacentStars(Result, S, N):-
    noAdjacentStars(Result, S, N, 1).

noAdjacentStars(Result, S, N, 1):-
    noAdjacentStarsOnRow(Result, S, 1),
    noAdjacentStars(Result, S, N, 2).
noAdjacentStars(_, _, N, Row):-
    Row #= N + 1.
noAdjacentStars(Result, S, N, Row):-
    Row #> 1,
    noAdjacentStarsOnRow(Result, S, Row),
    noAdjacentStarsWithPreviousRow(Result, S, Row),
    Row1 #= Row + 1,
    noAdjacentStars(Result, S, N, Row1).


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noAdjacentStarsOnRow(Result, S, Row):-
    StartPos #= (Row - 1) * S + 1,
    EndPos #= StartPos + S,
    validateStarsFromStartToEnd(Result, StartPos, EndPos).

validateStarsFromStartToEnd(Result, Start, End):-
    Next #= Start + 1,
    validateStarsFromStartToEnd(Result, Start, Next, End).

validateStarsFromStartToEnd(_, Start, _, End):-
    Start #= End - 1.
validateStarsFromStartToEnd(Result, Start, End, End):-
    Start1 #= Start + 1,
    Next #= Start1 + 1,
    validateStarsFromStartToEnd(Result, Start1, Next, End).
validateStarsFromStartToEnd(Result, Start, Next, End):-
    validateHorizontalDistanceBetweenStars(Result, Start, Next),
```

```
    Next1 #= Next + 1,
    validateStarsFromStartToEnd(Result, Start, Next1, End).


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noAdjacentStarsWithPreviousRow(Result, S, Row):-
    StartPos #= (Row - 1) * S + 1,
    EndPos #= StartPos + S,
    noAdjacentStarsWithPreviousRow(Result, S, Row, StartPos, EndPos).

noAdjacentStarsWithPreviousRow(_, _, _, EndPos, EndPos).
noAdjacentStarsWithPreviousRow(Result, S, Row, CurrentPos, EndPos):-
    % for each star of the row being validated,
    % validate horizontal distance to each star of the previous row
    PrevRow #= Row - 1,
    starIsNotAdjacentWithAnyOfThePreviousRow(Result, S, CurrentPos, PrevRow),
    % procceed to next row
    CurrentPos1 #= CurrentPos + 1,
    noAdjacentStarsWithPreviousRow(Result, S, Row, CurrentPos1, EndPos).

starIsNotAdjacentWithAnyOfThePreviousRow(Result, S, PivotStar, PrevRow):-
    FirstStarPos #= (PrevRow - 1) * S + 1,
    LastStarPos #= FirstStarPos + S,
    starIsNotAdjacentToAnyOtherStarFromFirstToLastPos(Result, PivotStar, FirstStarPos, LastStarPos).

starIsNotAdjacentToAnyOtherStarFromFirstToLastPos(_, _, LastStarPos, LastStarPos).
starIsNotAdjacentToAnyOtherStarFromFirstToLastPos(Result, PivotStar, CurrentStarPos, LastStarPos):-
    validateHorizontalDistanceBetweenStars(Result, PivotStar, CurrentStarPos),
    NextStarPos #= CurrentStarPos + 1,
    starIsNotAdjacentToAnyOtherStarFromFirstToLastPos(Result, PivotStar, NextStarPos, LastStarPos).


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validateHorizontalDistanceBetweenStars(Result, Pos1, Pos2):-
    element(Pos1, Result, Col1),
    element(Pos2, Result, Col2),
    Dist #= abs(Col2 - Col1),
    Dist #> 1.
```

printer.pl

```
%==============================%
```

```
%= @@ board printing functions =%
%==============================%
printBoard(Board):-
    getBoardSize(Board, N),
    printBoardTopBorder(N),
    printBoard(Board, 1, N),
    nl, !.
printResultBoard(Board, Result, S):-
    getBoardSize(Board, N),
    printBoardTopBorder(N),
    printBoard(Board, 1, N, Result, S),
    nl, !.

printBoardTopBorder(N):-
    N1 is N - 1, createSeparatorN(N1, '______', TopBorder),
    write(' '), printList(TopBorder), write('_____'), nl.

printBoard(Board, N, N):-
    printBoardRow(Board, N, N).
printBoard(Board, I, N):-
    printBoardRow(Board, I, N), !,
    I1 is I + 1,
    printBoard(Board, I1, N).
%-%-%-%-%-%-%
printBoard(Board, N, N, Result, S):-
    printBoardRow(Board, N, N, Result, S).
printBoard(Board, I, N, Result, S):-
    printBoardRow(Board, I, N, Result, S), !,
    I1 is I + 1,
    printBoard(Board, I1, N, Result, S).

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printBoardRow(Board, N, N):-
    write('|'), printBoardRowTop(Board, N, N, 1), nl, !,
    write('|'), printBoardRowMiddle(Board, N, N, 1), nl, !,
    write('|'), printBoardLastRowBottom(Board, N, N, 1), nl, !.
printBoardRow(Board, I, N):-
    write('|'), printBoardRowTop(Board, I, N, 1), nl, !,
    write('|'), printBoardRowMiddle(Board, I, N, 1), nl, !,
    write('|'), printBoardRowBottom(Board, I, N, 1), nl, !.
%-%-%-%-%-%-%
printBoardRow(Board, N, N, Result, S):-
    write('|'), printBoardRowTop(Board, N, N, 1), nl, !,
    write('|'), printBoardRowMiddle(Board, N, N, 1, Result, S), nl, !,
```

```
    write('|'), printBoardLastRowBottom(Board, N, N, 1), nl, !.
printBoardRow(Board, I, N, Result, S):-
    write('|'), printBoardRowTop(Board, I, N, 1), nl, !,
    write('|'), printBoardRowMiddle(Board, I, N, 1, Result, S), nl, !,
    write('|'), printBoardRowBottom(Board, I, N, 1), nl, !.

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printBoardRowTop(_, _, N, N):-
    write('     |').
printBoardRowTop(Board, I, N, Col):-
    getListElemAt(Board, I, Row),
    Col1 is Col + 1,
    element(Col, Row, V1),
    element(Col1, Row, V2),
    printCellTop(V1, V2),
    printBoardRowTop(Board, I, N, Col1).

% @@@ swap comment to toggle region display
%printBoardRowMiddle(Board, I, N, N):-
%   getListElemAt(Board, I, Row),
%   element(N, Row, V1),
%   write('  '), write(V1), write('  |').
printBoardRowMiddle(_, _, N, N):-
    write('     |').
printBoardRowMiddle(Board, I, N, Col):-
    getListElemAt(Board, I, Row),
    Col1 is Col + 1,
    element(Col, Row, V1),
    element(Col1, Row, V2),
    printValue(V1, V2),
    printBoardRowMiddle(Board, I, N, Col1).
%-%-%-%-%-%-%
printBoardRowMiddle(_, I, N, N, Result, S):-
    starExistsIn(Result, S, I, N),
    write('  *  |').
printBoardRowMiddle(_, _, N, N, _, _):-
    write('     |').
printBoardRowMiddle(Board, I, N, Col, Result, S):-
    starExistsIn(Result, S, I, Col),

    getListElemAt(Board, I, Row),
    Col1 is Col + 1,
    element(Col, Row, V1),
    element(Col1, Row, V2),
```

```
    printStar(V1, V2),
    printBoardRowMiddle(Board, I, N, Col1, Result, S).
printBoardRowMiddle(Board, I, N, Col, Result, S):-
    getListElemAt(Board, I, Row),
    Col1 is Col + 1,
    element(Col, Row, V1),
    element(Col1, Row, V2),
    printValue(V1, V2),
    printBoardRowMiddle(Board, I, N, Col1, Result, S).

printBoardRowBottom(Board, I, N, N):-
    getListElemAt(Board, I, Row),
    I1 is I + 1, getListElemAt(Board, I1, NextRow),

    element(N, Row, V1),
    element(N, NextRow, V3),

    printCellBottom(V1, V3).
printBoardRowBottom(Board, I, N, Col):-
    getListElemAt(Board, I, Row),
    I1 is I + 1, getListElemAt(Board, I1, NextRow),
    NextCol is Col + 1,

    element(Col, Row, V1),
    element(NextCol, Row, V2),
    element(Col, NextRow, V3),

    printCellBottom(V1, V2, V3),
    printBoardRowBottom(Board, I, N, NextCol).

printBoardLastRowBottom(_, _, N, N):-
    write('_____|').
printBoardLastRowBottom(Board, I, N, Col):-
    getListElemAt(Board, I, Row),
    NextCol is Col + 1,

    element(Col, Row, V1),
    element(NextCol, Row, V2),

    printLastRowCellBottom(V1, V2),
    printBoardLastRowBottom(Board, I, N, NextCol).

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printCellTop(V1, V1):-
```

```
    write('     .').
printCellTop(_, _):-
    write('     |').

% @@@ swap comment to toggle region display
%printValue(V, V):-
%   write('  '), write(V), write('  .').
printValue(V, V):-
    write('     .').

% @@@ swap comment to toggle region display
%printValue(V, _):-
%   write('  '), write(V), write('  |').
printValue(_, _):-
    write('     |').

printStar(V, V):-
    write('  *  .').
printStar(_, _):-
    write('  *  |').

printCellBottom(V, V, V):-
    write(' . . .').
printCellBottom(V, V, _):-
    write('_____.').
printCellBottom(V, _, V):-
    write(' . . |').
printCellBottom(_, _, _):-
    write('_____|').

printCellBottom(V, V):-
    write(' . . |').
printCellBottom(_, _):-
    write('_____|').

printLastRowCellBottom(V, V):-
    write('______').
printLastRowCellBottom(_, _):-
    write('_____|').


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createSeparatorN(0, _, []).
createSeparatorN(N, SS, [SS | Ls]):-
```

```
    N1 is N-1,
    createSeparatorN(N1, SS, Ls).


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starExistsIn(Result, S, Row, StarCol):-
    StartPos is (Row - 1) * S + 1,
    EndPos is StartPos + S,
    starExistsSomewhereBetween(Result, StartPos, EndPos, StarCol).

starExistsSomewhereBetween(Result, CurrentPos, _, StarCol):-
    element(CurrentPos, Result, ScanRes),
    StarCol =:= ScanRes.
starExistsSomewhereBetween(Result, CurrentPos, EndPos, StarCol):-
    NextPos is CurrentPos + 1,
    NextPos < EndPos,
    starExistsSomewhereBetween(Result, NextPos, EndPos, StarCol).


%================================%
%= @@ result printing functions =%
%================================%
printResult(Result, N, S):-
    write('Result:'), nl,
    printResultRow(Result, N, S, 1).


printResultRow(Result, N, S, N):-
    write('\t'), printResultRowValues(Result, N, S, N, 1).

printResultRow(Result, N, S, Row):-
    write('\t'), printResultRowValues(Result, N, S, Row, 1),

    Row1 is Row + 1,
    printResultRow(Result, N, S, Row1).


printResultRowValues(Result, _, S, Row, S):-
    Pos is (Row - 1) * S + S,
    getListElemAt(Result, Pos, Elem),
    write(Elem), nl.

printResultRowValues(Result, N, S, Row, Column):-
    Pos is (Row - 1) * S + Column,
```

```
    getListElemAt(Result, Pos, Elem),
    write(Elem), write(', '),

    Column1 is Column + 1,
    printResultRowValues(Result, N, S, Row, Column1).
```

containers.pl

```
%=================%
%= @@ containers =%
%=================%
% containers are indexed starting at 1, not 0.

%%% 1. matrix; 2. element row; 3. element column; 4. query element.
getMatrixElemAt([ListAtTheHead|_], 1, ElemCol, Elem):-
    getListElemAt(ListAtTheHead, ElemCol, Elem).
getMatrixElemAt([_|RemainingLists], ElemRow, ElemCol, Elem):-
    ElemRow > 1,
    ElemRow1 is ElemRow - 1,
    getMatrixElemAt(RemainingLists, ElemRow1, ElemCol, Elem).

% treats list as if it was a matrix of NRows x NCols and returns the Elem at ElemRow, ElemCol
getMatrixOfListElemAt(List, NRows, NCols, ElemRow, ElemCol, Elem):-
    ElemRow =< NRows, ElemCol =< NCols,
    Pos is (ElemRow - 1) * NCols + ElemCol,
    element(Pos, List, Elem).

%%% 1. list; 2. element position; 3. query element.
getListElemAt([ElemAtTheHead|_], 1, ElemAtTheHead).
getListElemAt([_|RemainingElems], Pos, Elem):-
    Pos > 1,
    Pos1 is Pos - 1,
    getListElemAt(RemainingElems, Pos1, Elem).

listPushBack([], Elem, [Elem]).
listPushBack([Head|Tail], Elem, [Head|NewTail]):-
    listPushBack(Tail, Elem, NewTail).

printList([]).
printList([Head|Tail]):-
    write(Head), printList(Tail).
```

utilities.pl

```
%================%
%= @@ utilities =%
%================%
clearConsole:-
    clearConsole(40), !.
clearConsole(0).
clearConsole(N):-
    nl,
    N1 is N-1,
    clearConsole(N1).

pressEnterToContinue:-
    write('Press <Enter> to show the solution.'), nl,
    waitForEnter, !.
waitForEnter:-
    get_char(_).

exactly(_, [], 0).
exactly(X, [Y|L], N) :-
    X #= Y #<=> B,
    N #= M + B,
    exactly(X, L, M).
```

starBattleTestBoards.pl

```
%======================================%
%= @@ function to retrieve test boards =%
%======================================%
getBoard(N, Board):-
    (
        N =:= 1 -> testBoard4x4_1(Board);
        N =:= 2 -> testBoard5x5_1(Board);
        N =:= 3 -> testBoard5x5_2(Board);
        N =:= 4 -> testBoard8x8_1(Board);
        N =:= 5 -> testBoard8x8_2(Board);
        N =:= 6 -> testBoard10x10_1(Board);
        N =:= 7 -> testBoard10x10_2(Board);

        nl,
        write('Error: the specified board does not exist.'),
        fail
    ).
```

```
%==================%
%= @@ test boards =%
%==================%
% expected answer:2413
testBoard4x4_1([
    [1, 2, 1, 1],
    [1, 1, 1, 3],
    [4, 1, 1, 1],
    [1, 1, 1, 1]]).

% expected answer: 14253
testBoard5x5_1([
    [1, 1, 2, 2, 2],
    [1, 2, 2, 3, 2],
    [1, 2, 2, 2, 2],
    [4, 2, 4, 2, 5],
    [4, 4, 4, 5, 5]]).

testBoard5x5_2([
    [1, 1, 1, 2, 2],
    [1, 3, 3, 3, 4],
    [1, 1, 3, 3, 4],
    [1, 5, 5, 5, 5],
    [1, 1, 1, 5, 5]]).

% expected answer: 2468246813571357
testBoard8x8_1([
    [1, 2, 3, 4, 5, 6, 7, 8],
    [1, 2, 3, 4, 5, 6, 7, 8],
    [1, 2, 3, 4, 5, 6, 7, 8],
    [1, 2, 3, 4, 5, 6, 7, 8],
    [1, 2, 3, 4, 5, 6, 7, 8],
    [1, 2, 3, 4, 5, 6, 7, 8],
    [1, 2, 3, 4, 5, 6, 7, 8],
    [1, 2, 3, 4, 5, 6, 7, 8]]).

% expected answer: 2468246813571357
testBoard8x8_2([
    [1, 1, 1, 1, 1, 1, 1, 1],
    [2, 2, 2, 2, 2, 2, 2, 2],
    [3, 3, 3, 3, 3, 3, 3, 3],
    [4, 4, 4, 4, 4, 4, 4, 4],
    [5, 5, 5, 5, 5, 5, 5, 5],
    [6, 6, 6, 6, 6, 6, 6, 6],
    [7, 7, 7, 7, 7, 7, 7, 7],
```

```
    [8, 8, 8, 8, 8, 8, 8, 8]]).

testBoard10x10_1([
    [1,  1,  1,  2,  2,  3,  3,  3,  3,  3],
    [1,  4,  4,  4,  2,  5,  3,  5,  3,  6],
    [1,  1,  1,  4,  2,  5,  3,  5,  6,  6],
    [1,  4,  4,  4,  2,  5,  5,  5,  6,  6],
    [1,  4,  7,  7,  7,  8,  9,  5,  9,  6],
    [1,  4,  4,  4,  7,  8,  9,  5,  9,  6],
    [1,  1,  7,  7,  7,  8,  9,  9,  9,  6],
    [10, 10, 7,  8,  8,  8,  8,  8,  9,  6],
    [10, 10, 7,  7,  7,  10, 6,  8,  9,  6],
    [10, 10, 10, 10, 10, 10, 6,  6,  6,  6]]).

testBoard10x10_2([
    [1,  1,  1,  2,  2,  2,  2,  2,  2,  2],
    [3,  3,  1,  1,  1,  1,  2,  2,  2,  2],
    [3,  4,  4,  4,  4,  5,  5,  5,  5,  2],
    [3,  4,  4,  4,  4,  5,  5,  5,  6,  2],
    [3,  7,  7,  7,  7,  7,  7,  5,  6,  2],
    [3,  7,  8,  6,  6,  6,  6,  6,  6,  2],
    [3,  7,  8,  8,  8,  9,  9,  9,  9,  2],
    [3,  8,  8,  8,  8,  9,  9,  9,  9,  2],
    [3,  3,  10, 10, 10, 10, 10, 10, 2,  2],
    [10, 10, 10, 10, 10, 10, 10, 10, 10, 10]]).
```

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If you wonder what LaTeX is and where it can be obtained, see the "*LaTeX project site*" (`http://www.latex-project.org`) and especially the webpage "*How to get it*" (`http://www.latex-project.org/ftp.html`) respectively.

When you use LaTeX together with our document class file, `llncs.cls`, your text is typeset automatically in Computer Modern Roman (CM) fonts. Please do *not* change the preset fonts. If you have to use fonts other than the preset fonts, kindly submit these with your files.

Please use the commands `\label` and `\ref` for cross-references and the commands `\bibitem` and `\cite` for references to the bibliography, to enable us to create hyperlinks at these places.

For preparing your figures electronically and integrating them into your source file we recommend using the standard LaTeX `graphics` or `graphicx` package. These provide the `\includegraphics` command. In general, please refrain from using the `\special` command.

Remember to submit any further style files and fonts you have used together with your source files.

Headings. Headings should be capitalized (i.e., nouns, verbs, and all other words except articles, prepositions, and conjunctions should be set with an initial capital) and should, with the exception of the title, be aligned to the left. Words joined by a hyphen are subject to a special rule. If the first word can stand alone, the second word should be capitalized.

Here are some examples of headings: "Criteria to Disprove Context-Freeness of Collage Language", "On Correcting the Intrusion of Tracing Non-deterministic Programs by Software", "A User-Friendly and Extendable Data Distribution System", "Multi-flip Networks: Parallelizing GenSAT", "Self-determinations of Man".

Lemmas, Propositions, and Theorems. The numbers accorded to lemmas, propositions, and theorems, etc. should appear in consecutive order, starting with Lemma 1, and not, for example, with Lemma 11.

6.1 Figures

For LaTeX users, we recommend using the *graphics* or *graphicx* package and the `\includegraphics` command.

Please check that the lines in line drawings are not interrupted and are of a constant width. Grids and details within the figures must be clearly legible and may not be written one on top of the other. Line drawings should have a resolution of at least 800 dpi (preferably 1200 dpi). The lettering in figures should have a height of 2 mm (10-point type). Figures should be numbered and should have a caption which should always be positioned *under* the figures, in contrast to the caption belonging to a table, which should always appear *above* the table; this is simply achieved as matter of sequence in your source.

Please center the figures or your tabular material by using the `\centering` declaration. Short captions are centered by default between the margins and typeset in 9-point type (Fig. 1 shows an example). The distance between text and figure is preset to be about 8 mm, the distance between figure and caption about 6 mm.

To ensure that the reproduction of your illustrations is of a reasonable quality, we advise against the use of shading. The contrast should be as pronounced as possible.

If screenshots are necessary, please make sure that you are happy with the print quality before you send the files.

Figura 1. One kernel at x_s (*dotted kernel*) or two kernels at x_i and x_j (*left and right*) lead to the same summed estimate at x_s. This shows a figure consisting of different types of lines. Elements of the figure described in the caption should be set in italics, in parentheses, as shown in this sample caption.

Please define figures (and tables) as floating objects. Please avoid using optional location parameters like "`[h]`"for "here".

Remark 1. In the printed volumes, illustrations are generally black and white (halftones), and only in exceptional cases, and if the author is prepared to cover the extra cost for color reproduction, are colored pictures accepted. Colored pictures are welcome in the electronic version free of charge. If you send colored figures that are to be printed in black and white, please make sure that they really are legible in black and white. Some colors as well as the contrast of converted colors show up very poorly when printed in black and white.

6.2 Formulas

Displayed equations or formulas are centered and set on a separate line (with an extra line or halfline space above and below). Displayed expressions should be numbered for reference. The numbers should be consecutive within each section or within the contribution, with numbers enclosed in parentheses and set on the right margin – which is the default if you use the *equation* environment, e.g.,

$$\psi(u) = \int_o^T \left[\frac{1}{2} \left(\Lambda_o^{-1} u, u \right) + N^*(-u) \right] dt \; . \tag{1}$$

Equations should be punctuated in the same way as ordinary text but with a small space before the end punctuation mark.

6.3 Footnotes

The superscript numeral used to refer to a footnote appears in the text either directly after the word to be discussed or – in relation to a phrase or a sentence – following the punctuation sign (comma, semicolon, or period). Footnotes should appear at the bottom of the normal text area, with a line of about 2 cm set immediately above them.[1]

[1] The footnote numeral is set flush left and the text follows with the usual word spacing.

6.4 Program Code

Program listings or program commands in the text are normally set in typewriter font, e.g., CMTT10 or Courier.

Example of a Computer Program

```
program Inflation (Output)
  {Assuming annual inflation rates of 7%, 8%, and 10%,...
   years};
   const
     MaxYears = 10;
   var
     Year: 0..MaxYears;
     Factor1, Factor2, Factor3: Real;
   begin
     Year := 0;
     Factor1 := 1.0; Factor2 := 1.0; Factor3 := 1.0;
     WriteLn('Year  7% 8% 10%'); WriteLn;
     repeat
       Year := Year + 1;
       Factor1 := Factor1 * 1.07;
       Factor2 := Factor2 * 1.08;
       Factor3 := Factor3 * 1.10;
       WriteLn(Year:5,Factor1:7:3,Factor2:7:3,Factor3:7:3)
     until Year = MaxYears
end.
```

(Example from Jensen K., Wirth N. (1991) Pascal user manual and report. Springer, New York)

6.5 Citations

For citations in the text please use square brackets and consecutive numbers: [1], [2], [4] – provided automatically by LaTeX's `\cite` ... `\bibitem` mechanism.

6.6 Page Numbering and Running Heads

There is no need to include page numbers. If your paper title is too long to serve as a running head, it will be shortened. Your suggestion as to how to shorten it would be most welcome.

7 LNCS Online

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8 BibTeX Entries

The correct BibTeX entries for the Lecture Notes in Computer Science volumes can be found at the following Website shortly after the publication of the book:
`http://www.informatik.uni-trier.de/~ley/db/journals/lncs.html`

Acknowledgments. The heading should be treated as a subsubsection heading and should not be assigned a number.

9 The References Section

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We only accept references written using the latin alphabet. If the title of the book you are referring to is in Russian or Chinese, then please write (in Russian) or (in Chinese) at the end of the transcript or translation of the title.

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Referências

1. Smith, T.F., Waterman, M.S.: Identification of Common Molecular Subsequences. J. Mol. Biol. 147, 195–197 (1981)
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3. Foster, I., Kesselman, C.: The Grid: Blueprint for a New Computing Infrastructure. Morgan Kaufmann, San Francisco (1999)
4. Czajkowski, K., Fitzgerald, S., Foster, I., Kesselman, C.: Grid Information Services for Distributed Resource Sharing. In: 10th IEEE International Symposium on High Performance Distributed Computing, pp. 181–184. IEEE Press, New York (2001)
5. Foster, I., Kesselman, C., Nick, J., Tuecke, S.: The Physiology of the Grid: an Open Grid Services Architecture for Distributed Systems Integration. Technical report, Global Grid Forum (2002)
6. National Center for Biotechnology Information, `http://www.ncbi.nlm.nih.gov`

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10 Checklist of Items to be Sent to Volume Editors

Here is a checklist of everything the volume editor requires from you:

- ☐ The final LaTeX source files
- ☐ A final PDF file
- ☐ A copyright form, signed by one author on behalf of all of the authors of the paper.
- ☐ A readme giving the name and email address of the corresponding author.