2. Realne funkcije realne varijable - 2. dio

1. Odredite asimptote funkcija i skicirajte njihove grafove:

(a)
$$f(x) = \frac{x^2}{x^2 - 4}$$
;

(b)
$$g(x) = \frac{1}{x^2 - 1}$$
;

(c)
$$h(x) = \frac{x^2 + 2x - 3}{x + 3}$$
;

(d)
$$f(x) = \frac{x^2 + 2x - 3}{x + 5}$$
;

(e)
$$f(x) = \frac{x^2 + 2x}{x - 2}$$
.

2. Nacrtajte grafove funkcija:

(a)
$$f(x) = |6 + x - x^2|$$
;

(b)
$$f(x) = -x|x|$$
;

(c)
$$f(x) = x^3 - 3x^2 + 4$$
;

(d)
$$f(x) = 4x - 3x^2 - x^3$$
.

3. Nacrtajte grafove funkcija:

(a)
$$f(x) = 2\sin\left(\frac{1}{2}x - \frac{\pi}{4}\right);$$

(b)
$$f(x) = \cos^2 x$$
.

4. Odredite domenu funkcija:

(a)
$$f(x) = \frac{x}{x}$$
;

(b)
$$f(x) = \frac{1}{1+x^2}$$
;

(c)
$$f(x) = \frac{1}{\sqrt{1-x^2}}$$
;

(d)
$$f(x) = \sqrt{x - x^3}$$
;

(e)
$$f(x) = \sqrt{(x-2)^4}$$
;

(f)
$$f(x) = (\sqrt{x-2})^4$$
;

(g)
$$f(x) = \ln(\sin x)$$
;

(h)
$$f(x) = \ln|\sin x|$$
.

5. Odredite domenu funkcija:

(a)
$$f(x) = \arctan(x+2) - \ln(-x);$$

(b)
$$f(x) = \arcsin \frac{x-3}{2} - \log (4-x);$$

(c)
$$f(x) = \log \frac{x^2 - 3x + 2}{x + 1}$$
;

(d)
$$f(x) = \sqrt{\log \frac{3 - 2x - 5x^2}{8x - 17}}$$
;

(e)
$$f(x) = \arccos(\log_{\frac{1}{3}} x);$$

(f)
$$f(x) = \ln(\arcsin\frac{1-x^2}{2+x})$$
.