

<b>Started on</b>	Saturday, 19 March 2022, 4:09 PM
<b>State</b>	Finished
<b>Completed on</b>	Saturday, 19 March 2022, 4:50 PM
<b>Time taken</b>	40 mins 19 secs
<b>Marks</b>	18.00/20.00
<b>Grade</b>	9.00 out of 10.00 (90%)

**Question 1**

Complete

Mark 1.00 out of 1.00

What are the median and mode of the following series : 2; 2; 2; 4; 4; 5; 5; 6; 8; 11; 12; 16; 18?

- ☐ a. 6 and 5
- ☒ b. 5 and 2
- ☐ c. 5.5 and 2
- ☐ d. 5 and 5
- ☐ e. None of the others

Question **2**

Complete

Mark 1.00 out of 1.00

Assume that human body temperatures are normally distributed with a mean of 98 (degree F) and a standard deviation of 0.5(degree F). Describe the sampling distribution for the sample mean body temperature of 50 selected persons.

- ☐ a. Approximately normal with a mean of 98(degree F) and a standard deviation of 0.07(degree F)
- ☐ b. None of the other choices is correct
- ☒ c. Normal with a mean of 98(degree F) and a standard deviation of 0.07(degree F)
- ☐ d. Approximately normal with a mean of 98(degree F) and a standard deviation of 0.01(degree F)
- ☐ e. Normal with a mean of 98(degree F) and a standard deviation of 0.01(degree F)

## Question 3

Complete

Mark 1.00 out of 1.00

Give  $f(x)=0,75 \cdot 0,25^x$ ,  $x = 0,1,2,\dots$  is the probability mass function. Which the following statement is NOT TRUE?

- ☐ a.  $P(X \leq 2) = 63/64$
- ☐ b.  $P(X = 2) = 3/64$
- ☒ c.  $P(X \geq 1) = 48/64$
- ☐ d. All of the others

Question **4**

Complete

Mark 1.00 out of 1.00

A population has a mean of  $m=100$  and a standard deviation of  $s=15$ . If we draw a simple random sample of size  $n=36$ , what is the probability that the sample mean  $\bar{x}$  will be less than 105? That is, what is  $P(\bar{x} < 105)$ ?

- ☐ a. 0.9901847
- ☐ b. 0.9522096
- ☐ c. 0.9087888
- ☒ d. 0.9772499

Question 5

Complete

Mark 0.00 out of 1.00

Two Web colors are used for a site advertisement with given probabilities:

Ad color	Affiliate (30%)	Search (70%)
Blue	0.7	0.4
Green	0.3	0.6

What is the probability that a visitor is from a **search site** given that the **green** ad was viewed?  
Round to 2 decimal places.

☐ a. 0.82

☒ b. 0.6

☐ c. 0.42

☐ d. 0.18

☐ e. None of these

$$P(\text{Green}) = P(\text{Green} \mid \text{Affiliate}) * P(\text{Affiliate}) + P(\text{Green} \mid \text{Search}) * P(\text{Search}) = 0.3 * 0.3 + 0.6 * 0.7$$
$$P(\text{Search} \mid \text{Green}) = \frac{P(\text{Green} \mid \text{Search}) * P(\text{Search})}{P(\text{Green})}$$
$$= \frac{(0.6 * 0.7)}{(0.3 * 0.3 + 0.6 * 0.7)}$$

Question **6**

Complete

Mark 1.00 out of 1.00

Choose the true statement(s):

- ☐ a. Population is any subset of the elements of a sample.
- ☐ b. In statistical inference, the reasoning is from population to a sample .
- ☐ c. Population is in sample.
- ☒ d. Population is any finite or infinite collection of individual units or objects.

## Question 7

Complete

Mark 1.00 out of 1.00

Suppose that after 10 years of service, 40% of computers have problems with motherboards (MB), 30% have problems with hard drives (HD), and 15% have problems with both MB and HD. What is the probability that a 10-year old computer has problems with MB or HD?

- ☐ a. 0.45
- ☒ b. 0.55
- ☐ c. 0.3
- ☐ d. 0.7
- ☐ e. 0.4

$$P(MB) = 0.4, P(HD) = 0.3, P(MB \cap HD) = 0.15$$

$$\Rightarrow P(MB \cup HD) = P(MB) + P(HD) - P(MB \cap HD) = 0.4 + 0.3 - 0.15 = 0.55$$

Question **8**

Complete

Mark 1.00 out of 1.00

Suppose that  $P(A|B) = 0.4$ ,  $P(A|B') = 0.3$ , and  $P(B) = 0.6$ . What is  $P(A)$ ?

- ☐ a. None of these  
☐ b. 0.12  
☐ c. 0.1  
☒ d. 0.36  
☐ e. 0.7

Apply total probability formula

$$\begin{aligned}
 P(A) &= P(A|B)P(B) + P(A|B')P(B') \\
 &= 0.4 * 0.6 + 0.3 * 0.4 \\
 &= 0.36
 \end{aligned}$$



## Question 9

Complete

Mark 1.00 out of 1.00

Construct a 98% confidence interval for the population mean. Assume the population has a normal distribution. A study of 14 bowlers showed that their average score was 192 with a standard deviation of 8. Let  $t_{0.01, 13} = 2.65$ .

- ☐ a. (222.3, 256.1)
- ☐ b. (328.3, 386.9)
- ☐ c. None of the other choices is correct
- ☒ d. (186.3, 197.7)
- ☐ e. (115.4, 158.8)

## Question 10

Complete

Mark 1.00 out of 1.00

A sample of five price/earnings ratios for companies in the Services sector follows.

15 11 14 17 12

A confidence interval for the population mean is requested. In order to construct the confidence interval one must assume

- ☐ a. No assumptions are needed
- ☐ b. None of choices are correct
- ☐ c. that the population standard deviation is known
- ☒ d. that the sample came from a normal distribution

Question **11**

Complete

Mark 1.00 out of 1.00

Let  $X$  represent the amount of time it takes a student to park in the library parking lot at the university. If we know that the distribution of parking times can be modelled using an exponential distribution with a mean of 4 minutes, find the probability that it will take a randomly selected student more than 10 minutes to park in the library lot.

- ☐ a. 0.670320
- ☐ b. None of the other choices is correct
- ☒ c. 0.082085
- ☐ d. 0.917915
- ☐ e. 0.329680

Question **12**

Complete

Mark 1.00 out of 1.00

If we select a sample with sample size 40 from a population with mean of 20 and standard deviation of 5 then:

- ☒ a. Sample mean will be approximately normally distributed with mean of 20 and standard deviation of 0.79.
- ☐ b. Sample mean will be exactly normally distributed with mean of 20 and standard deviation of 5.
- ☐ c. Sample mean will be approximately normally distributed with mean of 20 and standard deviation of 5.
- ☐ d. Sample mean will be exactly normally distributed with mean of 20 and standard deviation of 0.79.

Question **13**

Complete

Mark 1.00 out of 1.00

A salesperson knows that 20% of her presentations result in sales. Use the normal approximation formula for the Binomial distribution to find the probabilities that in the next 60 presentations at least 9 result in sales.

Let  $P(Z < -1.13) = 0.1268$  and  $P(Z < -0.81) = 0.2089$ .

- ☒ a. 0.8732
- ☐ b. 0.7911
- ☐ c. 0.6421
- ☐ d. 0.1241
- ☐ e. None of the other choices is correct

Question **14**

Complete

Mark 0.00 out of 1.00

The continuous random variable  $X$  has probability density function is  $f(x)=e^{-x}$ ,  $x>0$ . Find  $P(X=2010)$ .

- ☒ a. 1
- ☐ b. None of the others.
- ☐ c. 0
- ☐ d.  $1/e^{-2010}$

Question **15**

Complete

Mark 1.00 out of 1.00

Suppose that  $\mu = 16$  and  $\sigma^2 = 20$  for a population. In a sample where  $n = 100$  is randomly taken, what is the standard deviation for the sample mean?

- ☐ a. 0.2
- ☒ b. 0.45
- ☐ c. 0.02
- ☐ d. None of the other choices is correct
- ☐ e. 0.16

Question **16**

Complete

Mark 1.00 out of 1.00

An exciting computer game is released. Twenty percent of players will buy an **advanced version** of the game. Among 20 users, what is the expected number of people who will buy the **advanced version**?

- ☒ a. 4
- ☐ b. None of the others
- ☐ c. 10
- ☐ d. 20
- ☐ e. 5

Let  $X$  be the number of players who will buy the advanced version among 20 players.

Then  $X$  has a binomial distribution with parameter  $n = 20$ ,  $p = 0.2$

$$\implies E(X) = np = 20 \cdot 0.2 = 4$$

Question **17**

Complete

Mark 1.00 out of 1.00

A manufacturer of electronic calculators takes a random sample of 1200 calculators and finds that there are 8 defective units. Construct a 95% confidence interval on the population proportion. Let  $z_{0.025} = 1.96$ .

- ☐ a. [0.204, 0.208]
- ☒ b. [0.0021, 0.0113]
- ☐ c. None of others
- ☐ d. [0.0021, 0.274]

Question **18**

Complete

Mark 1.00 out of 1.00

The life in hours of a 400 - watt light is known to be normally distributed with standard deviation of 25 hours. A random sample of 20 lights has a mean life of 1014 hours. Construct a 95% two - sided confidence interval on the mean life. Let  $Z_{0.025} = 1.96$

- ☐ a. (1003, 1005)
- ☐ b. None of others.
- ☐ c. (1003, 1050)
- ☒ d. (1003, 1025)

Question **19**

Complete

Mark 1.00 out of 1.00

Eight measurements were made on the inside diameter of forged piston rings used in an automobile engine. The data (in millimeters) are 74.10; 74.30; 74.15; 74.00; 74.25; 74.20; 74.05; and 74.14. Calculate the sample mean.

- ☒ a. 74.14875
- ☐ b. 74.00875
- ☐ c. 74.00815
- ☐ d. None of these
- ☐ e. 74.00578



Question **20**

Complete

Mark 1.00 out of 1.00

Consider the time to recharge the flash in a camera. The probability that a camera passes the test is 0.9, and the cameras perform independently. What is the probability that the second failure is obtained at the fifth test?

- ☐ a. 0.003
- ☒ b. 0.029
- ☐ c. None of the others
- ☐ d. 0.035
- ☐ e. 0.047

Let X be the number of tests until the second failure.

Then X has a negative binomial distribution with parameter  $p = 0.1$  and  $r = 2$ .

We wish to find  $P(X = 5)$ .

$$P(X = 5) = \binom{4}{1} 0.1^2 (0.9)^3 = 0.029$$



