

Started on	Wednesday, 14 July 2021, 10:17 PM
State	Finished
Completed on	Wednesday, 14 July 2021, 10:28 PM
Time taken	11 mins 30 secs
Grade	9.00 out of 10.00 (90%)

## Question 1

Correct

Mark 1.00 out of 1.00

Given the adjacency matrix of a digraph.

$$\begin{matrix} & \begin{matrix} a & b & c & d \end{matrix} \\ \begin{matrix} a \\ b \\ c \\ d \end{matrix} & \begin{bmatrix} 0 & 1 & 1 & 1 \\ 1 & 1 & 0 & 2 \\ 0 & 1 & 0 & 1 \\ 2 & 1 & 0 & 1 \end{bmatrix} \end{matrix}$$

How many paths of length 4 from the vertex b to the vertex c?

- ☐ a. 11
- ☐ b. None of these
- ☐ c. 28
- ☐ d. 8
- ☒ e. 14



Your answer is correct.

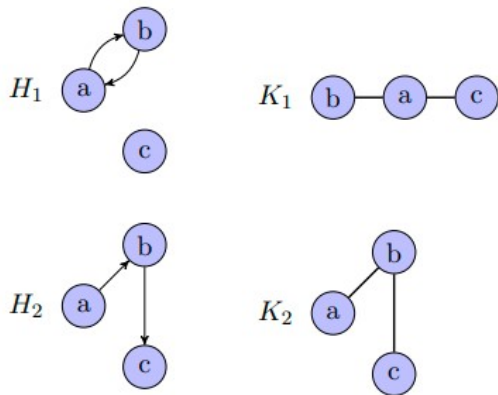
$$A^4 = \begin{matrix} & \begin{matrix} a & b & c & d \end{matrix} \\ \begin{matrix} a \\ b \\ c \\ d \end{matrix} & \begin{bmatrix} 36 & 37 & 11 & 47 \\ 53 & 53 & 14 & 68 \\ 28 & 29 & 8 & 37 \\ 50 & 49 & 14 & 63 \end{bmatrix} \end{matrix}$$

The correct answer is: 14

## Question 2

Correct

Mark 1.00 out of 1.00



State true or false.

(1)  $H_1$  and  $H_2$  are isomorphic(2)  $K_1$  and  $K_2$  are isomorphic

- ☐ a. (1) False, (2) False  
☐ b. (1) True, (2) True  
☐ c. (1) True, (2) False  
☒ d. (1) False, (2) True



Your answer is correct.

The correct answer is: (1) False, (2) True

## Question 3

Correct

Mark 1.00 out of 1.00

Given the adjacency matrix of a pseudograph  $G$ .

$$\begin{bmatrix} 1 & 2 & 0 & 1 \\ 2 & 0 & 3 & 0 \\ 0 & 3 & 1 & 1 \\ 1 & 0 & 1 & 0 \end{bmatrix}$$

How many edges does  $G$  have?

- ☐ a. 11  
☐ b. 16  
☐ c. 18  
☐ d. 8  
☒ e. 9



Your answer is correct.

The correct answer is: 9

## Question 4

Correct

Mark 1.00 out of 1.00

Given the adjacency matrix of a digraph.

	a	b	c	d	e
a	0	1	1	0	2
b	1	0	1	2	0
c	1	0	1	1	2
d	1	1	0	1	1
e	2	0	1	1	0

How many paths of length 2 from the vertex a to the vertex d?

- ☐ a. 4  
☒ b. 5  
☐ c. None of these  
☐ d. 2  
☐ e. 3



Your answer is correct.

row a      [0 1 1 0 2]

column d   [0 2 1 1 1]

result =  $0 + 2 + 1 + 0 + 2 = 5$

The correct answer is: 5

## Question 5

Correct

Mark 1.00 out of 1.00

The length of the longest simple circuit in  $K_5$  is \_\_\_\_.

- ☐ a. 8  
☐ b. 20  
☒ c. 10  
☐ d. 4!  
☐ e. 5!



Your answer is correct.

The longest simple circuit in  $K_5$  is an Euler circuit in  $K_5$ , which contains every edge of  $K_5$ .

$K_5$  has 10 edges.

The correct answer is: 10

## Question 6

Correct

Mark 1.00 out of 1.00

A simple graph is called **regular** if every vertex of this graph has the same degree. A regular graph is called  **$n$ -regular** if every vertex in this graph has degree  $n$ .

How many vertices does a regular graph of degree four with 10 edges have?

- ☒ a. 5
- ☐ b. 7
- ☐ c. 8
- ☐ d. 6



Your answer is correct.

The correct answer is: 5

## Question 7

Correct

Mark 1.00 out of 1.00

The graph  $K_{10}$  has \_\_\_ edges.

- ☐ a. 10
- ☒ b. 45
- ☐ c. 10!
- ☐ d. 90



Your answer is correct.

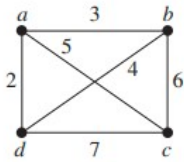
The correct answer is: 45

## Question 8

Correct

Mark 1.00 out of 1.00

Solve the traveling salesperson problem for this graph by finding the total weight of all Hamilton circuits and determining a circuit with minimum total weight.



What is the minimum total weight?

- ☒ a. 17
- ☐ b. 16
- ☐ c. 18
- ☐ d. 20
- ☐ e. 19



Your answer is correct.

$$a b c d a: 3 + 6 + 7 + 2 = 18$$

$$a b d c a: 3 + 4 + 7 + 5 = 19$$

$$a c b d a: 5 + 6 + 4 + 2 = 17$$

$$a c d b a: 5 + 7 + 4 + 3 = 19$$

$$a d b c a: 2 + 4 + 6 + 5 = 17$$

$$a d c b a: 2 + 7 + 6 + 3 = 18$$

The correct answer is: 17