Introduction to generative models of language

- » What are they?
- » Why they're important
- » Issues for counting words
- » Statistics of natural language
- » Unsmoothed n-gram models

Administrative stuff

- Course website:
 - http://www.cs.cornell.edu/courses/ cs4740/2015fa/
- Piazza
 - Signup link:
 - piazza.com/cornell/fall2015/cs4740
 - Class link:
 - piazza.com/cornell/fall2015/cs4740/ home
- CMS: turn ON notifications

Critiques

- How to do well on them
 - do not summarize the paper
 - do identify one or two points about the paper to discuss in more depth, e.g. a paragraph for each
- Due on CMS on Weds@11:59pm
- ALSO due in hardcopy form AT THE BEGINNING OF THE NEXT CLASS
- Grading: check (A-/B+), check+ (A), check- (C)
- Late assignments: 1/2 grade late per weekday

Collaboration on Critiques

- We encourage discussion of the paper with others in the class — in person and via Piazza, etc.
- The content of the critique must be yours and the writing of the critique must be done by you

***From last class

- How many word types are in this text?

Marseille is a dog. He might do a dog trick later.

[Assumptions: punctuation is treated as a word; capitalized and lowercase versions of words are treated the same.]

- A. 10
- B. 11
- C. 12
- D. 13
- E. something else

***From last class

- How many word tokens are in this text?

Marseille is a dog. He might do a dog trick later.

[Assumptions: punctuation is treated as a word; capitalized and lowercase versions of words are treated the same.]

- A. 10
- B. 11
- C. 12
- D. 13
- E. something else

Goals

- Determine the next word in a sequence
 - Probability distribution across all words in the language
 - $-P(W_{n} | W_{1} | W_{2} ... | W_{n-1})$
- Determine the probability of a sequence of words
 - $P (w_1 w_2 ... w_{n-1} w_n)$

***From last class

- We are studying n-gram models of word prediction. A bigram model is bases decisions on:
 - A. the preceding word
 - B. the two preceding words
 - C. the preceding and following word
 - D. no words in the context at all
 - E. I have no idea.

(possible) Models of word prediction

- Simplest model
 - Let any word follow any other word (equally likely)

$$> E.g., P(w_n | w_{n-1}) -> P(w_n | w_{n-1}) ->$$

P (word *n follows* word *n-1*)

Probability distribution at least obeys actual relative word frequencies

$$P (w_n | w_{n-1}) ->$$

Probability of a word sequence

• $P(w_1 w_2 ... w_{n-1} w_n)$

- Problem?
- Solution: approximate the probability of a word given all the previous words...

N-gram approximations

- Markov assumption: probability of some future event (next word) depends only on a limited history of preceding events (previous words)
- Bigram model

$$P(w_n|w_1^{n-1}) \approx P(w_n|w_{n-1})$$
 predict next word $P(w_1^n) \approx \prod_{k=1}^n P(w_k|w_{k-1})$ prob of a word sequence

- Trigram model
 - Conditions on the two preceding words
- N-gram approximation

$$P(w_1^n) pprox \prod_{k=1}^n \ P(w_k|w_{k-N+1}^{k-1})$$
 prob of a word sequence

Probability of a word sequence: bigram estimation

$$\begin{split} \mathsf{P} \left(\mathsf{W}_{1} \; \mathsf{W}_{2} \; \dots \; \mathsf{W}_{\mathsf{n-1}} \; \mathsf{W}_{\mathsf{n}} \right) \\ & P(w_{1}^{n}) = P(w_{1}) \; P(w_{2}|w_{1}) \; P(w_{3}|w_{2}^{2}) \; \dots P(w_{n}|w_{1}^{n-1}) \\ & = \mathsf{P}(\mathsf{W}_{1}) \; \mathsf{P}(\mathsf{W}_{2}|\mathsf{W}_{1}) \; \mathsf{P}(\mathsf{W}_{3}|\mathsf{W}_{2}) \; \dots \; \mathsf{P}(\mathsf{W}_{\mathsf{n}}|\mathsf{W}_{\mathsf{n-1}}) \\ & = \mathsf{P}(\mathsf{W}_{1}|<\mathsf{s}>) \; \mathsf{P}(\mathsf{W}_{2}|\mathsf{W}_{1}) \; \mathsf{P}(\mathsf{W}_{3}|\mathsf{W}_{2}) \; \dots \; \mathsf{P}(\mathsf{W}_{\mathsf{n}}|\mathsf{W}_{\mathsf{n-1}}) \\ & = \prod_{k=1}^{n} P(w_{k}|w_{1}^{k-1}) \end{split}$$