

Untitled

Problem 7.1

Function helping to make right choose about number of K

```
wssplot <- function(data, nc=15, seed=1234){  
  wss <- (nrow(data)-1)*sum(apply(data,2,var))  
  for (i in 2:nc){  
    set.seed(seed)  
    wss[i] <- sum(kmeans(data, centers=i)$withinss)}  
  plot(1:nc, wss, type="b", xlab="Number of Clusters",  
       ylab="Within groups sum of squares")}
```

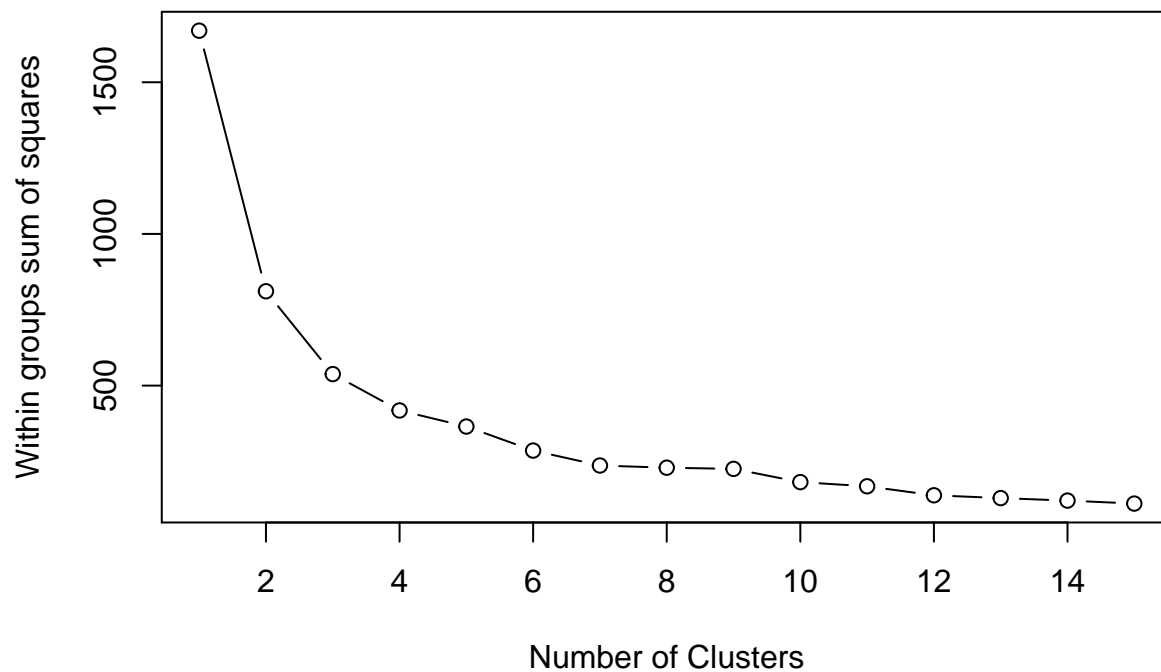
Data that we want to use for clusterization

```
kmeans.data <- data[4:6]  
head(kmeans.data)
```

```
##      Gm Age Salary  
## 1   74  28   9.50  
## 2   77  29   9.25  
## 3   83  29   9.00  
## 4   93  29   8.75  
## 5   81  29   8.75  
## 6  108  24   8.00
```

Scaling the data

```
kmeans.data.scaled <- scale(kmeans.data[-1])  
wssplot(kmeans.data.scaled)
```



Let's do some clusterization

3 clusters

```
# K-Means Cluster Analysis
fit3 <- kmeans(kmeans.data.scaled, 3)
# get cluster means
aggregate(kmeans.data.scaled, by=list(fit3$cluster), FUN=mean)
```

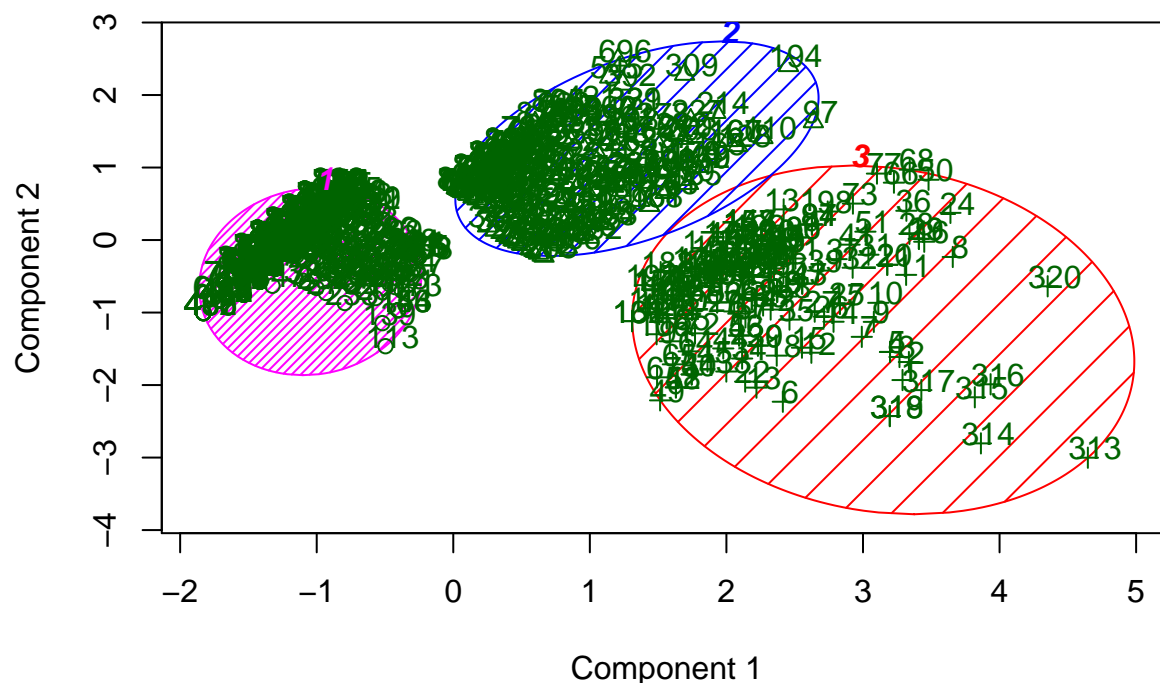
```
##   Group.1      Age      Salary
## 1      1 -0.7153821 -0.5447271
## 2      2  1.0839778 -0.1229349
## 3      3  0.5785685  1.6573821
```

```
# append cluster assignment
kmeans.data.scaled <- data.frame(kmeans.data.scaled, fit3$cluster)
```

Cluster Plot against 1st 2 principal components

```
# vary parameters for most readable graph
library(cluster)
clusplot(kmeans.data.scaled, fit3$cluster, color=TRUE, shade=TRUE, labels=2, lines=0)
```

CLUSPLOT(kmeans.data.scaled)



These two components explain 94.68 % of the point variability.

#Centroid Plot against 1st 2 discriminant functions

```
#library(fpc)
#plotcluster(kmeans.data, fit$cluster)
```

4 clusters

```
# K-Means Cluster Analysis
fit4 <- kmeans(kmeans.data.scaled, 4)
# get cluster means
aggregate(kmeans.data.scaled, by=list(fit4$cluster), FUN=mean)
```

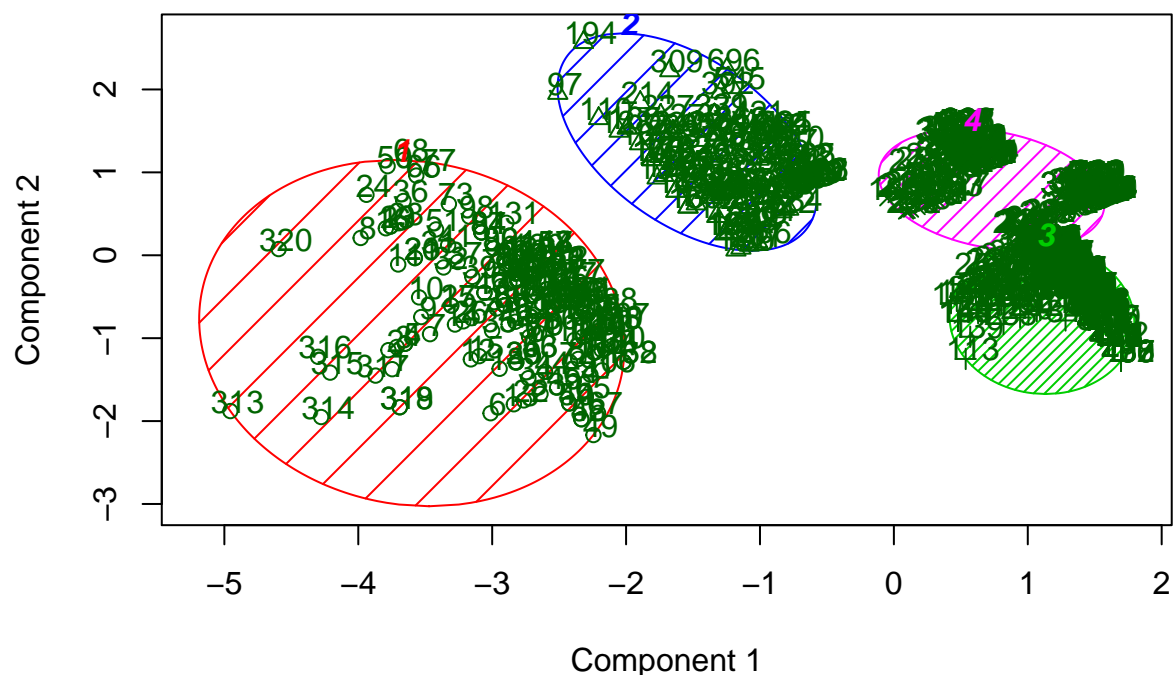
##	Group.1	Age	Salary	fit3.cluster
## 1	1	0.5785685	1.6573821	3.000000
## 2	2	1.5014941	0.0695924	2.000000
## 3	3	-0.8646274	-0.5612934	1.000000
## 4	4	0.2795692	-0.4223518	1.535714

```
# append cluster assignment
kmeans.data.scaled <- data.frame(kmeans.data.scaled, fit4$cluster)
```

Cluster Plot against 1st 2 principal components

```
# vary parameters for most readable graph
clusplot(kmeans.data.scaled, fit4$cluster, color=TRUE, shade=TRUE, labels=2, lines=0)
```

CLUSPLOT(kmeans.data.scaled)



These two components explain 89.93 % of the point variability.

7 clusters

```
# K-Means Cluster Analysis
fit7 <- kmeans(kmeans.data.scaled, 7)
# get cluster means
aggregate(kmeans.data.scaled, by=list(fit7$cluster), FUN=mean)
```

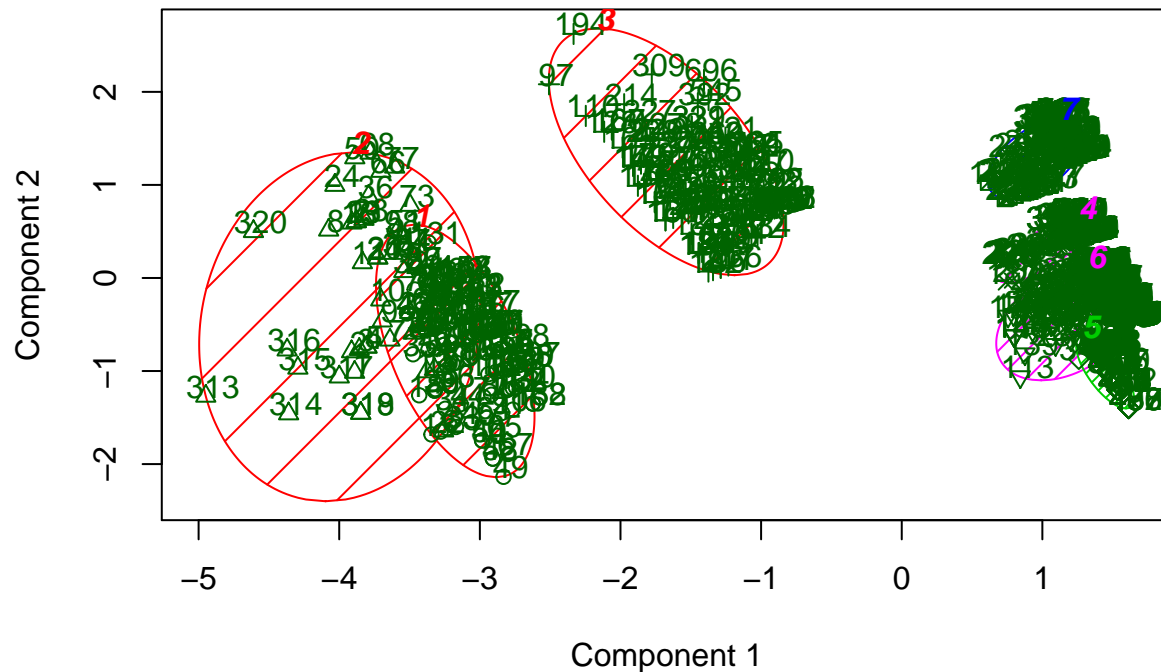
##	Group.1	Age	Salary	fit3.cluster	fit4.cluster
## 1	1	0.359074937	1.2872872	3	1
## 2	2	1.168762228	2.6525262	3	1
## 3	3	1.501494095	0.0695924	2	2
## 4	4	0.009796648	-0.4642320	1	4
## 5	5	-1.332381760	-0.6510886	1	3
## 6	6	-0.650539781	-0.5201948	1	3
## 7	7	0.513372139	-0.3860555	2	4

```
# append cluster assignment
kmeans.data.scaled <- data.frame(kmeans.data.scaled, fit7$cluster)
```

Cluster Plot against 1st 2 principal components

```
# vary parameters for most readable graph
clusplot(kmeans.data.scaled, fit7$cluster, color=TRUE, shade=TRUE, labels=2, lines=0)
```

CLUSPLOT(kmeans.data.scaled)



These two components explain 87.53 % of the point variability.

comparing 2 cluster solutions 3-means and 4-means

```
library(fpc)
d <- dist(kmeans.data.scaled)
cluster.stats(d, fit3$cluster, fit4$cluster)
```

```
## $n
## [1] 836
##
## $cluster.number
## [1] 3
##
## $cluster.size
## [1] 457 213 166
##
## $min.cluster.size
## [1] 166
##
## $noisen
## [1] 0
##
## $diameter
## [1] 3.217215 5.639870 5.162372
##
## $average.distance
## [1] 1.229784 2.733434 1.476078
##
## $median.distance
```

```

## [1] 1.202514 2.082944 1.360096
##
## $separation
## [1] 1.788345 1.765984 1.765984
##
## $average.toother
## [1] 4.445117 3.714490 5.530665
##
## $separation.matrix
##      [,1]      [,2]      [,3]
## [1,] 0.000000 1.788345 4.461521
## [2,] 1.788345 0.000000 1.765984
## [3,] 4.461521 1.765984 0.000000
##
## $ave.between.matrix
##      [,1]      [,2]      [,3]
## [1,] 0.000000 3.326944 5.879882
## [2,] 3.326944 0.000000 4.781407
## [3,] 5.879882 4.781407 0.000000
##
## $average.between
## [1] 4.50213
##
## $average.within
## [1] 1.495483
##
## $n.between
## [1] 208561
##
## $n.within
## [1] 140469
##
## $max.diameter
## [1] 5.63987
##
## $min.separation
## [1] 1.765984
##
## $within.cluster.ss
## [1] 1937.909
##
## $clus.avg.silwidths
##      1      2      3
## 0.62709171 0.05796035 0.69278774
##
## $avg.silwidth
## [1] 0.4951307
##
## $g2
## NULL
##
## $g3
## NULL
##

```

```

## $pearsongamma
## [1] 0.7198141
##
## $dunn
## [1] 0.3131249
##
## $dunn2
## [1] 1.21713
##
## $entropy
## [1] 0.9995311
##
## $wb.ratio
## [1] 0.3321723
##
## $ch
## [1] 932.4685
##
## $cwidegap
## [1] 1.799613 4.475266 1.054805
##
## $widestgap
## [1] 4.475266
##
## $sindex
## [1] 1.829292
##
## $corrected.rand
## [1] 0.704604
##
## $vi
## [1] 0.5621104

```

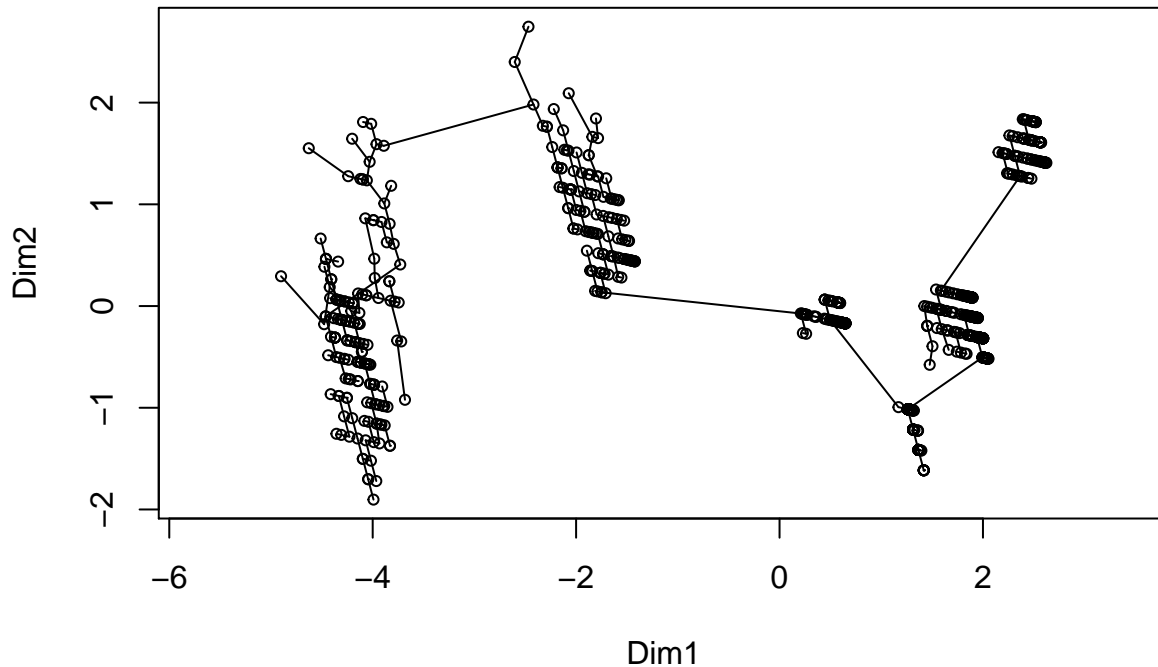
The correct choice of k is often ambiguous, with interpretations depending on the shape and scale of the distribution of points in a data set and the desired clustering resolution of the user. In addition, increasing k without penalty will always reduce the amount of error in the resulting clustering, to the extreme case of zero error if each data point is considered its own cluster (i.e., when k equals the number of data points, n). Intuitively then, the optimal choice of k will strike a balance between maximum compression of the data using a single cluster, and maximum accuracy by assigning each data point to its own cluster.

So, in our case we see that the total within-cluster sum of squares is reducing as k is getting bigger (from 165 for $k=3$ to 125 for $k=7$).

Problem 7.2

Build a minimum spanning tree connecting all points and delete 6 maximum edges step by step.

```
stdData <- kmeans.data.scaled
dis <- dist(stdData) #dissimilarity data
tr <- spantree(dis, tolong = 0) #build an MST
plot(tr, cmdscale(dis)) #plot an MST
```

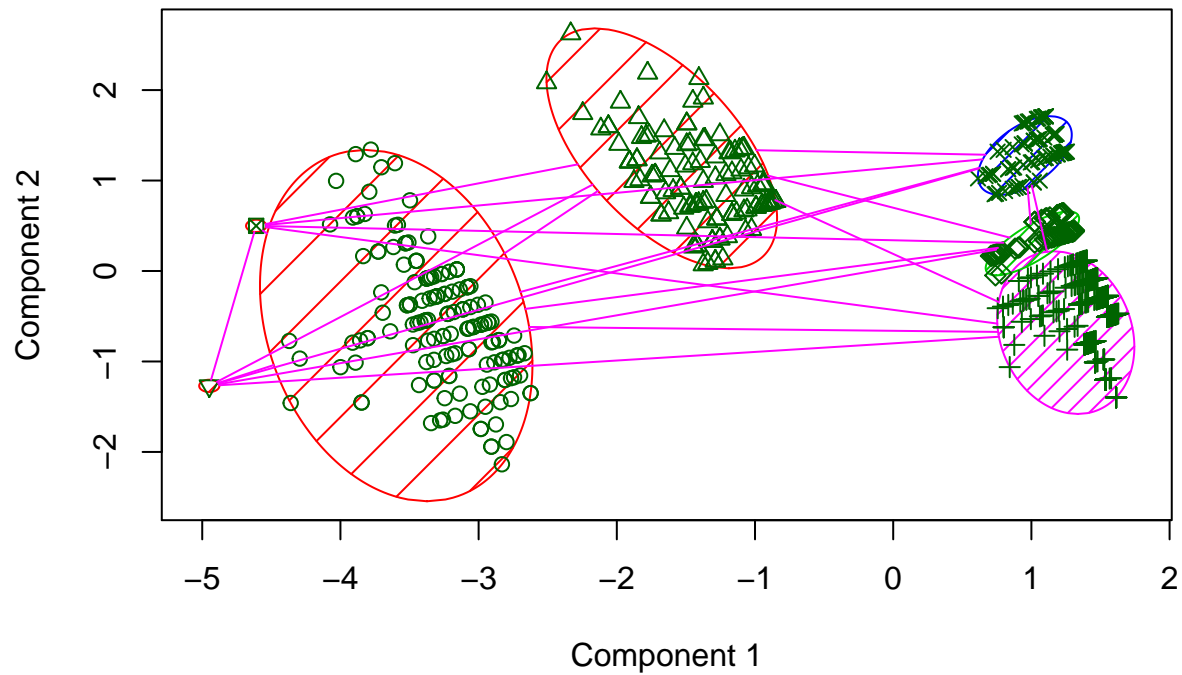


```
for(i in 1:6) #loop for finding 6 maximum edges in MST
{
  m <- which.max(tr$dist)
  tr$dist[m] <- NA
}
m <- which.max(tr$dist)
tres <- tr$dist[m] + 0.00001 #set a threshold
j <- distconnected(dis, tolong = tres) #find connected components in MST after deleting 6 edges
```

```
## Connectivity of distance matrix with threshold dissimilarity 1.024483
## Data are disconnected: 7 groups
## Groups sizes
##   1   2   3   4   5   6   7
## 164 123 379  90  78   1   1
```

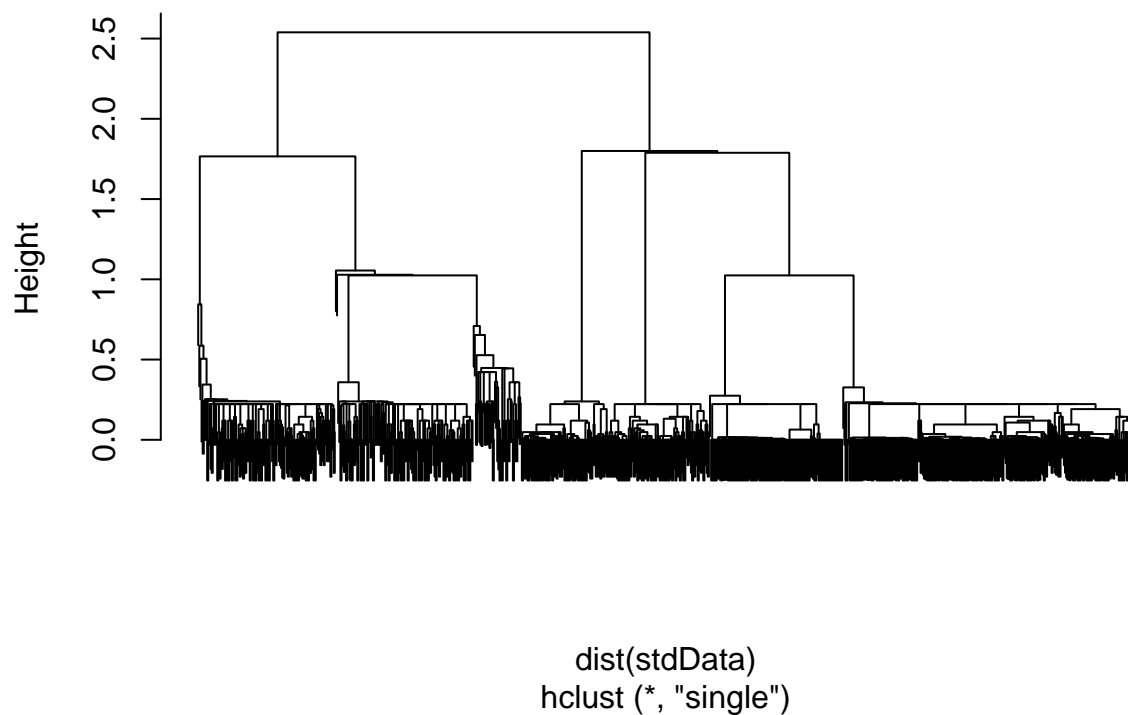
```
clusplot(stdData, j, color=TRUE, shade=TRUE) #plot clusters
```


CLUSPLOT(stdData)



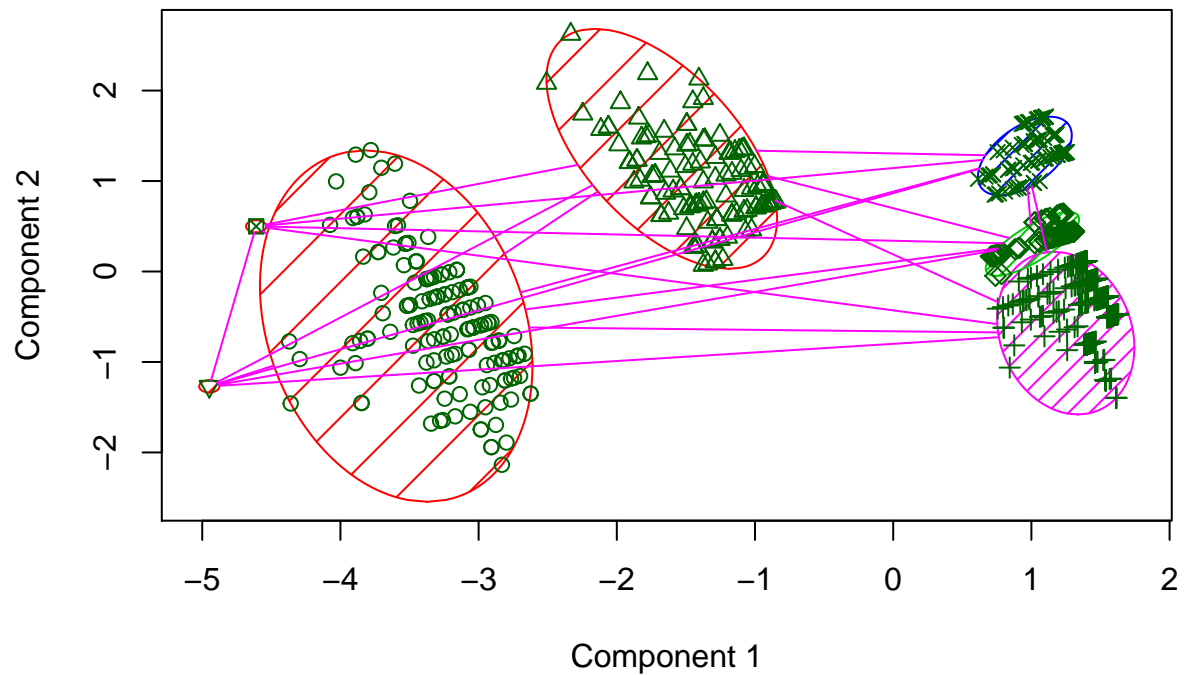
```
hc <- hclust(dist(stdData), method = "single")  
plot(hc, labels = FALSE)
```

Cluster Dendrogram



```
memb <- cutree(hc, k = 7)
clusplot(stdData, memb, color=TRUE, shade=TRUE)
```

CLUSPLOT(stdData)



These two components explain 87.53 % of the point variability.