Untitled

Problem 7.1

```
data = read.csv("data.csv", sep = ",")
summary(data)
```

```
##
                  Name
                                                Team
                                                                 Gm
                                 pos
##
                                           CGY
                                                                    1.00
    Aaron.Ekblad
                            D
                                    :290
                                                   : 31
                       1
                                                          Min.
##
    Aaron. Volpatti:
                        1
                            С
                                    :160
                                           EDM
                                                   : 31
                                                          1st Qu.: 28.00
                                                   : 29
##
    Adam.Burish
                            L
                                    : 73
                                           N.J
                                                          Median: 65.00
                        1
    Adam.Clendening:
##
                       1
                            R
                                    : 71
                                           CBJ
                                                   : 28
                                                          Mean
                                                                  : 55.69
##
    Adam.Cracknell:
                            RL
                                    : 70
                                           COL
                                                   : 28
                                                          3rd Qu.: 81.00
                       1
                                                   : 28
##
    Adam. Henrique
                       1
                            LR
                                    : 61
                                           NYI
                                                          Max.
                                                                  :108.00
##
    (Other)
                    :830
                            (Other):111
                                           (Other):661
##
                          Salary
                                                                 Α
         Age
                             : 0.550
##
    Min.
           :18.00
                     Min.
                                        Min.
                                               : 0.000
                                                          Min.
                                                                 : 0.00
##
    1st Qu.:23.00
                     1st Qu.: 0.750
                                        1st Qu.: 1.000
                                                          1st Qu.: 3.00
    Median :26.00
                     Median : 1.000
                                        Median : 5.000
##
                                                          Median :10.00
##
    Mean
           :26.24
                            : 2.217
                                        Mean
                                               : 8.219
                                                          Mean
                                                                  :14.07
                     Mean
##
    3rd Qu.:29.00
                     3rd Qu.: 3.362
                                        3rd Qu.:13.000
                                                          3rd Qu.:21.00
##
    Max.
            :42.00
                             :14.000
                                        Max.
                                               :58.000
                                                                  :65.00
                     Max.
                                                          Max.
##
##
          Ρ
                           G60
                                             A60
                                                                P60
##
    Min.
          : 0.00
                     Min.
                             :0.0000
                                        Min.
                                               :0.0000
                                                          Min.
                                                                  :0.000
##
    1st Qu.: 4.00
                     1st Qu.:0.1000
                                        1st Qu.:0.4200
                                                          1st Qu.:0.630
    Median :15.50
                     Median :0.3800
                                        Median :0.7300
                                                          Median :1.140
##
    Mean
            :22.28
                     Mean
                             :0.4603
                                        Mean
                                               :0.7812
                                                          Mean
                                                                  :1.242
##
    3rd Qu.:35.00
                     3rd Qu.:0.7100
                                        3rd Qu.:1.0800
                                                          3rd Qu.:1.780
##
    Max.
            :95.00
                     Max.
                             :5.0000
                                        Max.
                                               :5.5300
                                                          Max.
                                                                  :5.530
##
                              CF.
                                               PD0
                                                                  PSh.
##
         PenD
            :-25.0000
                                :20.00
                                                  : 50.00
                                                                    : 0.000
##
    Min.
                        Min.
                                          Min.
                                                            Min.
##
    1st Qu.: -4.0000
                        1st Qu.:44.44
                                          1st Qu.: 97.77
                                                            1st Qu.:
                                                                       2.840
    Median: 0.0000
                        Median :49.72
                                          Median: 99.81
                                                            Median: 6.705
##
    Mean
            : -0.8433
                        Mean
                                :49.40
                                          Mean
                                                  : 99.12
                                                            Mean
                                                                    : 7.210
    3rd Qu.: 2.0000
##
                         3rd Qu.:54.81
                                          3rd Qu.:101.17
                                                            3rd Qu.: 10.530
##
    Max.
           : 27.0000
                        Max.
                                :72.22
                                          Max.
                                                  :125.00
                                                            Max.
                                                                    :100.000
##
##
       ZSO.Rel
                            TOI.Gm
            :-55.810
                               : 4.49
##
    Min.
                       Min.
    1st Qu.: -8.533
                        1st Qu.:12.23
    Median : 1.785
                       Median :15.39
##
##
    Mean
              1.285
                       Mean
                               :15.26
##
    3rd Qu.: 12.110
                        3rd Qu.:18.23
##
    Max.
           : 58.620
                               :28.77
                        Max.
##
```

Function helping to make right chouse about number of K

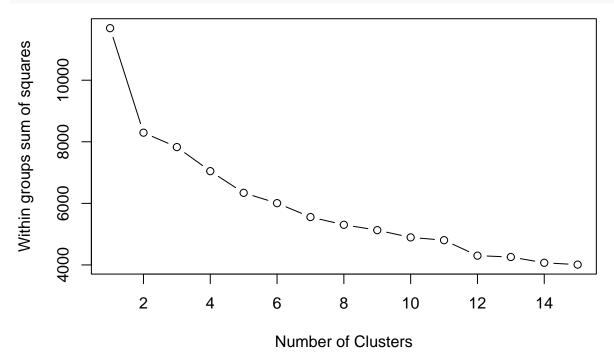
Data that we want to use for clusterization

```
kmeans.data <- data[4:18]
head(kmeans.data)
##
      Gm Age Salary G A P G60 A60 P60 PenD
                                                   CF.
                                                         PDO PSh. ZSO.Rel
## 1
     74
         28
              9.50 28 42 70 1.19 1.79 2.98
                                              3 61.43 101.02 12.56
                                                                      24.54
## 2
     77
         29
              9.25 23 31 54 0.94 1.27 2.22
                                              7 61.89 97.75 9.43
                                                                      12.99
## 3
         29
              9.00 43 30 73 1.69 1.18 2.87
                                             -2 57.51 101.12 16.73
                                                                      17.00
     83
     93
         29
              8.75 27 63 90 0.86 2.00 2.86 -14 54.74 100.20 11.30
                                                                      3.43
         29
              8.75 23 32 55 0.92 1.28 2.20
                                             -5 60.73 97.37 9.83
                                                                      -5.62
## 5
     81
## 6 108
         24
              8.00 50 40 90 1.44 1.15 2.60
                                             11 57.82 102.05 15.02
                                                                      24.30
##
     TOI.Gm
     19.07
## 1
## 2
     18.97
## 3
     18.36
## 4 20.30
```

Scaling the data

5 18.53 ## 6 19.25

```
kmeans.data.scaled <- scale(kmeans.data[-1])
wssplot(kmeans.data.scaled)</pre>
```



Let's do some clusterization

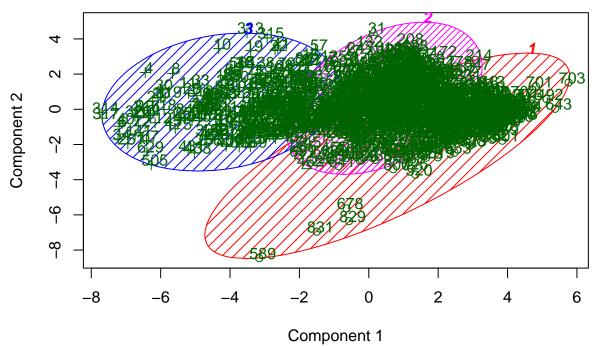
3 clusters

```
# K-Means Cluster Analysis
fit3 <- kmeans(kmeans.data, 3)</pre>
# get cluster means
aggregate(kmeans.data,by=list(fit3$cluster),FUN=mean)
##
     Group.1
                   Gm
                           Age
                                  Salary
                                                 G
## 1
           1 16.96099 24.68440 0.9641135 1.234043 2.205674 3.439716
## 2
           2 69.78274 27.20238 2.0880476 6.523810 12.110119 18.633929
## 3
           3 84.05505 26.76147 4.0370275 19.866972 32.422018 52.288991
##
           G60
                     A60
                               P60
                                         PenD
                                                    CF.
                                                             PDO
                                                                       PSh.
## 1 0.2882624 0.5518440 0.8401064 -0.6560284 47.93876 97.72191 5.141809
## 2 0.3896726 0.6703869 1.0602976 -2.4464286 46.70348 99.25080 6.923601
## 3 0.7918349 1.2486239 2.0405505 1.3853211 55.44344 100.74326 10.327615
##
       ZSO.Rel
                TOI.Gm
## 1 2.248298 12.22454
## 2 -6.948720 15.65595
## 3 12.729083 18.57009
# append cluster assignment
kmeans.data <- data.frame(kmeans.data, fit3$cluster)</pre>
```

Cluster Plot against 1st 2 principal components

```
# vary parameters for most readable graph
library(cluster)
clusplot(kmeans.data, fit3$cluster, color=TRUE, shade=TRUE, labels=2, lines=0)
```

CLUSPLOT(kmeans.data)



These two components explain 57.58 % of the point variability.

```
#Centroid Plot against 1st 2 discriminant functions
#library(fpc)
#plotcluster(kmeans.data, fit$cluster)
```

4 clusters

```
# K-Means Cluster Analysis
fit4 <- kmeans(kmeans.data, 4)
# get cluster means
aggregate(kmeans.data,by=list(fit4$cluster),FUN=mean)</pre>
```

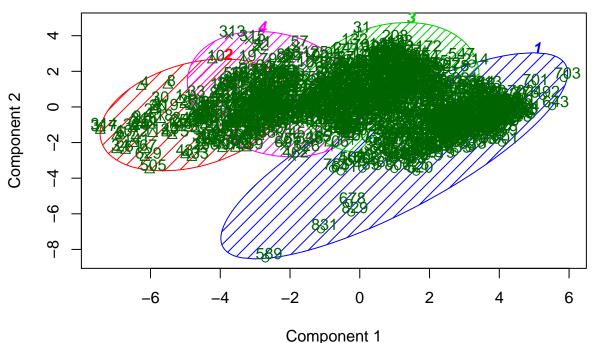
```
##
     Group.1
                                 Salary
                   Gm
                           Age
                                                          Α
## 1
           1 16.15018 24.56044 0.947326 1.175824 2.131868 3.307692
           2 87.42593 26.84259 4.811852 24.620370 39.861111 64.481481
## 3
           3 67.60700 27.58755 1.951023 4.941634 10.000000 14.941634
## 4
           4 77.41414 26.46970 2.898096 13.237374 21.727273 34.964646
                     A60
                               P60
           G60
                                         PenD
                                                   CF.
                                                             PD0
                                                                      PSh.
## 1 0.2865568 0.5535165 0.8400733 -0.6923077 48.12015 97.71839 5.107363
## 2 0.9154630 1.4550926 2.3703704 2.8611111 56.58500 101.32426 11.273426
## 3 0.3185603 0.5859533 0.9047860 -2.9105058 44.98681 98.90074 6.092685
## 4 0.6357071 0.9809091 1.6168687 -0.3888889 52.97061 100.15278 9.343838
                 TOI.Gm fit3.cluster
##
        ZSO.Rel
      2.749414 12.17300
                             1.000000
## 2 15.622870 19.00231
                             3.000000
## 3 -10.380506 15.32840
                             1.964981
      6.586465 17.37939
                             2.555556
```

```
# append cluster assignment
kmeans.data <- data.frame(kmeans.data, fit4$cluster)</pre>
```

Cluster Plot against 1st 2 principal components

```
# vary parameters for most readable graph
clusplot(kmeans.data, fit4$cluster, color=TRUE, shade=TRUE, labels=2, lines=0)
```

CLUSPLOT(kmeans.data)



These two components explain 56.61 % of the point variability.

7 clusters

```
# K-Means Cluster Analysis
fit7 <- kmeans(kmeans.data, 7)
# get cluster means
aggregate(kmeans.data,by=list(fit7$cluster),FUN=mean)</pre>
```

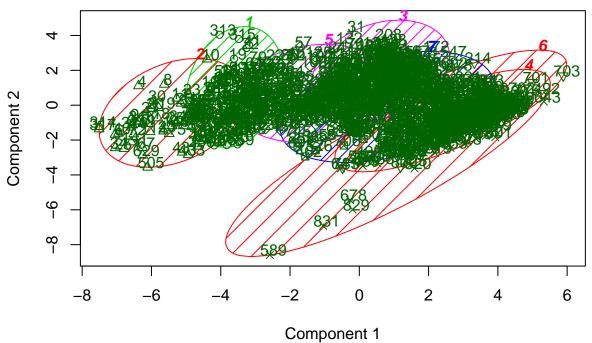
```
G
##
                           Age
                                  Salary
## 1
          1 83.29508 26.67213 3.6924426 17.5163934 29.918033 47.434426
          2 89.05172 27.03448 5.5573448 28.7413793 44.448276 73.189655
## 2
## 3
          3 77.09231 28.43846 2.0957692 5.0307692 10.761538 15.792308
## 4
          4 10.96552 23.83448 0.8535379 0.7862069
                                                    1.179310 1.965517
          5 77.05839 26.19708 2.3741752 11.0583942 18.394161 29.452555
## 5
          6 15.54444 25.73333 0.9842333 0.5777778 1.655556 2.233333
## 7
          7 49.73377 26.33117 1.7576364 4.7532468 8.389610 13.142857
##
          G60
                    A60
                               P60
                                        PenD
                                                   CF.
## 1 0.7157377 1.1627049 1.8781967 -0.9836066 55.29533 100.69180 9.731639
## 2 1.0337931 1.5789655 2.6132759 5.2586207 57.50759 101.54672 12.263793
## 3 0.2782308 0.5385385 0.8169231 -3.6000000 42.47015 98.74685 5.865846
```

```
## 4 0.3068966 0.4417931 0.7486897 -0.1931034 50.29945
                                                        97.48807 5.955655
## 5 0.5616058 0.8817518 1.4434307 0.1240876 50.74401 99.69584 8.726058
## 6 0.1715556 0.6385556 0.8100000 -0.9888889 42.69233 97.05000 2.661222
  7 0.4188961 0.6967532 1.1161688 -2.0909091 49.39948 99.53299 6.935519
        ZSO.Rel
                 TOI.Gm fit3.cluster fit4.cluster
## 1 12.522377 18.81697
                             3.000000
                                          3.180328
    17.352931 19.20241
                             3.000000
                                          2.000000
## 3 -18.630923 15.66492
                                          3.007692
                             2.000000
                             1.000000
     12.098069 11.59269
                                          1.000000
      1.511971 16.50547
                             2.277372
                                          3.817518
## 6 -14.980111 12.29289
                             1.011111
                                          1.111111
      2.265325 14.68571
                             1.688312
                                          2.525974
# append cluster assignment
kmeans.data <- data.frame(kmeans.data, fit7$cluster)</pre>
```

Cluster Plot against 1st 2 principal components

```
# vary parameters for most readable graph
clusplot(kmeans.data, fit7$cluster, color=TRUE, shade=TRUE, labels=2, lines=0)
```

CLUSPLOT(kmeans.data)



These two components explain 55.32 % of the point variability.

comparing 2 cluster solutions 3-means and 4-means

```
library(fpc)
d <- dist(kmeans.data)
cluster.stats(d, fit3$cluster, fit4$cluster)</pre>
```

\$n

```
## [1] 836
##
## $cluster.number
## [1] 3
## $cluster.size
## [1] 282 336 218
## $min.cluster.size
## [1] 218
## $noisen
## [1] 0
##
## $diameter
## [1] 123.32413 99.51566 93.59876
##
## $average.distance
## [1] 35.32876 34.00133 37.26233
## $median.distance
## [1] 32.47629 32.73185 35.24955
##
## $separation
## [1] 8.635514 8.579261 8.579261
## $average.toother
## [1] 77.96508 62.46557 76.41253
## $separation.matrix
##
             [,1]
                      [,2]
## [1,] 0.000000 8.635514 30.041718
## [2,] 8.635514 0.000000 8.579261
## [3,] 30.041718 8.579261 0.000000
## $ave.between.matrix
            [,1]
                     [,2]
## [1,] 0.00000 65.32813 97.44222
## [2,] 65.32813  0.00000 58.76262
## [3,] 97.44222 58.76262 0.00000
## $average.between
## [1] 71.83572
##
## $average.within
## [1] 35.08642
##
## $n.between
## [1] 229476
## $n.within
## [1] 119554
##
```

\$max.diameter

```
## [1] 123.3241
##
## $min.separation
## [1] 8.579261
## $within.cluster.ss
## [1] 601179.3
##
## $clus.avg.silwidths
           1
## 0.4374800 0.3488071 0.3340740
## $avg.silwidth
## [1] 0.3748764
##
## $g2
## NULL
##
## $g3
## NULL
##
## $pearsongamma
## [1] 0.611356
## $dunn
## [1] 0.06956677
## $dunn2
## [1] 1.576998
##
## $entropy
## [1] 1.083429
##
## $wb.ratio
## [1] 0.4884258
## $ch
## [1] 834.2156
##
## $cwidegap
## [1] 52.04894 28.18832 26.44934
## $widestgap
## [1] 52.04894
## $sindex
## [1] 11.77328
##
## $corrected.rand
## [1] 0.6785897
##
## $vi
```

[1] 0.668891

comparing 2 cluster solutions 3-means and 7-means

```
#cluster.stats(d, fit3$cluster, fit7$cluster)
```

comparing 2 cluster solutions 4-means and 7-means

#cluster.stats(d, fit4\$cluster, fit7\$cluster)