

Songs to Solve Electrodynamics to

Níckolas Alves

Departamento de Física-Matemática
Instituto de Física
Universidade de São Paulo

Recepção Tensorial 2019

Blank Space

Taylor Swift

All Star - Smash Mouth

$$\begin{cases} \nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0} \\ \nabla \times \mathbf{E} = \mathbf{0} \end{cases}$$

$$\Downarrow$$

$$\mathbf{E} = \frac{1}{4\pi\epsilon_0} \int \frac{\rho}{z^2} \hat{\mathbf{z}} d\tau'$$

$$\begin{cases} \nabla \cdot \mathbf{B} = 0 \\ \nabla \times \mathbf{B} = \mu_0 \mathbf{J} \end{cases}$$

$$\Downarrow$$

$$\mathbf{B} = \frac{\mu_0}{4\pi} \int \frac{\mathbf{J} \times \hat{\mathbf{z}}}{z^2} d\tau'$$

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Treat You Better - Shawn Mendes

$$\nabla \times \mathbf{E} = \mathbf{0}$$

$$\Downarrow$$

$$\mathbf{E} = -\nabla V$$

$$\Downarrow$$

$$\nabla^2 V = -\frac{\rho}{\epsilon_0}$$

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$$V = \frac{1}{4\pi\epsilon_0} \int \frac{\rho}{z} d\tau'$$

$$\nabla \cdot \mathbf{B} = 0$$

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Live While We're Young - One Direction

$$\begin{cases} \partial_\nu F^{\mu\nu} = \mu_0 J^\mu \\ \partial_\nu G^{\mu\nu} = 0 \end{cases}$$

Take On Me - a-ha

$$\left\{ \begin{array}{l} \nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0} \\ \nabla \cdot \mathbf{B} = 0 \\ \nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t} \\ \nabla \times \mathbf{B} = \mu_0 \mathbf{J} + \mu_0 \epsilon_0 \frac{\partial \mathbf{E}}{\partial t} \end{array} \right.$$

One of Us - Joan Osborne

$$\nabla \cdot \mathbf{B} = 0$$



$$\mathbf{B} = \nabla \times \mathbf{A}$$

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$



$$\nabla \times \left(\mathbf{E} + \frac{\partial \mathbf{A}}{\partial t} \right) = 0$$



$$\mathbf{E} + \frac{\partial \mathbf{A}}{\partial t} = -\nabla V$$

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$$\begin{aligned}\nabla \cdot \mathbf{B} &= 0 \\ \Downarrow \\ \mathbf{B} &= \nabla \times \mathbf{A}\end{aligned}$$
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Superman (It's Not Easy) - Five for Fighting

$$\nabla^2 V + \frac{\partial}{\partial t} (\nabla \cdot \mathbf{A}) = -\frac{\rho}{\epsilon_0}$$
$$\left(\nabla^2 \mathbf{A} - \mu_0 \epsilon_0 \frac{\partial^2 \mathbf{A}}{\partial t^2} \right) - \nabla \left(\nabla \cdot \mathbf{A} + \mu_0 \epsilon_0 \frac{\partial V}{\partial t} \right) = -\mu_0 \mathbf{J}$$

Somebody That I Used To Know - Gotye, Kimbra

$$\nabla^2 V - \frac{1}{c^2} \frac{\partial^2 V}{\partial t^2} = -\frac{\rho}{\epsilon_0}$$
$$\nabla^2 \mathbf{A} - \frac{1}{c^2} \frac{\partial^2 \mathbf{A}}{\partial t^2} = -\mu_0 \mathbf{J}$$

Somebody That I Used To Know - Gotye, Kimbra

$$\nabla^2 V - \frac{1}{\infty} \frac{\partial^2 V}{\partial t^2} = -\frac{\rho}{\epsilon_0}$$
$$\nabla^2 \mathbf{A} - \frac{1}{\infty} \frac{\partial^2 \mathbf{A}}{\partial t^2} = -\mu_0 \mathbf{J}$$

Somebody That I Used To Know - Gotye, Kimbra

$$\nabla^2 V = -\frac{\rho}{\epsilon_0}$$
$$\nabla^2 \mathbf{A} = -\mu_0 \mathbf{J}$$

Feel So Close - Calvin Harris

$$V(\mathbf{r}, t) = \frac{1}{4\pi\epsilon_0} \int \frac{\rho(\mathbf{r}', t)}{z} d\tau'$$

$$\mathbf{A}(\mathbf{r}, t) = \frac{\mu_0}{4\pi} \int \frac{\mathbf{J}(\mathbf{r}', t)}{z} d\tau'$$

Feel So Close - Calvin Harris

$$V(\mathbf{r}, t) = \frac{1}{4\pi\epsilon_0} \int \frac{\rho(\mathbf{r}', t - \frac{r}{c})}{r} d\tau'$$

$$\mathbf{A}(\mathbf{r}, t) = \frac{\mu_0}{4\pi} \int \frac{\mathbf{J}(\mathbf{r}', t - \frac{r}{c})}{r} d\tau'$$

Best Day Of My Life - American Authors

$$\mathbf{E}(\mathbf{r}, t) = -\nabla V - \frac{\partial \mathbf{A}}{\partial t}$$

$$\mathbf{B}(\mathbf{r}, t) = \nabla \times \mathbf{A}$$

Best Day Of My Life - American Authors

$$\mathbf{E}(\mathbf{r}, t) = \frac{1}{4\pi\epsilon_0} \int \frac{\hat{\mathbf{z}}}{z^2} [\rho] + \frac{\hat{\mathbf{z}}}{cz} \left[\frac{\partial \rho}{\partial t} \right] - \frac{1}{c^2 z} \left[\frac{\partial \mathbf{J}}{\partial t} \right] d\tau'$$

$$\mathbf{B}(\mathbf{r}, t) = \frac{\mu_0}{4\pi} \int \left[\frac{1}{z^2} [\mathbf{J}] + \frac{1}{cz} \left[\frac{\partial \mathbf{J}}{\partial t} \right] \right] \times \hat{\mathbf{z}} d\tau'$$

A Cruel Angel's Thesis

Yoko Takahashi

Deja Vu (Initial D) - Tsuko G

$$\left\{ \begin{array}{l} \nabla \cdot \mathbf{D} = \rho \\ \nabla \cdot \mathbf{B} = 0 \\ \nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t} \\ \nabla \times \mathbf{H} = \mathbf{J} + \frac{\partial \mathbf{D}}{\partial t} \end{array} \right.$$

$$\left\{ \begin{array}{l} \mathbf{D} = \epsilon_0 \mathbf{E} + \mathbf{P} \\ \mathbf{H} = \frac{1}{\mu_0} \mathbf{B} - \mathbf{M} \end{array} \right.$$

Deja Vu (Initial D) - Tsuko G

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$$\left\{ \begin{array}{l} \mathbf{D} = \epsilon \mathbf{E} \\ \mathbf{H} = \frac{1}{\mu} \mathbf{B} \end{array} \right.$$

Don't Go Breaking My Heart - Backstreet Boys

$$\left\{ \begin{array}{l} \nabla^2 \mathbf{E} - \mu \epsilon \frac{\partial^2 \mathbf{E}}{\partial t^2} = \frac{1}{\epsilon} \nabla \rho + \rho \nabla \frac{1}{\epsilon} - \nabla \left(\frac{\mathbf{E} \cdot \nabla \epsilon}{\epsilon} \right) \\ \quad + \mu \frac{\partial \mathbf{J}}{\partial t} + \mu \nabla \left(\frac{1}{\mu} \right) \times (\nabla \times \mathbf{E}) \\ \nabla^2 \mathbf{B} - \mu \epsilon \frac{\partial^2 \mathbf{B}}{\partial t^2} = \mathbf{J} \times \nabla \mu - \mu \nabla \times \mathbf{J} - \nabla \times \left[\mu \mathbf{B} \times \nabla \left(\frac{1}{\mu} \right) \right] \\ \quad + \left[\frac{\nabla \times \mathbf{B}}{\mu \epsilon} - \frac{\mathbf{J}}{\epsilon} - \frac{\mathbf{B} \times \nabla \left(\frac{1}{\mu} \right)}{\epsilon} \right] \times [\mu \nabla \epsilon + \epsilon \nabla \mu] \end{array} \right.$$

I Want It That Way - Backstreet Boys

Hipóteses sobre o meio:

- 1 linear;
- 2 dielétrico ($\mu = \mu_0$);
- 3 homogêneo ($\nabla \epsilon = 0$).

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Happier - Marshmello, Bastille

$$\left\{ \begin{aligned} \nabla^2 \mathbf{E} - \mu_0 \epsilon \frac{\partial^2 \mathbf{E}}{\partial t^2} &= \frac{1}{\epsilon} \nabla \rho + \cancel{\rho \nabla \frac{1}{\epsilon}}^0 - \nabla \left(\frac{\mathbf{E} \cdot \cancel{\nabla \epsilon}}{\epsilon} \right)^0 \\ &\quad + \mu_0 \frac{\partial \mathbf{J}}{\partial t} + \mu_0 \cancel{\nabla \left(\frac{1}{\mu_0} \right)}^0 \times (\nabla \times \mathbf{E}) \\ \nabla^2 \mathbf{B} - \mu_0 \epsilon \frac{\partial^2 \mathbf{B}}{\partial t^2} &= \mathbf{J} \times \cancel{\nabla \mu_0}^0 - \mu_0 \nabla \times \mathbf{J} - \nabla \times \left[\mu_0 \mathbf{B} \times \cancel{\nabla \left(\frac{1}{\mu_0} \right)}^0 \right] \\ &\quad + \left[\frac{\nabla \times \mathbf{B}}{\mu_0 \epsilon} - \frac{\mathbf{J}}{\epsilon} - \frac{\mathbf{B} \times \cancel{\nabla \left(\frac{1}{\mu_0} \right)}^0}{\epsilon} \right]^0 \times \left[\mu_0 \cancel{\nabla \epsilon}^0 + \epsilon \cancel{\nabla \mu_0}^0 \right]^0 \end{aligned} \right.$$

Happier - Marshmello, Bastille

$$\begin{cases} \nabla^2 \mathbf{E} - \mu_0 \epsilon \frac{\partial^2 \mathbf{E}}{\partial t^2} = \frac{1}{\epsilon} \nabla \rho + \mu_0 \frac{\partial \mathbf{J}}{\partial t} \\ \nabla^2 \mathbf{B} - \mu_0 \epsilon \frac{\partial^2 \mathbf{B}}{\partial t^2} = -\mu_0 \nabla \times \mathbf{J} \end{cases}$$

Wouldn't It Be Nice - The Beach Boys

$$\mathbf{E}(\mathbf{r}, t) = \frac{1}{4\pi\epsilon_0} \int_{\mathcal{V}_0} \text{solução no vácuo} d\tau' + \frac{1}{4\pi\epsilon_1} \int_{\mathcal{V}_1} \text{solução no meio} d\tau'$$

God Only Knows - The Beach Boys

Propriedades esperadas de uma solução:

- 1 reflexão e refração;
- 2 mudanças de velocidade;
- 3 presença de um dielétrico afeta a solução;
- 4 et cetera.

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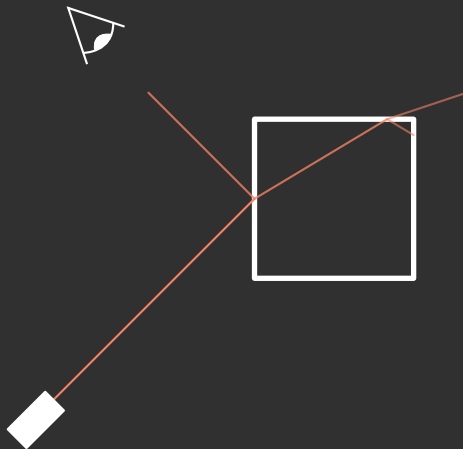
In The End

Linkin Park

Everybody (Backstreet's Back)

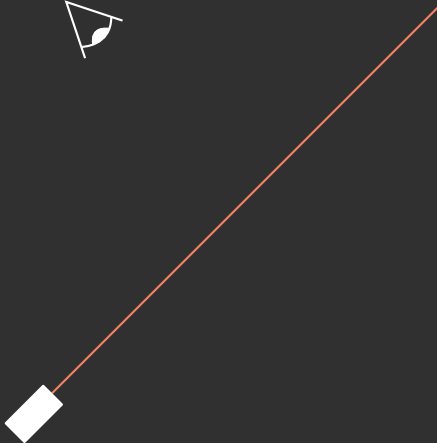
Backstreet Boys

You Found Me - The Fray

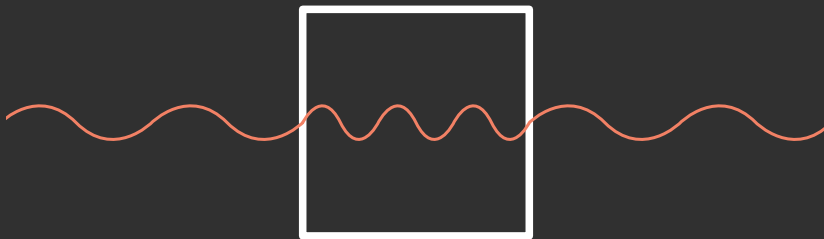


Volar

Don't Matter - Akon

[Voltar](#)

Stop - Spice Girls



Voltar

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