Basic

vimrc 1.1

```
| se nu ai hls et ru ic is sc cul
2 se re=1 ts=4 sts=4 sw=4 ls=2 mouse=a
 syntax on
4 hi cursorline cterm=none ctermbg=89
 set bg=dark
6 inoremap {<CR> {<CR>}<Esc>ko<tab>
```

Data-Structure

2.1 DLX

```
1 struct DLX {
   int n, m, tot, ans;
   vi first, siz, L, R, U, D, col, row, stk;
   DLX(int n, int m) : n(n), m(m), tot(m)
       ) {
     int sz = n * m;
     first = siz = L = R = U = D = col = row
          = stk = vi(sz);
     REP(i, m + 1) {
       L[i] = i - 1, R[i] = i + 1;
       U[i] = D[i] = i;
     L[0] = m, R[m] = 0;
   void insert(int r, int c) {
     col[++tot] = c, row[tot] = r, ++siz[c];
     D[tot] = D[c], U[D[c]] = tot, U[tot] = c
          , D[c] = tot;
     if(!first[r]) first[r] = L[tot] = R[tot]
           = tot;
       L[R[tot] = R[first[r]]] = tot;
       R[L[tot] = first[r]] = tot;
   #define TRAV(i, X, j) for(i = X[j]; i != j
        ; i = X[i]
   void remove(int c) {
     int i, j;
     L[R[c]] = L[c], R[L[c]] = R[c];
     TRAV(i, D, c) TRAV(j, R, i) {
       D[U[D[i]] = U[i]] = D[i];
       siz[col[j]]--;
   void recover(int c) {
     TRAV(i, U, c) TRAV(j, L, i) {
       U[D[j]] = D[U[j]] = j;
       siz[col[j]]++;
     L[R[c]] = R[L[c]] = c;
```

```
bool dance(int dep) {
      if(!R[0]) return ans = dep, true;
      int i, j, c = R[0];
      TRAV(i, R, 0) if(siz[i] < siz[c]) c = i;
      remove(c):
      TRAV(i, D, c) {
        stk[dep] = row[i];
        TRAV(j, R, i) remove(col[j]);
        if(dance(dep + 1)) return true;
        TRAV(j, L, i) recover(col[j]);
      recover(c);
      return false;
    vi solve() {
      if(!dance(1)) return {};
      return vi(stk.begin() + 1, stk.begin() +
            ans):
58 };
```

2.2 fast-set

```
1 // Can correctly work with numbers in range
2 // Supports all std::set operations in O(1)
      on random queries / dense arrays, O(
      log 64(N)) in worst case (sparce array).
  // Count operation works in O(1) always.
                                                 52
  template < uint MAXN >
                                                 53
  class fast set {
                                                 54
  private:
   static const uint PREF = (MAXN <= 64 ? 0 :</pre>
                  MAXN <= 4096 ? 1 :
                  MAXN <= 262144 ? 1 + 64 :
                  MAXN <= 16777216 ? 1 + 64 +
                       4096:
                  MAXN <= 1073741824 ? 1 + 64
                       + 4096 + 262144 : 227) +
                        1;
    static constexpr ull lb(int x) {
     if(x == 64) return ULLONG MAX:
      return (1ULL << x) - 1;</pre>
   static const uint SZ = PREF + (MAXN + 63)
        / 64 + 1;
    ull m[SZ] = \{0\}:
    inline uint left(uint v) const { return (v
          - 62) * 64; }
    inline uint parent(uint v) const { return
        v / 64 + 62; }
    inline void setbit(uint v) { m[v >> 6] |=
        1ULL << (v & 63); }
   inline void resetbit(uint v) { m[v >> 6]
                                                 69
         &= ~(1ULL << (v & 63)); }
   inline uint getbit(uint v) const { return
         m[v >> 6] >> (v & 63) & 1; }
   inline ull childs value(uint v) const {
         return m[left(v) >> 6]; }
                                                 72 };
    inline int left go(uint x, const uint c)
         const {
      const ull rem = x \& 63;
```

2.3 lazvsegtree

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uint bt = PREF * 64 + x;

parent(bt)) { const ull rem = bt & 63:

if(bt == 62) **return** -1;

return bt - PREF * 64;

const ull rem = x & 63;

parent(bt)) {

num);

if(bt == 62) **return** -1;

return bt - PREF * 64;

if(num) {

break:

(62); }

(62); }

setbit(v); }

resetbit(PREF * 64 + x);

)) resetbit(v);

void erase(uint x) {

public:

uint bt = PREF * 64 + x;

if(num) return (x ^ rem) |

builtin ctzll(num);

const ull rem = bt & 63;

__lg(m[bt - 62]);

if(num) {

break:

ull num = m[bt >> 6] & lb(rem + c);

num = m[bt >> 6] & lb(rem);

if(num) return (x ^ rem) | lg(num); for(bt = parent(bt); bt > 62; bt =

 $bt = (bt ^ rem) | lg(num);$

while(bt < PREF * 64) bt = left(bt) |</pre>

inline int right_go(uint x, const uint c)

ull num = $m[bt >> 6] \& \sim lb(rem + c);$

for(bt = parent(bt); bt > 62; bt =

num = $m[bt >> 6] \& \sim lb(rem + 1);$

while(bt < PREF * 64) bt = left(bt) |</pre>

fast_set() { assert(PREF != 228); setbit

bool empty() const {return getbit(63);}

void clear() { fill(m, m + SZ, 0); setbit

bool count(uint x) const { return m[PREF +

(x >> 6)] >> (x & 63) & 1; }

if(!getbit(PREF * 64 + x)) return;

int find_next(uint x) const { return

int find prev(uint x) const { return

right go(x, 0); $} // >=$

left go(x, 1); $}$ // <=

void insert(uint x) { for(uint v = PREF *

64 + x; !getbit(v); v = parent(v))

for(uint v = parent(PREF * 64 + x); v >

62 && !childs_value(v); v = parent(v 48

__builtin_ctzll(m[bt - 62]);

bt = (bt ^ rem) | builtin ctzll(

27

```
1 template < class S,</pre>
           S (*e)(),
            S (*op)(S, S),
            class F.
           F (*id)(),
            S (*mapping)(F, S),
            F (*composition)(F, F)>
  struct lazy_segtree {
    int n, size, log;
    vector<S> d; vector<F> lz;
    void update(int k) { d[k] = op(d[k << 1],</pre>
         d[k << 1 | 1]); }
    void all_apply(int k, F f) {
      d[k] = mapping(f, d[k]);
      if(k < size) lz[k] = composition(f, lz[k</pre>
15
    void push(int k) {
      all_apply(k << 1, lz[k]);
      all_apply(k << 1 | 1, lz[k]);
19
      lz[k] = id();
20
    lazy_segtree(int _n) : lazy_segtree(vector
         <S>( n, e())) {}
    lazy_segtree(const vector<S>& v) : n(sz(v)
      log = __lg(2 * n - 1), size = 1 << log;
      d.resize(size * 2, e());
      lz.resize(size, id());
      REP(i, n) d[size + i] = v[i];
      for(int i = size - 1; i; i--) update(i);
28
    void set(int p, S x) {
      p += size:
      for(int i = log; i; --i) push(p >> i);
      d[p] = x;
      for(int i = 1; i <= log; ++i) update(p</pre>
           >> i);
    S get(int p) {
36
      p += size;
      for(int i = log; i; i--) push(p >> i);
      return d[p];
    S prod(int 1, int r) {
      if(1 == r) return e();
      1 += size; r += size;
      for(int i = log; i; i--) {
        if(((1 >> i) << i) != 1) push(1 >> i);
        if(((r >> i) << i) != r) push(r >> i);
      S sml = e(), smr = e();
      while(1 < r) {</pre>
        if(1 \& 1) sml = op(sml, d[1++]);
        if(r \& 1) smr = op(d[--r], smr);
        1 >>= 1;
        r >>= 1;
52
54
      return op(sml, smr);
    S all prod() const { return d[1]; }
    void apply(int p, F f) {
      p += size;
```

```
for(int i = log; i; i--) push(p >> i);
                                                                                                                                                              // TODO
       d[p] = mapping(f, d[p]);
                                                                 r = r << 1 | 1;
                                                                                                       45
                                                                                                                  return 1 - size;
       for(int i = 1; i <= log; i++) update(p</pre>
                                                                 if(g(op(d[r], sm))) sm = op(d[r])
                                                                                                                                                            7 void pull(Node*& v) {
                                                                                                                                                               v\rightarrow sz = 1 + size(v\rightarrow l) + size(v\rightarrow r);
                                                                      --], sm);
                                                                                                                sm = op(sm, st[1++]);
                                                                                                              } while((1 & -1) != 1);
     void apply(int 1, int r, F f) {
                                                               return r + 1 - size;
                                                                                                              return n:
       if(1 == r) return;
                                                                                                                                                           void push(Node*& v) {
       1 += size; r += size;
                                                             sm = op(d[r], sm);
                                                                                                            template < class F> int min left(int r, F f)
                                                                                                                                                               if(v->rev) {
       for(int i = log; i; i--) {
                                                          } while((r & -r) != r);
                                                                                                                                                                 swap(v->1, v->r);
                                                                                                              assert(0 <= r && r <= n && f(e()));
         if(((1 >> i) << i) != 1) push(1 >> i); 125
                                                           return 0;
                                                                                                                                                                 if(v->1) v->1->rev ^= 1;
         if(((r \rightarrow i) << i) != r) push((r - 1)
                                                                                                              if(r == 0) return 0;
                                                                                                                                                          15
                                                                                                                                                                 if(v->r) v->r->rev ^= 1;
              >> i);
                                                                                                              r += size;
                                                                                                                                                          16
                                                                                                                                                                 v->rev = false;
                                                                                                              S sm = e();
                                                                                                                                                          17
                                                                                                              do {
                                                                                                                                                          18 }
         int 12 = 1, r2 = r;
                                                                                                                                                           Node* merge(Node* a, Node* b) {
                                                      2.4 segtree
                                                                                                                                                               if(!a | | !b) return (a ? a : b);
         while(1 < r) {</pre>
                                                                                                                while(r > 1 && (r & 1)) r >>= 1;
           if(1 & 1) all_apply(1++, f);
                                                                                                                if(!f(op(st[r], sm))) {
                                                                                                                                                               push(a), push(b);
           if(r & 1) all_apply(--r, f);
                                                                                                                  while(r < size) {</pre>
                                                                                                                                                               if(a->pri > b->pri) {
           1 >>= 1:
                                                                                                                    r = r << 1 | 1;
                                                                                                                                                                 a \rightarrow r = merge(a \rightarrow r, b);
                                                      template < class S, S (*e)(), S (*op)(S, S)>
           r >>= 1;
                                                                                                                    if(f(op(st[r], sm))) sm = op(st[r
                                                                                                                                                          24
                                                                                                                                                                 pull(a); return a;
                                                      struct segtree {
                                                                                                                                                               } else {
                                                        int n, size, log;
                                                                                                                         --1, sm);
         1 = 12:
                                                                                                                                                                 b->l = merge(a, b->l);
                                                        vector<S> st;
                                                                                                                                                                 pull(b); return b;
                                                                                                                                                          27
         r = r2;
                                                        void update(int v) { st[v] = op(st[v <<</pre>
                                                                                                                  return r + 1 - size;
                                                             1], st[v << 1 | 1]); }
                                                                                                                                                          28
                                                        segtree(int _n) : segtree(vector<S>(_n, e
       for(int i = 1; i <= log; i++) {</pre>
                                                                                                                sm = op(st[r], sm);
                                                                                                                                                          29 }
         if(((1 >> i) << i) != 1) update(1 >> i
                                                              ())) {}
                                                                                                              } while((r & -r) != r);
                                                                                                                                                           30 pair<Node*, Node*> split(Node* v, int k) {
                                                                                                              return 0;
                                                                                                                                                               if(!v) return {NULL, NULL};
                                                        segtree(const vector<S>& a): n(sz(a)) {
         if(((r >> i) << i) != r) update((r -
                                                                                                                                                               push(v);
                                                          log = __lg(2 * n - 1), size = 1 << log;
                                                                                                                                                          32
                                                                                                                                                               if(size(v->1) >= k) {
              1) >> i);
                                                           st.resize(size << 1, e());</pre>
                                                           REP(i, n) st[size + i] = a[i];
                                                                                                                                                                 auto p = split(v->1, k);
                                                                                                                                                                 if(p.first) p.first->p = NULL;
                                                           for(int i = size - 1; i; i--) update(i);
     template < class G> int max_right(int 1, G g
                                                                                                                                                                 v \rightarrow 1 = p.second;
                                                                                                          2.5 sparse-table
                                                                                                                                                                 pull(v); return {p.first, v};
                                                        void set(int p, S val) {
       assert(0 <= 1 && 1 <= n && g(e()));
                                                           st[p += size] = val;
                                                                                                                                                                } else {
       if(1 == n) return n;
                                                                                                                                                                 auto p = split(v->r, k - size(v->l) - 1)
                                                           for(int i = 1; i <= log; ++i) update(p</pre>
       1 += size;
                                                                >> i);
                                                                                                        i template < class T, T (*op)(T, T)>
       for(int i = log; i; i--) push(l >> i);
                                                                                                        2 struct sparse table {
                                                                                                                                                                 if(p.second) p.second->p = NULL;
       S sm = e();
                                                                                                           int n;
                                                                                                                                                                 v->r = p.first;
                                                        S get(int p) const {
                                                           return st[p + size];
                                                                                                            vector<vector<T>> b;
                                                                                                                                                                 pull(v); return {v, p.second};
         while(!(1 & 1)) 1 >>= 1;
                                                                                                            sparse_table(const vector<T>& a) : n(sz(a)
         if(!g(op(sm, d[1]))) {
                                                        S prod(int 1, int r) const {
           while(1 < size) {</pre>
                                                           assert(0 <= 1 && 1 <= r && r <= n);
                                                                                                              int lg = __lg(n) + 1;
                                                                                                                                                             int get_position(Node* v) { // 0-indexed
             push(1);
                                                                                                              b.resize(lg); b[0] = a;
                                                                                                                                                               int k = (v->1 != NULL ? v->1->sz : 0);
                                                           S sml = e(), smr = e();
                                                                                                              for(int j = 1; j < lg; ++j) {
                                                                                                                                                               while(v->p != NULL) {
             1 <<= 1:
                                                          1 += size, r += size;
             if(g(op(sm, d[1]))) sm = op(sm, d[
                                                                                                                                                                 if(v == v->p->r) {
                                                           while(1 < r) {
                                                                                                                b[j].resize(n - (1 << j) + 1);
                  1++]);
                                                             if(1 \& 1) sml = op(sml, st[1++]);
                                                                                                                REP(i, n - (1 << j) + 1) b[j][i] = op( 49
                                                             if(r & 1) smr = op(st[--r], smr);
                                                                                                                                                                   if(v\rightarrow p\rightarrow 1 != NULL) k += v\rightarrow p\rightarrow 1\rightarrow sz;
                                                                                                                     return 1 - size;
                                                            1 >>= 1:
                                                                                                                      - 1))]);
                                                                                                                                                                 v = v \rightarrow p;
                                                            r >>= 1;
                                                                                                       11
                                                                                                                                                          52
         sm = op(sm, d[1++]);
                                                                                                       12
                                                                                                                                                          53
       } while((1 & -1) != 1);
                                                           return op(sml, smr);
                                                                                                            T prod(int from, int to) {
103
                                                                                                       13
                                                                                                                                                               return k;
       return n;
                                                                                                              int \lg = \lg(to - from + 1);
104
                                                        S all prod() const { return st[1]; }
                                                                                                              return op(b[lg][from], b[lg][to - (1 <<</pre>
     template < class G> int min left(int r, G g)
                                                        template < class F> int max right(int 1, F f
                                                                                                                   lg) + 1]);
                                                             ) const {
                                                                                                                                                                   動態凸包
                                                           assert(0 <= 1 && 1 <= n && f(e()));
       assert(0 <= r \&\& r <= n \&\& g(e()));
                                                                                                       17 };
       if(r == 0) return 0;
                                                          if(1 == n) return n;
       r += size;
                                                          1 += size;
       for(int i = log; i >= 1; i--) push((r -
                                                          S sm = e();
                                                                                                                                                           1 struct line t {
                                                                                                                                                               mutable 11 k, m, p;
            1) >> i):
                                                           do {
                                                                                                          2.6 treap
       S sm = e();
111
                                                             while(~1 & 1) 1 >>= 1;
                                                                                                                                                               bool operator<(const line_t& o) const {</pre>
112
       do {
                                                             if(!f(op(sm, st[1]))) {
                                                                                                                                                                    return k < o.k; }</pre>
                                                               while(1 < size) {</pre>
                                                                                                                                                               bool operator<(ll x) const { return p < x;</pre>
113
                                                                                                        1 struct Node {
         while(r > 1 \&\& (r \& 1)) r >>= 1;
114
                                                                1 <<= 1:
                                                                                                           bool rev = false:
         if(!g(op(d[r], sm))) {
                                                                                                            int sz = 1, pri = rng();
115
                                                                 if(f(op(sm, st[1]))) sm = op(sm,
           while(r < size) {</pre>
                                                                      st[1++]);
                                                                                                           Node *1 = NULL, *r = NULL, *p = NULL;
                                                                                                                                                           6 template < bool MAX >
```

```
7 struct CHT : multiset<line t, less<>>> {
    const ll INF = 1e18L;
    bool isect(iterator x, iterator v) {
      if(y == end()) return x->p = INF, 0;
      if(x->k == y->k) {
        x->p = (x->m > y->m ? INF : -INF);
         x \rightarrow p = floor div(y \rightarrow m - x \rightarrow m, x \rightarrow k - y)
              ->k); // see Math
      return x->p >= y->p;
    void add_line(ll k, ll m) {
      if(!MAX) k = -k, m = -m;
      auto z = insert(\{k, m, 0\}), y = z++, x =
      while(isect(y, z)) z = erase(z);
      if(x != begin() && isect(--x, y)) isect(
            x, y = erase(y));
      while((y = x) != begin() && (--x)->p >=
           y->p) isect(x, erase(y));
    11 get(11 x) {
      assert(!empty());
      auto 1 = *lower bound(x);
      return (l.k * x + l.m) * (MAX ? +1 : -1)
30 };
```

回滾 DSU

```
1 struct RollbackDSU {
   int n; vi sz, tag;
   vector<tuple<int, int, int, int>> op;
   void init(int _n) {
     n = n;
     sz.assign(n, -1);
     tag.clear();
   int leader(int x) {
     while(sz[x] >= 0) x = sz[x];
     return x;
   bool merge(int x, int y) {
     x = leader(x), y = leader(y);
     if(x == y) return false;
     if(-sz[x] < -sz[y]) swap(x, y);</pre>
     op.eb(x, sz[x], y, sz[y]);
     sz[x] += sz[y]; sz[y] = x;
     return true;
   int size(int x) { return -sz[leader(x);] }
   void add_tag() { tag.pb(sz(op)); }
   void rollback() {
     int z = tag.back(); tag.ppb();
     while(sz(op) > z) {
       auto [x, sx, y, sy] = op.back(); op.
            ppb();
       sz[x] = sx;
       sz[y] = sy;
```

3 Flow-Matching

31 | };

Dinic-LowerBound

template < class T>

```
struct DinicLowerBound {
 using Maxflow = Dinic<T>;
 int n:
 Maxflow d;
  vector<T> in;
 DinicLowerBound(int _n) : n(_n), d(_n + 2)
       , in(_n) {}
  int add_edge(int from, int to, T low, T
    assert(0 <= low && low <= high);
   in[from] -= low, in[to] += low;
    return d.add edge(from, to, high - low);
 T flow(int s, int t) {
   T sum = 0;
    REP(i, n) {
     if(in[i] > 0) {
       d.add_edge(n, i, in[i]);
        sum += in[i];
     if(in[i] < 0) d.add_edge(i, n + 1, -in</pre>
          [i]);
    d.add_edge(t, s, numeric_limits<T>::max
    if(d.flow(n, n + 1) < sum) return -1;</pre>
    return d.flow(s, t);
```

Dinic

```
1 template < class T>
 class Dinic {
 public:
   struct Edge {
     int from, to;
     Edge(int x, int y, T z) : from(x), to(y)
          , cap(z) {}
   constexpr T INF = 1e9;
   int n;
   vector<Edge> edges;
   vector<vi> g;
   vi cur, h; // h : Level graph
   Dinic(int _n) : n(_n), g(_n) {}
   void add_edge(int u, int v, T c) {
     g[u].pb(sz(edges));
     edges.eb(u, v, c);
     g[v].pb(sz(edges));
```

```
edges.eb(v, u, 0);
    bool bfs(int s, int t) {
      h.assign(n, -1);
      queue<int> q;
      h[s] = 0;
      q.push(s);
      while(!q.empty()) {
        int u = q.front(); q.pop();
        for(int i : g[u]) {
          const auto& e = edges[i];
          int v = e.to;
          if(e.cap > 0 && h[v] == -1) {
            h[v] = h[u] + 1;
            if(v == t) return true;
            q.push(v);
      return false;
    T dfs(int u, int t, T f) {
      if(u == t) return f;
      Tr = f:
      for(int& i = cur[u]; i < sz(g[u]); ++i)</pre>
        int j = g[u][i];
        const auto& e = edges[j];
        int v = e.to;
        T c = e.cap;
        if(c > 0 \&\& h[v] == h[u] + 1) {
          T = dfs(v, t, min(r, c));
          edges[j].cap -= a;
          edges[j ^ 1].cap += a;
          if((r -= a) == 0) return f;
      return f - r;
55
    T flow(int s, int t, T f = INF) {
      T ans = 0;
      while(f > 0 && bfs(s, t)) {
        cur.assign(n, 0);
        T cur = dfs(s, t, f);
        ans += cur;
```

3.3 Flow 建模

f -= cur;

return ans;

20

- · Maximum/Minimum flow with lower bound / Circulation problem
 - 1. Construct super source S and sink T.
 - 2. For each edge (x, y, l, u), connect $x \to y$ with capacity u-l.
 - 3. For each vertex v, denote by in(v) the difference between the sum of incoming lower bounds and the sum of outgoing lower bounds.
 - 4. If in(v) > 0, connect $S \rightarrow v$ with capacity in(v), otherwise, connect $v \to T$ with capacity -in(v).

- To maximize, connect $t \to s$ with capacity ∞ (skip this in circulation problem), and let f be the maximum flow from Sto T. If $f \neq \sum_{v \in V, in(v) > 0} in(v)$, there's no solution. Otherwise, the maximum flow from s to t is the answer.
- To minimize, let f be the maximum flow from S to T. Connect $t \rightarrow s$ with capacity ∞ and let the flow from S to T be f'. If $f + f' \neq \sum_{v \in V, in(v) > 0} in(v)$, there's no solution. Otherwise, f' is the answer
- 5. The solution of each edge e is $l_e + f_e$, where f_e corresponds to the flow of edge e on the graph.
- · Construct minimum vertex cover from maximum matching M on bipartite graph (X, Y)
 - 1. Redirect every edge: $y \to x$ if $(x, y) \in M$, $x \to u$ otherwise.
 - 2. DFS from unmatched vertices in X.
 - 3. $x \in X$ is chosen iff x is unvisited.
 - 4. $y \in Y$ is chosen iff y is visited.
- · Minimum cost cyclic flow
 - 1. Consruct super source S and sink T
 - 2. For each edge (x, y, c), connect $x \to y$ with (cost, cap) = (c, 1) if c > 0, otherwise connect $y \to x$ with (cost, cap) = (-c, 1)
 - 3. For each edge with c < 0, sum these cost as K, then increase d(y) by 1, decrease d(x) by 1
 - 4. For each vertex v with d(v) > 0, connect $S \to v$ with (cost, cap) = (0, d(v))
 - 5. For each vertex v with d(v) < 0, connect $v \to T$ with (cost, cap) = (0, -d(v))
 - 6. Flow from S to T, the answer is the cost of the flow C + K
- · Maximum density induced subgraph
 - 1. Binary search on answer, suppose we're check-
 - 2. Construct a max flow model, let K be the sum of all weights
 - 3. Connect source $s \to v, v \in G$ with capacity K
 - 4. For each edge (u, v, w) in G, connect $u \to v$ and $v \to u$ with capacity w
 - 5. For $v \in G$, connect it with sink $v \to t$ with capacity $K + 2T - (\sum_{e \in E(v)} w(e)) - 2w(v)$
 - 6. T is a valid answer if the maximum flow f <K|V|
- · Minimum weight edge cover
 - 1. For each $v \in V$ create a copy v', and connect $u' \to v'$ with weight w(u, v).
 - 2. Connect $v \rightarrow v'$ with weight $2\mu(v)$, where $\mu(v)$ is the cost of the cheapest edge incident to
 - 3. Find the minimum weight perfect matching on
- Project selection problem
 - 1. If $p_v > 0$, create edge (s, v) with capacity p_v ; otherwise, create edge (v, t) with capacity $-p_v$.
 - 2. Create edge (u, v) with capacity w with w being the cost of choosing u without choosing v.
 - 3. The mincut is equivalent to the maximum profit of a subset of projects.

```
• 0/1 quadratic programming
                                                          REP(x, n) if(!v1[x] && !s1k[x] && !
                                                                                                                if(!ing[e.to]) {
                                                                                                                                                              mate[u] = -1;
                                                               check(x)) return;
                                                                                                                  q.push(e.to);
                                                                                                                                                     24
       \sum_{x} c_{x} x + \sum_{y} c_{y} \bar{y} + \sum_{xy} c_{xy} x \bar{y} + \sum_{xyx'y'} c_{xyx'y'} (x \bar{y} + \chi'_{1})
                                                                                                                  inq[e.to] = true;
                                                                                                                                                            return false:
                                                     T solve() {
                                                                                                                                                          void add_edge(int a, int b) {
       can be minimized by the mincut of the following graph: 44
                                                        fill(all(fl), -1);
                                                                                                            }
                                                                                                                                                            auto f = [&](int a, int b) {
                                                                                                                                                              es.eb(b, g[a]);
                                                        fill(all(fr), -1);
                                                        fill(all(hr), 0);
                                                                                                          return found:
                                                                                                                                                              g[a] = sz(es) - 1;
          1. Create edge (x, t) with capacity c_x and create 46
                                                        REP(i, n) hl[i] = *max element(all(w[i])
             edge (s, y) with capacity c_y.
          2. Create edge (x, y) with capacity c_{xy}.
                                                                                                        pair<S, T> flow(int s, int t, S f = INF) { 32
                                                                                                                                                            f(a, b); f(b, a);
                                                        REP(i, n) bfs(i);
                                                                                                         S cap = 0:
          3. Create edge (x, y) and edge (x', y') with capac-
                                                       T ans = 0;
                                                                                                          T cost = 0;
                                                                                                                                                          int solve() {
             ity c_{xux'u'}.
                                                                                                          while(f > 0 && spfa(s, t)) {
                                                        REP(i, n) ans += w[i][fl[i]]; // i 跟 fl 52
                                                                                                                                                            vi o(n);
                                                            [i] 配對
                                                                                                            S send = f:
                                                                                                                                                            iota(all(o), 0);
                                                                                                                                                            int ans = 0:
                                                                                                            int u = t:
                                                        return ans:
 3.4 KM
                                                                                                            while(u != s) {
                                                                                                                                                            REP(it, 100) {
                                                                                                              const Edge& e = edges[pedge[u]];
                                                                                                                                                               shuffle(all(o), rng);
                                                                                                              send = min(send, e.cap);
                                                                                                                                                              vis.assign(n, false);
i template < class T>
                                                                                                              u = e.from:
                                                                                                                                                              for(auto i : o) if(mate[i] == -1) ans
2 struct KM {
                                                                                                            }
                                                                                                                                                                   += dfs(i):
   static constexpr T INF = numeric limits<T</pre>
                                                    3.5 MCMF
                                                                                                            u = t;
                                                                                                            while(u != s) {
        >::max();
                                                                                                                                                            return ans;
   int n, ql, qr;
                                                                                                              Edge& e = edges[pedge[u]];
   vector<vector<T>> w;
                                                                                                              e.cap -= send:
                                                   template < class S, class T>
   vector<T> hl, hr, slk:
                                                   class MCMF {
                                                                                                              Edge& b = edges[pedge[u] ^ 1];
   vi fl, fr, pre, qu;
                                                   public:
                                                                                                              b.cap += send;
   vector<bool> v1, vr;
                                                     struct Edge {
                                                                                                              u = e.from:
                                                                                                                                                        3.7 一般圖最小權完美匹配
   KM(int n) : n(n), w(n, vector<T>(n, -INF))
                                                       int from, to;
        , hl(n), hr(n), slk(n), fl(n), fr(n),
                                                                                                            cap += send;
                                                        S cap;
        pre(n), qu(n), vl(n), vr(n) {}
                                                                                                            f -= send:
                                                        T cost;
   void add_edge(int u, int v, int x) { w[u][
                                                                                                            cost += send * d[t];
                                                        Edge(int u, int v, S x, T y) : from(u),
                                                                                                                                                       1 struct Graph {
        v] = x; } // 最小值要加負號
                                                             to(v), cap(x), cost(y) {}
                                                                                                                                                         // Minimum General Weighted Matching (
   bool check(int x) {
                                                                                                          return {cap, cost};
                                                                                                                                                                Perfect Match) 0-base
     vl[x] = 1;
                                                      const ll INF = 1e18L;
                                                                                                                                                          static const int MXN = 105;
     if(fl[x] != -1) return vr[qu[qr++] = fl[
                                                                                                                                                          int n, edge[MXN][MXN];
                                                      int n:
                                                                                                                                                          int match[MXN], dis[MXN], onstk[MXN];
                                                      vector<Edge> edges;
     while(x != -1) swap(x, fr[fl[x] = pre[x
                                                      vector<vi>g;
                                                                                                                                                          vector<int> stk;
                                                      vector<T> d;
                                                                                                                                                          void init(int _n) {
     return 0;
                                                      vector<bool> ing;
                                                                                                      3.6 一般圖最大匹配
                                                                                                                                                            for(int i=0; i<n; i++)</pre>
   void bfs(int s) {
                                                      MCMF(int _n) : n(_n), g(_n), d(_n), inq(_n
                                                                                                                                                              for(int j=0; j<n; j++)</pre>
     fill(all(slk), INF);
                                                           ), pedge(_n) {}
                                                                                                                                                                edge[i][j] = 0;
                                                                                                                                                      11
                                                                                                    1 struct GeneralMaxMatch {
                                                      void add_edge(int u, int v, S cap, T cost)
     fill(all(vl), 0);
                                                                                                                                                      12
                                                                                                       int n;
                                                                                                                                                          void add edge(int u, int v, int w) { edge[
     fill(all(vr), 0);
                                                                                                        vector<pii> es:
     ql = qr = 0, qu[qr++] = s, vr[s] = 1;
                                                                                                                                                               u][v] = edge[v][u] = w; }
                                                        g[u].pb(sz(edges));
                                                                                                        vi g, vis, mate; // i 與 mate[i] 配對 (
                                                                                                                                                           bool SPFA(int u){
     while(true) {
                                                        edges.eb(u, v, cap, cost);
                                                                                                             mate[i] == -1 代表沒有匹配)
                                                        g[v].pb(sz(edges));
                                                                                                                                                            if(onstk[u]) return true;
                                                                                                                                                      15
                                                                                                        GeneralMaxMatch(int n) : n(n), g(n, -1),
        while(ql < qr) {</pre>
                                                        edges.eb(v, u, 0, -cost);
                                                                                                                                                      16
                                                                                                                                                            stk.push back(u):
         for(int x = 0, y = qu[ql++]; x < n;
                                                                                                             mate(n, -1) {}
                                                                                                                                                            onstk[u] = 1;
                                                      bool spfa(int s, int t) {
                                                                                                        bool dfs(int u) {
                                                                                                                                                      18
                                                                                                                                                            for(int v=0; v<n; v++){</pre>
           if(!vl[x] \&\& slk[x] >= (d = hl[x]
                                                       bool found = false:
                                                                                                          if(vis[u]) return false;
                                                                                                                                                              if(u != v && match[u] != v && !onstk[v
                                                                                                          vis[u] = true;
                + hr[y] - w[x][y])) {
                                                        fill(all(d), INF);
             pre[x] = y;
                                                        d[s] = 0:
                                                                                                          for(int ei = g[u]; ei != -1; ) {
                                                                                                                                                                 int m = match[v];
                                                                                                                                                      20
             if(d) slk[x] = d;
                                                        inq[s] = true;
                                                                                                            auto [x, y] = es[ei]; ei = y;
                                                                                                                                                                 if(dis[m] > dis[u] - edge[v][m] +
                                                                                                                                                      21
                                                                                                                                                                     edge[u][v]){
             else if(!check(x)) return;
                                                        queue<int> q;
                                                                                                            if(mate[x] == -1) {
                                                        q.push(s);
                                                                                                              mate[mate[u] = x] = u;
                                                                                                                                                                   dis[m] = dis[u] - edge[v][m] +
                                                        while(!q.empty()) {
                                                                                                   13
                                                                                                              return true;
                                                                                                                                                                        edge[u][v];
                                                          int u = q.front(); q.pop();
                                                                                                                                                                  onstk[v] = 1;
                                                                                                                                                      23
                                                          if(u == t) found = true;
                                                                                                                                                                   stk.push back(v);
                                                                                                                                                      24
                                                                                                                                                                  if(SPFA(m)) return true;
       REP(x, n) if(!vl[x] \&\& d > slk[x]) d =
                                                          inq[u] = false;
                                                                                                          for(int ei = g[u]; ei != -1; ) {
                                                                                                                                                     25
                                                          for(auto& id : g[u]) {
                                                                                                            auto [x, y] = es[ei]; ei = y;
             slk[x];
                                                                                                                                                      26
                                                                                                                                                                   stk.pop_back();
       REP(x, n) {
                                                                                                            int nu = mate[x];
                                                            const auto& e = edges[id];
                                                                                                                                                                  onstk[v] = 0;
         if(vl[x]) hl[x] += d;
                                                            if(e.cap > 0 && d[u] + e.cost < d[e.
                                                                                                            mate[mate[u] = x] = u;
         else slk[x] -= d;
                                                                                                            mate[nul = -1:
                                                                 to]) {
                                                                                                            if(dfs(nu)) return true;
         if(vr[x]) hr[x] -= d;
                                                              d[e.to] = d[u] + e.cost;
```

mate[mate[nu] = x] = nu;

onstk[u] = 0;

pedge[e.to] = id;

```
stk.pop_back();
                                                               q.push(rhs[v]);
33
      return false:
    int solve() {
      for(int i = 0; i < n; i += 2) match[i] =</pre>
            i + 1, match[i+1] = i;
                                                       bool dfs(int u) {
      while(true) {
                                                         for(auto v : g[u]) {
        int found = 0:
                                                           if(rhs[v] == -1) {
        for(int i=0; i<n; i++) dis[i] = onstk[</pre>
                                                             rhs[lhs[u] = v] = u;
             i] = 0;
                                                             return true;
         for(int i=0; i<n; i++){</pre>
          stk.clear();
          if(!onstk[i] && SPFA(i)){
                                                         for(auto v : g[u]) {
                                                           if(dist[rhs[v]] == dist[u] + 1 && dfs(
            found = 1;
            while(stk.size()>=2){
                                                                rhs[v])) {
              int u = stk.back(); stk.pop_back
                                                             rhs[lhs[u] = v] = u;
                                                             return true;
               int v = stk.back(); stk.pop_back
                    ();
              match[u] = v;
                                                         return false:
              match[v] = u;
                                                       int solve() {
                                                         int ans = 0;
                                                         while(true) {
        if(!found) break;
                                                           bfs();
                                                           int aug = 0;
      int ans = 0:
                                                           REP(i, n) if(lhs[i] == -1) aug += dfs(
      for(int i=0; i<n; i++) ans += edge[i][</pre>
                                                                i);
           match[i]];
                                                           if(!aug) break;
      return ans / 2;
                                                           ans += aug;
58 }graph;
                                                         return ans;
```

3.8 二分圖最大匹配

```
1 struct bipartite matching {
   int n, m; // 二分圖左右人數 (0 ~ n-1), (0
       \sim m-1)
   vector<vi> g;
   vi lhs, rhs, dist; // i 與 Lhs[i] 配對 (
        Lhs[i] == -1 代表沒有配對)
   bipartite_matching(int _n, int _m) : n(_n)
        , m(_m), g(_n), lhs(_n, -1), rhs(_m,
        -1), dist( n) {}
   void add_edge(int u, int v) { g[u].pb(v);
   void bfs() {
     queue<int> q;
     REP(i, n) {
       if(lhs[i] == -1) {
         q.push(i);
         dist[i] = 0;
       } else {
         dist[i] = -1;
     while(!q.empty()) {
       int u = q.front(); q.pop();
       for(auto v : g[u]) {
         if(rhs[v] != -1 && dist[rhs[v]] ==
           dist[rhs[v]] = dist[u] + 1;
```

4 Geometry

4.1 convex-hull

4.2 point-in-convex-hull

```
i| int point in_convex_hull(const vector<P>& a, 26| }
        P p) {
   // -1 ON, 0 OUT, +1 IN
    // 要先逆時針排序
    int n = sz(a);
    if(btw(a[0], a[1], p) || btw(a[0], a[n -
        1], p)) return -1;
    int 1 = 0, r = n - 1;
    while(1 <= r) {
      int m = (1 + r) / 2;
      auto a1 = cross(a[m] - a[0], p - a[0]);
      auto a2 = cross(a[(m + 1) % n] - a[0], p
      if(a1 >= 0 && a2 <= 0) {
        auto res = cross(a[(m + 1) % n] - a[m]
             ], p - a[m]);
        return res > 0 ? 1 : (res >= 0 ? -1 :
      if(a1 < 0) r = m - 1;
      else 1 = m + 1;
17
   return 0;
```

4.3 point

using P = pair<ll, ll>;

```
2 P operator+(P a, P b) { return P{a.X + b.X,
       a.Y + b.Y;
3 P operator-(P a, P b) { return P{a.X - b.X,
       a.Y - b.Y}; }
4 P operator*(P a, 11 b) { return P{a.X * b, a
       .Y * b}; }
5 P operator/(P a, 11 b) { return P{a.X / b, a
       .Y / b}; }
6 11 dot(P a, P b) { return a.X * b.X + a.Y *
       b.Y; }
7 | 11 cross(P a, P b) { return a.X * b.Y - a.Y
       * b.X; }
8 11 abs2(P a) { return dot(a, a); }
9 double abs(P a) { return sqrt(abs2(a)); }
int sign(ll x) { return x < 0 ? -1 : (x == 0)</pre>
        ? 0 : 1); }
int ori(P a, P b, P c) { return sign(cross(b
        - a, c - a)); }
  bool collinear(P a, P b, P c) { return sign(
       cross(a - c, b - c)) == 0; }
13 bool btw(Pa, Pb, Pc) {
   if(!collinear(a, b, c)) return 0;
   return sign(dot(a - c, b - c)) <= 0;</pre>
16
17 bool seg intersect(Pa, Pb, Pc, Pd) {
    int a123 = ori(a, b, c);
    int a124 = ori(a, b, d);
    int a341 = ori(c, d, a);
    int a342 = ori(c, d, b);
    if(a123 == 0 && a124 == 0) {
      return btw(a, b, c) || btw(a, b, d) ||
           btw(c, d, a) || btw(c, d, b);
24
    return a123 * a124 <= 0 && a341 * a342 <=
```

```
26
27
28
P intersect(P a, P b, P c, P d) {
29
int a123 = cross(b - a, c - a);
30
int a124 = cross(b - a, d - a);
return (d * a123 - c * a124) / (a123 - a124);
32
}
33
struct line { P A, B; };
P vec(line L) { return L.B - L.A; }
P projection(P p, line L) { return L.A + vec
(L) / abs(vec(L)) * dot(p - L.A, vec(L))
/ abs(vec(L)); }
```

4.4 polar-angle-sort

4.5 最近點對

```
| const | INF = 9e18L + 5;
vector<P> a;
3 sort(all(a), [](P a, P b) { return a.x < b.x</pre>
       ; });
4 11 SQ(11 x) { return x * x; }
  ll solve(int l, int r) {
    if(1 + 1 == r) return INF;
    int m = (1 + r) / 2;
    11 \text{ midx} = a[m].x;
    11 d = min(solve(1, m), solve(m, r));
    inplace merge(a.begin() + 1, a.begin() + m
         , a.begin() + r, [](P a, P b) {
      return a.y < b.y;</pre>
    vector<P> p;
    for(int i = 1; i < r; ++i) if(SQ(a[i].x -
         midx) < d) p.pb(a[i]);
    REP(i, sz(p)) {
      for(int j = i + 1; j < sz(p); ++j) {</pre>
17
          d = min(d, SQ(p[i].x - p[j].x) + SQ(
               p[i].y - p[j].y));
18
        if(SQ(p[i].y - p[j].y) > d) break;
19
20
    return d; // 距離平方
```

Graph

2-SAT

```
i struct two sat {
   int n; SCC g;
    vector<bool> ans;
   two sat(int n) : n(n), g(n * 2) {}
    void add_or(int u, bool x, int v, bool y)
      g.add edge(2 * u + !x, 2 * v + y);
     g.add_edge(2 * v + !y, 2 * u + x);
    bool solve() {
      ans.resize(n);
      auto id = g.solve();
     REP(i, n) {
        if(id[2 * i] == id[2 * i + 1]) return
        ans[i] = (id[2 * i] < id[2 * i + 1]);
      return true;
18 };
```

centroid-tree

```
pair<int, vector<vi>>> centroid tree(const
      vector<vi>& g) {
   int n = sz(g);
   vi siz(n):
   vector<bool> vis(n);
   auto dfs sz = [&](auto f, int u, int p) ->
         void {
     siz[u] = 1;
     for(auto v : g[u]) {
  if(v == p || vis[v]) continue;
       f(f, v, u);
       siz[u] += siz[v];
   auto find cd = [&](auto f, int u, int p,
        int all) -> int {
     for(auto v : g[u]) {
       if(v == p | | vis[v]) continue;
       if(siz[v] * 2 > all) return f(f, v, u,
             all):
     return u;
   vector<vi> h(n);
   auto build = [&](auto f, int u) -> int {
     dfs sz(dfs sz, u, -1);
     int cd = find_cd(find_cd, u, -1, siz[u])
     vis[cd] = true;
     for(auto v : g[cd]) {
       if(vis[v]) continue;
       int child = f(f, v);
       h[cd].pb(child);
```

```
int root = build(build, 0);
   return {root, h};
 5.3 HLD
1 struct HLD {
   int n;
   vector<vi> g;
   vi siz, par, depth, top, tour, fi, id;
   sparse_table<pii, min> st;
   HLD(int _n) : n(_n), g(_n), siz(_n), par(
        n), depth( n), top( n), fi( n), id( n
     tour.reserve(n);
   void add_edge(int u, int v) {
     g[u].push back(v);
     g[v].push_back(u);
   void build(int root = 0) {
     par[root] = -1;
     top[root] = root;
     vector<pii> euler_tour;
     euler tour.reserve(2 * n - 1);
     dfs sz(root);
     dfs_link(euler_tour, root);
     st = sparse table<pii, min>(euler_tour);
   int get lca(int u, int v) {
     int L = fi[u], R = fi[v];
     if(L > R) swap(L, R);
     return st.prod(L, R).second;
   bool is anc(int u, int v) {
     return id[u] <= id[v] && id[v] < id[u] +</pre>
           siz[u];
   bool on path(int a, int b, int x) {
     return (is ancestor(x, a) || is ancestor
          (x, b)) && is_ancestor(get_lca(a, b)
          , x);
   int get_dist(int u, int v) {
     return depth[u] + depth[v] - 2 * depth[(
          get lca(u, v))];
   int kth anc(int u, int k) {
     if(depth[u] < k) return -1;</pre>
     int d = depth[u] - k;
      while(depth[top[u]] > d) u = par[top[u
     return tour[id[u] + d - depth[u]];
   int kth_node_on_path(int a, int b, int k)
     int z = get_lca(a, b);
     int fi = depth[a] - depth[z];
     int se = depth[b] - depth[z];
     if(k < 0 || k > fi + se) return -1;
```

return cd;

```
if(k < fi) return kth anc(a, k);</pre>
      return kth anc(b, fi + se - k);
    vector<pii> get_path(int u, int v, bool
         include lca = true) {
      if(u == v && !include lca) return {};
      vector<pii> seg;
      while(top[u] != top[v]) {
        if(depth[top[u]] > depth[top[v]]) swap
        seg.eb(id[top[v]], id[v]);
        v = par[top[v]];
      if(depth[u] > depth[v]) swap(u, v); // u
      if(u != v || include_lca) seg.eb(id[u] +
           !include_lca, id[v]);
      return seg;
    void dfs_sz(int u) {
      if(par[u] != -1) g[u].erase(find(all(g[u
           ]), par[u]));
      siz[u] = 1;
      for(auto& v : g[u]) {
        par[v] = u;
        depth[v] = depth[u] + 1;
        dfs sz(v);
        siz[u] += siz[v];
        if(siz[v] > siz[g[u][0]]) swap(v, g[u
             1[0]);
    void dfs link(vector<pii>& euler tour, int 43
      fi[u] = sz(euler tour);
      id[u] = sz(tour);
      euler_tour.eb(depth[u], u);
      tour.pb(u);
      for(auto v : g[u]) {
        top[v] = (v == g[u][0] ? top[u] : v);
        dfs link(euler tour, v);
        euler_tour.eb(depth[u], u);
83
  5.4 lowlink
| struct lowlink {
   int n, cnt = 0, tecc cnt = 0, tvcc cnt =
```

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```
vector<vector<pii>>> g;
vector<pii> edges;
vi roots, id, low, tecc_id, tvcc_id;
vector<bool> is_bridge, is_cut,
    is tree edge;
lowlink(int _n) : n(_n), g(_n), is_cut(_n,
      false), id(_n, -1), low(_n, -1) {}
void add edge(int u, int v) {
  g[u].eb(v, sz(edges));
  g[v].eb(u, sz(edges));
  edges.eb(u, v);
  is_bridge.pb(false);
```

```
is_tree_edge.pb(false);
  tvcc id.pb(-1);
void dfs(int u, int peid = -1) {
 static vi stk;
  static int rid:
  if(peid < 0) rid = cnt;</pre>
  if(peid == -1) roots.pb(u);
  id[u] = low[u] = cnt++;
  for(auto [v, eid] : g[u]) {
   if(eid == peid) continue;
    if(id[v] < id[u]) stk.pb(eid);</pre>
    if(id[v] >= 0) {
      low[u] = min(low[u], id[v]);
    } else {
      is tree edge[eid] = true;
      dfs(v, eid):
      low[u] = min(low[u], low[v]);
      if((id[u] == rid && id[v] != rid +
          1) || (id[u] != rid && low[v] >=
           id[u])) {
       is_cut[u] = true;
      if(low[v] >= id[u]) {
        while(true) {
          int e = stk.back();
          stk.pop back();
          tvcc id[e] = tvcc cnt;
          if(e == eid) break;
        tvcc_cnt++;
void build() {
  REP(i, n) if (id[i] < 0) dfs(i);
  REP(i, sz(edges)) {
    auto [u, v] = edges[i];
   if(id[u] > id[v]) swap(u, v);
    is bridge[i] = (id[u] < low[v]);</pre>
vector<vi>two_ecc() { // 邊雙
  tecc cnt = 0:
  tecc_id.assign(n, -1);
  vi stk;
  REP(i, n) {
   if(tecc_id[i] != -1) continue;
    tecc_id[i] = tecc_cnt;
    stk.pb(i);
    while(sz(stk)) {
     int u = stk.back(); stk.pop back();
      for(auto [v, eid] : g[u]) {
        if(tecc_id[v] >= 0 || is_bridge[
             eid]) {
          continue;
        tecc id[v] = tecc cnt;
        stk.pb(v);
    tecc_cnt++;
  vector<vi> comp(tecc_cnt);
```

```
REP(i, n) comp[tecc_id[i]].pb(i);
      return comp;
77
    vector<vi> bcc_vertices() { // 點雙
      vector<vi> comp(tvcc cnt);
      REP(i, sz(edges)) {
        comp[tvcc id[i]].pb(edges[i].first);
        comp[tvcc id[i]].pb(edges[i].second);
      for(auto& v : comp) {
        sort(all(v));
        v.erase(unique(all(v)), v.end());
      REP(i, n) if(g[i].emptv()) comp.pb({i});
      return comp:
    vector<vi> bcc_edges() {
      vector<vi> ret(tvcc cnt);
      REP(i, sz(edges)) ret[tvcc_id[i]].pb(i);
      return ret;
96 };
```

6 Math

37 };

6.1 Aliens

5.5 SCC

```
1 struct SCC {
   int n;
   vector<vi> g, h;
   SCC(int _n) : n(_n), g(_n), h(_n) {}
   void add_edge(int u, int v) {
     g[u].pb(v);
     h[v].pb(u);
   vi solve() { // 回傳縮點的編號
     vi id(n), top;
     top.reserve(n);
     #define GO if(id[v] == 0) dfs1(v);
     function<void(int)> dfs1 = [&](int u) {
       id[u] = 1;
       for(auto v : g[u]) GO;
       top.pb(u);
     REP(v, n) GO;
     fill(all(id), -1);
     function<void(int, int)> dfs2 = [&](int
          u, int x) {
       id[u] = x;
       for(auto v : h[u]) {
         if(id[v] == -1) {
           dfs2(v, x);
     for(int i = n - 1, cnt = 0; i >= 0; --i)
       int u = top[i];
       if(id[u] == -1) {
         dfs2(u, cnt);
         cnt += 1;
     return id;
```

6.2 Berlekamp-Massey

```
1 | // - [1, 2, 4, 8, 16] \rightarrow (1, [1, -2])
2 // - [1, 1, 2, 3, 5, 8] \rightarrow (2, [1, -1, -1])
 998244352]) (mod 998244353)
 // - [] -> (0, [1])
 // - [0, 0, 0] \rightarrow (0, [1])
 // - [-2] -> (1, [1, 2])
 template < class T>
 pair<int, vector<T>> BM(const vector<T>& S)
   using poly = vector<T>;
   int N = SZ(S);
   poly C_rev{1}, B{1};
   int L = 0, m = 1;
   T b = 1:
   auto adjust = [](poly C, const poly &B, T
        d, T b, int m) -> poly {
     C.resize(max(SZ(C), SZ(B) + m));
     Ta = d / b;
     REP(i, SZ(B)) C[i + m] -= a * B[i];
     return C;
   REP(n, N) {
     T d = S[n];
     REP(i, L) d += C rev[i + 1] * S[n - 1 -
          i];
     if(d == 0) m++;
     else if (2 * L <= n) {
       poly Q = C_rev;
       C_rev = adjust(C_rev, B, d, b, m);
       L = n + 1 - L, B = Q, b = d, m = 1;
     } else C_rev = adjust(C_rev, B, d, b, m
          ++);
   return {L, C_rev};
```

```
31 }
33 // Calculate x^N \b d f(x)
34 // Complexity: $0(K^2 \setminus \log N)$ ($K$: deg. of
2)
37 template < class T>
38 vector<T> monomial_mod_polynomial(long long
      N, const vector<T> &f rev) {
    assert(!f_rev.empty() && f_rev[0] == 1);
    int K = SZ(f_rev) - 1;
    if(!K) return {};
    int D = 64 - __builtin_clzll(N);
    vector<T> ret(K, 0);
    ret[0] = 1:
    auto self_conv = [](vector<T> x) -> vector
        <T> {
      int d = SZ(x);
      vector<T> ret(d * 2 - 1);
      REP(i, d) {
        ret[i * 2] += x[i] * x[i];
        REP(j, i) ret[i + j] += x[i] * x[j] *
52
      return ret;
53
    for(int d = D; d--;) {
      ret = self conv(ret);
      for(int i = 2 * K - 2; i >= K; i--) {
        REP(j, k) ret[i - j - 1] -= ret[i] *
            f rev[j + 1];
      ret.resize(K);
      if (N >> d & 1) {
        vector<T> c(K);
        c[0] = -ret[K - 1] * f_rev[K];
        for(int i = 1; i < K; i++) c[i] = ret[</pre>
            i - 1] - ret[K - 1] * f_rev[K - i
             1;
        ret = c;
                                               12
    return ret;
70 // Guess k-th element of the sequence,
      assumina linear recurrence
  template < class T>
  T guess kth term(const vector<T>& a, long
      long k) {
    assert(k >= 0);
    if(k < 1LL * SZ(a)) return a[k];</pre>
    auto f = BM<T>(a).second;
    auto g = monomial_mod_polynomial<T>(k, f);
    T ret = 0;
    REP(i, SZ(g)) ret += g[i] * a[i];
    return ret;
```

3 Chinese-Remainder

```
1 // (rem, mod) {0, 0} for no solution
2 pair<11, 11> crt(11 r0, 11 m0, 11 r1, 11 m1)
   r0 = (r0 \% m0 + m0) \% m0;
   r1 = (r1 \% m1 + m1) \% m1;
   if(m0 < m1) swap(r0, r1), swap(m0, m1);</pre>
   if(m0 \% m1 == 0) {
     if(r0 % m1 != r1) return {0, 0};
   11 g, im, qq;
   g = ext gcd(m0, m1, im, qq);
   ll u1 = (m1 / g);
   if((r1 - r0) % g) return {0, 0};
   11 x = (r1 - r0) / g % u1 * im % u1;
   r0 += x * m0:
   m0 *= u1;
   if(r0 < 0) r0 += m0;
   return {r0, m0};
```

6.4 Discrete-Log

6.5 extgcd

```
1  // ax + by = gcd(a, b)
2  ll ext_gcd(ll a, ll b, ll& x, ll& y) {
3    if(b == 0) {
4         x = 1, y = 0;
5         return a;
6    }
7   ll x1, y1;
8   ll g = ext_gcd(b, a % b, x1, y1);
9         x = y1, y = x1 - (a / b) * y1;
11   return g;
11 }
```

6.6 Floor-Sum

6.7 FWHT

```
assert(SZ(f) == SZ(g));
                                                     phi[i] = i - 1;
int n = SZ(f);
                                                     mobius[i] = -1;
assert(ppc(n) == 1):
const int lg = __lg(n);
                                                   for(auto j : primes) {
vector<vector<T>> fhat(lg + 1, vector<T>(n
                                                     if(i * j > n) break;
    )), ghat(fhat);
                                                     least[i * j] = j;
REP(i, n) fhat[ppc(i)][i] = f[i], ghat[ppc
                                                     if(i % j == 0) {
     (i)][i] = g[i];
                                                       mobius[i * j] = 0;
                                                       phi[i * j] = phi[i] * j;
REP(i, lg + 1) or transform(fhat[i], false 16
    ), or_transform(ghat[i], false);
                                                       break:
vector<vector<T>> h(lg + 1, vector<T>(n));
                                                     } else {
REP(m, n) REP(i, lg + 1) REP(j, i + 1) h[i]
                                                       mobius[i * j] = -mobius[i];
     ][m] += fhat[j][m] * ghat[i - j][m];
                                                       phi[i * j] = phi[i] * phi[j];
REP(i, lg + 1) or transform(h[i], true);
vector<T> res(n);
                                            22
REP(i, n) res[i] = h[ppc(i)][i];
                                            23
return res:
                                            24 }
```

8 if(n == -1) n = m - 1; 9 vi inv(n + 1); 10 inv[0] = inv[1] = 1; for(int i = 2; i <= n; i++) inv[i] = m - 1 LL * (m / i) * inv[m % i] % m; 12 return inv; 13 }</pre>

| #define ppc builtin popcount template < class T, class F> void fwht(vector<T>& a, F f) { int n = SZ(a): assert(ppc(n) == 1); for(int i = 1; i < n; i <<= 1) {</pre> for(int j = 0; j < n; j += i << 1) {</pre> REP(k, i) f(a[j + k], a[i + j + k]);template<class T> void or transform(vector<T>& a, bool inv) { $fwht(a, [\&](T\& x, T\& y) { y += x * (inv)}$? -1 : +1); }) } 14 template < class T> 15 void and transform(vector<T>& a, bool inv) { 15 $fwht(a, [\&](T\& x, T\& y) \{ x += y * (inv 16) \}$? -1 : +1); }); } 16 template < class T> void xor transform(vector<T>& a, bool inv) { fwht(a, [](T& x, T& y) { Tz = x + y;y = x - y;x = z: }); if(inv) { Tz = T(1) / T(SZ(a));for(auto& x : a) x *= z;template<class T> vector<T> convolution(vector<T> a, vector<T> assert(SZ(a) == SZ(b)); transform(a, false), transform(b, false); REP(i, SZ(a)) a[i] *= b[i]; transform(a, true); return a: 36 template < class T> 37 vector<T> subset convolution(const vector<T</pre> >& f, const vector<T>& g) {

6.8 Gauss-Jordan

```
i int GaussJordan(vector<vector<ld>>& a) {
   // -1 no sol, 0 inf sol
   int n = SZ(a);
   REP(i, n) assert(SZ(a[i]) == n + 1);
   REP(i, n) {
     int p = i;
     REP(j, n) {
       if(j < i && abs(a[j][j]) > EPS)
       if(abs(a[j][i]) > abs(a[p][i])) p = j;
     REP(j, n + 1) swap(a[i][j], a[p][j]);
     if(abs(a[i][i]) <= EPS) continue;</pre>
     REP(j, n) {
       if(i == j) continue;
       ld delta = a[j][i] / a[i][i];
       FOR(k, i, n + 1) a[j][k] -= delta * a[
            i][k];
   bool ok = true;
   REP(i, n) {
     if(abs(a[i][i]) <= EPS) {</pre>
       if(abs(a[i][n]) > EPS) return -1;
       ok = false;
   return ok;
```

6.9 Linear-Sieve

```
vi primes, least = {0, 1}, phi, mobius;
void LinearSieve(int n) {
   least = phi = mobius = vi(n + 1);
   for(int i = 2; i <= n; i++) {
      if(!least[i]) {
        least[i] = i;
      primes.pb(i);
}</pre>
```

6.10 Miller-Rabin

```
| bool is_prime(ll n, vector<ll> x) {
   11 d = n - 1;
    d >>= builtin ctzll(d);
    for(auto a : x) {
      if(n <= a) break;</pre>
      11 t = d, y = 1, b = t;
      while(b) {
        if(b \& 1) y = i128(y) * a % n;
        a = i128(a) * a % n;
        b >>= 1;
      while(t != n - 1 && y != 1 && y != n -
        y = i128(y) * y % n;
        t <<= 1;
      if(y != n - 1 && t % 2 == 0) return
           false:
    return true;
  bool is prime(ll n) {
    if(n <= 1) return false;</pre>
    if(n % 2 == 0) return n == 2;
    if (n < (1LL << 30)) return is prime(n, \{2,
          7, 61});
    return is prime(n, {2, 325, 9375, 28178,
         450775, 9780504, 1795265022});
25 }
```

6.11 Mod-Inv

6.12 Pollard-Rho

```
1 | void PollardRho(map<11, int>& mp, 11 n) {
    if(n == 1) return;
    if(is prime(n)) return mp[n]++, void();
    if(n % 2 == 0) {
      mp[2] += 1;
      PollardRho(mp, n / 2);
      return;
    11 x = 2, y = 2, d = 1, p = 1;
    #define f(x, n, p) ((i128(x) * x % n + p)
    while(true) {
      if(d!=1 && d!=n) {
        PollardRho(mp, d);
13
        PollardRho(mp, n / d);
        return;
      p += (d == n);
      x = f(x, n, p), y = f(f(y, n, p), n, p);
      d = \underline{gcd(abs(x - y), n)};
20
    #undef f
22
  vector<ll> get divisors(ll n) {
    if(n == 0) return {};
    map<ll, int> mp;
    PollardRho(mp, n);
    vector<pair<ll, int>> v(all(mp));
    vector<ll> res:
    auto f = [&](auto f, int i, ll x) -> void
      if(i == sz(v)) {
32
        res.pb(x);
33
        return:
34
      for(int j = v[i].second; ; j--) {
        f(f, i + 1, x);
        if(j == 0) break;
        x *= v[i].first;
40
    f(f, 0, 1);
    sort(all(res));
42
    return res;
```

6.13 Primes

1 /* 12721 13331 14341 75577 123457 222557 556679 999983 1097774749 1076767633 100102021 999997771 1001010013 1000512343 987654361 999991231 999888733 98789101 987777733 999991921 1010101333 1010102101 10000000000039 1000000000000037 2305843009213693951 4611686018427387847 9223372036854775783 18446744073709551557 */

6.14 估計值

- Estimation
 - The number of divisors of n is at most around 100 for n < 5e4, 500 for n < 1e7, 2000 for n < 1e7,n < 1e10, 200000 for n < 1e19.
 - The number of ways of writing n as a sum of positive integers, disregarding the order of the summands. 1, 1, 2, 3, 5, 7, 11, 15, 22, 30 for $n = 0 \sim 9,627 \text{ for } n = 20, \sim 2e5 \text{ for }$ $n = 50, \sim 2e8 \text{ for } n = 100.$
 - Total number of partitions *n* distinct elements: B(n)1, 1, 2, 5, 15, 52, 203, 877, 4140, 21147, 115975, 678570, 42135976 (a_1, b_1), ..., (a_n, b_n) of nonnegative in-27644437, 190899322,

6.15 定理

· Cramer's rule

$$ax + by = e \qquad x = \frac{ed - bf}{ad - bc}$$
$$cx + dy = f \Rightarrow y = \frac{af - ec}{ad - bc}$$

· Vandermonde's Identity

$$C(n+m,k) = \sum_{i=0}^{k} C(n,i)C(m,k-i)$$

· Kirchhoff's Theorem

Denote L be a $n \times n$ matrix as the Laplacian matrix of graph G, where $L_{ii} = d(i)$, $L_{ij} = -c$ where c is the number of edge (i, j) in G.

- The number of undirected spanning in G is $|\det(L_{11})|$.
- The number of directed spanning tree rooted at r in G is $|\det(L_{rr})|$.
- · Tutte's Matrix

Let D be a $n \times n$ matrix, where $d_{ij} = x_{ij}$ (x_{ij} is chosen uniformly at random) if i < j and $(i, j) \in E$, otherwise $d_{ij} = -d_{ji}$. $\frac{rank(D)}{2}$ is the maximum matching on G.

- · Cayley's Formula
 - Given a degree sequence d_1, d_2, \ldots, d_n for each labeled vertices, there are
 - $\begin{array}{c} \frac{(n-2)!}{(d_1-1)!(d_2-1)!\cdots(d_n-1)!} \text{ spanning trees.} \\ \text{ Let } T_{n,k} \text{ be the number of labeled forests on} \end{array}$ n vertices with k components, such that vertex $1, 2, \ldots, k$ belong to different components. Then $T_{n,k} = kn^{n-k-1}$.
- Erd□s–Gallai theorem

A sequence of nonnegative integers $d_1 > \cdots > d_n$ can be represented as the degree sequence of a finite simple graph on n vertices if and only if $d_1 + \cdots + d_n$ is even and $\sum_{i=1}^k d_i \leq k(k-1) + \sum_{i=k+1}^n \min(d_i,k)$ holds for

· Gale-Ryser theorem

A pair of sequences of nonnegative integers $a_1 \ge$ $\cdots \geq a_n$ and b_1, \ldots, b_n is bigraphic if and only if $\sum_{i=1}^{n} a_i = \sum_{i=1}^{n} b_i \text{ and } \sum_{i=1}^{n} a_i \leq \sum_{i=1}^{n} \min(b_i, k) \text{ holds}$

· Fulkerson-Chen-Anstee theorem

teger pairs with $a_1 \geq \cdots \geq a_n$ is digraphic if and only $\text{if } \sum_{i=1}^{n} a_i = \sum_{i=1}^{n} b_i \text{ and } \sum_{i=1}^{k} a_i \leq \sum_{i=1}^{k} \min(b_i, k-1) +$ $\sum \min(b_i, k) \text{ holds for every } 1 \le k \le n.$

M□bius inversion formula

$$\begin{array}{llll} -f(n) &=& \sum_{d\mid n}g(d) & \Leftrightarrow & g(n) &= \\ & \sum_{d\mid n}\mu(d)f(\frac{n}{d}) \\ -f(n) &=& \sum_{n\mid d}g(d) & \Leftrightarrow & g(n) &= \\ & \sum_{n\mid d}\mu(\frac{d}{2})f(d) & & \end{array}$$

- · Spherical cap
 - A portion of a sphere cut off by a plane.
 - r: sphere radius, a: radius of the base of the cap,
 - h: height of the cap, θ : $\arcsin(a/r)$. Volume = $\pi h^2(3r h)/3 = \pi h(3a^2 + h^2)/6 = \pi r^3(2 + \cos\theta)(1 \cos\theta)^2/3$. Area = $2\pi rh = \pi(a^2 + h^2) = 2\pi r^2(1 \cos\theta)^2/3$.
 - $\cos \theta$).

6.16 整數除法

6.17 數字

· Bernoulli numbers

$$\begin{split} B_0 - 1, B_1^{\pm} &= \pm \tfrac{1}{2}, B_2 = \tfrac{1}{6}, B_3 = 0 \\ \sum_{j=0}^m \binom{m+1}{j} B_j &= 0, \text{ EGF is } B(x) = \tfrac{x}{e^x-1} = \\ \sum_{n=0}^{\infty} B_n \frac{x^n}{n!}. \end{split}$$

· Stirling numbers of the second kind Partitions of n distinct elements into exactly k groups.

$$S(n,k) = S(n-1,k-1) + kS(n-1,k), S(n,1) = S(n,n) = 1$$

$$S(n,k) = \frac{1}{k!} \sum_{i=0}^{k} (-1)^{k-i} {k \choose i} i^{n}$$

$$x^{n} = \sum_{i=0}^{n} S(n,i)(x)_{i}$$

· Pentagonal number theorem

$$\prod_{n=1}^{\infty} (1 - x^n) = 1$$

$$\sum_{k=1}^{\infty} (-1)^k \left(x^{k(3k+1)/2} + x^{k(3k-1)/2} \right)$$

· Catalan numbers

$$C_n^{(k)} = \frac{1}{(k-1)n+1} {kn \choose n}$$
$$C^{(k)}(x) = 1 + x[C^{(k)}(x)]^k$$

Eulerian numbers

Number of permutations $\pi \in S_n$ in which exactly k elements are greater than the previous element. k j:s s.t. $\pi(i) > \pi(i+1), k+1$ j:s s.t. $\pi(i) > i, k$ j:s s.t.

$$E(n,k) = (n-k)E(n-1,k-1) + (k+1)E(n-1,k)$$

$$E(n,0) = E(n, n-1) = 1$$

$$E(n,k) = \sum_{j=0}^{k} (-1)^{j} {n+1 \choose j} (k+1-j)^{n}$$

歐幾里得類算法 6.18

- $m = |\frac{an+b}{a}|$
- Time complexity: $O(\log n)$

$$\begin{array}{l} \text{Bernoulli numbers} \\ B_0-1, B_1^{\pm}=\pm \frac{1}{2}, B_2=\frac{1}{6}, B_3=0 \\ \\ \sum_{j=0}^m {m+1 \choose j} B_j = 0, \text{ EGF is } B(x) = \frac{x}{e^x-1} = \\ \sum_{j=0}^\infty \frac{x^n}{e^x-1} = \frac{x^n}{e^x-1} = \frac{\int_{-\infty}^\infty \left\lfloor \frac{ai+b}{c} \right\rfloor \cdot (n+1)}{2} \\ = \begin{cases} \left\lfloor \frac{a}{c} \right\rfloor \cdot \frac{n(n+1)}{2} + \left\lfloor \frac{b}{c} \right\rfloor \cdot (n+1) \\ +f(a \bmod c, b \bmod c, c, n), & a \geq c \vee b \\ 0, & n < 0 \vee a \\ nm - f(c, c - b - 1, a, m - 1), & \text{otherwise} \end{cases}$$

$$\begin{split} i(a,b,c,n) &= \sum_{i=0}^{n} i \left\lfloor \frac{a-c}{c} \right\rfloor \\ &= \begin{cases} \left\lfloor \frac{a}{c} \right\rfloor \cdot \frac{n(n+1)(2n+1)}{6} + \left\lfloor \frac{b}{c} \right\rfloor \cdot \frac{n(n+1)}{2} \\ +g(a \bmod c, b \bmod c, c, n), \\ 0, \\ \frac{1}{2} \cdot (n(n+1)m - f(c, c-b-1, a, m-1) \\ -h(c, c-b-1, a, m-1)), \end{cases} \end{split}$$

$$\begin{split} h(a,b,c,n) &= \sum_{i=0}^n \left\lfloor \frac{ai+b}{c} \right\rfloor^2 \\ &= \begin{cases} \left\lfloor \frac{a}{c} \right\rfloor^2 \cdot \frac{n(n+1)(2n+1)}{6} + \left\lfloor \frac{b}{c} \right\rfloor^2 \cdot (n+1) \\ + \left\lfloor \frac{a}{c} \right\rfloor \cdot \left\lfloor \frac{b}{c} \right\rfloor \cdot n(n+1) \\ + h(a \bmod c, b \bmod c, c, n) \\ + 2 \left\lfloor \frac{a}{c} \right\rfloor \cdot g(a \bmod c, b \bmod c, c, n) \\ + 2 \left\lfloor \frac{b}{c} \right\rfloor \cdot f(a \bmod c, b \bmod c, c, n), \\ 0, \\ nm(m+1) - 2g(c, c-b-1, a, m-1) \\ - 2f(c, c-b-1, a, m-1) - f(a, b, c, n) \end{cases} \end{split}$$

6.19 牛成函數

• Ordinary Generating Function $A(x) = \sum_{i>0} a_i x^i$

$$-A(rx) \Rightarrow r^n a_n$$

$$-A(x) + B(x) \Rightarrow a_n + b_n$$

$$-A(x)B(x) \Rightarrow \sum_{i=0}^n a_i b_{n-i}$$

$$-A(x)^k \Rightarrow \sum_{i_1+i_2+\dots+i_k=n} a_{i_1} a_{i_2} \dots a_{i_k}$$

$$-xA(x)' \Rightarrow n a_n$$

$$-\frac{A(x)}{1-x} \Rightarrow \sum_{i=0}^n a_i$$

• Exponential Generating Function A(x) $\sum_{i>0} \frac{a_i}{i!} x_i$

$$-A(x) + B(x) \Rightarrow a_n + b_n -A^{(k)}(x) \Rightarrow a_{n+k} -A(x)B(x) \Rightarrow \sum_{i=0}^{n} {n \choose i} a_i b_{n-i} -A(x)^k \Rightarrow \sum_{i_1+i_2+\dots+i_k=n}^{n} {n \choose i,i_2,\dots,i_k} a_{i_1} a_i -xA(x) \Rightarrow na_n$$

· Special Generating Function

$$- (1+x)^{n} = \sum_{i \ge 0} {n \choose i} x^{i}
- \frac{1}{(1-x)^{n}} = \sum_{i \ge 0} {n \choose i-1} x^{i}$$

7 Misc

7.1 **fast**

7.2 next-combination

7.3 PBDS

7.4 python

```
1 | from decimal import Decimal, getcontext
2 | getcontext().prec = 1000000000
3 | getcontext().Emax = 999999999
4 | a = pow(Decimal(2), 82589933) - 1
```

7.5 rng

```
inline ull rng() {
    static ull Q = 48763;
    Q ^= Q << 7;
    Q ^= Q >> 9;
    return Q & Øxfffffffffflll;
}
```

7.6 rotate90

7.7 timer

7.8 矩形覆蓋面積

```
const int N = 2e6 + 5; // [-1e6, 1e6]
int tag[N * 4], seg[N * 4];
void pull(int v, int l, int r) {
  seg[v] = 0;
  if(tag[v] > 0) seg[v] = r - l + 1;
  else if(l < r) seg[v] = seg[v * 2] + seg[v
       * 2 + 1];
void update(int ql, int qr, int x, int v =
    1, int 1 = 0, int r = N - 1) {
  if(ql > r \mid | qr < 1) return;
  if(ql <= 1 && r <= qr) {
    tag[v] += x;
  } else {
    int m = (1 + r) / 2;
    update(q1, qr, x, v * 2, 1, m);
    update(ql, qr, x, v * 2 + 1, m + 1, r);
 pull(v, 1, r);
int main() {
 int n: cin >> n:
  vector<array<int, 4>> ev(2 * n);
  REP(i, n) {
    int x, y, x2, y2;
    cin >> x >> y >> x2 >> y2;
    x += N / 2; y += N / 2;
    x2 += N / 2; y2 += N / 2;
    ev[2 * i] = \{x, y, y2, +1\};
    ev[2 * i + 1] = \{x2, y, y2, -1\};
  sort(all(ev));
  11 ans = 0, prev = 0;
  REP(i, 2 * n) {
    ans += (ev[i][0] - prev) * seg[1];
    int j = i;
    while(j < 2 * n && ev[i][0] == ev[j][0])
      update(ev[j][1], ev[j][2] - 1, ev[j
           ][3]);
```

8 String

8.1 AC

```
1 template < int ALPHABET = 26, char MIN CHAR =</pre>
        'a'>
2 struct ac_automaton {
    struct Node {
      int fail = 0, cnt = 0;
      array<int, ALPHABET> go{};
    vector<Node> node;
    vi que;
    int new node() { return node.eb(), SZ(node
    Node& operator[](int i) { return node[i];
    ac_automaton() { new_node(); }
    int insert(const string& s) {
      int p = 0;
      for(char c : s) {
        int v = c - MIN CHAR;
        if(node[p].go[v] == 0) node[p].go[v] =
              new node();
        p = node[p].go[v];
      node[p].cnt++;
20
      return p;
21
    void build() {
      que.reserve(SZ(node)); que.pb(0);
      REP(i, SZ(que)) {
25
        int u = que[i];
        REP(j, ALPHABET) {
26
           if(node[u].go[j] == 0) node[u].go[j]
                 = node[node[u].fail].go[j];
           else {
28
29
             int v = node[u].go[j];
             node[v].fail = (u == 0 ? u : node[
30
                  node[u].fail].go[j]);
             que.pb(v);
32
33
34
35
      for(auto u : que) node[u].cnt += node[
           node[u].fail].cnt;
36
37 };
```

8.2 KMP

```
1  // abacbaba -> [0, 0, 1, 0, 0, 1, 2, 3]
2  vi KMP(const vi& a) {
3    int n = SZ(a);
4    vi k(n);
5    for(int i = 1; i < n; ++i) {
6        int j = k[i - 1];
7        while(j > 0 && a[i] != a[j]) j = k[j -
1];
8        j += (a[i] == a[j]);
9        k[i] = j;
9        k[i] = j;
10    }
11    return k;
12 }
```

8.3 LCP

8.4 manacher

```
ı | // length: (z[i] - (i & 1)) / 2 * 2 + (i &
       1)
2 vi manacher(string t) {
    string s = "\&";
    for(char c : t) s.pb(c), s.pb('%');
    int 1 = 0, r = 0;
    vi z(sz(s));
    REP(i, sz(s)) {
      z[i] = r > i ? min(z[2 * 1 - i], r - i)
      while(s[i + z[i]] == s[i - z[i]]) z[i
      if(z[i] + i > r) r = z[i] + 1, l = i;
10
11
    }
12
    return z;
```

8.5 rolling-hash

```
const ll M = 911382323, mod = 972663749;
ll Get(vector<ll>& v, int l, int r) {
    if(!!) return h[r]; // p[i] = M^i % mod
    ll ans = (h[r] - h[l - 1] * p[r - 1 + 1])
        % mod;
    return (ans + mod) % mod;
}
vector<ll> Hash(string s) {
    vector<ll> ans(sz(s));
    ans[0] = s[0];
    for(int i = 1; i < sz(s); i++) ans[i] = (
        ans[i - 1] * M + s[i]) % mod;
    return ans;
}</pre>
```

8.6 SAIS

1 // mississippi

```
2 // 10 7 4 1 0 9 8 6 3 5 2
3 vi SAIS(string a) {
   #define QQ(i, n) for(int i = (n); i >= 0;
   int n = sz(a), m = *max element(all(a)) +
   vi pos(m + 1), x(m), sa(n), val(n), lms;
   for(auto c : a) pos[c + 1]++;
   REP(i, m) pos[i + 1] += pos[i];
   vector<bool> s(n);
   QQ(i, n - 2) s[i] = a[i] != a[i + 1] ? a[i]
        ] < a[i + 1] : s[i + 1];
   auto ind = [&](const vi& ls){
     fill(all(sa), -1);
     auto L = [\&](int i) \{ if(i >= 0 \&\& !s[i]) \}
          ]) sa[x[a[i]]++] = i; };
     auto S = [&](int i) { if(i >= 0 && s[i])
           sa[--x[a[i]]] = i; };
     REP(i, m) x[i] = pos[i + 1];
     QQ(i, sz(ls) - 1) S(ls[i]);
     REP(i, m) x[i] = pos[i];
     L(n - 1);
     REP(i, n) L(sa[i] - 1);
     REP(i, m) x[i] = pos[i + 1];
     QQ(i, n - 1) S(sa[i] - 1);
   auto ok = [&](int i) { return i == n || (! 32|)
        s[i - 1] && s[i]); };
   auto same = [&](int i,int j) {
     do {
       if(a[i++] != a[j++]) return false;
     } while(!ok(i) && !ok(j));
     return ok(i) && ok(j);
   for (int i = 1; i < n; i++) if (ok(i)) lms.
        pb(i);
   ind(lms);
   if(sz(lms)) {
     int p = -1, w = 0;
     for(auto v : sa) if(v && ok(v)) {
       if(p != -1 \&\& same(p, v)) w--;
       val[p = v] = w++;
```

```
auto b = lms;
for(auto& v : b) v = val[v];
b = SAIS(b);
for(auto& v : b) v = lms[v];
ind(b);
}
return sa;
}
```

8.7 **SAM**

```
1|// cnt 要先用 bfs 往回推, 第一次出現的位置是
       state.first_pos - |S| + 1
 struct Node { int go[26], len, link, cnt,
      first_pos; };
 Node SA[N]; int sz;
 void sa_init() { SA[0].link = -1, SA[0].len
      = 0, sz = 1; 
 int sa_extend(int p, int c) {
   int u = sz++;
   SA[u].first_pos = SA[u].len = SA[p].len +
   SA[u].cnt = 1;
   while(p != -1 && SA[p].go[c] == 0) {
     SA[p].go[c] = u;
     p = SA[p].link;
   if(p == -1) {
     SA[u].link = 0;
     return u;
   int q = SA[p].go[c];
   if(SA[p].len + 1 == SA[q].len) {
     SA[u].link = q;
     return u;
   int x = sz++;
   SA[x] = SA[q];
   SA[x].cnt = 0;
   SA[x].len = SA[p].len + 1;
   SA[q].link = SA[u].link = x;
   while(p != -1 && SA[p].go[c] == q) {
     SA[p].go[c] = x;
     p = SA[p].link;
   return u;
```

8.8 smallest-rotation

```
string small_rot(string s) {
   int n = sz(s), i = 0, j = 1;
   s += s;

while(i < n && j < n) {
   int k = 0;
   while(k < n && s[i + k] == s[j + k]) k
   ++;

if(s[i + k] <= s[j + k]) j += k + 1;
   else i += k + 1;</pre>
```

```
9     if(i == j) j++;
10     }
11     int ans = i < n ? i : j;
12     return s.substr(ans, n);
13 }</pre>
```

8.9 Z

```
1  // abacbaba -> [0, 0, 1, 0, 0, 3, 0, 1]
2  vi z_algorithm(const vi& a) {
3    int n = sz(a);
4    vi z(n);
5    for(int i = 1, j = 0; i < n; ++i) {
6        if(i <= j + z[j]) z[i] = min(z[i - j], j + z[j] - i);
7        while(i + z[i] < n && a[i + z[i]] == a[z [i]]) z[i]++;
8    if(i + z[i] > j + z[j]) j = i;
9    }
10    return z;
11 }
```

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1	Basic	1	4	Geometry	5		6.9	Linear-Sieve	8		8.1 AC	10
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	sparse taste	_			9		0.17	~~ 3	_		*** =	

ACM ICPC Judge Test Angry Crow Takes Flight!

C++ Resource Test

```
#include <bits/stdc++.h>
using namespace std;

namespace system_test {

const size_t KB = 1024;
const size_t MB = KB * 1024;
const size_t GB = MB * 1024;
```

```
chrono::duration<double> diff = end -
10 size t block size, bound;
                                                          begin;
  void stack size dfs(size t depth = 1) {
                                                     return diff.count():
   if (depth >= bound)
                                                   void runtime error 1() {
    int8_t ptr[block_size]; // 若無法編譯將
                                                     // Segmentation fault
         block size 改成常數
                                                     int *ptr = nullptr;
    memset(ptr, 'a', block_size);
                                                     *(ptr + 7122) = 7122;
    cout << depth << endl;</pre>
                                                 42 }
    stack_size_dfs(depth + 1);
                                                   void runtime_error_2() {
                                                     // Segmentation fault
  void stack_size_and_runtime_error(size_t
                                                     int *ptr = (int *)memset;
       block size, size t bound = 1024) {
                                                     *ptr = 7122;
    system test::block size = block size;
                                                 48 }
    system_test::bound = bound;
    stack size dfs();
                                                   void runtime_error_3() {
                                                     // munmap_chunk(): invalid pointer
                                                     int *ptr = (int *)memset;
  double speed(int iter num) {
                                                     delete ptr;
    const int block_size = 1024;
    volatile int A[block size];
    auto begin = chrono::high resolution clock
                                                   void runtime_error_4() {
         ::now();
                                                     // free(): invalid pointer
    while (iter_num--)
                                                     int *ptr = new int[7122];
      for (int j = 0; j < block_size; ++j)</pre>
                                                     ptr += 1;
                                                     delete[] ptr;
    auto end = chrono::high resolution clock::
```

```
63 void runtime error 5() {
    // maybe illegal instruction
    int a = 7122, b = 0;
    cout << (a / b) << endl;</pre>
  void runtime error 6() {
    // floating point exception
    volatile int a = 7122, b = 0;
    cout << (a / b) << endl;
73 }
  void runtime error 7() {
    // call to abort.
    assert(false);
78 }
  } // namespace system test
82 #include <sys/resource.h>
void print_stack_limit() { // only work in
       Linux
    struct rlimit 1;
    getrlimit(RLIMIT STACK, &1);
    cout << "stack_size = " << l.rlim_cur << "</pre>
          byte" << endl;</pre>
87 }
```