

## Exercise 1

Average and dispersion in product characteristics.

```

> print(dispersion)
      PPK_Stk    PBB_Stk    PFl_Stk    PHse_Stk    PGen_Stk    PImp_Stk    PSS_Tub    PPK_Tub
0.0226554865 0.0144797566 0.0018399974 0.0141208621 0.0012366513 0.0131437214 0.0037468593 0.0008836431
      PFl_Tub    PHse_Tub
0.0001975293 0.0052497277
> average=apply(as.matrix(choiceprice[,3:12]),2,mean)
> print(average)
      PPK_Stk    PBB_Stk    PFl_Stk    PHse_Stk    PGen_Stk    PImp_Stk    PSS_Tub    PPK_Tub    PFl_Tub    PHse_Tub
0.5184362 0.5432103 1.0150201 0.4371477 0.3452819 0.7807785 0.8250895 1.0774094 1.1893758 0.5686734
~ #Market share and market share by choiceprice characteristic

```

Market share, and market share by product characteristics.

```

> share
      pk_stk    bb_stk    fl_stk    hse_stk    gen_stk    imp_stk    ss_tub    pk_tub
[1,] 0.3164004 0.1230866 0.09887261 0.09316123 0.04474122 0.02247123 0.09984262 0.08753436
      fl_tub    hse_tub
[1,] 0.1075665 0.006323178

```

By type

```

> share_type
      [,1]      [,2]
      "stick"    "tub"
share_type "69.8733351848051" "30.1266648151949"
>

```

Illustrate the mapping between observed attributes and choices.

```

> merge(choiceprice, demös, by = "hhid", all.x = TRUE)
      hhid choice PPK_Stk PBB_Stk PFl_Stk PHse_Stk PGen_Stk PImp_Stk PSS_Tub PPK_Tub PFl_Tub PHse_Tub sales
1  2100016      1    0.66    0.67    1.09    0.57    0.36    0.93    0.85    1.09    1.19    0.33    0.66
2  2100016      1    0.63    0.67    0.99    0.57    0.36    1.03    0.85    1.09    1.19    0.37    0.63
3  2100016      1    0.29    0.50    0.99    0.57    0.36    0.69    0.79    1.09    1.19    0.59    0.29
4  2100016      1    0.62    0.61    0.99    0.57    0.36    0.75    0.85    1.09    1.19    0.59    0.62
5  2100016      1    0.50    0.58    0.99    0.45    0.33    0.72    0.85    1.07    1.19    0.59    0.50
6  2100016      4    0.58    0.45    0.99    0.45    0.33    0.72    0.85    1.07    1.19    0.59    0.45
7  2100016      1    0.29    0.51    0.99    0.29    0.33    0.72    0.85    1.07    1.19    0.59    0.29
8  2100024      1    0.66    0.45    1.08    0.57    0.36    0.93    0.85    1.09    1.19    0.33    0.66
9  2100024      4    0.66    0.59    1.08    0.57    0.36    0.93    0.85    1.09    1.34    0.33    0.57
10 2100024      1    0.66    0.67    1.09    0.57    0.36    0.93    0.85    1.09    1.19    0.33    0.66
11 2100024      4    0.63    0.59    1.08    0.57    0.36    0.93    0.85    1.09    1.19    0.59    0.57
12 2100024      8    0.63    0.59    0.99    0.57    0.36    0.88    0.85    1.09    1.19    0.59    1.09
13 2100024      4    0.62    0.61    0.99    0.49    0.33    0.75    0.85    1.09    1.19    0.59    0.49
14 2100024      3    0.58    0.45    0.99    0.45    0.33    0.72    0.65    1.07    1.19    0.59    0.99
15 2100024      1    0.58    0.58    0.99    0.29    0.34    0.72    0.85    1.07    1.19    0.59    0.58
16 2100024      1    0.29    0.50    0.99    0.33    0.33    0.72    0.85    1.07    1.19    0.59    0.29
17 2100024      1    0.39    0.58    0.99    0.29    0.33    0.69    0.79    1.09    1.19    0.56    0.39
18 2100024      1    0.19    0.58    0.99    0.29    0.34    0.69    0.79    1.09    1.19    0.56    0.19
19 2100495      1    0.25    0.61    0.99    0.45    0.33    0.75    0.85    1.09    1.19    0.59    0.25
20 2100495      1    0.58    0.61    0.99    0.45    0.34    0.75    0.85    1.07    1.19    0.59    0.58
21 2100495      1    0.50    0.58    0.99    0.45    0.34    0.72    0.86    1.07    1.19    0.59    0.50

```

## Exercise 2

We are interested in the effect of price on demand. Propose a model specification.

To consider the effect of price, we can use Conditional logit model

Interpret the coefficient on price.

```

> estimateLogit(choiceprice, demös, logitreg, x=price, method = "bfgs")
[1] -6.6566340 -0.9543259 1.2969965 -1.7173298 -2.9040264 -1.5153021 0.2517927 1.4648942 2.3575437
[10] -3.8966267
>

```

-6.65 means that if price increases, the demand of choosing alternatives will decrease.  
-0.95 ~ -3.89 are intercepts.

### Exercise 3

We are interested in the effect of family income on demand

family income varies among individuals are not the alternatives, use Multinomial logit model

Interpret the coefficient on family

```
[1] -0.003156338 0.014507166 0.003980338 -0.001328126 0.030527384 -0.007002723 0.022807121 0.017661767
[9] 0.010698254 -0.843545649 -2.397656003 -1.199428121 -1.688616844 -4.137055731 -1.529169108 -2.846055103
[17] -2.573291074 -4.279712751
```

For -0.003 ~ 0.0107 are beta, for example, -0.003 means that if income increases, the demand of choosing the first choice will decrease.

-0.84 ~ -4.279 are intercepts.

### Exercise 4

#### Model 1

	V1	c2	c3	c4	c5	c6	c7	c8	c9	c10
me_1	-0.005445123	0.0257883274	-0.002369137	0.0093607645	0.0012362530	-0.0047487142	-0.0097322916	-2.660125e-03	-0.0099320814	-0.0014978724
me_2	0.009441594	-0.0245109415	-0.000733189	0.0109781919	0.0033886871	0.0007139751	0.0015043232	8.066422e-04	-0.0022713999	0.0006821166
me_3	-0.003052725	-0.0039661740	0.003974207	-0.0033627107	-0.0016207354	0.0009496521	0.0024570433	9.808530e-04	0.0032920827	0.0003485076
me_4	0.005430990	-0.0019480329	0.001021167	-0.0084423676	0.0072759930	0.0006231949	-0.0041844119	-1.749300e-03	0.0025010528	-0.0005282851
me_5	-0.005001979	-0.0044114959	0.005240391	-0.0045305572	-0.0018993181	0.0010527309	0.0048465905	2.543472e-04	0.0041854229	0.0002638679
me_6	-0.000491919	-0.0013467361	0.001110464	-0.0007926256	-0.0003632848	0.0003699668	0.0003805465	1.869490e-04	0.0007791040	0.0001675357
me_7	0.008613176	0.0069350729	-0.014000196	0.0047601420	-0.0001714568	0.0012668334	-0.0009180520	-1.361555e-03	-0.0054080124	0.0002840482
me_8	-0.004738241	0.0031729439	0.002063896	-0.0035410825	-0.0040360370	-0.0002702457	0.0020691270	2.297484e-03	0.0027509550	0.0002312007
me_9	-0.003666668	-0.0008142912	0.003147927	-0.0037813006	-0.0030375824	0.0001950433	0.0028837401	1.183046e-03	0.0037776213	0.0001124649
me_10	-0.001086302	0.0010876174	0.000545847	-0.0006397423	-0.0007768236	-0.0001526322	0.0006985302	6.146215e-05	0.0003270326	-0.0000649895

Element in table

For example, in me\_1 – v1:

-0.00544 means that one unit increase in the price of product 1 will decrease 0.00544 in the probability to buy the product 1

#### Model2

```

      [,1]
[1,] -0.0010504137
[2,] -0.0009016311
[3,]  0.0006266867
[4,]  0.0001660472
[5,] -0.0002794477
[6,]  0.0004431356
[7,] -0.0006821378
[8,]  0.0008861440
[9,]  0.0007338590
[10,] 0.0000577577

```

For example, -0.0010504 means that one unit change increase in family income will decrease 0.0010504 in the probability of choosing first choice compared with other 9 choices

## Exercise 5

Beta\_f

```

> beta_f
[1] -6.659699884 -0.004333800  0.014258958  0.004025557 -0.001264787  0.029710007 -0.009327126  0.021914644
[9]  0.016902350  0.008674428 -0.838705945  0.891148169 -1.826370582 -2.871247434 -2.454001559  0.498968897
[17]  0.805453868  1.866785193 -4.140083624

```

Beta\_r

Remove choice 1

```

> beta_r
[1]  2.059202266  0.016721323  0.006614508  0.001215756  0.032891379 -0.003689518  0.025468878  0.020231747
[9]  0.012479752 -1.470467400 -1.261403167 -0.565696438 -2.812995853 -1.139907155 -2.511165831 -2.759864325
[17] -4.705006196

```

MTT

MTT is 7821.209

MTT > the critical value of chi\_square, reject the null hypothesis that the two results are the same.