BIELEFELD UNIVERSITY

Masters Thesis

Simulating sedation-induced unconsciousness in a Neural-Mass-Model

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BIELEFELD UNIVERSITY

Abstract

Faculty of Technology Neuroinformatics Groups

Master of Science

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by Felix Friese

Patients with severe Traumatic Brain Injuries (TBI) often remain in a state of unresponsive wakefulness. Brain-Computer-Interface (BCI)-based systems promise to improve the state assessment and to open a communication channel for patients to express their intent while in conscious states. Developing such a BCI-System (e.g. with EEG), including the necessary algorithms to assess a patients current wakefulness or consciousness state from EEG data is a challenging task. Development, testing and evaluation of these algorithms requires labeled data (ground truth), which is almost impossible to obtain given the patients' lack of communication capabilities. Therefore, it would be desirable to generate a synthetic signal, which should ideally resemble real EEG data in all relevant features.

We previously developed a simple ICA-based model, which generates a multichannel EEG from base-signals with configurable spectral features. While this proved useful for testing numerous components of our signal-analysis framework, it lacks biological plausibility and explanatory power to model the changes in the signal's properties given an altered state of consciousness.

In this thesis, we propose an approach towards overcoming these issues while sticking with the original goal of generating realistic, practically useful surrogate data. A biologically motivated Neural Mass Model (NMM) on cortical-column level is implemented, which is able to approximate the effects of sedation-induced unconsciousness on the generated signal. The model is then shown to be able to reproduce the characteristic effects that sedation has on the EEG-Signals of real subjects. This is a first step to a model of consciousness-altering processes in the brain, which could ultimately be extended to realistically simulate other processes like sleep and trauma-induced DoC, facilitating better detection algorithms and furthering the goal to develop working BCI-Systems in the given context.

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List of Abbreviations

NMM Neural Mass Model

DoC Disorder of Consciousness
 TBI Traumatic Brain Injury
 BCI Brain Computer Interface

ICA Independent Component Analysis

 $\mathbf{PSP} \qquad \mathbf{Post\text{-}Synaptic\text{-}Potential}$

EPSP Excitatory Post-Synaptic-PotentialIPSP Inhibitory Post-Synaptic-Potential

 $\mathbf{GABA} \quad \mathbf{G}amma\text{-}\mathbf{A}mino\mathbf{b}utyric \ \mathbf{A}cid$

EEG Electroencephalography

PC Pyramidal Cell

EIN Excitatory Interneuron IIN Inhibitory Interneuron

Chapter 1

Introduction

1.1 Motivation Deutsch

Die hochkomplexen Prozesse der Änderung von Bewusstseinszuständen im menschlichen Gehirn sind nach wie vor kaum verstanden. Die Definition und Feststellung von Bewusstseinszuständen beruht in der Praxis weiterhin stark auf Verhaltensbasierten Beobachtungen (e.g. Reiz-Reaktions Tests) [hier möglicherweise Glasgow Coma Scale erwähnen]. Insbesondere bei Menschen die unter traumatischen Hirnschädigungen leiden, ist diese Herangehensweise jedoch unzureichend, da die Gründe für ausbleibende externe Reaktionen vielseitig sein können. Daher werden zunehmend Messungen der Hirnaktivität durch Neuroimaging (fMRT, EEG, ...) herangezogen um Bewusstseinszustände zu bestimmen und zu erforschen, sowie bestimmte Zustandsgrenzen neu zu definieren. Dabei gibt es bereits beeindruckende Erfolge, wie beispielsweise eine basale Kommunkation über BCI-Systeme mit Trauma-Patienten die über keinerlei äußerlich erkennbare Regung als aufmerksam zu erkennen gewesen wären. Die genauen Mechanismen hinter Zustandsänderungen sowie klare objektive Grenzen zwischen Zuständen sind aber immer noch der Gegenstand von Grundlagenforschung. Ein Ansatz um Stück für Stück bessere Einsicht in diese Prozesse zu erlangen, ist die Computer-Simulation von kontrollierten Zustandsveränderungen, beispielsweise einer Anästhesie, um ein Verständnis für die Veränderung von Dynamiken der Gehirnaktivtät und deren Auswirkungen zu entwickeln. Das Betäubungsmittel Propofol wird in der Medizin verwendet um im kontrollierten Rahmen einen völligen Bewusstseinsverlust zur Durchführung von Operationen herbeizuführen. Der neurochemische Wirkmechanismus von Propofol auf synaptische Rezeptoren ist bereits gut erforscht und bietet eine solide Grundlage für die Erforschung von Sedationsprozessen. Diese Arbeit beschäftigt sich mit der Möglichkeit diese Wirkmechanismen auf Computermodelle von Neuronenpopulationen im Gehirn anzuwenden und das entstehende Verhalten des Systems zu analysieren sowie Vergleiche zu den bisherigen neurologischen Erkenntnissen im Bereich Anästhesie zu ziehen. Ein gängiges Messverfahren um Anästhesie zu beobachten ist das EEG, das insbesondere wegen seines non-invasiven, portablen und relativ kostengünstigen Einsatzes Verwendung findet. Als Modell zur Simulation von EEG-ähnlichen Signalen bieten sich sogenannte Neural-Mass-Models (NMMs) an, die sich auf die Modellierung der Dynamiken von größeren Neuronenpopulationen fokussieren.

1.2 Related Work

There have been many efforts to simulate different states of consciousness with NMMs. A particularly sophisticated example is Bensaid et al.'s COALIA Framework [23], which is able to produce realistic resting-state EEG-like signals for sleep and wakefulness, by using the output of over 60 interconnected NMMs and applying a transformation onto scalp electrodes using a realistic head-model with tissue conductivities. Liang et al. [19] focussed on relating propofol-induction to effect-site concentration, which is an important parameter in any model for anaesthesia-simulation.

1.3 Collection of Quotes

'Although our understanding of the actions of propofol at the molecular level is quite extensive, we do not entirely understand how these molecular effects translate into alterations in cellular, synaptic and neural network function, and in turn cause unconsciousness [88]. This knowledge gap is, at least in part, the result of a lack of a generally accepted theory of consciousness. In recent years, cognitive neuroscience has seen a resurgence of interest in this topic, with attempts to integrate anaesthesia and sleep research in order to address this deficiency. This resurgence has revealed several brain areas that play a crucial role in generation of consciousness, and which are extensively influenced by hypnotic drugs.' [21]

Chapter 2

Technical Concepts

2.1 Neurobiology

2.1.1 Units for propofol concentration

Some papers [12] cite propofol concentrations in $\frac{\mu g}{mL}$, while others [11], [13] use μM (micromolar = $\frac{\mu mol}{L}$). To get comparable numbers, we first need to establish the following relation for Propofol (molar mass: 178.27 g):

$$1 \frac{\mu g}{mL} = \frac{1 \frac{\mu g}{mL}}{178.27 \frac{g}{mol}} = 5.609 \, \mu M$$

In this work, we will settle on μM and only mention values in $\frac{\mu g}{mL}$ where they are taken from a source, but then provide the converted value as well.

2.1.2 Realistic propofol concentrations during general anaesthesia (GA)

During GA, effect-site concentrations (c_e , concentration near the synaptic receptors) of propofol may easily range up to $5 \, \frac{\mu g}{mL} (\approx 28 \, \mu M)$. Loss of Consciousness (LOC) occurs on average at $c_e \sim 2.0 \, \frac{\mu g}{mL} (\approx 11.2 \, \mu M)$, while the Return of Consciousness (ROC) averages at $c_e \sim 1.8 \, \frac{\mu g}{mL} (\approx 10.1 \, \mu M)$. Both values may vary substantially for individual subjects. LOC has a strong tendency to occur at higher concentrations than ROC [12], [25]. Throughout GA, effect-site concentration is commonly derived from measured blood-plasma concentration (c_p) using more or less complex Pharmacokinetic (PK)-Models (e.g. [18], [19]), as direct measurement is impractical for obvious reasons. Since our model will work with c_e directly, we will disregard this for now - however, it should be kept in mind.

2.1.3 Effects of propofol on the IPSP

Research on the effect of propofol on the IPSC (Inhibitory Post-Synaptic Current) and EPSC has shown that propofol strongly affects the IPSP decay time [11], [13]. The EPSP and the amplitude of the IPSP are unaffected by propofol. Effect-site concentrations at clinically relevant levels increase the IPSP decay time significantly (e.g. around $10\,\mu\text{M}$ the decay time roughly doubles) [11].

Using the data-points from [11] and assuming a very rough manual logarithmic fit (see Fig. 2.1), the function

$$\mathcal{D}(c_e) = 0.65 * ln((c_e/2) + 1) + 1$$

will be used to calculate the decay-time factor λ from a given effect-site concentration in μM .

As there unfortunately were only a few data-points (and none above $10\,\mu\text{M}$, leaving a large part of the relevant parameter space empty), a computational model-fit might have over-valued those points. A visually fitted logarithmic function (assuming eventual effect saturation) seemed like a sensible choice for this use-case. However, since inter-subject variations are substantial in any case, the exact values do not matter as much as the order of magnitude.

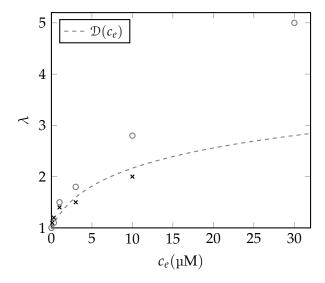


Figure 2.1: very rough manual logarithmic fit of decay-time factor to measured values from [11].

2.1.4 Hysteresis of propofol

If the state of a system depends not only on its parameters, but also the systems history, this dependency is called hysteresis. The human body often reacts differently to the same concentration of a drug, depending on whether the concentration is rising or decaying. Hysteresis is well documented during propofol-induced GA [7], [12], [22], [25], [26]. The most prominent effect being a counter-clockwise hysteresis for LOC and ROC (as mentioned in 2.1.2). The effects on responsiveness of subjects usually start at higher concentrations than they end. While some of that effect might be caused by inaccurate PK-Models, misgauging the actual effect-site concentration, there is a growing body of research that supports the notion that the observed effect is independent of pharmacokinetic interference [15], [26].

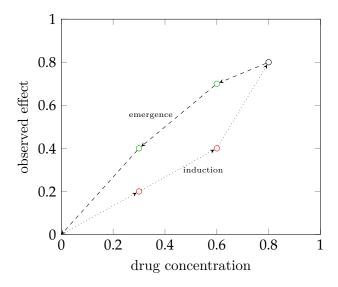


Figure 2.2: Example of counter-clockwise drug hysteresis

2.2 **EEG**

2.2.1 Measurement

2.2.2 Advantages/Disadvantages

Todo spatial/temporal resolution, invasiveness, ...

2.2.3 States of Consciousness in the EEG Signal

☐ Todo how do the states differ in the signal

2.2.4 Biphasic Effect

A biphasic effect (an initial increase of an effect, that decreases with higher concentrations) in the EEG can be observed for many sedatives [7], [8]. For propofol, a temporary steep increase in EEG amplitude in the 2–20 Hz ranges, loosely correlated with the onset of LOC, as well as ROC can be observed.

2.2.5 Simulation

2.2.5.1 Motivation

☐ Todo what can we hope to achieve by simulating an EEG signal

2.2.5.2 Approaches

™ Todo which tools are at our disposal (naive frequency mixing, population models, simulating individual neurons, ...)

2.2.5.3 Model Choice

 $ightharpoonup ext{Todo}$ argue about models \Rightarrow why did we land on NMMs/population models?

2.3 Neural Mass Models

2.3.1 The Jansen-Rit Model

The widely used Jansen-Rit Model [5], [6], is based on earlier models by Wilson & Cowan [1], Lopes da Silva et al. [2], [3] and Zetterberg et al. [4]. It represents a cortical column in the brain, which is made up of three main components, each modeling a population of neurons with distinct characteristics.

The basic schema of the model is visualized in Fig. 2.3, showing the connections

between the main components. There is a population of Pyramidal Cells which receives input from two populations of inter-neurons, one of which is excitatory while the other is inhibitory. Each of the inter-neuron-populations receives the output of the PC population. Additionally, there is external excitatory input to the PC population from other regions of the brain.

The Block Diagram (Fig. 2.4) shows the individual modules of the model. A population consists of two types of blocks: The *PSP-Block* models the behavior of the synapses and neuronal somata. It can be either excitatory or inhibitory and converts the incoming aver-

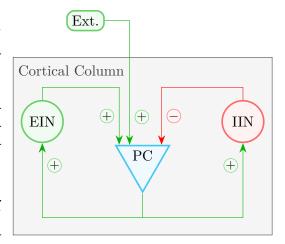


Figure 2.3: Basic Schema of the Jansen-Rit Model: Three populations of neurons

age pre-synaptic pulse density to an average post-synaptic membrane potential by convolving it with an impulse response function $(h_e(t))$ and $h_i(t)$, for excitation and inhibition respectively). The second block (sometimes called *Potential-To-Rate-Block* after it's functionality) calculates the populations response to this stimulation, transforming the incoming average membrane potential back into an average pulse density of action potentials. It may be roughly viewed as a functional counterpart to the axon hillock by establishing a firing threshold and is usually implemented by a Sigmoid Function (Sigm). External input from other regions of the brain is represented by p(t). The Connectivity Constants C_1 , C_2 , C_3 and C_4 are a proportional representation of the average number of synapses between the populations. The signal most closely related to the EEG and therefore the variable of interest, is the summed average membrane potential of the PC population $(y_1(t) - y_2(t))$ in Fig. 2.4).

 $oxed{arrange}$ Todo explain neurophysiology why $EEG pprox y_1 - y_2$, or reference back to explanation in EEG section

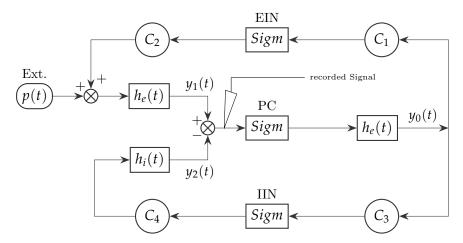


Figure 2.4: Simple Block Diagram after [6]: It's structure might be somewhat confusing when trying to visualize the biological analogy, where each population would have individual afferent PSP-Blocks. However, the fact that the two interneuron populations share a single excitatory PSP Block, because it produces identical results for both of them (disregarding their individual connectivity factor, which is simply applied afterwards), is a computational performance gain, thus likely explaining the authors' choice.

2.3.1.1 Potential-To-Rate Block

For a neuron to fire an action potential, its membrane potential needs to surpass a certain threshold. Since we are modeling not a single neuron but a whole population, we need an operator that can transform the mean membrane potential that the neurons of the population receive as input into an average firing rate for the whole population. While neurons within the population may have individual firing-thresholdit can be assumed due to their sheer number, that these thresholds are normally distributed around some mean value v_0 . An additional assumption that this approach rests on, is that the number of afferent (i.e. incoming) connections to the individual neurons is sufficiently large to justify the assertion that all neurons receive roughly the same stimulation. This must be modeled by a monotonically increasing function. The Potential-To-Rate Block represents this process with a Sigmoid. After multiple iterations by Zetterberg [4], Lopes da Silva [3] and others, Jansen and Rit [5], [6] landed on the following equation:

$$Sigm(v) = \frac{2e_0}{1 + e^{r(v_0 - v)}} \tag{2.1}$$

The parameter values (Table 2.1) are empirically determined [5]. The maximum firing rate the population can achieve is set at 5Hz. A mean membrane potential of 6mV (equal to the populations average firing threshold) elicits half of the maximum firing rate, while $\frac{0.56}{mV}$ defines the steepness. The plot in Fig. 2.5 visualizes these properties.

Parameter	Default Value	Unit	
half of maximum firing rate	e_0	2.5	Hz
average firing threshold	v_0	6.0	mV
sigmoidal steepness	r	0.56	mV^{-1}

Table 2.1: Parameters of the Sigmoid Function

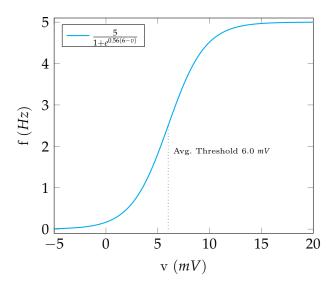


Figure 2.5: Sigmoid (Eq. 2.1) [5]

2.3.1.2 PSP-Blocks

In Physics, Linear Time-Invariant Systems (LTI systems) are oftentimes used to describe the response of electrical circuits to arbitrary input signals. They consist of a kernel function (or impulse-response function), that models the system's response to a single unit-impulse. The PSP-Blocks are an LTI system, fully represented by an impulse response function. It describes a PSP relative to the onset of a pulse. Since the PSP differs depending on the type of cell (excitatory or inhibitory), there are two different impulse-response functions. The parameters for the EPSP (Eq. 2.2) and IPSP (Eq. 2.3) are given in Table 2.2. The respective plots are visualized in Fig. 2.6.

Parameter		Default Value	Unit
Exc maxámplitude / e	Α	3.25	mV
Lumped reprof sum of excdelays	а	100	Hz
Inh. max. amplitude / e	В	22	mV
Lumped reprof sum of inhdelays	b	50	Hz

Table 2.2: Parameters of the PSP Blocks

Excitatory impulse response:

$$h_e(t) = \begin{cases} Aate^{-at} & t \ge 0\\ 0 & t < 0 \end{cases}$$
 (2.2)

Inhibitory impulse response:

$$h_i(t) = \begin{cases} Bbte^{-bt} & t \ge 0\\ 0 & t < 0 \end{cases}$$
 (2.3)

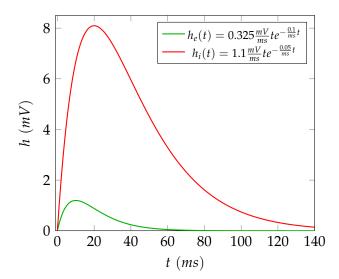


Figure 2.6: Impulse Response Functions: Note the small EPSP (Eq. 2.2) and the large IPSP (Eq. 2.3) [5]

Jansen and Rit [5] justify the difference in amplitude by referencing Lopes da Silva et al. [3] and stating that inhibitory neurons synapse closer to the somata of pyramidal cells (often on the cell body) than excitatory cells, increasing the effect of an inhibitory neuron about 10-fold.

The output of the Linear System defined by the PSP-Blocks is calculated by a convolution (denoted by *) of the incoming impulse density x(t) with the impulse response function h(t) (Eq. 2.4).

Remark (Convolution). The convolution of two functions f(t) and g(t) is defined as the integral of their product after one function has been reversed and shifted ¹:

$$f(t) * g(t) = \int_{-\infty}^{+\infty} f(\tau)g(t-\tau)d\tau$$

If f(t) is a unit-impulse $\delta(t)$ (in our case that would mean each cell of the previous population firing a single action potential at the same time) the result is just g(t)(in our case representing a single fullamplitude impulse response as the mean

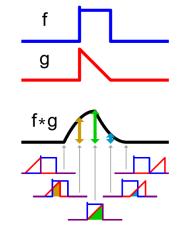


Figure 2.7: Convolution: The area enclosed by $f(\tau)$ and $g(t-\tau)$ is the value of (f*g)(t).

There is a very intuitive explanation of convolutions by Kalid Azad on his website https://betterexplained.com/articles/intuitive-convolutions/mglee - Own work, CC BY-SA 3.0 https://commons.wikimedia.org/w/index.php?curid=20206883

membrane potential):

$$\delta(t) * g(t) = \int_{-\infty}^{+\infty} \delta(\tau) g(t - \tau) d\tau = g(t)$$

In the general case, this process can be used to mathematically model the integration of incoming action potential densities in the soma.

Importantly, the Convolution Theorem states that the convolution of f(t) and g(t) becomes a simple multiplication when applying the Laplace Transform:

$$\mathcal{L}\lbrace f(t) * g(t) \rbrace = \mathcal{L}\lbrace f(t) \rbrace \mathcal{L}\lbrace g(t) \rbrace = F(s)G(s)$$

That means you can calculate a convolution with the inverse Laplace-Transform of the multiplication of the functions' individual Laplace-Transforms:

$$f(t) * g(t) = \mathcal{L}^{-1}{F(s)G(s)}$$

Since the convolution in the time-domain is a computationally heavy operation, it is oftentimes faster to transform the equation into the Laplace-Domain (see Eq. 2.5), apply the Convolution Theorem and perform the multiplication there, and transform the results back to the time-domain. This results in a second order differential equation (Eq. 2.6) that can be efficiently solved by numerical integration. To obtain this form, we need the Laplace transform $H_e(s)$ (in this context also called *Transfer Function*) of our response function $h_e(t)$:

$$H_e(s) = \mathcal{L}\{h_e(t)\} = \mathcal{L}\{Aate^{-at}\} = \frac{Aa}{(s+a)^2} = \frac{Aa}{s^2 + 2as + a^2}$$

With that, we can start to transform our initial equation into the desired Second Order System:

$$\underbrace{y(t)}^{\text{PSP}} = \underbrace{h_e(t)}^{\text{impulse response impulse density}} * \underbrace{x(t)} (2.4)$$

applying the Laplace-Transform eliminates the convolution:

$$\stackrel{\mathcal{L}}{\iff} Y(s) = H_{e}(s) \cdot X(s) \qquad (2.5)$$

$$\iff Y(s) = \frac{AaX(s)}{s^2 + 2as + a^2}$$

$$\iff (s^2 + 2as + a^2)Y(s) = AaX(s)$$

$$\iff s^2Y(s) + 2asY(s) + a^2Y(s) = AaX(s)$$

reversing the Laplace-Transform yields a differential equation in the time domain:

which can be expressed as a system of two coupled first order equations:

$$\dot{y}(t) = z(t) \tag{2.7}$$

$$\dot{z}(t) = Aax(t) - 2az(t) - a^2y(t)$$
 (2.8)

where y(t) is the resulting PSP and x(t) the incoming pulse density. This works analogously for the inhibitory case with $h_i(t)$.

2.3.1.3 Full Linear System

Taking the two first order equations for $\dot{y}(t)$ (Eq. 2.7) and $\dot{z}(t)$ (Eq. 2.8), and the Block diagram (Fig. 2.8) as a base, we can now state the equations for the full Jansen-Rit Model with it's three populations. Each PSP-Block h(t) needs it's own system of coupled differential equations. The value of x(t) can be easily taken from the Block Diagram. $y_0(t)$ is the EPSP received by both the EIN and IIN population, while $y_1(t)$ is the EPSP and $y_2(t)$ the IPSP received by the PC population:

$$\dot{y}_{0}(t) = z_{0}(t)
\dot{z}_{0}(t) = AaSigm[y_{1}(t) - y_{2}(t)] - 2az_{0}(t) - a^{2}y_{0}(t)
\dot{y}_{1}(t) = z_{1}(t)
\dot{z}_{1}(t) = Aa(p(t) + C_{2}Sigm[C_{1}y_{0}(t)]) - 2az_{1}(t) - a^{2}y_{1}(t)
\dot{y}_{2}(t) = z_{2}(t)
\dot{z}_{2}(t) = Bb(C_{4}Sigm[C_{3}y_{0}(t)]) - 2bz_{2}(t) - b^{2}y_{2}(t)$$
(2.9)

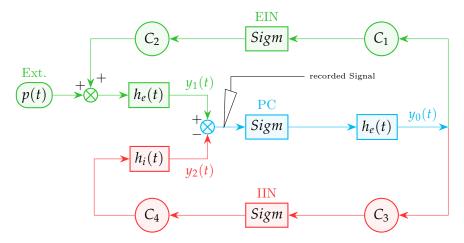


Figure 2.8: Colored Block diagram, visualizing the components of (Eq. 2.9)

2.3.1.4 Connectivity Constants

A sensible choice for the Connectivity Constants C_1 to C_4 was determined by Jansen and Rit empirically by defining a histologically motivated relationship between them $(C = C_1 = \frac{C_2}{0.8} = \frac{C_3}{0.25} = \frac{C_4}{0.25})$ and varying C until the system produced the desired natural alpha-like activity at $C = C_1 = 135 \Rightarrow C_2 = 108$; $C_3 = C_4 = 33.75$. Varying C can account for common synaptic phenomena like neurotransmitter depletion [6].

2.3.1.5 Model Input

The model input p(t) represents the average activity of populations outside the modeled column that synapse on the columns PC population. Since this activity's source is so diverse, it is modeled by white noise (120-320 Hz).

₹ Todo go more into detail why the input is modeled like this

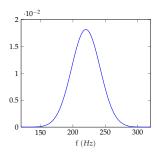


Figure 2.9: Input distribution. The input frequency representing p(t) is sampled from a normal distribution with $\mu = 220$ and $\sigma = 22$

2.3.1.6 Model Output

The simulated data from $y_1 - y_2$ while varying C looks like this:

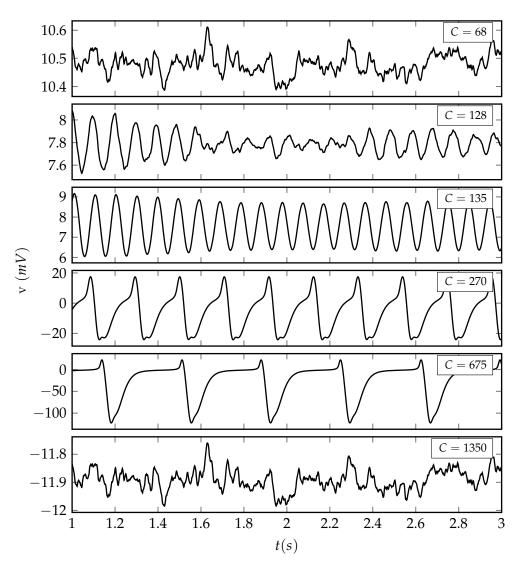


Figure 2.10: Model Output for varying C. Well defined alpha-activity is visible at C = 135.

2.3.2 The David and Friston Model

A Section Incomplete preliminary

the whole David-Friston-Section is still very much

While the Jansen-Rit model succeeds in generating realistic alpha activity, real EEG Signals contain much richer spectra [9]. David and Fristion [10] proposed a modification to the Jansen-Rit model, that could produce a more realistic frequency spectrum by introducing sub-populations to the model. They can be tuned individually to produce oscillations in different frequencies.

2.3.2.1 Introducing sub-populations

David and Friston slightly redefine h(t) by introducing the parameters H and τ (see Table 2.3), which is just a minor alteration of A and a.

$$h(t) = Aate^{-at} => h(t) = \frac{H}{\tau} te^{-\frac{1}{\tau}}$$

Furthermore, as they are tweaking these parameters to produce slower or faster sub-populations, they define the products $H_e\tau_e=0.0325mVs$ and $H_i\tau_i=0.44mVs$ as constants. This is done to preserve the oscillatory behavior of each population [10]. When varying τ , H is therefore adjusted accordingly ($H_e=\frac{0.0325mVs}{\tau_e}$, $H_i=\frac{0.44mVs}{\tau_i}$).

Parameter		Value	Unit	Relation to [6]
Excitatory delays	$ au_e$	0.01	s	$ au_e = rac{1}{a}$
Inhibitory delays	$ au_i$	0.02	S	$ au_i = rac{1}{b}$
Excitatory synaptic gain	H_e	3.25	mV	$H_e = A$
Inhibitory synaptic gain	H_i	22	mV	$H_i = B$

Table 2.3: Parameters of the PSP Blocks after [10]

Attention: From now on, the indices [0, ..., N] for y, h, τ and H refer only to the subpopulations within a single population. The indices used above in the formulation for the Simple Jansen-Rit Model (and the Block Diagram) should not be confused with these. However, e and i as indices still denote excitatory and inhibitory populations respectively.

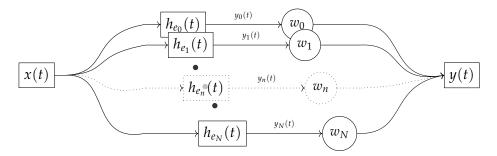


Figure 2.11: Example of subpopulations $(h_{e_0}(t), \ldots, h_{e_N}(t))$ forming an excitatory population $h_e(t)$

By introducing subpopulations, we split up the general impulse response function h(t) in N individual sub-functions:

$$h_n(t) = \frac{H_n}{\tau_n} t e^{-\frac{1}{\tau_n}}$$

The previously defined general PSP-Block Equation:

$$y(t) = h(t) * x(t)$$

then becomes:

$$y(t) = \sum_{n=0}^{N} (w_n \cdot h_n(t) * x(t))$$
 with $\sum_{n=0}^{N} w_n = 1$ and $0 \le w_n \le 1$

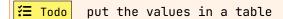
with N individually weighted (w_n) and parameterized $(h_n(t))$ subpopulations. We can then declare:

$$y_n(t) = h_n(t) * x(t)$$
 and $y(t) = \sum_{n=0}^{N} (w_n y_n)$

which produces the following differential equations for a single PSP Block:

$$\dot{y}_{0}(t) = z_{0}(t)
\dot{z}_{0}(t) = \frac{H_{0}}{\tau_{0}}x(t) - \frac{2}{\tau_{0}}z_{0}(t) - \left(\frac{1}{\tau_{0}}\right)^{2}y_{0}(t)
\dots
\dot{y}_{N}(t) = z_{N}(t)
\dot{z}_{N}(t) = \frac{H_{N}}{\tau_{N}}x(t) - \frac{2}{\tau_{N}}z_{N}(t) - \left(\frac{1}{\tau_{N}}\right)^{2}y_{N}(t)
y(t) = w_{1}y_{1} + \dots + w_{N}y_{N}$$
(2.10)

David and Friston further propose an example with two subpopulations for each population with the following parameters: $\tau_{e_1} = 10.8ms$, $\tau_{i_1} = 22ms$, $\tau_{e_2} = 4.6ms$, $\tau_{i_2} = 2.9ms$. While the kinetics for the first subpopulation were still close to those of the original populations ($\tau_e = 10ms$, $\tau_i = 20ms$, which produce alpha activity), the second population's parameters were chosen to produce gamma activity.



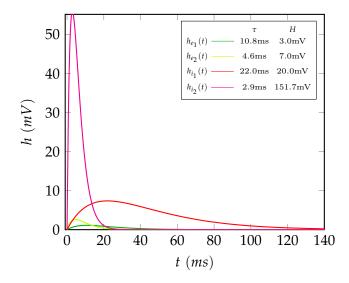


Figure 2.12: PSP functions for Subpopulations: — and — are faster subpopulations

Chapter 3

Methodology

3.1 PyRates Framework

▲ Section Incomplete
preliminary

The whole PyRates section is still very much

The PyRates Framework is a Python software framework, written by Richard Gast and Daniel Rose at the Max-Plank-Institute in Leipzig. It can simulate a wide range of graph-representable neural models, while setting a focus on rate-based population models [24]. It wraps computational backends like Numpy and Tensorflow and offers predefined nodes and edges (components that model units like cells or cell populations and the connections between them with mathematical equations) to be used, replaced or extended with custom equations. Furthermore it provides two simple ways to define these components and the derived network configurations: either by YAML-File or within Python code. These configurations are then compiled into optimized executable code with respect to the chosen backend before being executed. It comes with pre-configured model-definitions for some of the most frequently used models, e.g. the basic Jansen-Rit Circuit [6] and the Montbrio-Model [20], as well as some variations thereof. It's ease of use, the fact that it could easily reproduce the characteristics of the basic Jansen-Rit model out of the box, and the open-source character made it a sensible choice for this thesis.

3.1.1 Network Representations

3.1.1.1 YAML Representation

```
JansenRitSynapse: # name of the template
         description: ... # optional descriptive text
 2
         base: OperatorTemplate # parent template or Python class to use
 3
         equations: # unordered list of equations
         - 'd/dt * V = V_t'
         - 'd/dt * V_t = h/tau * r_in - (1./tau)^2 * V - 2.*1./tau*V_t'
         - 'd/dt * V_t = h/tau * r_in - (1./tau)^2 * V - 2.*1./tau*V_t'
         variables: # additional information to define variables in equations
             r_in:
                 default: input # defines variable type
10
             ۷:
11
                 default: output
12
             V_t:
13
                 description: integration variable # optional
                 default: variable
15
             tau:
16
                 description: Synaptic time constant
17
                 default: constant
19
                 default: constant
20
```

Figure 3.1: Example YAML Synapse

```
JansenRitCircuit:
1
         base: CircuitTemplate
         nodes: # list nodes and label them
3
             EIN: ExcitatoryInterneurons
             IIN: InhibitoryInterneurons
             PC: PyramidalCellPopulation
         edges: # assign edges between nodes
         # [<source>, <target>, <template_or_operators>, <values>]
         - [PC/PRO/r_out, IIN/RPO_e/r_in, null, {weight: 33.75}]
         - [PC/PRO/r_out, EIN/RPO_e/r_in, null, {weight: 135.}]
10
         - [EIN/PRO/r_out, PC/RPO_e/r_in, null, {weight: 108.}]
11
         - [IIN/PRO/r_out, PC/RPO_i/r_in, null, {weight: 33.75}]
```

Figure 3.2: Example YAML Circuit

3.1.1.2 Python Representation

```
from pyrates.frontend import OperatorTemplate
1
     from copy import deepcopy
2
3
     pro = OperatorTemplate(
         name='PRO', path=None,
5
         equations=[
6
              # R_{out} = \frac{2e_0}{1 + e^{r(v_0 - v)}}
              "rate_out = 2.*e_0 / (1 + exp(r*(v_0 - v)))"],
8
         variables={
9
              'rate_out': {'default': 'output'}, # output pulse density mout
10
              'v': {'default': 'input'}, # incoming avg. membrane potential v
11
              'v_0': {'default': 6e-3}, # avg. firing thresh. v_0 = 6mV
12
              'e_0': {'default': 2.5}, # half of max. firing rate e_0 = 2.5Hz
              'r': {'default': 560.0}}, # sigmoidal steepness r = 560V^{-1}
14
         description="sigmoidal potential-to-rate operator")
15
16
     rpo_e = OperatorTemplate(
^{17}
         name='RPO_e', path=None,
18
         equations=[
19
              # \dot{y}(t) = z(t)
20
              'd/dt * y = z',
21
              # \dot{z}(t) = \frac{H}{\tau}x(t) - \frac{2}{\tau}z(t) - \frac{1}{\tau}^2 y(t)
22
              'd/dt * z = H/tau * x - 2 * z/tau - y/tau^2'],
23
         variables={
24
              'y': {'default': 'output'}, # output membrane potential y(t)
25
              'z': {'default': 'variable'}, # helper variable z(t)=\dot{y}(t)
              'x': {'default': 'input'}, # incoming pulse density x(t)
27
              'tau': {'default': 0.01}, # exc. delays \tau_e=0.01s
28
              'H': {'default': 0.00325}}, # exc. synaptical gain H_e = 3.25mV
         description="excitatory rate-to-potential operator")
30
31
32
     rpo_i = deepcopy(rpo_e).update_template(
         name='RPO_i', path='',
33
         variables={
34
              'tau': {'default': 0.02}, # inh. delays \tau_i = 0.02s
35
              'H': {'default': 0.022}}, # inh. synaptical gain H_i=22mV
36
         description="inhibitory rate-to-potential operator")
37
38
```

Figure 3.3: Python Example for the relevant Operators

3.1.2 Implementation of the Jansen-Rit Model

PyRates works with population models by compositing multiple operators, like the PSP- (or Rate-To-Potential-) and Sigmoid- (or Potential-To-Rate) Block into nodes. These nodes represent populations that can then be connected via edges (synapses). For example one might combine two PSP-Blocks (for excitatory and inhibitory input respectively) with a Sigmoid Block to create a PC-Node. This node can then receive

rate-input to each of it's PSP-Blocks and produces rate-output from it's Sigmoid-Block. The EIN- and IIN- nodes are functionally identical and just combine an excitatory PSP-Block with a Sigmoid Block. By connecting these Blocks (see Fig. 3.4) and adding random input to the excitatory PSP-Block of the PC-Node, the simple Jansen-Rit Circuit is already complete.

$$\frac{d}{dt}PSP_{EIN} = PSP_{t_{EIN}}$$

$$\frac{d}{dt}PSP_{t_{EIN}} = \frac{H_e}{\tau_e} \cdot C_1Sigm[PSP_{PC}] - \frac{2}{\tau_e} \cdot PSP_{t_{EIN}} - \left(\frac{1}{\tau_e}\right)^2 \cdot PSP_{EIN}$$

$$\frac{d}{dt}PSP_{IIN} = PSP_{t_{IIN}}$$

$$\frac{d}{dt}PSP_{t_{IIN}} = \frac{H_e}{\tau_e} \cdot C_3Sigm[PSP_{PC}] - \frac{2}{\tau_e} \cdot PSP_{t_{IIN}} - \left(\frac{1}{\tau_e}\right)^2 \cdot PSP_{IIN}$$

$$\frac{d}{dt}PSP_{PC_E} = PSP_{t_{PC_E}}$$

$$\frac{d}{dt}PSP_{t_{PC_E}} = \frac{H_e}{\tau_e} \cdot (p(t) + C_2Sigm[PSP_{EIN}]) - \frac{2}{\tau_e} \cdot PSP_{t_{PC_E}} - \left(\frac{1}{\tau_e}\right)^2 \cdot PSP_{PC_E}$$

$$\frac{d}{dt}PSP_{PC_I} = PSP_{t_{PC_I}}$$

$$\frac{d}{dt}PSP_{t_{PC_I}} = \frac{H_i}{\tau_i} \cdot C_4Sigm[PSP_{IIN}]) - \frac{2}{\tau_i} \cdot PSP_{t_{PC_I}} - \left(\frac{1}{\tau_i}\right)^2 \cdot PSP_{PC_I}$$

$$PSP_{PC} = PSP_{PC_E} - PSP_{PC_I}$$

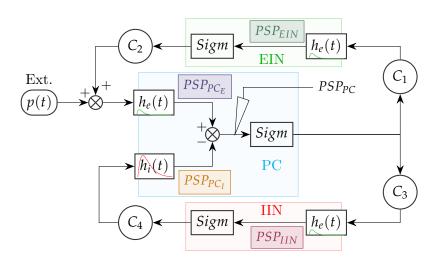


Figure 3.4: Jansen-Rit Block Diagram as implemented in PyRates: Each population can be clearly identified by one or more afferent PSP-Blocks and a single Sigmoid that calculates the populations output. This approach is more modular and simplifies conceptual understanding while staying mathematically equivalent. However, due to the explicit fourth PSP-Block it gives up the performance boost.

Todo possibly the backend-graph-optimization takes care of this?
maybe check this later on...

```
rpo_e = OperatorTemplate(
 1
          name='RPO_e', path=None,
2
          equations=[
3
               #-----
               # Subpopulation 0: h_0(t)
 5
               # \dot{y}_0 = z_0
 6
               'd/dt * y_0 = z_0',
               # \dot{z}_0 = \frac{H_0}{\tau_0} x - \frac{2}{\tau_0} z_0 - \frac{1}{\tau_0}^2 y_0
               'd/dt * z_0 = H_0/tau_0 * x - 2./tau_0 * z_0 - (1./tau_0)^2. * y_0'
9
10
               # Subpopulation 1: h_1(t)
11
               # \dot{y}_1 = z_1
12
               'd/dt * y_1 = z_1',
13
               # \dot{z}_1 = \frac{H_1}{\tau_1} x - \frac{2}{\tau_1} z_1 - \frac{1}{\tau_1}^2 y_1
                'd/dt * z_1 = H_1/tau_1 * x - 2./tau_1 * z_1 - (1./tau_1)^2. * y_1',
15
16
               # Population output:
17
               # y = \sum_{n=0}^{N} (w_n y_n)
18
               'PSP = w_0*y_0 + w_1*y_1'
19
20
               ],
21
          variables={
22
               'PSP': {'default': 'output'},
23
               **{var: {'default': 'variable'} for var in ['y_0', 'y_1', 'z_0', 'z_1']},
24
               'x': {'default': 'input'},
25
               'w_0': {'default': 1.0},
26
               'w_1': {'default': 0.0},
27
               'tau_0': {'default': tau_0},
28
                'tau_1': {'default': tau_1},
29
               'H_0': {'default': h_0},
30
               'H_1': {'default': h_1}},
31
          description="rate-to-potential operator")
32
```

Figure 3.5: PSP Block with two Sub-populations in PyRates

3.1.3 Simulating GABA-A Sedatives

 $\stackrel{\text{\frac{12}}}{=}$ Todo why does the reduction of C represent inhibition of the whole system - what is the difference between thalamic regulation (natural sleep, etc) and GABA-A-receptor binding substances (sedation)?

3.2 Simulating the effects of propofol

3.3 Implementing decay-time modulation

To simulate the effects of propofol on the GABA_A receptors, the IPSP (inhibitory response function h_i) time-constant τ_i is increased by a factor λ [14]:

$$h_i(t) = \frac{H_i}{\lambda \cdot \tau_i} t e^{-\frac{1}{\lambda \cdot \tau_i}}$$

The effect of increasing λ for h_{i_1} and h_{i_2} is visualized in Fig. 3.6.

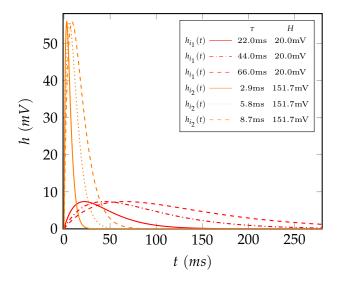


Figure 3.6: Inhibitory PSP functions with varying λ :

The duration of the effect increases while the amplitude stays constant, effectively increasing the charge transfer. (λ in [1.0 (no drug-effect, solid lines), 2.0 (dotted), 3.0 (dashed)])

Varying λ between 1 (0 μM) and 3.0 (\sim 30 μM) appears to be a sensible choice for the clinically relevant range, given Fig. 2.1.

Chapter 4

Results

4.1 Simulating over the parameter space

When simulating over the selected parameter space $\lambda \in [1,3]$ (see Fig 4.1 **A**), the following phenomena can be observed:

- 1. Steadily inreasing λ , from 1.0 first leads to a slight decrease in signal voltage, while roughly maintaining oscillation-amplitude (Fig 4.1 **B**). Additionally, the dominant frequencies from the 10-12Hz range slowly shift towards 5-10Hz (**C**). Overall the system appears to be in a stable state.
- 2. Starting from $\lambda \sim 1.85$, the system enters an unstable state, oscillating heavily and dramatically increasing signal amplitude and frequency amplitudes below 25 Hz. Further increasing λ has the same minimal effects on the disturbed signal, as the increase had before exiting the stable state.
- 3. At $\lambda \sim 2.05$, the disturbances disappear again, with the system having apparently reached a different stable state at visibly lower voltage. The dominant frequencies have jumped below 10 Hz.
- 4. Up to $\lambda = 3.0$, the signal voltage slowly continues to decrease as before, however the frequency distribution appears to have settled. Maintaining peak dosage has no further effects.
- 5. Decreasing from $\lambda = 3.0$ has the expected reverse effect: only the signal voltage increases as well.
- 6. At $\lambda \sim 1.95$ (somewhat lower than 2.05!), disturbances begin to form again. The system undergoes similar effects in reverse as it did in the other direction. Noteworthy is however, that the unstable state prevails until λ reaches ~ 1.48 .

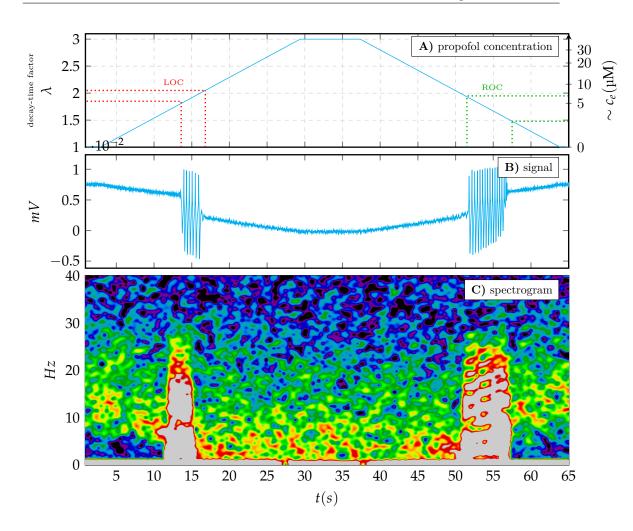


Figure 4.1: Simulation of a sedation: A): timeline of the simulated IPSP stretch factor λ (roughly representing c_e) B): timeline of the simulated signal C): spectrogram

Chapter 5

Discussion

While the NMM used for simulation is a very rough abstraction of cortical dynamics, multiple parallels to effects observed during GA can be drawn:

- 1. Two, distinguishable **stable states** can be observed. The frequency changes bear strong similarities to the switch to unconsciousness in GA [16], [17].
- 2. Induction and Emergence are asymmetrical (hysteresis). The system predicts that the state-change 'LOC' occurs at higher concentrations than 'ROC'.
- 3. During state transitions, there is a strong **biphasic effect**. The system predicts that the frequency range below 25 Hz receives a temporary amplitude boost during the phase transitions, which disappears while the parameter changes continue in the same direction.
- 4. In the 'unconscious' state, frequency distribution stabilizes independent of further increasing decay-time (slow-wave-activity saturation? [16]).

5.1 Outlook

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