## SMT-RAT 22.06

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SMT-RAT [2] is an open-source C++ toolbox for strategic and parallel SMT solving consisting of a collection of SMT compliant implementations of methods for solving quantifier-free first-order formulas with a focus on non-linear real and integer arithmetic. Further supported theories include linear real and integer arithmetic, difference logic, bit-vectors and pseudo-Boolean constraints. A more detailed description of SMT-RAT can be found at <a href="https://smtrat.github.io/">https://smtrat.github.io/</a>.

SMT-RAT-MCSAT uses our implementation of the MCSAT framework [3]. We employ incomplete methods to handle simpler problem classes more efficiently. Thus, our implementation is equipped with multiple explanation backends based on Fourier-Motzkin variable elimination, interval constraint propagation, virtual substitution as in [8], a novel level-wise variant (currently under review) of the one-cell CAD [1] and NLSAT-style model-based CAD projections [6], which are called in this order. The level-wise one-cell CAD uses linear approximations of some cell boundaries which would otherwise be defined by polynomials with high degree, as described in [7]. The general MCSAT framework is integrated in our adapted minisat [4] solver, but is not particularly optimized yet. Furthermore, our variable ordering is fully dynamic as suggested in [5].

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## References

- [1] Christopher W Brown and Marek Košta. Constructing a single cell in cylindrical algebraic decomposition. Journal of Symbolic Computation, 70:14–48, 2015.
- [2] Florian Corzilius, Gereon Kremer, Sebastian Junges, Stefan Schupp, and Erika Ábrahám. SMT-RAT: an open source C++ toolbox for strategic and parallel SMT solving. In *Proceedings of SAT 2015*, pages 360–368.
- [3] Leonardo de Moura and Dejan Jovanović. A model-constructing satisfiability calculus. In *Proceedings of VMCAI 2013*, pages 1–12.
- [4] Niklas Eén and Niklas Sörensson. An extensible SAT-solver. In Proceedings of SAT 2013, pages 502–518.
- [5] Dejan Jovanović, Clark Barrett, and Leonardo de Moura. The design and implementation of the model constructing satisfiability calculus. In *Proceedings of FMCAD 2013*, pages 173–180.
- [6] Dejan Jovanović and Leonardo De Moura. Solving non-linear arithmetic. In *International Joint Conference on Automated Reasoning*, pages 339–354. Springer, 2012.

- [7] Valentin Promies. Underapproximating cell bounds in MCSAT using low-degree polynomials. Msc thesis, RWTH Aachen University, 2022.
- [8] Erika Ábrahám, Jasper Nalbach, and Gereon Kremer. Embedding the virtual substitution method in the model constructing satisfiability calculus framework. In  $Proceedings\ of\ SC^2\ 2017\ at\ ISSAC$ , volume 1974 of  $CEUR\ Workshop\ Proceedings$ .