

Texture Packing

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目录

Chapter 1: Introduction

Input Specification(example)

Output Specification(example)

Chapter 2: Data Structure / Algorithm Specification

- 2.1 结构体介绍
 - 2.1.1 Texture
 - 2.1.2 Partition
- 2.2 主要函数介绍
 - 2.2.1 BST相关
 - 2.2.2 Partition 相关
- 2.3 主函数

Chapter 3: Testing Results

- 3.1 测试目的及结果
 - 3.1.1 正确性测试
 - 3.1.2 高度差异对比测试
 - 3.1.3 与 Best Fit 的算法对比
- 3.2 测试结果分析

Chapter 4: Analysis and Comments

- 4.1 时间复杂度分析
- 4.2 空间复杂度分析
- 4.3 算法评价与近似比分析 近似比影响因素分析

Appendix

Source Code

Partition_heap.h

Rectangle_BST.h

file_input.c

manual_input.c

correctness_test.c

Generator.c

References

Author List

Declaration

Chapter 1: Introduction

本项目研究的主题是 Textur Packing 。Texture Packing 问题是一类矩形装箱问题,常用于计算机图形学和游戏开发领域。其目标是将多个矩形形状的纹理 (texture) 紧密地打包到一个更大的矩形纹理中。具体来说,题目要求如下:

- 1. 输入: 若干矩形纹理, 每个纹理有固定的宽度和高度。
- 2. 输出: 一个大的矩形纹理, 其宽度固定, 要求设计一种方法尽量减少所需的高度。
- 3. 限制条件: 大矩形纹理的宽度是给定的, 最终纹理必须尽可能紧凑。

由于题目没有明确给出输入输出,在此介绍我们项目当中期望的输入输出格式:

Input Specification(example)

- 10
 5
 4 3
 3 2
 6 5
 5 3
 7 1
 - 1. 首先读取的两个数字分别是大纹理(容器)的最大宽度以及小纹理(小矩形)的个数n;
 - 2. 接着为 n 行的小矩形数据,宽x高的格式依次输入。

在实际执行时,可以调整宏定义中的 Element_type ,来选择 int 与 float 来作为矩形的尺寸。由于二者在我们的算法当中处理等价,因此均以整型作为输入数据的类型。 将浮点数类型的尺寸输入作为 3.1.1 中的测试,以展示正确性。

Output Specification(example)

- 1.表示的是依次插入小矩形的过程信息;
- 2. 最后分别输出 Approximation Ratio 与最终高度。其中 Approximation Ratio 采用算法得到的最终高度/理想高度 optimal_height, 后者通过 area_sum/container_width 得到,即将所有的矩形面积除以容器宽度。因此,此处的"近似比"实际上并非采用真正的理想高度进行计算。
- 3. 输出"近似比"的目的是为了从一定程度上衡量算法插入时的空间利用率,比较不同输入规模与不同算法下的表现。

Chapter 2: Data Structure / Algorithm Specification

2.1 结构体介绍

以 int 类型的输入为例,实际上为 Element_type 的类型,且可以在宏定义中修改。

2.1.1 Texture

```
typedef struct {
    int width;
    int height;
} Rectangle;

// BST node structure
typedef struct TreeNode {
    Rectangle rect;
    struct TreeNode *left;
    struct TreeNode *right;
} TreeNode;
```

- 1. 为了表示存储单个 Texture (下称小矩形),我们定义结构体 Rectangle ,其内部属性分别为整形的 宽与高;
- 2. 然后,我们将小矩形作为 BST 的节点根据属性 width 构造二叉树,方便后续根据宽度快速寻找符合条件的小矩形;

2.1.2 Partition

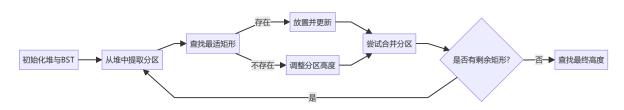
- 1. Partition 是我们表示大容器内部存储状态的结构体;
- 2. 分区 Partition 内部的属性功能简介如下:
 - 1. start_index: 该分区在容器当中的起始位置;
 - 2. width与height:分别表示该分区的宽度与高度;
 - 3. struct Partition *left 与 struct Partition *right: 分别指向容器当中相邻的分区,方便在出入矩形后,合并相同高度的分区操作;
 - 4. int heap_index: 用来存储在小顶堆中的实际索引。因为我们使用小顶堆方便取用最小宽度 (用 width 来建堆) ,因此如果需要删除某个特定的节点时,利用该索引可以直接访问对应的 节点,避免了遍历小顶堆的操作。
- 3. MinHeap 的作用已经在 2 有所提及,也就是我们利用 Partition 作为堆的内部节点,并根据其width 来建堆;其 \max_{height} 属性用于存储当前容器当中所有分区的最大高度,在每次插入新的分区时更新,避免在最后以 O(W) 的代价遍历小顶堆(W为容器宽度)。

相关操作

- o 利用分区作为小顶堆的节点建堆(初始化为高度为0,宽度为 container_width 的分区),然后每次取用堆顶元素(宽度最小)
- 在BST当中选择合适的小矩形插入到当前的位置,同时更新小顶堆中的分区:先调整其高度与 宽度,然后检查是否需要合并;
- 如果在第二步当中无法找到适合的小矩形,将该分区的高度设置为相邻区域的较小高度(表示弃用),合并之后然后继续搜索。

具体实现在 2.2 中给出。

2.2 主要函数介绍



在开始介绍函数前,请先了解整体流程(将在2.3中补充介绍)。

2.2.1 BST相关

• 创建与插入节点

```
Function CreateNode(Rectangle rect) Returns TreeNode*

Create a new TreeNode object

If memory allocation fails

Output "Memory allocation failed!" error message

Exit the program

Set the node's rectangle to the provided rect

Set the node's left and right children to NULL

Return the newly created node

End Function
```

```
Function Insert(root, Rectangle rect) -> TreeNode*
    If root == NULL
        Return CreateNode(rect)

If rect.width < root.rect.width
        root.left = Insert(root.left, rect)

Else
        root.right = Insert(root.right, rect)

Return root
End Function</pre>
```

这部分与常规的BST操作相同:

- 1. 创建节点时提供矩形结构体作为节点的 rectangle 属性;
- 2. 插入时依据 width 进行排序。

• 寻找最合适的节点

```
Function FindLargestFit(root, targetwidth) -> TreeNode*
   If root == NULL
        Return NULL

result = NULL

// If current node's width is greater than targetwidth, search the left
subtree

If root.rect.width > targetwidth
        result = FindLargestFit(root.left, targetwidth)

Else

// If current node fits, search the right subtree
   result = root
   rightResult = FindLargestFit(root.right, targetwidth)

If rightResult != NULL AND rightResult.rect.width > result.rect.width
   result = rightResult
```

```
End If
End If

Return result
End Function
```

这个函数是与传统BST查找的较大区别,因为我们需要查找的是**不大于** targetwidth **且宽度最大的矩形**。

- 1. 由于我们构建BST时,是利用矩形的 width 属性进行排序,因此我们在搜索时也利用这一属性:
- 2. 如果当前节点的 width 已经大于 targetwidth, 那么直接向其左子树继续搜索;
- 3. 如果当前节点的 width 小于等于 targetwidth ,将返回值 result 先赋值为当前节点 root ,然后继续在其右子树中寻找;
- 4. 递归逻辑如 2,3 步所示,如果找不到符合要求的节点,返回 NULL。

• 删除指定节点

```
Function DeleteNode(root, Rectangle rect) -> TreeNode*
    If root == NULL
        Return NULL
   // Search for the node to delete
   If rect.width < root.rect.width</pre>
        root.left = DeleteNode(root.left, rect)
    Else If rect.width > root.rect.width
        root.right = DeleteNode(root.right, rect)
    Else
        // Node found
        // Case 1: Leaf node
        If root.left == NULL AND root.right == NULL
            Free root
            Return NULL
        // Case 2: Single child
        If root.left == NULL
            temp = root.right
            Free root
            Return temp
        If root.right == NULL
            temp = root.left
            Free root
            Return temp
        // Case 3: Two children
        // Find the smallest node in the right subtree
        successor = root.right
        successorParent = root
```

```
While successor.left != NULL
    successorParent = successor
    successor = successor.left

If successorParent != root
    successorParent.left = successor.right

Else
    successorParent.right = successor.right

// Copy successor's value to current node
    root.rect = successor.rect
    Free successor
End If

Return root
End Function
```

- 1. **递归查找节点**: 首先递归查找待删除的节点。如果待删除的矩形宽度小于当前节点的矩形宽度,则向左子树递归;如果大于,则向右子树递归。
- 2. 节点删除的情况:
- **叶子节点**:如果当前节点没有左子树和右子树,则直接释放该节点并返回 NULL。
- 单个子节点: 如果当前节点只有一个子节点, 替换当前节点并返回该子节点。
- **两个子节点**:如果当前节点有两个子节点,找到右子树中的最小节点(即右子树中最左的节点),用其值替换当前节点,并删除该最小节点。

2.2.2 Partition 相关

• 维护堆的性质

```
Function HeapifyUp(heap, index)
    While index > 0
        parent = (index - 1) / 2
        If heap[index].height < heap[parent].height
            Swap heap[index] and heap[parent]
            Update heap_index for swapped elements
            //Move up the heap
            index = parent
        Else
            Break the loop
        End If
End While
End Function</pre>
```

从指定索引 (index) 开始,检查其父节点索引 (parent)。

如果当前节点的高度小于其父节点的高度,交换两者的位置以维护最小堆的性质。

交换后,更新节点和父节点的堆索引(heap_index)。

将当前索引设置为父节点索引,继续向上调整。

```
Function HeapifyDown(heap, index)
    smallest = index
    left = 2 * index + 1
    right = 2 * index + 2
    // Check if left child is smaller than the current smallest
    If left < heap.size AND heap[left].height < heap[smallest].height</pre>
        smallest = left
    End If
   // Check if right child is smaller than the current smallest
   If right < heap.size AND heap[right].height < heap[smallest].height</pre>
        smallest = right
    End If
    // If the smallest is not the current index, perform a swap
    If smallest != index
        // Swap heap[index] and heap[smallest]
        temp = heap[index]
        heap[index] = heap[smallest]
        heap[smallest] = temp
        // Update heap_index for swapped elements
        heap[index].heap_index = index
        heap[smallest].heap_index = smallest
        // Recursively heapify down the affected subtree
        HeapifyDown(heap, smallest)
    End If
End Function
```

初始化:设置当前节点为最小值节点(smallest),计算左子节点(left)和右子节点(right)的索引。

检查并更新:比较左右子节点与当前节点,寻找其中的 smallest。

交换并递归:

- 如果 smallest 更新为其他节点,说明当前节点不满足最小堆性质。
- 交换当前节点与 smallest 节点的内容, 并更新它们的 heap_index 。
- 调用 HeapifyDown 递归处理被影响的子树。

结束条件:如果当前节点已经满足最小堆性质(smallest == index),函数直接返回。

• 插入分区

```
Function InsertPartition(heap, part)
  // Update max_height if the new partition's height is greater
  If part.height > heap.max_height
    heap.max_height = part.height
```

```
End If
    // Check if the heap is full and needs resizing
    If heap.size == heap.capacity
        heap.capacity = heap.capacity * 2
        temp = Reallocate heap.heap with size = heap.capacity
        If temp == NULL
            Print "Memory allocation failed!" and terminate program
        heap.heap = temp
    End If
    // Insert the new partition at the end of the heap
    i = heap.size
    heap.heap[i] = part
    part.heap_index = i
    heap.size = heap.size + 1
    // Restore the min-heap property
    HeapifyUp(heap, i)
End Function
```

- 1.与插入到普通的小顶堆操作类似:将新分区初始化放置在末尾,更新相应的属性,然后利用 Heapifyup 从插入位置向上调整。
- 2. extractMin 等常规小顶堆操作不再赘述,请详见 Appendix 。

• 删除指定分区

```
Function RemovePartition(heap, part)
  index = part.heap_index

// Check for invalid index
If index >= heap.size OR index < 0
    Return
End If

// Replace the partition with the last element in the heap
heap.heap[index] = heap.heap[heap.size - 1]
heap.heap[index].heap_index = index
heap.size = heap.size - 1

// Adjust the heap to maintain min-heap property
HeapifyDown(heap, index)
HeapifyUp(heap, index)
End Function</pre>
```

删除分区的操作借助于结构体的属性 heap_index ,快速在堆中定位,然后将堆尾节点替换当前节点,接着在此处位置向上与向下调整,维持堆的结构。由此将删除指定节点操作的时间复杂度降低为O(logW).

• 检查 (并合并) 指定分区的相邻区域

```
Function CombinePartitions(heap, part)
    merged = false
    // Merge with left neighbor if possible
    If part.left exists AND part.left.height == part.height
        Merge part with part.left
        Remove part.left from heap
        Update left pointer of part
        merged = true
    End If
    // Merge with right neighbor if possible
    If part.right exists AND part.right.height == part.height
        Merge part with part.right
        Remove part.right from heap
        Update right pointer of part
        merged = true
    End If
    // Rebalance the heap if merging occurred
    If merged
        RebalanceHeap(heap, part)
    End If
End Function
```

- 1. 该函数在每次搜索时调用,检查对应的分区是否需要合并(包括矩形无法插入的情况,因为 我们调整了无法被插入矩形的分区的高度为相邻的较低高度,也相当于"插入"了矩形,且该情 况一定需要合并);
- 2. 利用 Partition 邻域指针,快速检查对应的高度是否相等,如果相等则合并。合并时,将 Part 的宽度更新、邻域指针的指向更新,然后删除邻域中被合并的分区,并维护堆的性质 (与上一个函数类似,RebalanceHeap 通过在此处向上、向下 heapify 实现)。

2.3 主函数

```
Function PartitionPacking(rectangles, n, containerWidth) -> int

1. Initialize the partition heap for the container.

2. Calculate the total area of all rectangles.

3. Insert all rectangles into a Binary Search Tree (BST) based on their widths.

4. While there are remaining rectangles:

- Extract the smallest partition from the heap.

- Find the best-fitting rectangle for the partition in the BST.

- If a rectangle is found:

- Place the rectangle into the partition.

- Adjust the partition's height and possibly create new partitions.

- If no rectangle fits:

- Adjust the partition's height to minimize wasted space.

- Attempt to merge the partition with neighboring partitions.

- Reinsert updated partitions into the heap.
```

- 5. Calculate the final height of the container.
- 6. Print the approximation ratio and cleanup resources.
- 7. Return the final container height.

End Function

这是算法的主函数,通过动态分区和二叉搜索树 (BST) 进行矩形管理。整体流程如下:

初始化:

创建一个分区堆用于管理和跟踪容器内的动态分区,同时计算所有矩形的总面积,为后续效率评估 提供依据。

矩形组织:

将矩形按宽度存储在二叉搜索树(BST)中,以便快速查找最适合某个分区的矩形。

矩形放置:

- 从分区堆中提取最小分区。
- 寻找宽度最适合分区的矩形。
- 如果找到合适的矩形,将其放入分区,并调整分区的高度和宽度。
- 如果没有找到合适的矩形,则调整分区高度。

分区合并:

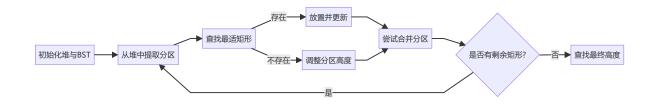
每次矩形放置或分区调整后,尝试合并相邻分区以优化利用率。

结果计算:

放置完成后,计算容器的最终高度,并根据总矩形面积计算近似比,评估打包效率。

资源清理:

清理分区堆和BST等数据结构,返回容器的最终高度。



Chapter 3: Testing Results

3.1 测试目的及结果

输入、输出格式已在 Chapter 1 中说明。

3.1.1 正确性测试

测试目的:验证程序的正确性与鲁棒性

• 样例测试

input:

```
10
5
4 3
3 2
6 5
5 3
7 1
```

output:

```
Extracted partition: start_index=0.00, width=10.00, height=0.00
Selected partition: start_index=0.00, width=10.00, height=0.00
Placing rectangle: width=7.00, height=1.00 in partition at index 0.00
New partition created: start_index=7.00, width=3.00, height=0.00
Remaining rectangles to place: 4
partition 0's height is 0.00
partition 1's height is 1.00
Extracted partition: start_index=7.00, width=3.00, height=0.00
Selected partition: start_index=7.00, width=3.00, height=0.00
Placing rectangle: width=3.00, height=2.00 in partition at index 7.00
Remaining rectangles to place: 3
partition 0's height is 1.00
partition 1's height is 2.00
Extracted partition: start_index=0.00, width=7.00, height=1.00
Selected partition: start_index=0.00, width=7.00, height=1.00
Placing rectangle: width=6.00, height=5.00 in partition at index 0.00
New partition created: start_index=6.00, width=1.00, height=1.00
Remaining rectangles to place: 2
partition 0's height is 1.00
partition 1's height is 2.00
partition 2's height is 6.00
Extracted partition: start_index=6.00, width=1.00, height=1.00
```

```
Selected partition: start_index=6.00, width=1.00, height=1.00
No suitable rectangle found for partition at index 6.00. Adjusting partition...
Partition adjusted: start_index=6.00,, height=2.00
Merging with right neighbor at index 7.000000.
Partition after merging: start_index=6.00, width=4.00, height=2.00
partition 0's height is 2.00
partition 1's height is 6.00
Extracted partition: start_index=6.00, width=4.00, height=2.00
Selected partition: start_index=6.00, width=4.00, height=2.00
Placing rectangle: width=4.00, height=3.00 in partition at index 6.00
Remaining rectangles to place: 1
partition 0's height is 5.00
partition 1's height is 6.00
Extracted partition: start_index=6.00, width=4.00, height=5.00
Selected partition: start_index=6.00, width=4.00, height=5.00
No suitable rectangle found for partition at index 6.00. Adjusting partition...
partition 0's height is 5.00
partition 1's height is 6.00
Extracted partition: start_index=6.00, width=4.00, height=5.00
Selected partition: start_index=6.00, width=4.00, height=5.00
No suitable rectangle found for partition at index 6.00. Adjusting partition...
partition 1's height is 6.00
Extracted partition: start_index=6.00, width=4.00, height=5.00
Selected partition: start_index=6.00, width=4.00, height=5.00
No suitable rectangle found for partition at index 6.00. Adjusting partition...
Extracted partition: start_index=6.00, width=4.00, height=5.00
Selected partition: start_index=6.00, width=4.00, height=5.00
No suitable rectangle found for partition at index 6.00. Adjusting partition...
Extracted partition: start_index=6.00, width=4.00, height=5.00
Selected partition: start_index=6.00, width=4.00, height=5.00
No suitable rectangle found for partition at index 6.00. Adjusting partition...
Selected partition: start_index=6.00, width=4.00, height=5.00
No suitable rectangle found for partition at index 6.00. Adjusting partition...
Partition adjusted: start_index=6.00,, height=6.00
Merging with left neighbor at index 0.00.
Partition after merging: start_index=0.00, width=10.00, height=6.00
No suitable rectangle found for partition at index 6.00. Adjusting partition...
Partition adjusted: start_index=6.00,, height=6.00
Merging with left neighbor at index 0.00.
Partition after merging: start_index=0.00, width=10.00, height=6.00
Partition adjusted: start_index=6.00,, height=6.00
Merging with left neighbor at index 0.00.
Partition after merging: start_index=0.00, width=10.00, height=6.00
Partition after merging: start_index=0.00, width=10.00, height=6.00
```

- 1. 观察过程输出,发现主函数部分正常执行,包括最适矩形的寻找,插入后分区的更新、合并等操作,且最终输出合理。
- 2. 后续将直接展示 conclusion 部分。

• 输入合法性测试

input:

```
5
3
3 4
5 6
7 8
```

output:

```
Error: Invalid rectangle size! Width must be >0 and <= container width, height must be >0
```

输入的矩形宽度大于容器宽度,无法正确插入,程序报错中止。

• 非整型输入测试

input:

```
5.5
3
2.5 3.9
4 6
1.8 4.5
```

```
Extracted partition: start_index=0.00, width=5.50, height=0.00
Selected partition: start_index=0.00, width=5.50, height=0.00
Placing rectangle: width=4.00, height=6.00 in partition at index 0.00
New partition created: start_index=4.00, width=1.50, height=0.00
Remaining rectangles to place: 2
partition 0's height is 0.00
partition 1's height is 6.00
Extracted partition: start_index=4.00, width=1.50, height=0.00
Selected partition: start_index=4.00, width=1.50, height=0.00
No suitable rectangle found for partition at index 4.00. Adjusting partition...
Partition adjusted: start_index=4.00,, height=6.00
Merging with left neighbor at index 0.00.
Partition after merging: start_index=0.00, width=5.50, height=6.00
partition 0's height is 6.00
Extracted partition: start_index=0.00, width=5.50, height=6.00
Selected partition: start_index=0.00, width=5.50, height=6.00
Placing rectangle: width=2.50, height=3.90 in partition at index 0.00
New partition created: start_index=2.50, width=3.00, height=6.00
Remaining rectangles to place: 1
partition 0's height is 6.00
partition 1's height is 9.90
Extracted partition: start_index=2.50, width=3.00, height=6.00
Selected partition: start_index=2.50, width=3.00, height=6.00
Placing rectangle: width=1.80, height=4.50 in partition at index 2.50
New partition created: start_index=4.30, width=1.20, height=6.00
Remaining rectangles to place: 0
partition 0's height is 6.00
partition 1's height is 9.90
partition 2's height is 10.50
----- Conclusion -----
Approximation ratio: 137.9928%
Final height dealing with 3 rectangles by Partition packing algorithm:10.50
```

可以正常处理浮点型的数据。

• 最大输入测试

input: (file: size_10000.txt)

```
50
10000
...
```

output:

Approximation ratio: 100.2564%

- Final height dealing with 10000 rectangles by Partition_heap packing algorithm: 28023.00

3.1.2 高度差异对比测试

测试目的: 检查高度范围对近似比的影响

容器宽度固定为 10, 小矩形的宽度范围为 1~10, 不同矩形高度范围下的 Approximation Ratio:

| 矩形高度 | 10 | 100 | 1000 | 10000 |
|------|-----------|-----------|-----------|-----------|
| 较高 | 113.7500% | 104.1260% | 102.2160% | 100.5645% |
| 较低 | 115.3846% | 105.9524% | 102.4718% | 100.5248% |

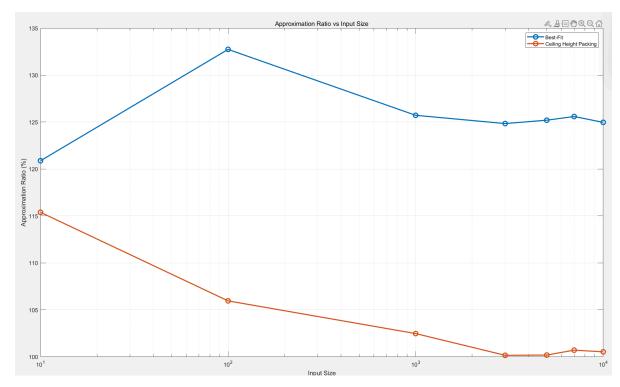
- 1. 较高的范围为 1~50, 较低矩形的高度范围为 1~5.
- 2. 由实验结果可见,高度差异对近似比的影响较小。但同时当前输入的设置整体有关,从而导致差异不明显。

3.1.3 与 Best Fit 的算法对比

测试目的: 与现有的 strip 算法进行比较

用上述的 short 类文件作为输入,不同规模输入下的,二者算法的"近似比":

| 算法 / 输入规模 | 10 | 100 | 1000 | 3000 | 5000 | 7000 | 10000 |
|------------------------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| Best-Fit | 120.88% | 132.74% | 125.72% | 124.84% | 125.20% | 125.59% | 124.97% |
| Ceiling_height packing | 115.3846% | 105.9524% | 102.4718% | 100.1554% | 100.1825% | 100.7064% | 100.5248% |



- 1. best-fit 算法将输入的矩形按照高度排序,优先处理较高的小矩形;每次将对应的矩形插入到最合适的位置(具有最小剩余宽度且能够安放的区间),直至不存在没有插入的矩形;
- 2. best-fit 的算法与我们的程序差别在于,前者按照矩形高度进行处理,后者根据当前的容器情况 选取最合适宽度的矩形进行处理,具有动态和贪心的特征;

3.2 测试结果分析

- 1. 3.1.1 的正确性测试表明,对于正常的输入、边界输入以及非法输入,我们的程序都能够分别给出期望的正确输出;
- 2. 3.1.2 中,我们对于不同规模的输入分别测试了高度较高和较低的矩形输入(对应宽度保持一致),结果的近似比数据显示:高度较高的矩形,其对应结果的近似比往往较低与高度较低的矩形输入组;
- 3. [3.1.3],我们对比了我们的算法与 Best-Fit 算法,发现:
 - 1. 不同规模下, Best-Fit 返回结果的"近似比"(空间利用率)总是高于我们的算法;
 - 2. Partition_heap packing 算法的"近似比"随着输入规模的增大呈现明显的下降趋势,逐渐趋近于1。 这是因为,该算法总是从分区堆中提取最小高度的分区,然后从BST当中寻找最为合适的矩形。输入规模的扩大意味着每次选取最佳矩形的机会增加,因此越来越接近于最优解。

Chapter 4: Analysis and Comments

4.1 时间复杂度分析

• BST构建阶段:

对n个矩形进行BST插入,每次插入为O(log n),总共需要n次插入操作;

这一阶段的复杂度为O(n log n)

• 装箱循环阶段:

while 循环执行 n 次 (n 为小矩形的个数) , 在每次循环中: (w 为容器的宽度)

```
- extractMinPartition(): O(log W) //从堆中提取最小分区,需要heapifyDown且分区数目最多为容器宽度;
- findLargestFit(): O(log n) //在 BST 中查找最佳矩形,最多有n个节点,下同 - deleteNode(): O(log n) //从 BST 中删除节点
- insertPartition():O(log W) //将分区插入堆中
- combinePartitions(): O(log W) //如果需要合并,维护堆的性质所需的时间为O(log W) - heapifyUp()/heapifyDown(): O(log W) //调整堆
- 每次循环的复杂度为 O(log n + log W)
- 总循环复杂度为 O(n * (log n + log W))
```

因此,**总体时间复杂度**为: $O(n \cdot (\log n + \log W))$.

当容器宽度 w 远大于 n 时,时间复杂度为 $O(n \cdot \log W)$,为多项式时间复杂度。

4.2 空间复杂度分析

1. 分区堆 MinHeap: 最多存在 W 个分区(分区的宽度均为1时),所以为O(W);

2. 二叉搜索树 BST: 存储输入的 n 个矩形, 所以为O(n);

3. 读取时设置的矩形数组: O(n);

4. 其他辅助变量: O(1)

因此, 总体空间复杂度为: O(W+n).

4.3 算法评价与近似比分析

评价

- 1. 由时间复杂度分析可知,该算法的时间复杂度与容器宽度 w 相关,当 w 显著大于 n 时,算法的时间复杂度主要与 w 相关。
- 2. 算法的"近似比"随着 n 的输入规模的增大趋近于 1,具有显著优于 Best-Fit 的表现。
- 3. 实际中,算法的近似比率会受到矩形的大小和排列方式的影响。

近似比影响因素分析

• 矩形数量

当小矩形的数量 n 增大时,意味着每次选择最佳矩形进行插入的空间增大,更有利于"完美插入",此时近似比越低,即 ρ 与 n 呈负相关;

• 矩形宽度

记小矩形的宽度 w_i 与容器宽度 W 的比值 w_i /W为 α ;

当 α 减小时,对于相同规模 n 的输入,更有机会寻找到矩形完成"完美插入",因此此时近似比降低,即 ρ 与 α 呈正相关;

• 矩形高度

记小矩形 r_i 的高度为 h_i ,根据 3.1.2 的测试结果可知,在其他条件不变的情况下,矩形的 h_i 较大时,"近似比"有轻微的优势,但是差异不大;

因此, 记所有矩形的高度期望值为 E_h , 我们猜测 ρ 可能与 E_h 呈负相关;

• 贪心逻辑

由于在该算法当中,总是选取**第一个**最低分区,然后选取**第一个**最适矩形。这可能导致实际上存在 多个最适矩形,且高度不同的情况下,我们的算法无法实现局部最优的贪心。

这也是导致我们算法在处理较大规模输入时,与实际最优情况存在偏差的原因。

Appendix

Source Code

Partition_heap.h

```
#include <stdio.h>
#include <stdlib.h>
#include <stdbool.h>
#include <limits.h>
#include "Rectangle_BST.h"
#define Element_type float
// Part 2: Partition Structure and Min-Heap Operations
typedef struct Partition {
   Element_type start_index; // Starting x-coordinate
   Element_type width; // Width of the partition
                          // Current height
   Element_type height;
   struct Partition *left; // Pointer to left neighbor
   struct Partition *right; // Pointer to right neighbor
   Element_type heap_index; // Current index in the heap
} Partition;
// Min-heap structure for partitions
typedef struct {
   Partition **heap; // Array of partitions
   int size;
                   // Current size of the heap
   int capacity; // Maximum capacity
   Element_type max_height; // max_height of all partitions
} MinHeap;
// Create a new partition
Partition* createPartition(Element_type start_index, Element_type width,
Element_type height) {
   Partition *part = (Partition*)malloc(sizeof(Partition));
   if (part == NULL) {
       fprintf(stderr, "Memory allocation failed!\n");
       exit(1);
   }
   part->start_index = start_index;
   part->width = width;
   part->height = height;
   part->left = NULL;
   part->right = NULL;
   part->heap_index = -1; // Initial value
   return part;
}
```

```
// Initialize the min-heap for partitions
MinHeap* initialize_partition_heap(Element_type containerWidth) {
    MinHeap *heap = (MinHeap*)malloc(sizeof(MinHeap));
    if (heap == NULL) {
        fprintf(stderr, "Memory allocation failed!\n");
        exit(1);
    }
    heap->heap = (Partition**)malloc(sizeof(Partition*) * 1000); // Initial
capacity
    if (heap->heap == NULL) {
        fprintf(stderr, "Memory allocation failed!\n");
        exit(1);
    }
    heap->size = 0;
    heap->capacity = 1000;
    heap->max_height = 0;  //set max_height to 0 initially
    // Create initial partition covering the entire width
    Partition *initial = createPartition(0, containerWidth, 0);
    initial->heap_index = heap->size;
    heap->heap[heap->size++] = initial;
    return heap;
}
// Heapify up to maintain min-heap property
void heapifyUp(MinHeap *heap, int index) {
    while (index > 0) {
        // Find parent index
        int parent = (index - 1) / 2;
        if (heap->heap[index]->height < heap->heap[parent]->height) {
            // Swap partitions
            Partition *temp = heap->heap[index];
            heap->heap[index] = heap->heap[parent];
            heap->heap[parent] = temp;
            // Update heap_index
            heap->heap[index]->heap_index = index;
            heap->heap[parent]->heap_index = parent;
            index = parent;
        } else {
            break;
        }
    }
}
// Heapify down to maintain min-heap property
void heapifyDown(MinHeap *heap, int index) {
    int smallest = index;
    // Find smallest child index
   int left = 2 * index + 1;
    int right = 2 * index + 2;
    if (left < heap->size & heap->heap[left]->height < heap->heap[smallest]-
>height)
```

```
smallest = left;
    if (right < heap->size && heap->heap[right]->height < heap->heap[smallest]-
>height)
        smallest = right;
    // If smallest is not the current index
    if (smallest != index) {
        // Swap partitions
        Partition *temp = heap->heap[index];
        heap->heap[index] = heap->heap[smallest];
        heap->heap[smallest] = temp;
        // Update heap_index
        heap->heap[index]->heap_index = index;
        heap->heap[smallest]->heap_index = smallest;
        heapifyDown(heap, smallest);
    }
}
// Insert a new partition into the min-heap
void insertPartition(MinHeap *heap, Partition *part) {
    // Update max_height if necessary
    if(part->height > heap->max_height)
        heap->max_height = part->height;
    // Resize the heap if necessary
    if (heap->size == heap->capacity) {
        heap->capacity *= 2;
        Partition **temp = (Partition**)realloc(heap->heap, sizeof(Partition*) *
heap->capacity);
        if (temp == NULL) {
            fprintf(stderr, "Memory allocation failed during realloc!\n");
            exit(1);
        heap->heap = temp;
    }
    // Insert the partition into the heap
    int i = heap->size;
    heap->heap[i] = part;
    part->heap_index = i;
    heap->size += 1;
    heapifyUp(heap, i); // Maintain min-heap property
}
// Extract the partition with the smallest height and remove it from the heap
Partition* extractMinPartition(MinHeap *heap) {
    if (heap->size == 0) return NULL;
    Partition *min = heap->heap[0];
    heap->heap[0] = heap->heap[heap->size - 1]; // Replace root with last element
    heap \rightarrow heap[0] \rightarrow heap\_index = 0;
    heap->size--;
    heapifyDown(heap, 0); // Maintain min-heap property
```

```
printf("\nExtracted partition: start_index=%.2f, width=%.2f, height=%.2f\n",
        (float)min->start_index,(float) min->width, (float)min->height);
    return min;
}
// Remove a specified partition from the heap
void removePartition(MinHeap *heap, Partition *part) {
    int index = part->heap_index; // Get the index of the partition in the heap
    if (index >= heap->size || index < 0) return; // Invalid index</pre>
    // Replace with the last partition
    heap->heap[index] = heap->heap[heap->size - 1];
    heap->heap[index]->heap_index = index;
    heap->size--;
    // Adjust heap to maintain min-heap property
    heapifyDown(heap, index);
    heapifyUp(heap, index);
}
// Combine the current partition with its left and/or right neighbors if heights
void combinePartitions(MinHeap *heap, Partition *part) {
    bool merged = false;
    // Check and merge with left neighbor
    if (part->left != NULL && part->left->height == part->height) {
        printf("Merging with left neighbor at index %.2f.\n", (float)part->left-
>start_index);
        // Update current partition's start_index and width
        part->start_index = part->left->start_index;
        part->width += part->left->width;
        // Remove the left neighbor from the heap
        removePartition(heap, part->left);
        // Update the left pointer
        part->left = part->left->left;
        if (part->left != NULL) {
            part->left->right = part;
        }
        merged = true;
    }
    // Check and merge with right neighbor
    if (part->right != NULL && part->right->height == part->height) {
        printf("Merging with right neighbor at index %f.\n", (float)part->right-
>start_index);
        // Update current partition's width
        part->width += part->right->width;
        // Remove the right neighbor from the heap
        removePartition(heap, part->right);
```

```
// Update the right pointer
       part->right = part->right->right;
       if (part->right != NULL) {
           part->right->left = part;
       merged = true;
   }
   if (merged) {
       // Reinsert the updated partition into the heap to maintain heap
properties
       heapifyUp(heap, part->heap_index);
       heapifyDown(heap, part->heap_index);
       printf("Partition after merging: start_index=%.2f, width=%.2f,
height=%.2f\n'',
              (float)part->start_index, (float)part->width, (float)part-
>height);
   }
}
// Part 3: Main Packing Algorithm and Integration
// Clean up the entire heap
void cleanupHeap(MinHeap *heap) {
   for(int i = 0; i < heap->size; i++) {
       free(heap->heap[i]);
   }
   free(heap->heap);
   free(heap);
}
// Main packing algorithm using partitions and BST
Element_type partitionPacking(Rectangle *rectangles, int n, Element_type
containerWidth) {
   MinHeap *heap = initialize_partition_heap(containerWidth);
   Element_type area_sum = 0; // Calculate the sum of all areas
   TreeNode* root = NULL;
   for (int i = 0; i < n; i++) {
       root = insertBST(root, rectangles[i]);
       area_sum += rectangles[i].width * rectangles[i].height;
   }
   int remainingRects = n; // Remaining rectangles to place
   while (remainingRects > 0) {
       Partition *part = extractMinPartition(heap); // Get the partition with
the smallest height
       if (part == NULL) break;
       printf("\nSelected partition: start_index=%.2f, width=%.2f,
height=%.2f\n'',
```

```
(float)part->start_index, (float)part->width, (float)part-
>height);
        TreeNode* bestFit = findLargestFit(root, part->width); // Find the
largest rectangle that fits in the partition
        if (bestFit != NULL) {
            Rectangle bestRect = bestFit->rect;
            printf("Placing rectangle: width=%.2f, height=%.2f in partition at
index %.2f\n",
                   (float)bestRect.width, (float)bestRect.height, (float)part-
>start_index);
            // Place the rectangle
            if (bestRect.width < part->width) {
                // Split the partition into two parts
                Partition *newPart = createPartition(part->start_index +
bestRect.width, part->width - bestRect.width, part->height);
                // Update the left and right pointers of the current partition
and the new partition
                newPart->left = part;
                newPart->right = part->right;
                if (part->right != NULL) {
                    part->right->left = newPart;
                }
                part->right = newPart;
                // Insert the new partition into the heap
                insertPartition(heap, newPart);
                printf("New partition created: start_index=%.2f, width=%.2f,
height=%.2f\n",
                    (float)newPart->start_index, (float)newPart->width,
(float)newPart->height);
            // Update the partition's height and width
            part->height += bestRect.height;
            part->width = bestRect.width;
            // Insert the updated partition into the heap
            insertPartition(heap, part);
            // Remove the rectangle from the BST
            root = deleteNode(root, bestRect);
            remainingRects--;
            printf("Remaining rectangles to place: %d\n", remainingRects);
        } else {
            // No suitable rectangle found for the partition. Adjust the
partition's height.
            printf("No suitable rectangle found for partition at index %.2f.
Adjusting partition...\n", (float)part->start_index);
            Element_type slow_height = part->height;
```

```
//find the slowest height of the partition's left and right subtrees
           if(!part->left)
               slow_height = part->right->height;
           else if(!part->right){
               slow_height = part->left->height;
           }
           else{
               slow_height = part->left->height < part->right->height ?
                   part->left->height : part->right->height;
           //adjust the partition's height to the slowest height of its left and
right subtrees
           part->height = slow_height;
           printf("Partition adjusted: start_index=%.2f,, height=%.2f\n",
               (float)part->start_index, (float)part->height);
           insertPartition(heap, part); // Reinsert the updated partition into
the heap
       }
       // Combine the current partition with its left and/or right neighbors if
heights match
       combinePartitions(heap, part);
       for(int i = 0; i < heap->size; i++)
           printf("partition %d's height is %.2f\n", i, (float)heap->heap[i]-
>height);
    }
    //get the final height of the container
    Element_type finalHeight = heap->max_height;
   printf("\n-----\n");
    // printf("Final container height: %d\n", finalHeight);
    // printf("Total area of rectangles: %d\n", area_sum);
    printf("Approximation ratio: %.4f%%\n", (float)finalHeight / (area_sum /
(float)containerWidth) * 100);
    // Clean up the heap and BST
    cleanupBST(root);
    cleanupHeap(heap);
    return finalHeight; // Final height of the container
}
```

Rectangle_BST.h

```
#include <stdio.h>
#include <stdlib.h>
#include <stdbool.h>
#include <limits.h>

#define Element_type float
```

```
// Part 1: Rectangle Structure and BST Operations
typedef struct {
   Element_type width;
   Element_type height;
} Rectangle;
// BST node structure
typedef struct TreeNode {
   Rectangle rect;
   struct TreeNode *left;
   struct TreeNode *right;
} TreeNode;
// Create a new BST node
TreeNode* createNode(Rectangle rect) {
   TreeNode* node = (TreeNode*)malloc(sizeof(TreeNode));
   if (node == NULL) {
       fprintf(stderr, "Memory allocation failed!\n");
       exit(1);
   }
   node->rect = rect;
   node->left = node->right = NULL;
   return node;
}
// Insert a rectangle into the BST (sorted by width)
TreeNode* insertBST(TreeNode* root, Rectangle rect) {
   if (root == NULL) {
       return createNode(rect);
   if (rect.width < root->rect.width) {
       root->left = insertBST(root->left, rect);
   } else {
       root->right = insertBST(root->right, rect);
   return root;
}
// Find the largest rectangle that fits within the given width
TreeNode* findLargestFit(TreeNode* root, Element_type targetWidth) {
   if (root == NULL) return NULL;
   TreeNode* result = NULL;
   if (root->rect.width > targetWidth) {
       result = findLargestFit(root->left, targetWidth);
   } else {
       result = root;
       TreeNode* rightResult = findLargestFit(root->right, targetWidth);
       if (rightResult != NULL && rightResult->rect.width > result->rect.width)
{
           result = rightResult;
```

```
}
    return result;
}
// Delete a specified rectangle from the BST
TreeNode* deleteNode(TreeNode* root, Rectangle rect) {
    if (root == NULL) return NULL;
   if (rect.width < root->rect.width) {
        root->left = deleteNode(root->left, rect);
    } else if (rect.width > root->rect.width) {
        root->right = deleteNode(root->right, rect);
    } else {
        // Node found
        if (root->left == NULL) {
            TreeNode* temp = root->right;
            free(root);
            return temp;
        }
        if (root->right == NULL) {
            TreeNode* temp = root->left;
            free(root);
            return temp;
        }
        // Node with two children: Get the inorder successor (smallest in the
right subtree)
        TreeNode* successor = root->right;
        while (successor->left != NULL) {
            successor = successor->left;
        }
        root->rect = successor->rect;
        root->right = deleteNode(root->right, successor->rect);
    return root;
}
// Clean up the entire BST
void cleanupBST(TreeNode* root) {
    if (root != NULL) {
        cleanupBST(root->left);
        cleanupBST(root->right);
        free(root);
    }
}
```

file_input.c

```
#include "Partition_heap.h"
#include <stdio.h>
#include <stdlib.h>

#define Element_type float // Change Element_type to int if you want to use
integer input
```

```
#ifdef Element_type
    #if Element_type == float
        #define ELEMENT_TYPE_FLOAT
    #else
        #define ELEMENT_TYPE_INT
    #endif
#endif
int main() {
    FILE *fp;
    Element_type containerWidth; // Maximum width of the container
    int n; // Number of rectangles
    fp = fopen("Generate_input/size_100_short.txt", "r"); // Open input file,
please change the file name to your own
    if (fp == NULL) {
        printf("Error: Cannot open input file\n");
        return 1;
    }
    // Read the container width and number of rectangles from the input file
    #ifdef ELEMENT_TYPE_FLOAT
        fscanf(fp, "%f", &containerwidth);
    #else
        fscanf(fp, "%d", &containerWidth);
    #endif
    fscanf(fp, "%d", &n);
    Rectangle* rectangles = (Rectangle*)malloc(n * sizeof(Rectangle));
    if (rectangles == NULL) {
        fprintf(stderr, "Memory allocation failed!\n");
        fclose(fp);
        return 1;
    }
    for (int i = 0; i < n; i++) {
       #ifdef ELEMENT_TYPE_FLOAT
        fscanf(fp, "%f %f", &rectangles[i].width, &rectangles[i].height);
        #else
            fscanf(fp, "%d %d", &rectangles[i].width, &rectangles[i].height);
        #endif
        //check if the rectangle size is valid
        if (rectangles[i].width <= 0 || rectangles[i].height <= 0 ||</pre>
            rectangles[i].width > containerWidth) {
            printf("Error: Invalid rectangle size! Width must be > 0 and <=</pre>
container width, height must be > 0\n");
            free(rectangles);
            fclose(fp);
            return 1;
        }
    }
```

```
fclose(fp);

float finalHeight = partitionPacking(rectangles, n, containerwidth); // Call
the packing function

printf("- Final height dealing with %d rectangles by Partition_heap packing
algorithm: %.2f\n", n, finalHeight);

free(rectangles);
return 0;
}
```

manual_input.c

```
#include "Partition_heap.h"
#include <stdio.h>
#include <stdlib.h>
#define Element_type float
#ifdef Element_type
    #if Element_type == float
        #define ELEMENT_TYPE_FLOAT
    #else
        #define ELEMENT_TYPE_INT
    #endif
#endif
int main() {
    Element_type containerWidth; //maximum width of the container
    int n; //number of rectangles
    printf("Enter container width: ");
    // Read container width
    #ifdef ELEMENT_TYPE_FLOAT
        scanf("%f", &containerWidth);
    #else
    scanf("%d", &containerWidth);
    #endif
    printf("Enter number of rectangles: ");
    scanf("%d", &n);
    Rectangle* rectangles = (Rectangle*)malloc(n * sizeof(Rectangle));
    if (rectangles == NULL) {
        fprintf(stderr, "Memory allocation failed!\n");
        return 1;
    }
    // Read input rectangles
    for (int i = 0; i < n; i++) {
```

```
printf("Enter width and height for rectangle %d (format: width height):
", i + 1);
        #ifdef ELEMENT_TYPE_FLOAT
            scanf("%f %f", &rectangles[i].width, &rectangles[i].height);
        scanf("%d %d", &rectangles[i].width, &rectangles[i].height);
        #endif
        // Check for invalid input
        if (rectangles[i].width <= 0 || rectangles[i].height <= 0 ||</pre>
            rectangles[i].width > containerWidth) {
            printf("Error: Invalid rectangle size! Width must be > 0 and <=</pre>
container width, height must be > 0 \n");
            free(rectangles);
            return 1;
        }
   }
   Element_type finalHeight = partitionPacking(rectangles, n, containerWidth); //
Pack rectangles into container
    printf("Final height dealing with %d rectangles by Partition packing
algorithm:%.2f\n", n,(float)finalHeight);
    free(rectangles); // Free memory
    return 0;
}
```

correctness_test.c

Generator.c

```
#include <stdio.h>
#include <stdlib.h>
#include <time.h>
// Define the maximum container width and number of rectangles
#define CONTAINER_WIDTH 10
#define NUMBER 7000
// Function to generate random integers within range [min, max]
int random_int(int min, int max) {
    return min + rand() % (max - min + 1);
int main() {
   // Set random seed
    srand((unsigned int)time(NULL));
    // Open the output files for short and high
    FILE *fileShort = fopen("size_7000_short.txt", "w");
    FILE *fileHigh = fopen("size_7000_high.txt", "w");
    if (fileShort == NULL || fileHigh == NULL) {
        printf("Failed to create one or both of the files!\n");
        return 1;
    }
    // Write container_width and number to both files
    fprintf(fileShort, "%d\n", CONTAINER_WIDTH);
    fprintf(fileShort, "%d\n", NUMBER);
    fprintf(fileHigh, "%d\n", CONTAINER_WIDTH);
    fprintf(fileHigh, "%d\n", NUMBER);
    // Generate rectangle data for both files
    for (int i = 0; i < NUMBER; i++) {
        int width = random_int(1, CONTAINER_WIDTH); // Ensure width does not
exceed CONTAINER_WIDTH
        int shortHeight = random_int(1, 5);  // Short height is within
range [1, 5]
        int highHeight = random_int(1, 50);
        // Write data to the short file
        fprintf(fileShort, "%d %d\n", width, shortHeight);
        // Write data to the high file (height is independently random within
[shortHeight*10, shortHeight*10 + 9])
        fprintf(fileHigh, "%d %d\n", width, highHeight);
    }
    // Close the files
    fclose(fileShort);
    fclose(fileHigh);
```

```
printf("Data has been generated for both short and high files\n");
return 0;
}
```

best_fit.c

```
#include <stdio.h>
#include <stdlib.h>
#include <stdbool.h>
#include <limits.h>
#define MAX_WIDTH 1000
typedef struct {
   int width;
    int height;
} Rectangle;
typedef struct {
    int x;
              // x coordinate
    int height; // current height at this x coordinate
} Position;
// Compare rectangles by height in descending order
int compareRectangles(const void *a, const void *b) {
    Rectangle *rectA = (Rectangle *)a;
    Rectangle *rectB = (Rectangle *)b;
    return rectB->height - rectA->height;
}
// Find the position with minimum height that can fit the current rectangle
int findBestFit(Position *positions, int containerWidth, int rectWidth, int
*minX) {
   int minHeight = INT_MAX;
    int bestX = -1;
    // Try each possible x position
    for (int x = 0; x \leftarrow containerwidth - rectwidth; <math>x++) {
        // Find maximum height in the range [x, x+width-1]
        int maxHeight = 0;
        bool canFit = true;
        for (int i = x; i < x + rectWidth; i++) {
            if (positions[i].height > maxHeight) {
                maxHeight = positions[i].height;
            }
        }
        // If this position has the lowest height so far, update best position
        if (maxHeight < minHeight) {</pre>
            minHeight = maxHeight;
            bestX = x;
        }
```

```
*minX = bestX;
    return minHeight;
}
int bestFitPacking(Rectangle *rectangles, int n, int containerWidth) {
    qsort(rectangles, n, sizeof(Rectangle), compareRectangles);
    // Initialize positions array to track height at each x coordinate
    Position *positions = (Position *)calloc(containerWidth, sizeof(Position));
    for (int i = 0; i < containerWidth; i++) {
       positions[i].x = i;
       positions[i].height = 0;
    }
    float area_sum = 0;
    int totalHeight = 0;
   // Place each rectangle
    for (int i = 0; i < n; i++) {
       Rectangle currentRect = rectangles[i];
        int bestx:
       int baseHeight = findBestFit(positions, containerWidth,
currentRect.width, &bestX);
       if (bestX != -1) {
           // Update heights for the width of the rectangle
           int newHeight = baseHeight + currentRect.height;
           for (int x = bestX; x < bestX + currentRect.width; x++) {</pre>
               positions[x].height = newHeight;
           }
           // Update total height if necessary
           if (newHeight > totalHeight) {
               totalHeight = newHeight;
           }
       }
       area_sum += currentRect.width * currentRect.height;
    }
    // Calculate and output metrics
    float optimal_height = area_sum / containerwidth;
    float ratio = totalHeight / optimal_height * 100;
    printf("\nOptimal height (area/width): %.2f\n", optimal_height);
    printf("Actual container height: %d\n", totalHeight);
    printf("Total rectangle area: %.2f\n", area_sum);
    printf("Approximation Ratio for Best Fit packing: %.2f%\\n", ratio);
    printf("\n-----\n");
    free(positions);
    return totalHeight;
```

```
int main() {
    FILE *fp;
    int containerWidth; // Maximum width of the container
    int n; // Number of rectangles
    fp = fopen("../Generate_input/size_7000_short.txt", "r"); // Open input file,
please change the file name to your own
    if (fp == NULL) {
        printf("Error: Cannot open input file\n");
        return 1;
    }
    fscanf(fp, "%d", &containerWidth);
    fscanf(fp, "%d", &n);
    Rectangle* rectangles = (Rectangle*)malloc(n * sizeof(Rectangle));
    if (rectangles == NULL) {
        fprintf(stderr, "Memory allocation failed!\n");
        fclose(fp);
        return 1;
    }
    for (int i = 0; i < n; i++) {
        fscanf(fp, "%d %d", &rectangles[i].width, &rectangles[i].height);
        // Check if the rectangle size is valid
        if (rectangles[i].width <= 0 || rectangles[i].height <= 0 ||</pre>
            rectangles[i].width > containerWidth) {
            printf("Error: Invalid rectangle size! Width must be > 0 and <=</pre>
container width, height must be > 0\n");
            free(rectangles);
            fclose(fp);
            return 1;
        }
    }
    fclose(fp);
   // Call the Best Fit packing function
    int finalHeight = bestFitPacking(rectangles, n, containerWidth);
    printf("\nFinal container height with Best Fit packing: %d\n", finalHeight);
    // Free the allocated memory for rectangles
    free(rectangles);
    return 0;
}
```

具体的关系请参见 README

References

Author List

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Declaration

We hereby declare that all the work done in this project titled "**Texture Packing**" is of our independent effort as a group.