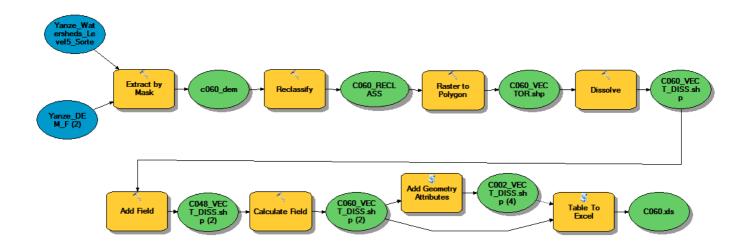
Hypsometric Curves and Integrals of Yanze Sub-Catchments

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I. Overview

In order to simplify the process of generating data required to draw an hypsometric curve of each sub-catchment in Yanze watershed, an ArcMap model was developed to perform the five steps involved in this process in one go. These steps are: 1) extract the DEM of the sub-catchment, 2) reclassify the DEM into classes of equidistant elevation height, 3) convert the reclassified DEM to vector using the 'Value' field, 4) dissolve the features using the 'Value' field, 5) calculate the area of each polygon, 6) export the table to a text file.



ArcGIS Hypsometric Integral Model

The present report outlines the results of this process. For each of the 93 sub-catchments of Yanze watershed, we will import the text file generated from ArcMap and process it to generate the hypsometric curve and integral for the sub-catchment.

II. Used R Packages

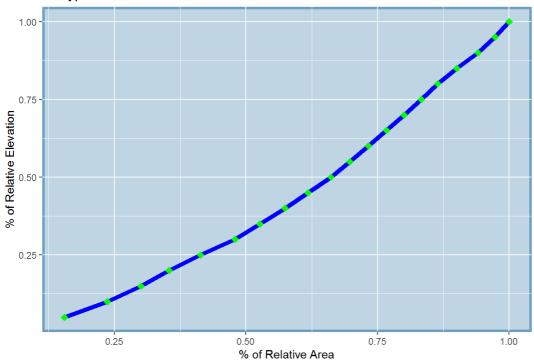
In addition to the core R libraries, the following are the packages that we will be using to generate hypsometric curves and integrals for Yanze sub-catchments:

```
library(dplyr) # For preprocessing data
library(ggplot2) # For drawing the hypsometric curve
library(sjPlot) # For producing the coefficient table of the fitted model
library(PolynomF) # For building a polynomial equation of the model and integrating it
library(knitr)
```

III. Results Per Sub-Catchment

The text file exported from ArcMap will be imported into R for processing. First, the unnecessary variables will be deleted and only the elevation intervals and corresponding areas will remain. Secondly, the data will be normalized (for elevation, we first substract the minimum elevation and then divide by the range. For area, we divide each entry by the total area of the sub-catchment). Thirdly, we plot the data on a 2D chart showing the curve drawn from the normalized data. Finally, we fit a 3rd degree polynomial equation to the data and integrate it within the limits of 0 and 1 to produce the hypsometric integral metric of the sub-catchment.

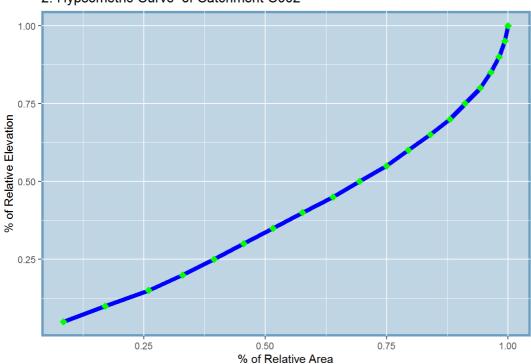
```
watersheds <- 1:60
min max <- read.csv("Minimum-Maximum.csv", header = TRUE)</pre>
all_data <- list()
for (i in watersheds) {
   if (i < 10)
      n <- paste("C00", i, sep = "")</pre>
      n <- paste("CO", i, sep = "")</pre>
# Read in the data and preprocess it
minimum <- min max$minimum[i]</pre>
maximum <- min_max$maximum[i]</pre>
file <- paste(n, ".csv", sep = "")
data <- read.csv(file)</pre>
data <- data %>% select(ELEV, AREA_GEO)
data <- mutate(data, ELEV_NORM = (ELEV - minimum)/(maximum - minimum))</pre>
data <- mutate(data, AREA_NORM = cumsum(AREA_GEO)/sum(AREA_GEO))</pre>
# Build the Hypsometric curve object
g <- ggplot(data = data, aes(x = AREA NORM, y = ELEV NORM))
g <- g + geom_line(color = "blue", size = 2)</pre>
g <- g + geom_point(color = "green", size = 3, shape = 18)
g \leftarrow g + labs(title = paste(i, ". Hypsometric Curve" of Catchment ", n, sep = ""), x = "% of Relative Area"
, y = "% of Relative Elevation")
g <- g + theme(panel.background = element_rect(fill = "#BFD5E3", colour = "#6D9EC1", size = 2, linetype = "s
olid"), panel.grid.major = element line(size = 0.5, linetype = 'solid',colour = "white"), panel.grid.minor
= element_line(size = 0.25, linetype = 'solid', colour = "white"))
# Determine the Hypsometric Integral
# First, let's define a polynomial equation that fits the curve
fit = lm(ELEV_NORM ~ poly(AREA_NORM, 3), data = data)
# Second, we display the coefficients of the fitted equation in a well-formatted table
# If the p-values of any of them is too high or the R-squared value is too low, then a better model will nee
d to be fitted
coef_table <- tab_model(fit)</pre>
# Finally, we build the polynomial equation and calculate the integral
x <- polynom()
p = summary(fit) $coefficients[2,1] * x + summary(fit)$coefficients[3,1] * x^2 + summary(fit)$coefficients[4,1] * x + s
,1] * x^3
HI \leftarrow integral(p, c(0,1))
# Output the results
print(a)
#print(coef table)
print(paste("The polynomial equation of sub-catchment ", n, " is ", p, sep = ""))
print(paste("The hypsometric integral of sub-catchment ", n, " is ", round(HI, 3), sep = ""))
#Build the main data frame
catchment_details <- list("minimum" = minimum, "maximum" = maximum, "data" = data, "equation" = p, "h_integr
al" = HI)
all data[[n]] <- catchment details</pre>
```



[1] "The polynomial equation of sub-catchment C001 is 1.27761218182317*x + 0.171301171778388*x^2 - 0.0051 3597889262782*x^3"

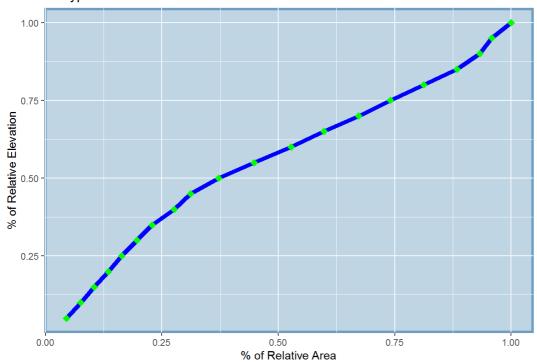
[1] "The hypsometric integral of sub-catchment C001 is 0.695"

2. Hypsometric Curve of Catchment C002



[1] "The polynomial equation of sub-catchment C002 is 1.2629321551127*x + 0.222579470326882*x^2 + 0.0973174654596634*x^3"

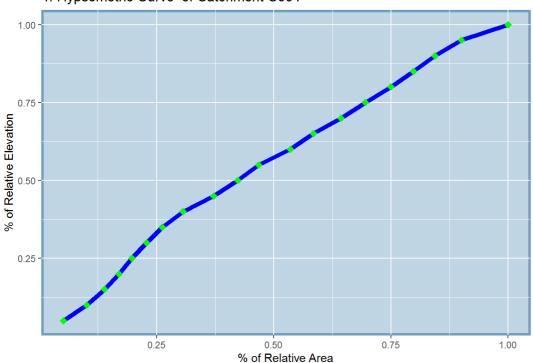
[1] "The hypsometric integral of sub-catchment C002 is 0.73"



[1] "The polynomial equation of sub-catchment C003 is $1.27484986253041*x - 0.135721454620197*x^2 + 0.133895850061023*x^3"$

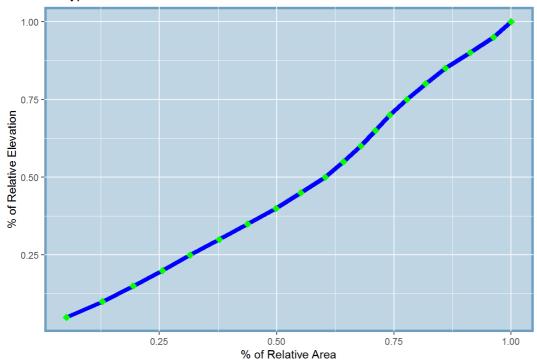
[1] "The hypsometric integral of sub-catchment C003 is 0.626"

4. Hypsometric Curve of Catchment C004



[1] "The polynomial equation of sub-catchment C004 is 1.28304863090052*x - 0.10715647093451*x^2 + 0.037387222937117*x^3"

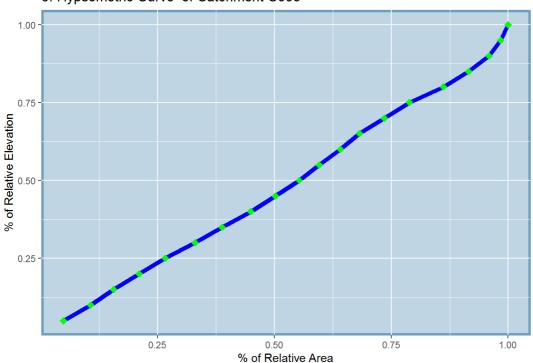
[1] "The hypsometric integral of sub-catchment C004 is 0.615"



[1] "The polynomial equation of sub-catchment C005 is $1.28044618582375*x + 0.136881677669805*x^2 - 0.0238119490422969*x^3"$

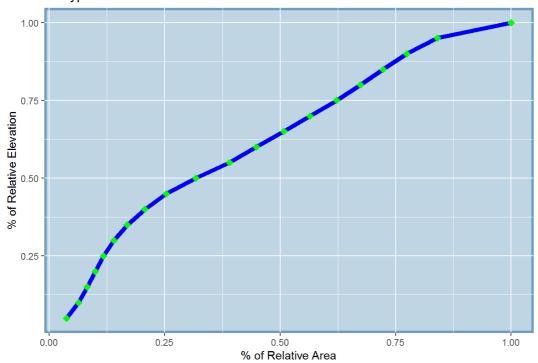
[1] "The hypsometric integral of sub-catchment C005 is 0.68"

6. Hypsometric Curve of Catchment C006



[1] "The polynomial equation of sub-catchment C006 is 1.28716839730947*x + 0.0469243916539962*x^2 + 0.008 1950770262518*x^3"

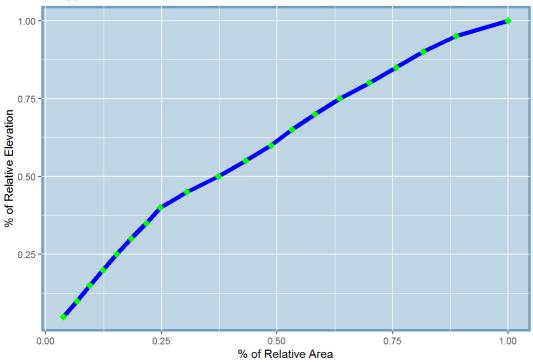
[1] "The hypsometric integral of sub-catchment C006 is 0.661"



[1] "The polynomial equation of sub-catchment C007 is $1.26616631131587*x - 0.193304447107123*x^2 + 0.0816663952397969*x^3"$

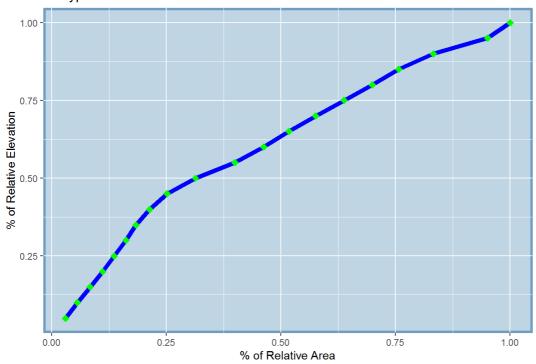
[1] "The hypsometric integral of sub-catchment C007 is 0.589"

8. Hypsometric Curve of Catchment C008



[1] "The polynomial equation of sub-catchment C008 is 1.27629596035856*x - 0.163531874097781*x^2 + 0.0483456547366394*x^3"

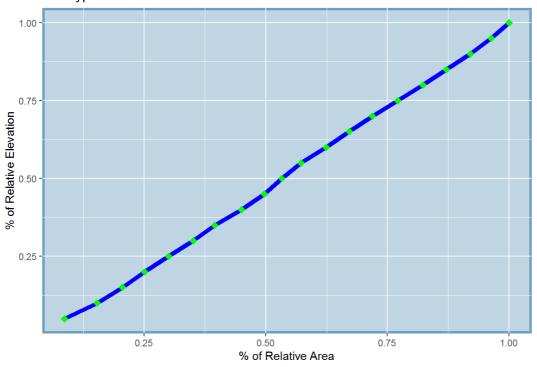
[1] "The hypsometric integral of sub-catchment C008 is 0.596"



[1] "The polynomial equation of sub-catchment C009 is $1.2661381101438*x - 0.206363605916641*x^2 + 0.100411423501086*x^3"$

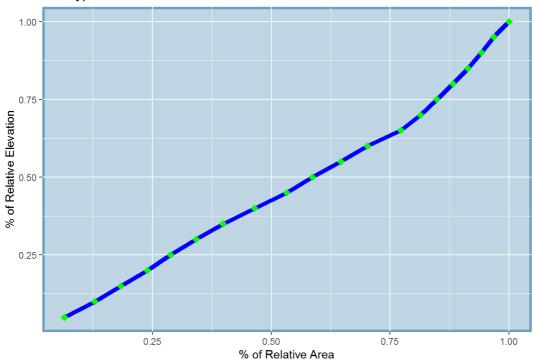
[1] "The hypsometric integral of sub-catchment C009 is 0.589"

10. Hypsometric Curve of Catchment C010



[1] "The polynomial equation of sub-catchment C010 is 1.28891811902337*x + 0.011956467818896*x^2 - 0.0165834789322343*x^3"

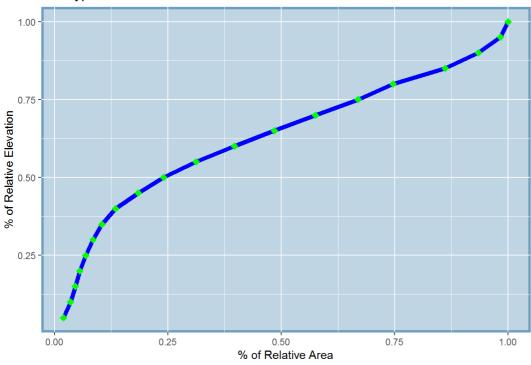
[1] "The hypsometric integral of sub-catchment C010 is 0.644"



[1] "The polynomial equation of sub-catchment C011 is 1.28113825577415*x + 0.106813695532629*x^2 + 0.0884 16263376668*x^3"

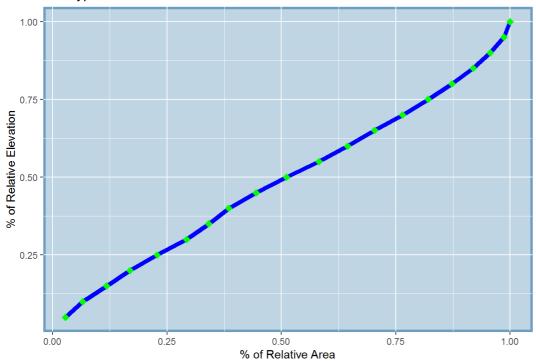
[1] "The hypsometric integral of sub-catchment C011 is 0.698"

12. Hypsometric Curve of Catchment C012



[1] "The polynomial equation of sub-catchment C012 is 1.24359725085384*x - 0.229279885192258*x^2 + 0.213072855393587*x^3"

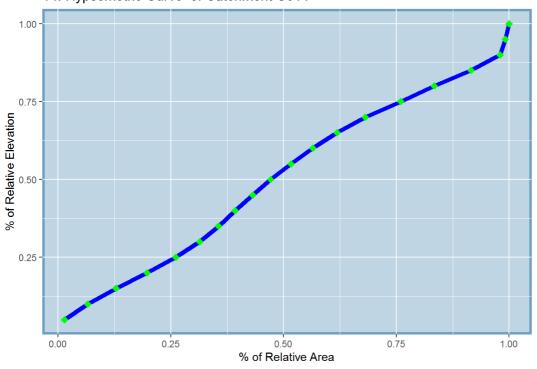
[1] "The hypsometric integral of sub-catchment C012 is 0.599"



[1] "The polynomial equation of sub-catchment C013 is 1.28613044642308*x + 0.0306528465970845*x^2 + 0.0711655919757962*x^3"

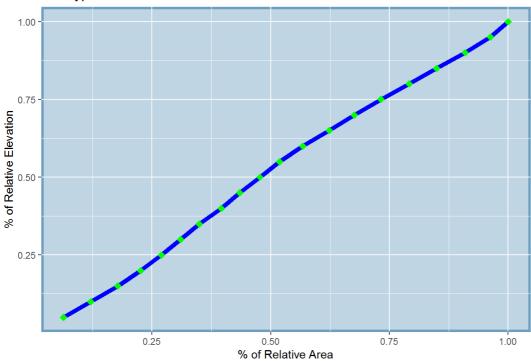
[1] "The hypsometric integral of sub-catchment C013 is 0.671"

14. Hypsometric Curve of Catchment C014



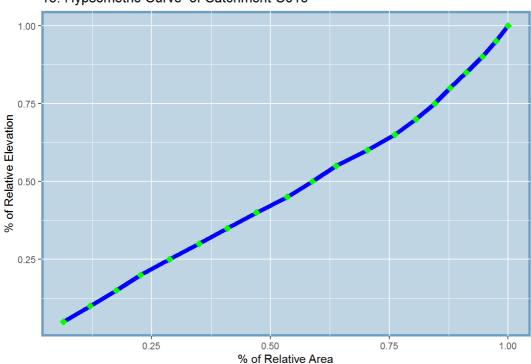
[1] "The polynomial equation of sub-catchment C014 is 1.28423323144377*x - 0.0433971182254848*x^2 - 0.0413260410513917*x^3"

[1] "The hypsometric integral of sub-catchment C014 is 0.617"



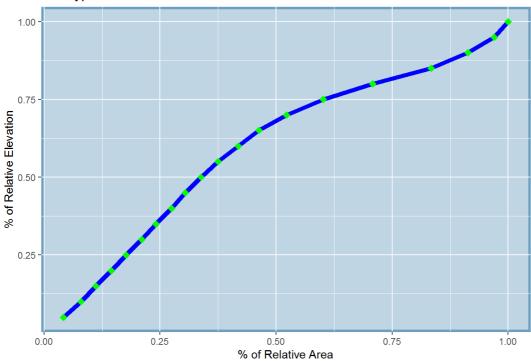
[1] "The polynomial equation of sub-catchment C015 is 1.28699326928903*x - 0.0609393741977899*x^2 - 0.023 0013033564739*x^3"

16. Hypsometric Curve of Catchment C016



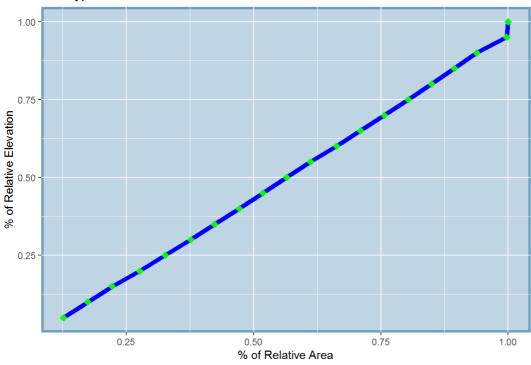
[1] "The polynomial equation of sub-catchment C016 is 1.28187225037501*x + 0.112204111221902*x^2 + 0.0769014834091043*x^3"

[1] "The hypsometric integral of sub-catchment C016 is 0.698"



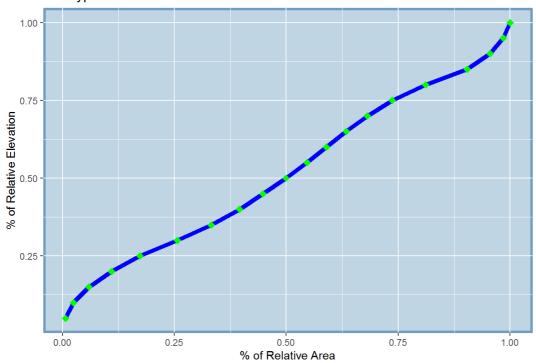
[1] "The polynomial equation of sub-catchment C017 is $1.25352829888515*x - 0.285400295713206*x^2 + 0.0548846030477538*x^3"$

18. Hypsometric Curve of Catchment C018



[1] "The polynomial equation of sub-catchment C018 is 1.28859227639044*x + 0.0280822561862533*x^2 + 0.007 20293960791559*x^3"

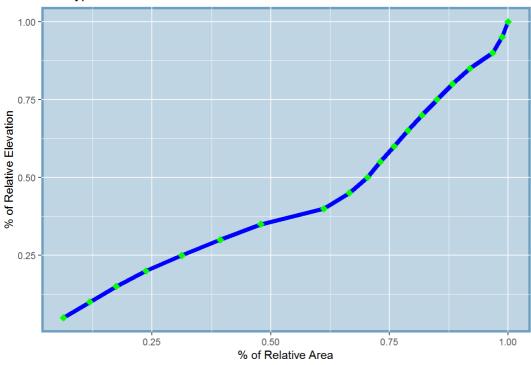
[1] "The hypsometric integral of sub-catchment C018 is 0.655"



[1] "The polynomial equation of sub-catchment C019 is 1.28610367544731*x + 0.0161430102952616*x^2 - 0.001 76681054789048*x^3"

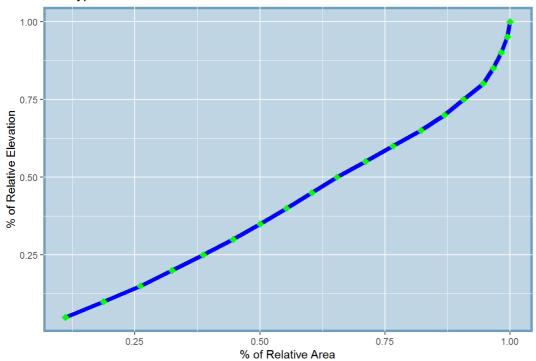
[1] "The hypsometric integral of sub-catchment C019 is 0.648"

20. Hypsometric Curve of Catchment C020



[1] "The polynomial equation of sub-catchment C020 is 1.25638067249527*x + 0.252169855904079*x^2 + 0.106254777110315*x^3"

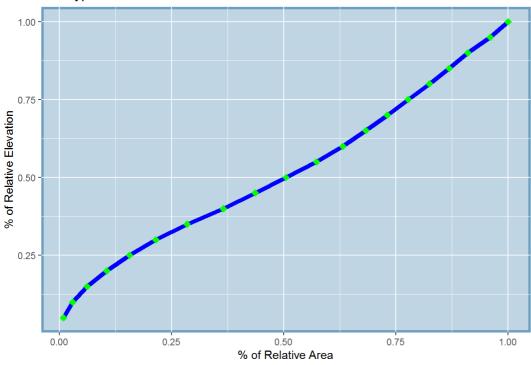
[1] "The hypsometric integral of sub-catchment C020 is 0.739"



[1] "The polynomial equation of sub-catchment CO21 is 1.27303017389804*x + 0.160514326701456*x^2 + 0.0714072386773223*x^3"

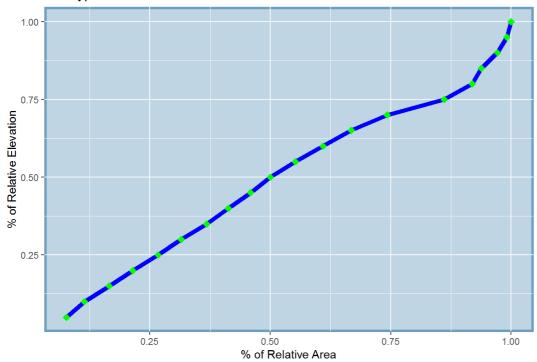
[1] "The hypsometric integral of sub-catchment C021 is 0.708"

22. Hypsometric Curve of Catchment C022



[1] "The polynomial equation of sub-catchment C022 is 1.28454019611061*x + 0.053182127129581*x^2 + 0.0832826652509102*x^3"

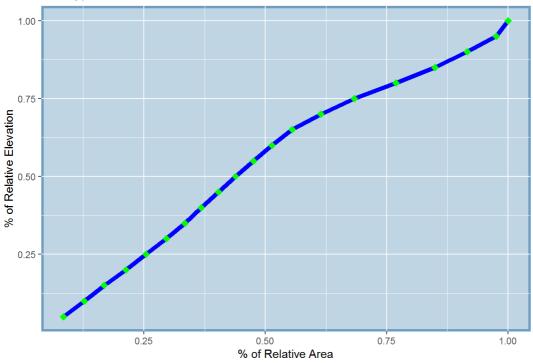
[1] "The hypsometric integral of sub-catchment C022 is 0.681"



[1] "The polynomial equation of sub-catchment C023 is $1.2828248980157*x - 0.0408485947128282*x^2 + 0.0486411002544701*x^3"$

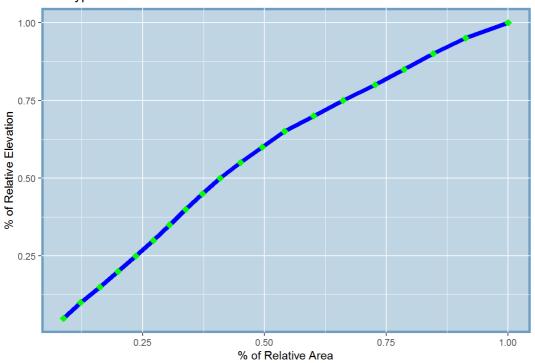
[1] "The hypsometric integral of sub-catchment C023 is 0.64"

24. Hypsometric Curve of Catchment C024



[1] "The polynomial equation of sub-catchment C024 is 1.27618612015661*x - 0.165667613501*x^2 - 0.0156104 502739941*x^3"

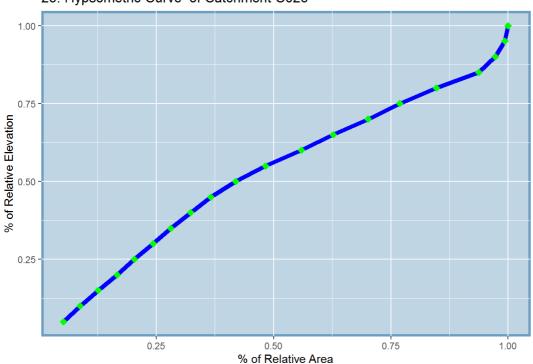
[1] "The hypsometric integral of sub-catchment C024 is 0.579"



[1] "The polynomial equation of sub-catchment C025 is 1.27642004808936*x - 0.178127471580244*x^2 + 0.0025 4464836607342*x^3"

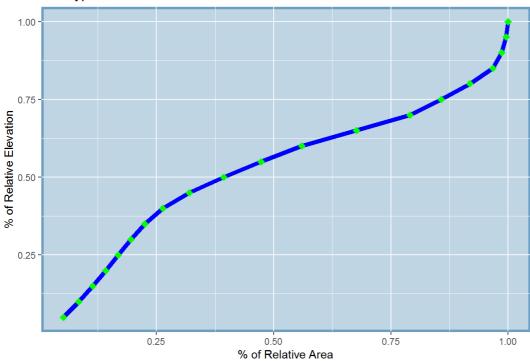
[1] "The hypsometric integral of sub-catchment C025 is 0.579"

26. Hypsometric Curve of Catchment C026



[1] "The polynomial equation of sub-catchment C026 is 1.27875129063079*x - 0.119221665316888*x^2 + 0.0867 383690068952*x^3"

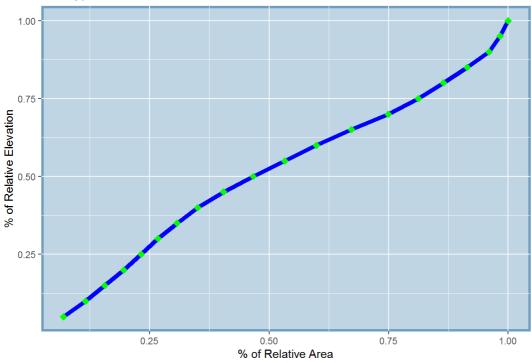
[1] "The hypsometric integral of sub-catchment C026 is 0.621"



[1] "The polynomial equation of sub-catchment C027 is 1.26437310974189*x - 0.122763027035182*x^2 + 0.2022 99818276498*x^3"

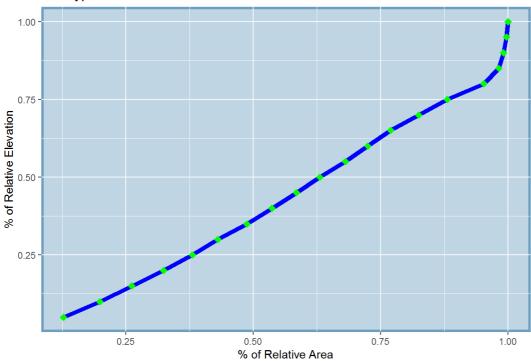
[1] "The hypsometric integral of sub-catchment C027 is 0.642"

28. Hypsometric Curve of Catchment C028



[1] "The polynomial equation of sub-catchment C028 is 1.28239143813282*x - 0.0641360655846747*x^2 + 0.101992559146493*x^3"

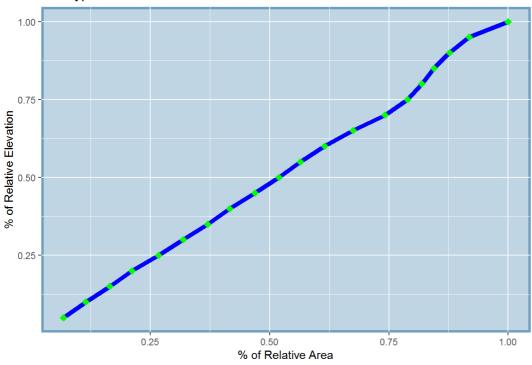
[1] "The hypsometric integral of sub-catchment C028 is 0.645"



[1] "The polynomial equation of sub-catchment CO29 is 1.28018695870478*x + 0.0973149641458673*x^2 + 0.0186489647165711*x^3"

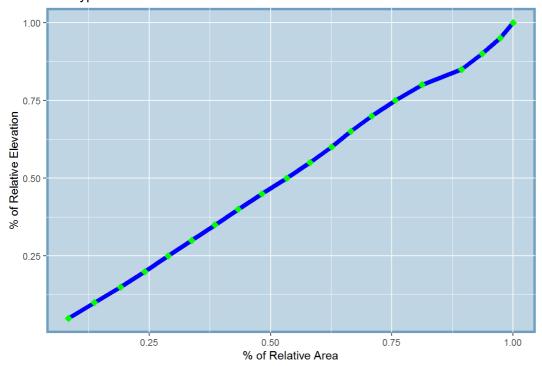
[1] "The hypsometric integral of sub-catchment C029 is 0.677"

30. Hypsometric Curve of Catchment C030



[1] "The polynomial equation of sub-catchment C030 is 1.28742566638042*x + 0.0337550429670693*x^2 + 0.0191796644995827*x^3"

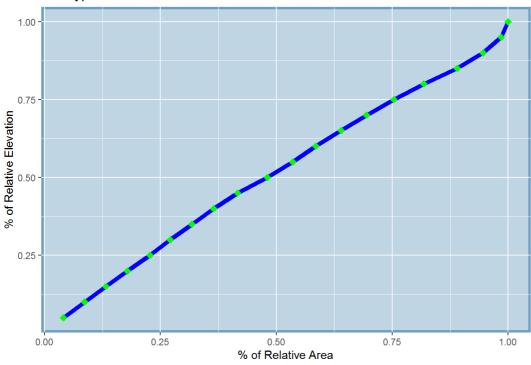
[1] "The hypsometric integral of sub-catchment C030 is 0.66"



[1] "The polynomial equation of sub-catchment CO31 is 1.28857350519038*x - 0.00231646401003393*x^2 - 0.0139108435258136*x^3"

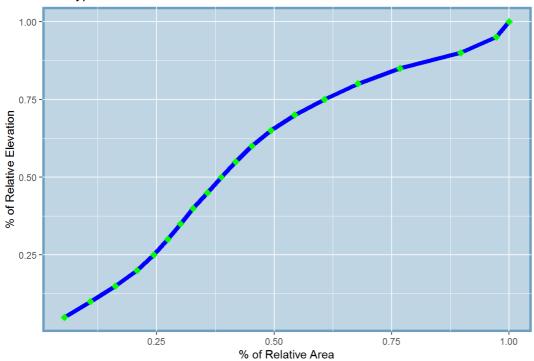
[1] "The hypsometric integral of sub-catchment CO31 is 0.64"

32. Hypsometric Curve of Catchment C032



[1] "The polynomial equation of sub-catchment C032 is 1.28749237583819*x - 0.0472693865526811*x^2 + 0.0276134346800396*x^3"

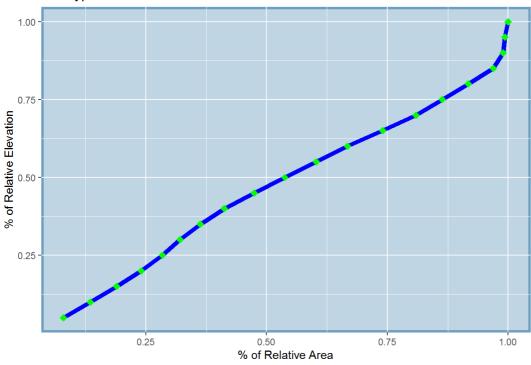
[1] "The hypsometric integral of sub-catchment C032 is 0.635"



[1] "The polynomial equation of sub-catchment C033 is $1.25722997029658*x - 0.254955420708251*x^2 - 0.0566279415093859*x^3"$

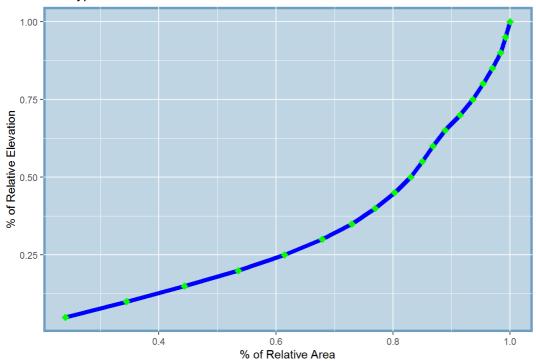
[1] "The hypsometric integral of sub-catchment C033 is 0.529"

34. Hypsometric Curve of Catchment C034



[1] "The polynomial equation of sub-catchment C034 is 1.28223679548389*x + 0.000469322829572341*x^2 + 0.0826855933397754*x^3"

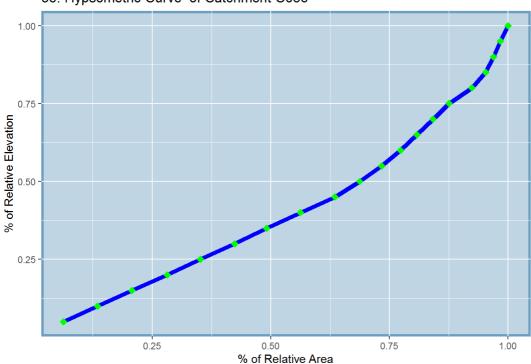
[1] "The hypsometric integral of sub-catchment C034 is 0.662"



[1] "The polynomial equation of sub-catchment C035 is 1.20670880480719*x + 0.427002414679821*x^2 + 0.1461 58116006252*x^3"

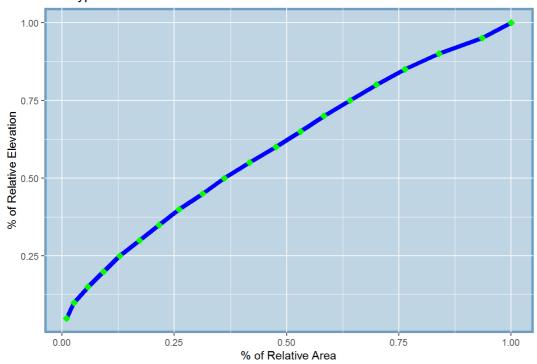
[1] "The hypsometric integral of sub-catchment C035 is 0.782"

36. Hypsometric Curve of Catchment C036



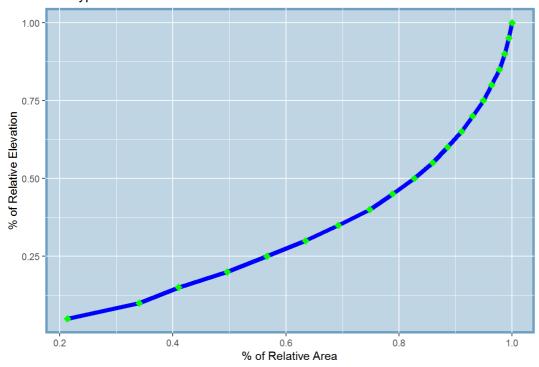
[1] "The polynomial equation of sub-catchment C036 is 1.26449321830936*x + 0.226489133812401*x^2 + 0.0970681130550851*x^3"

[1] "The hypsometric integral of sub-catchment C036 is 0.732"



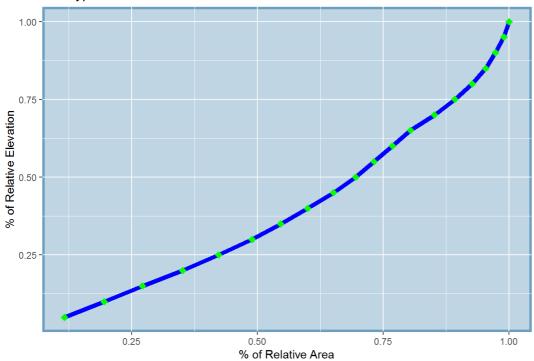
[1] "The polynomial equation of sub-catchment C037 is $1.27935687267828*x - 0.152833697709948*x^2 + 0.0289935372063837*x^3"$

38. Hypsometric Curve of Catchment C038



[1] "The polynomial equation of sub-catchment C038 is 1.21725865472522*x + 0.373556953150406*x^2 + 0.170551100000897*x^3"

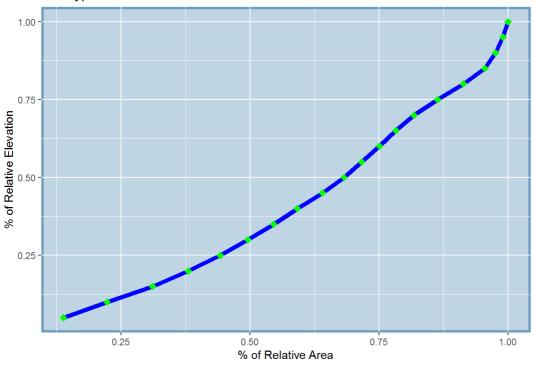
[1] "The hypsometric integral of sub-catchment C038 is 0.776"



[1] "The polynomial equation of sub-catchment C039 is 1.26577195135516*x + 0.23208740145983*x^2 + 0.0530196042060589*x^3"

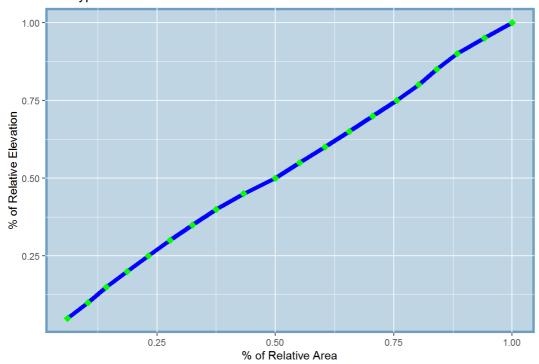
[1] "The hypsometric integral of sub-catchment C039 is 0.724"

40. Hypsometric Curve of Catchment C040



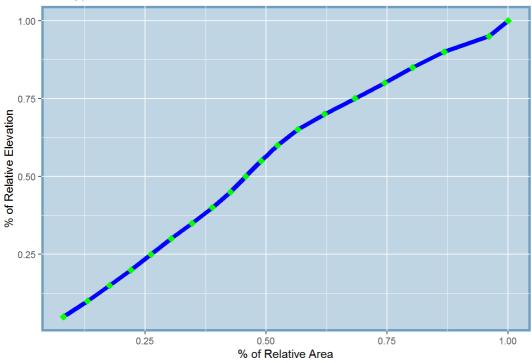
[1] "The polynomial equation of sub-catchment C040 is 1.2724226441497*x + 0.196874545047254*x^2 - 0.0033695753326692*x^3"

[1] "The hypsometric integral of sub-catchment C040 is 0.701"



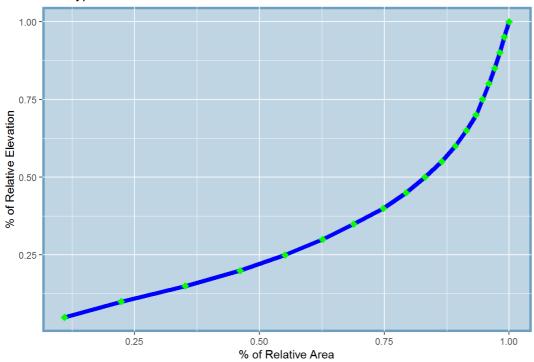
[1] "The polynomial equation of sub-catchment CO41 is 1.28841925048401*x - 0.00812884410587891*x^2 + 0.03 59857278829095*x^3"

42. Hypsometric Curve of Catchment C042



[1] "The polynomial equation of sub-catchment C042 is 1.28057450184189*x - 0.129466920382362*x^2 - 0.0534511252973178*x^3"

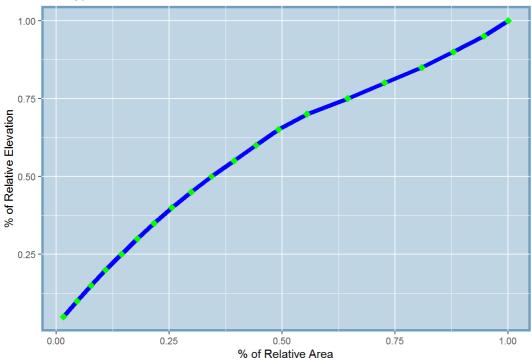
[1] "The hypsometric integral of sub-catchment C042 is 0.584"



[1] "The polynomial equation of sub-catchment C043 is 1.19124192026037*x + 0.427687763765586*x^2 + 0.2119 00338117855*x^3"

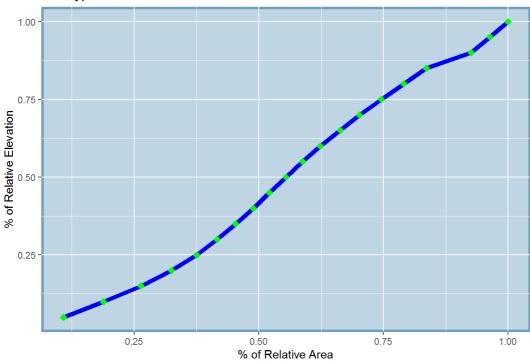
[1] "The hypsometric integral of sub-catchment C043 is 0.791"

44. Hypsometric Curve of Catchment C044



[1] "The polynomial equation of sub-catchment C044 is 1.27068520657246*x - 0.208228399634919*x^2 + 0.0613 145537768993*x^3"

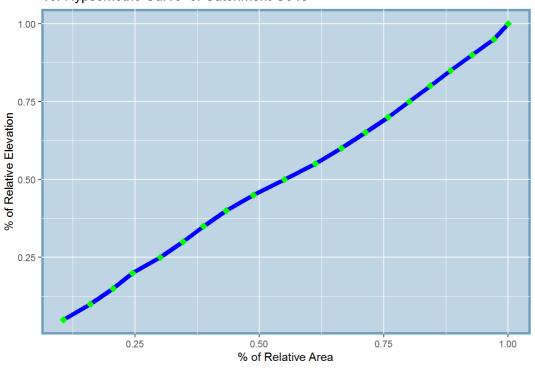
[1] "The hypsometric integral of sub-catchment C044 is 0.581"



[1] "The polynomial equation of sub-catchment C045 is $1.28264863453384*x + 0.0213466768667033*x^2 - 0.119924736860762*x^3"$

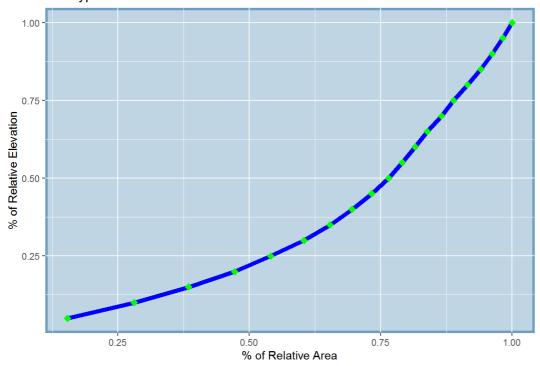
[1] "The hypsometric integral of sub-catchment C045 is 0.618"

46. Hypsometric Curve of Catchment C046



[1] "The polynomial equation of sub-catchment C046 is 1.2878839158049*x + 0.0292804060943213*x^2 + 0.0465781227155415*x^3"

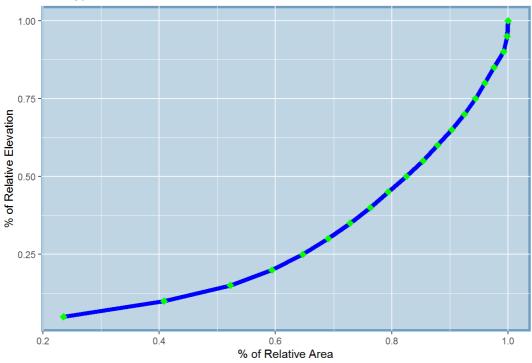
[1] "The hypsometric integral of sub-catchment C046 is 0.665"



[1] "The polynomial equation of sub-catchment CO47 is 1.23181724957754*x + 0.374094288905986*x^2 + 0.0634 161576510671*x^3"

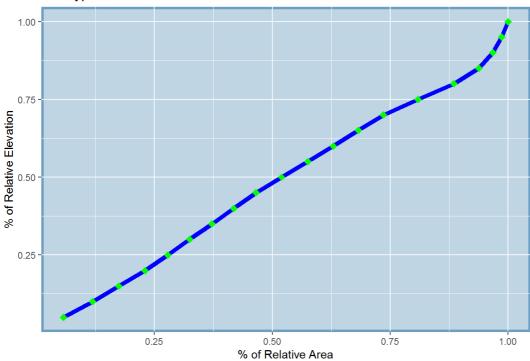
[1] "The hypsometric integral of sub-catchment C047 is 0.756"

48. Hypsometric Curve of Catchment C048



[1] "The polynomial equation of sub-catchment C048 is 1.2061353222591*x + 0.437053773390657*x^2 + 0.102837438841376*x^3"

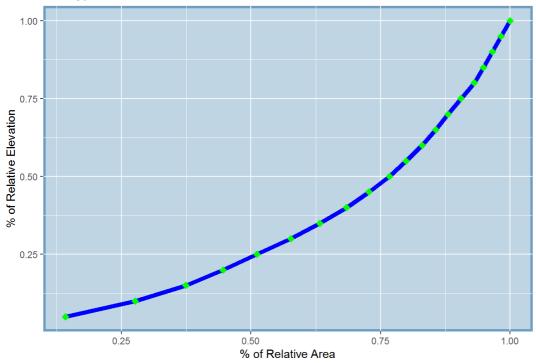
[1] "The hypsometric integral of sub-catchment C048 is 0.774"



[1] "The polynomial equation of sub-catchment CO49 is 1.28656288633172*x - 0.00602819410832792*x^2 + 0.020301190668794*x^3"

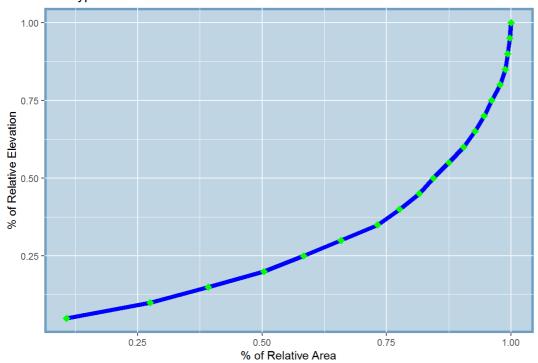
[1] "The hypsometric integral of sub-catchment C049 is 0.646"

50. Hypsometric Curve of Catchment C050



[1] "The polynomial equation of sub-catchment C050 is 1.2368314301777*x + 0.349054369726396*x^2 + 0.0982785007536756*x^3"

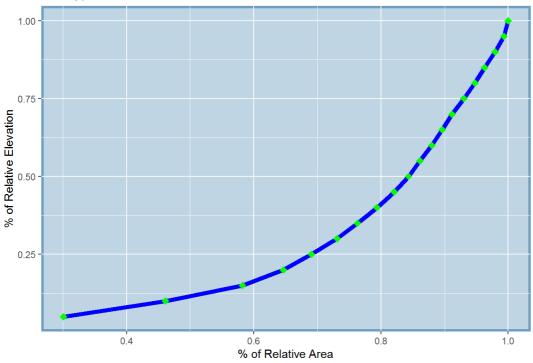
[1] "The hypsometric integral of sub-catchment C050 is 0.759"



[1] "The polynomial equation of sub-catchment C051 is 1.17888194039112*x + 0.451996734839404*x^2 + 0.2118 98627798948*x^3"

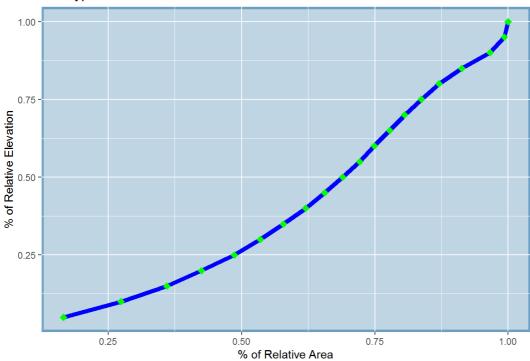
[1] "The hypsometric integral of sub-catchment C051 is 0.793"

52. Hypsometric Curve of Catchment C052



[1] "The polynomial equation of sub-catchment C052 is 1.1911269486409*x + 0.482675815607605*x^2 + 0.0994989673341095*x^3"

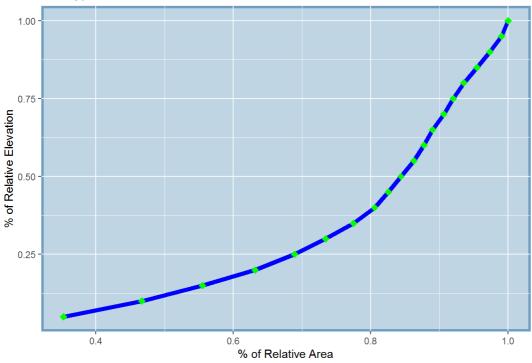
[1] "The hypsometric integral of sub-catchment C052 is 0.781"



[1] "The polynomial equation of sub-catchment C053 is 1.26814688657089*x + 0.216196391643668*x^2 - 0.0599612709875136*x^3"

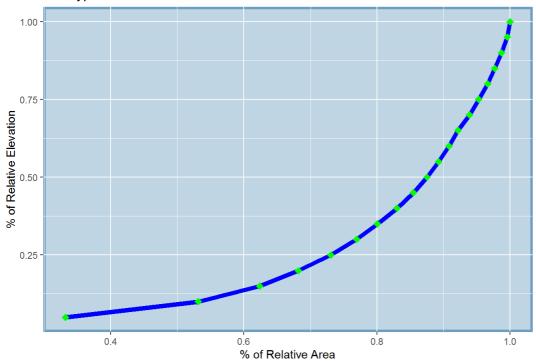
[1] "The hypsometric integral of sub-catchment C053 is 0.691"

54. Hypsometric Curve of Catchment C054



[1] "The polynomial equation of sub-catchment C054 is 1.20108129972929*x + 0.451592067568326*x^2 + 0.1028 89174737825*x^3"

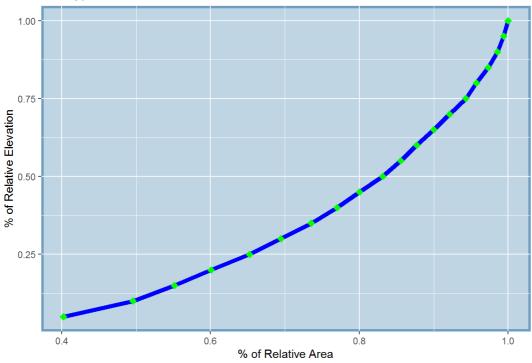
[1] "The hypsometric integral of sub-catchment C054 is 0.777"



[1] "The polynomial equation of sub-catchment C055 is $1.16717068974855*x + 0.52097294429153*x^2 + 0.160243237485564*x^3"$

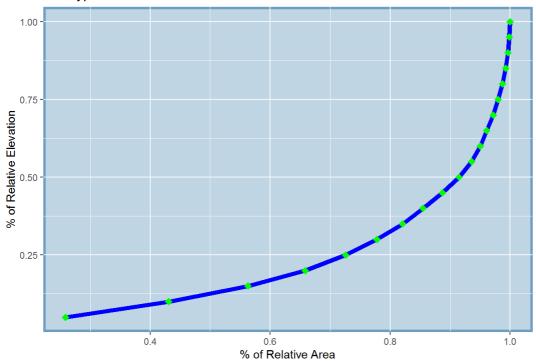
[1] "The hypsometric integral of sub-catchment C055 is 0.797"

56. Hypsometric Curve of Catchment C056



[1] "The polynomial equation of sub-catchment C056 is 1.24551191179111*x + 0.315591250084385*x^2 + 0.0882 424043163123*x^3"

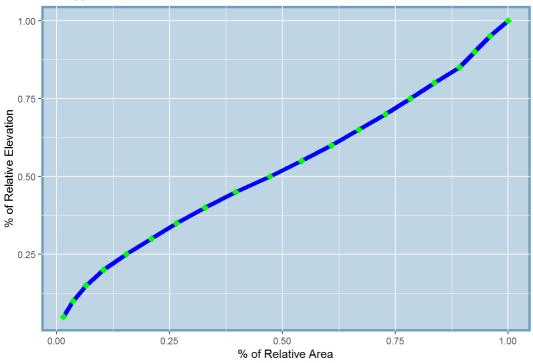
[1] "The hypsometric integral of sub-catchment C056 is 0.75"



[1] "The polynomial equation of sub-catchment C057 is 1.12546439012818*x + 0.520854788190361*x^2 + 0.268482471249938*x^3"

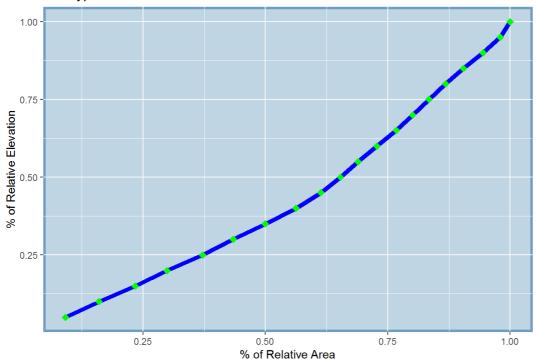
[1] "The hypsometric integral of sub-catchment C057 is 0.803"

58. Hypsometric Curve of Catchment C058



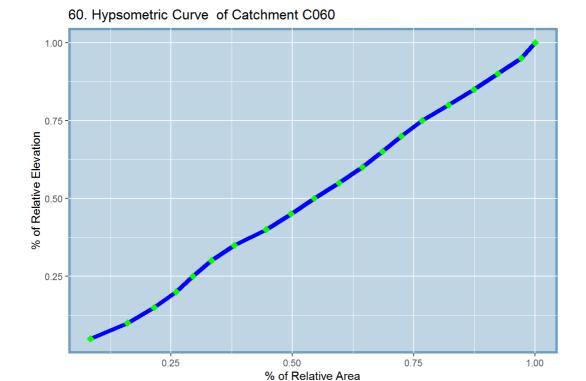
[1] "The polynomial equation of sub-catchment C058 is 1.28485214888492*x + 0.00458088975259705*x^2 + 0.10 3040301627517*x^3"

[1] "The hypsometric integral of sub-catchment C058 is 0.67"



[1] "The polynomial equation of sub-catchment C059 is 1.27319062695545*x + 0.199057856924446*x^2 + 0.0214 547991819763*x^3"

[1] "The hypsometric integral of sub-catchment C059 is 0.708"



[1] "The polynomial equation of sub-catchment C060 is 1.28855141197897*x + 0.0183974349015636*x^2 - 0.003 98425644516104*x^3"

[1] "The hypsometric integral of sub-catchment C060 is 0.649"

IV. Summary of Results

```
summary_table <- data.frame(x1 = character(),</pre>
                      x2 = numeric(),
                      x3 = numeric(),
                     x4 = numeric(),
                     x5 = numeric(),
                     stringsAsFactors = FALSE)
colnames(summary_table)<-c("CODE","MIN_ELEV", "MAX_ELEV", "AREA", "H_INTEGRAL")</pre>
for (i in watersheds) {
    if (i < 10)
   n <- paste("C00", i, sep = "")</pre>
 else
  n <- paste("C0", i, sep = "")
 CODE <- n
MIN_ELEV <- all_data[[n]]$minimum
MAX_ELEV <- all_data[[n]]$maximum</pre>
AREA <- round(sum(all_data[[n]]$data$AREA_GEO),2)</pre>
H_INTEGRAL <- round(all_data[[n]]$h_integral,3)</pre>
summary_table[i,] <- c(CODE, MIN_ELEV, MAX_ELEV, AREA, H_INTEGRAL)</pre>
kable(summary_table)
```

CODE	MIN_ELEV	MAX_ELEV	AREA	H_INTEGRAL
C001	1370	1667	43.7	0.695
C002	1378	1718	35.35	0.73
C003	1394	1784	23.96	0.626
C004	1395	1805	36.51	0.615
C005	1400	1674	35.85	0.68
C006	1410	1760	60.15	0.661
C007	1419	1810	44.85	0.589
C008	1433	1826	42.8	0.596
C009	1428	1778	50.5	0.589
C010	1423	1760	27.47	0.644
C011	1437	1827	56.23	0.698
C012	1451	1849	48.74	0.599
C013	1454	1890	116.83	0.671
C014	1504	1824	129.39	0.617
C015	1534	1952	95.29	0.617
C016	1540	1934	72.25	0.698
C017	1546	1781	150.45	0.545
C018	1556	1761	54.52	0.655
C019	1681	1996	92.08	0.648
C020	1561	2055	276.46	0.739
C021	1565	1807	58.24	0.708
C022	1631	2071	215.4	0.681
C023	1569	1838	38.83	0.64
C024	1571	1843	65.12	0.579
C025	1574	1855	45.82	0.579
C026	1580	1910	63.65	0.621
C027	1584	1985	103.36	0.642
C028	1586	1968	98.3	0.645

CODE	MIN_ELEV	MAX_ELEV	AREA	H_INTEGRAL
C029	1589	1895	58.76	0.677
C030	1594	1923	55.77	0.66
C031	1599	1977	150.96	0.64
C032	1604	2048	313.53	0.635
C033	1606	2008	147.45	0.529
C034	1607	2010	90.8	0.662
C035	1609	1952	74.24	0.782
C036	1611	2012	188.29	0.732
C037	1656	1963	111.75	0.596
C038	1613	1784	103.83	0.776
C039	1621	2011	212.27	0.724
C040	1622	1956	102.17	0.701
C041	1621	1946	131.63	0.65
C042	1631	2007	130.34	0.584
C043	1637	2002	81.3	0.791
C044	1687	2009	121.94	0.581
C045	1639	2047	163.58	0.618
C046	1643	1950	42.79	0.665
C047	1646	2044	126.82	0.756
C048	1655	1946	106.17	0.774
C049	1664	1995	68.18	0.646
C050	1661	2006	108.94	0.759
C051	1670	1786	29.47	0.793
C052	1639	1933	78.37	0.781
C053	1631	1959	187.36	0.691
C054	1624	1890	61.49	0.777
C055	1633	1874	64.52	0.797
C056	1647	1871	23.54	0.75
C057	1653	2076	116.72	0.803
C058	1675	2092	127.68	0.67
C059	1666	2134	133.8	0.708
C060	1673	2169	181.8	0.649