

Carlo.

-(M, g) Riem. mfd $\dim M = n$

$$\rightarrow R(u, v) = -R(v, u)$$

$$\langle R(u, v)w, z \rangle = -\langle w, R(u, v)z \rangle$$

$$\rightarrow 1^{\text{st}} \text{ Bianchi: } R(u, v)w + R(v, w)u + R(w, u)v = 0$$

$$\rightarrow 2^{\text{nd}} \text{ Bianchi: } \nabla_u R(v, w) + \nabla_v R(w, u) + \nabla_w R(u, v) = 0$$

$$\begin{aligned} \text{- of course, } (\nabla_u R)(v, w)z &= \nabla_u (R(v, w)z) - R(\nabla_u v, w)z \\ &\quad - R(v, \nabla_u w)z - R(v, w)\nabla_u z. \end{aligned}$$

\rightarrow maybe we could be smarter than to write it all out (36 terms..)

\rightarrow compute in local coords. ? still hard

\rightarrow use tensor property to extend v.f.s to convenient ones \rightarrow take constant v.f.s