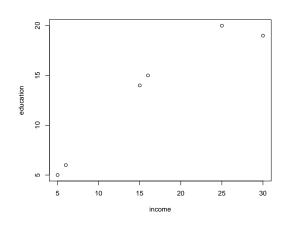
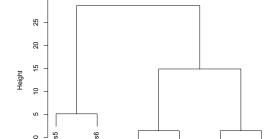
CLUSTER ANALYSIS

- > #cluster analysis with toy example
- > library(cluster)
- > clus.dat <- matrix(c(5,5,6,6,15,14,16,15,25,20,30,19),nrow = 6, ncol=2,byrow=TRUE)
- > rownames(clus.dat) <- c("s1","s2","s3","s4","s5","s6")
- > colnames(clus.dat) <- c("income", "education")</pre>
- > clus.dat

	income	education
s1	5	5
s2	6	6
s3	15	14
s4	16	15
s5	25	20
s6	30	19

- > clus.compl<-hclust(dist(clus.dat), method = "complete") #or single, average, centroid, ward
- > # names(clus.compl)
- > par(mfrow=c(1,2))
- > par(mar=c(5,5,5,5))
- > plot(clus.dat) #plot data
- > plot(clus.compl,cex=0.5) #plot dendogram





Cluster Dendrogram

dist(clus.dat)

\$2

> clus.compl\$merge #shows the iterations

[,1] [,2]

[1,] -1 -2

[2,] -3 -4

[3,] -5 -6

[4,] 1 2 [5,] 3 4

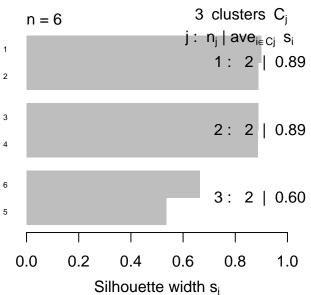
> clust3 <- cutree(clus.compl, k=3) # cut tree into 3 clusters</pre>

> clust3

```
s1 s2 s3 s4 s5 s6
1 1 2 2 3 3
```

- > dd = dd= dist(clus.dat) #computes the distance matrix
- > silout= silhouette(clust3,dd) #computes information for silhouette plot for 3 clusters
- > plot(silout,cex.main=1,cex = 0.5) #plot silhouette

Silhouette plot of (x = clust3, dist =



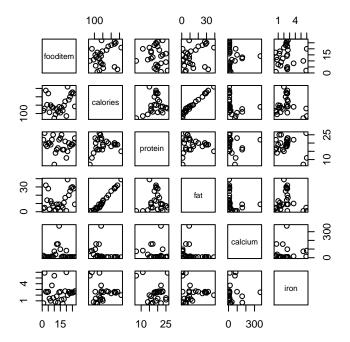
Average silhouette width: 0.79

- > #cluster analysis with calories etcetera of food items
- >
- > dcal <- read.table("C:/R/rmmva/calories.txt", header=T, quote="\"")</pre>
- > attach(dcal)
- > dcal

	fooditem	calories	protein	fat	calcium	iron
1	Braised_beef	340	20	28	9	2.6
2	Hamburger	245	21	17	9	2.7
3	Roast_beef	420	15	39	7	2.0
4	Beef_steak	375	19	32	9	2.6
5	Canned_beef	180	22	10	17	3.7
6	Broiled_chicken	115	20	3	8	1.4
7	Canned_chicken	170	25	7	12	1.5
8	Beef_heart	160	26	5	14	5.9
9	Roast_lamb_leg	265	20	20	9	2.6
10	${\tt Roast_lamb_shoulder}$	300	18	25	9	2.3
11	Smoked_ham	340	20	28	9	2.5
12	Roast_pork	340	19	29	9	2.5

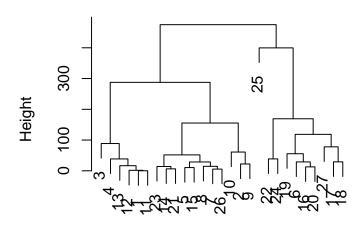
13	Simmered_pork	355	19	30	9	2.4
14	Beef_tongue	205	18	14	7	2.5
15	Veal_cutlet	185	23	9	9	2.7
16	Baked_bluefish	135	22	4	25	0.6
17	Raw_clams	70	11	1	82	6.0
18	Canned_clams	45	7	1	74	5.4
19	Canned_crabmeat	90	14	2	38	0.8
20	Fried_haddock	135	16	5	15	0.5
21	Broiled_mackerel	200	19	13	5	1.0
22	Canned_mackerel	155	16	9	157	1.8
23	Fried_perch	195	16	11	14	1.3
24	Canned_salmon	120	17	5	159	0.7
25	Canned_sardines	180	22	9	367	2.5
26	Canned_tuna	170	25	7	7	1.2
27	Canned_shrimp	110	23	1	98	2.6

> plot(dcal)



- > #complete linkage
- > distcal <- dist(dcal)</pre>
- > # distcal
- > clus.compl<-hclust(distcal, method = "complete") #or single, average, centroid, ward
- > #names(clus.comp1)
- > plot(clus.compl,cex=0.5) #plot dendogram

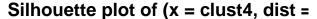
Cluster Dendrogram

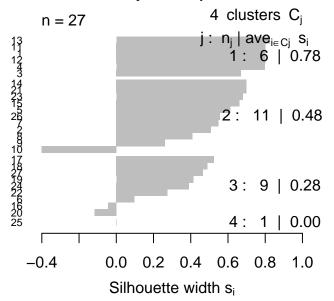


distcal hclust (*, "complete")

- > #clus.compl\$merge #shows the iterations
- > clust4 <- cutree(clus.compl, k=4) # cut tree into 4 clusters
- > clust4

- > silout= silhouette(clust4, distcal) #computes information for silhouette plot for 4 clusters
- > plot(silout,cex = 0.7) #plot silhouette





Average silhouette width: 0.46

- > #k means clustering
- > # 3 cluster solution and random initial clusters
- > clus.kmeans <- kmeans(dcal[,-1], 4) # 3 cluster solution and random initial clusters
- > clus.kmeans

K-means clustering with 4 clusters of sizes 7, 10, 7, 3

Cluster means:

calories protein fat calcium iron
1 352.8571 18.57143 30.142857 8.714286 2.414286
2 197.5000 21.50000 11.300000 10.300000 2.510000
3 100.0000 16.14286 2.428571 48.571429 2.471429
4 151.6667 18.33333 7.666667 227.666667 1.666667

Clustering vector:

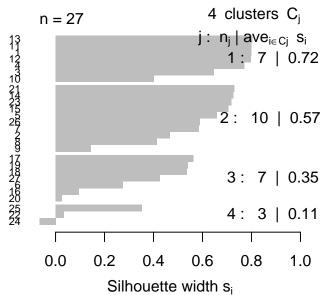
Within cluster sum of squares by cluster:
[1] 8433.126 10712.669 14706.660 30972.313
(between_SS / total_SS = 84.9 %)

Available components:

- [1] "cluster" "centers" "totss" "withinss" "tot.withinss" "betweenss"
- [7] "size"

> ss = silhouette(clus.kmeans\$cluster,distcal)

Silhouette plot of (x = clus.kmeans)



Average silhouette width: 0.5

```
> #PAM partitioning around mediods
> library(MASS)
> library(cluster)
> library(fpc)
> p=pam(dcal[,-1],3)
> p
Medoids:
   ID calories protein fat calcium iron
[1,] 11
        340
             20 28
                     9 2.5
[2,] 7
        170
             25
                7
                     12 1.5
[3,] 27
        110
                1
                     98 2.6
Clustering vector:
```

Objective function:

build swap

44.21261 44.02536

Available components:

- [1] "medoids" "id.med" "clustering" "objective" "isolation" "clusinfo" "silinfo"
- [8] "diss" "call" "data"
- > # plot(p,cex=0.5,cex.main=0.5) #creates (among others) silhouette plots

```
> #Mixture modelling
> library(FisherEM)
> #remove canned sardines
> dcalwcs = subset(dcal,calcium < 360)</pre>
> #dcalwcs
> #only seems to work if nr of variables larger than nr of clusters
> #the function fem fits a finite mixture model and at the same time
> #reduces the number of dimensions to plot the results in 2 dimensions
> #res = fem(dcalwcs[,-1],3,model="AkB")
> res = fem(dcalwcs[,-1],3,model="all")
model: DkBk
            bic: -356.1142
model: DkB
           bic: -388.0045
model: DBk
           bic: -400.2387
model: DB
           bic: -421.7061
model: AkjBk bic: -368.9642
model: AkjB bic: -407.1148
model: AkBk bic: -403.2533
model: AkB bic: -411.1244
model: AjBk bic: -409.9689
model: AjB bic: -440.6903
model: ABk
           bic: -410.0535
model: AB
           bic: -450.4718
The best model is: DkBk with a bic equal to: -356.1142
> res$cls
 > round(res$P,5) #P are the posterior probabilities, print 5 decimals
              [,2]
        [,1]
                     [,3]
 [1,] 1.00000 0.00000 0.00000
 [2,] 0.00434 0.00000 0.99566
 [3,] 1.00000 0.00000 0.00000
 [4,] 1.00000 0.00000 0.00000
 [5,] 0.00000 0.00000 1.00000
 [6,] 0.00000 0.99870 0.00130
 [7,] 0.00000 0.00053 0.99947
 [8,] 0.00000 0.00908 0.99092
[9,] 0.99939 0.00000 0.00061
[10,] 1.00000 0.00000 0.00000
[11,] 1.00000 0.00000 0.00000
[12,] 1.00000 0.00000 0.00000
[13,] 1.00000 0.00000 0.00000
[14,] 0.00000 0.00000 1.00000
[15,] 0.00000 0.00040 0.99960
[16,] 0.00000 0.99990 0.00010
[17,] 0.00000 1.00000 0.00000
```

- [18,] 0.00000 1.00000 0.00000
- [19,] 0.00000 1.00000 0.00000
- [20,] 0.00000 1.00000 0.00000
- [21,] 0.00000 0.00000 1.00000
- [22,] 0.00000 1.00000 0.00000
- [23,] 0.00000 1.00000 0.00000
- [24,] 0.00000 1.00000 0.00000
- [25,] 0.00000 0.00037 0.99963
- [26,] 0.00000 1.00000 0.00000

> res\$prms\$prop

[1] 0.3078357 0.3849612 0.3072030

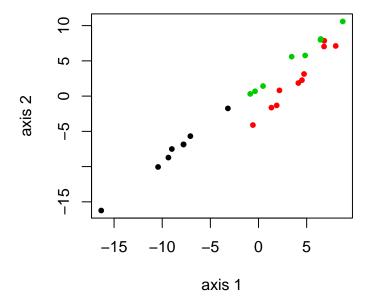
> res\$prms\$my#estimated mean in the original space

- [1,] 341.8283 18.75112 28.869238 8.750116 2.437630
- [2,] 117.0466 16.20941 4.201328 66.952491 2.113502
- [3,] 189.3736 22.37073 10.252225 9.995831 2.646188

> res\$prms\$mean #estimated mean in the subspace

- [1,] -8.866252 -7.951395
- [2,] 3.988375 2.308575
- [3,] 3.643949 5.055173

> plot.fem(res,dcalwcs[,-1])



```
> #Model based clustering
> library(mclust)
> # The R function Mclust performs model-based clustering for a range of models
> # and a variety of values of k:
> mclustout <- Mclust(dcalwcs[,-1], G=2:9)</pre>
> # By default, the models considered are:
> # "EII": spherical, equal volume
> # "VII": spherical, unequal volume
> # "EEI": diagonal, equal volume and shape
> # "VEI": diagonal, varying volume, equal shape
> # "EVI": diagonal, equal volume, varying shape
> # "VVI": diagonal, varying volume and shape
> # "EEE": ellipsoidal, equal volume, shape, and orientation
> # "EEV": ellipsoidal, equal volume and equal shape
> # "VEV": ellipsoidal, equal shape
> # "VVV": ellipsoidal, varying volume, shape, and orientation
> # Plotting the BIC values:
> plot(mclustout, data=dcalwcs, what="BIC")
> mclustout
'Mclust' model object:
best model: ellipsoidal, equal shape (VEV) with 6 components
> mclustout$classification
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 26 27
1 \quad 2 \quad 1 \quad 1 \quad 3 \quad 4 \quad 3 \quad 3 \quad 2 \quad 2 \quad 1 \quad 1 \quad 1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 5 \quad 4 \quad 4 \quad 2 \quad 6 \quad 2 \quad 6 \quad 3 \quad 5
> names(mclustout)
[1] "call"
                     "modelName"
                                      "n"
                                                      "d"
                                                                       "G"
[6] "BIC"
                     "bic"
                                      "loglik"
                                                      "df"
                                                                       "parameters"
[11] "classification" "uncertainty"
                                      "2"
> round(mclustout$parameters$pro,2)
[1] 0.23 0.23 0.19 0.15 0.12 0.08
> round(mclustout$parameters$mean,2)
           [,1]
                 [,2] [,3]
                             [,4] [,5]
                                           [,6]
calories 361.67 235.00 173.0 118.75 75.00 137.50
protein 18.67 18.67 24.2 18.00 13.67 16.50
                       7.6 3.50 1.00
         31.00 16.67
          8.67
                8.83 11.8 21.50 84.67 158.00
calcium
                       3.0 0.82 4.67 1.25
          2.43
                 2.07
> # This gives the probabilities of belonging to each cluster for every object:
```

> round(mclustout\$z,2)

	[,1]	[,2]	[,3]	[,4]	[,5]	[,6]
1	1	0	0	0	0	0
2	0	1	0	0	0	0
3	1	0	0	0	0	0
4	1	0	0	0	0	0
5	0	0	1	0	0	0
6	0	0	0	1	0	0
7	0	0	1	0	0	0
8	0	0	1	0	0	0
9	0	1	0	0	0	0
10	0	1	0	0	0	0
11	1	0	0	0	0	0
12	1	0	0	0	0	0
13	1	0	0	0	0	0
14	0	1	0	0	0	0
15	0	0	1	0	0	0
16	0	0	0	1	0	0
17	0	0	0	0	1	0
18	0	0	0	0	1	0
19	0	0	0	1	0	0
20	0	0	0	1	0	0
21	0	1	0	0	0	0
22	0	0	0	0	0	1
23	0	1	0	0	0	0
24	0	0	0	0	0	1
26	0	0	1	0	0	0
27	0	0	0	0	1	0