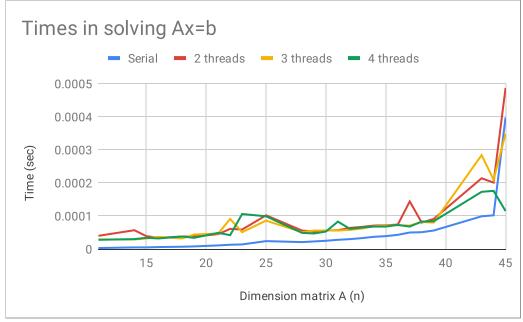
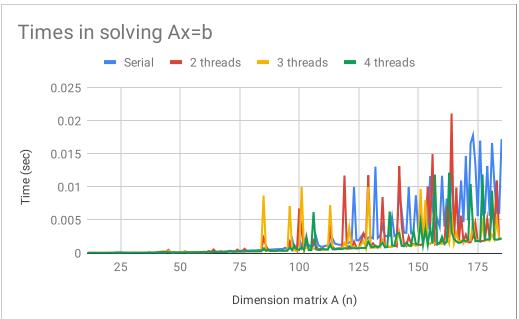
## Speed analysis in solving linear system of equations for different dimensions and nthreads





The first thing to notice is that the serial algorithm has better performance than the parallelization strategy (regardless amount of threads) for small matrices with dimension smaller than around 50x50. A possible reason for this is that the amount of work of synchronizing the threads is not worth the amount of work each of them do in parallel.

As the dimension of the matrix increases, especially over 100x100, parallelization becomes more useful and increases performance compared to serialized version. From the graph it seems clear that using the more cores we use to parallelize, the better for the performance. Over 150x150, serial performance is very poor. An important conclusion from this exercise is that we shall always study our problem and its dimension so as to decide if a serial or parallel approach is most efficient.

\*Outliers points have been removed from analysis

| Dimension(n) | Serial   | 2 threads | 3 threads | 4 threads |
|--------------|----------|-----------|-----------|-----------|
| 11           | 0.000003 | 0.00004   | 0.000029  | 0.000028  |
|              |          |           |           |           |
| 14           | 0.000005 | 0.000057  | 0.000029  | 0.00003   |
| 15           | 0.00005  | 0.000039  | 0.000032  | 0.000034  |
| 16           | 0.000006 | 0.000034  | 0.000037  | 0.000032  |
| 18           | 0.000007 | 0.000038  | 0.000032  | 0.000038  |
| 19           |          | 0.000038  | 0.000044  | 0.000034  |
| 10           | 0.00000  | 0.00000   | 0.000011  | 0.000001  |
| 21           | 0.000011 | 0.000045  | 0.000047  | 0.000049  |
| 22           | 0.000013 | 0.000061  | 0.000091  | 0.000042  |
| 23           | 0.000014 | 0.000059  | 0.000051  | 0.000106  |
| 25           | 0.000024 | 0.000102  | 0.000086  | 0.000099  |
|              |          |           |           |           |
| 20           | 0.000021 | 0.000056  | 0.000051  | 0.000040  |
| 28           |          | 0.000056  | 0.000051  | 0.000049  |
| 29           |          | 0.000053  | 0.000056  | 0.000047  |
| 30           |          | 0.000056  | 0.000056  | 0.000053  |
| 31           |          | 0.000057  | 0.000056  | 0.000083  |
| 32           |          | 0.000064  | 0.000058  | 0.000061  |
| 33           |          | 0.000067  | 0.000062  | 0.000065  |
| 34           |          | 0.000071  | 0.000069  | 0.000068  |
| 35           |          | 0.000072  | 0.000071  | 0.000068  |
| 36           |          | 0.000074  | 0.000072  | 0.000073  |
| 37           |          | 0.000144  | 0.000071  | 0.000068  |
| 38           |          | 0.00008   | 0.000082  | 0.000083  |
| 39           | 0.000056 | 0.000091  | 0.00008   | 0.000084  |
|              |          |           |           |           |
|              |          |           |           |           |
| 43           | 0.000099 | 0.000214  | 0.000284  | 0.000173  |
| 44           | 0.000102 | 0.000201  | 0.00021   | 0.000176  |
| 45           | 0.000398 | 0.000487  | 0.000348  | 0.000115  |
| 46           | 0.00008  | 0.000091  | 0.000089  | 0.000093  |
| 47           | 0.000085 | 0.000096  | 0.000094  | 0.00014   |
| 48           | 0.000087 | 0.000102  | 0.000096  | 0.000099  |
| 49           | 0.000094 | 0.000103  | 0.000101  | 0.000104  |

| 50 | 0.0001   | 0.000109 | 0.000104 | 0.000102 |
|----|----------|----------|----------|----------|
| 51 | 0.000106 | 0.000107 | 0.000111 | 0.000091 |
| 52 | 0.000112 | 0.000292 | 0.000271 | 0.000114 |
| 53 | 0.000118 | 0.000117 | 0.000112 | 0.000116 |
| 54 | 0.000126 | 0.000097 | 0.000123 | 0.000116 |
| 55 | 0.000124 | 0.000126 | 0.000118 | 0.000114 |
| 56 | 0.000132 | 0.000118 | 0.000115 | 0.000116 |
| 57 | 0.000138 | 0.000133 | 0.00011  | 0.000122 |
| 58 | 0.000145 | 0.000127 | 0.000127 | 0.000125 |
| 59 | 0.000156 | 0.000138 | 0.000132 | 0.000158 |
| 60 | 0.000161 | 0.000124 | 0.000132 | 0.000188 |
| 61 | 0.00017  | 0.000143 | 0.000136 | 0.000143 |
| 62 | 0.00021  | 0.000306 | 0.000121 | 0.000198 |
| 63 | 0.000188 | 0.000155 | 0.000154 | 0.000148 |
| 64 | 0.000389 | 0.000538 | 0.000156 | 0.000165 |
| 65 | 0.000206 | 0.000162 | 0.000159 | 0.000161 |
| 66 | 0.000216 | 0.000168 | 0.00017  | 0.000168 |
| 67 | 0.000232 | 0.000298 | 0.000176 | 0.000155 |
| 68 | 0.000235 | 0.000178 | 0.000181 | 0.00017  |
| 69 | 0.000247 | 0.000182 | 0.000189 | 0.000158 |
|    |          |          |          |          |
| 71 | 0.000345 | 0.000276 | 0.000229 | 0.000229 |
| 72 | 0.000295 | 0.000207 | 0.000199 | 0.000206 |
| 73 | 0.000308 | 0.000215 | 0.000214 | 0.000197 |
| 74 | 0.000325 | 0.000527 | 0.000216 | 0.000217 |
| 75 | 0.000336 | 0.000231 | 0.000226 | 0.000229 |
| 76 | 0.000352 | 0.000255 | 0.000209 | 0.00023  |
| 77 | 0.000365 | 0.000645 | 0.00025  | 0.00022  |
| 78 | 0.000375 | 0.000297 | 0.000242 | 0.000265 |
| 79 | 0.00037  | 0.00025  | 0.000239 | 0.000242 |
| 80 | 0.000411 | 0.000268 | 0.000239 | 0.000269 |
| 81 | 0.0004   | 0.00026  | 0.000253 | 0.000251 |
| 82 | 0.000415 | 0.000267 | 0.00026  | 0.00026  |
| 83 | 0.000458 | 0.0003   | 0.000267 | 0.000269 |
| 84 | 0.000445 | 0.000266 | 0.000271 | 0.000274 |
| 85 | 0.000462 | 0.002252 | 0.008701 | 0.000694 |
| 86 | 0.000936 | 0.001136 | 0.000336 | 0.00034  |
| 87 | 0.000508 | 0.000325 | 0.000298 | 0.000518 |
| 88 | 0.000525 | 0.000338 | 0.000309 | 0.000307 |
| 89 | 0.000543 | 0.000325 | 0.000315 | 0.000315 |
| 90 | 0.000587 | 0.000324 | 0.000405 | 0.000343 |
| 91 | 0.000575 | 0.000337 | 0.00032  | 0.000388 |
| 92 | 0.000609 | 0.000398 | 0.000334 | 0.000385 |

| 93  | 0.000596 | 0.000348 | 0.00034  | 0.000336     |
|-----|----------|----------|----------|--------------|
| 94  | 0.0008   | 0.00036  | 0.000354 | 0.000354     |
| 95  | 0.000638 | 0.000389 | 0.000366 | 0.000357     |
| 96  | 0.00087  | 0.001692 | 0.007079 | 0.000829     |
| 97  | 0.002169 | 0.000524 | 0.000456 | 0.000452     |
| 98  | 0.000751 | 0.001003 | 0.000374 | 0.001154     |
| 99  | 0.000724 | 0.000395 | 0.00039  | 0.000565     |
| 100 | 0.002306 | 0.006731 | 0.000482 | 0.000482     |
| 101 | 0.000871 | 0.003409 | 0.009948 | 0.000868     |
| 102 | 0.002142 | 0.000499 | 0.000431 | 0.000456     |
| 103 | 0.000966 | 0.002488 | 0.000909 | 0.00235      |
| 104 | 0.00123  | 0.00048  | 0.000654 | 0.000449     |
| 105 | 0.000863 | 0.000532 | 0.000446 | 0.000448     |
| 106 | 0.001133 | 0.001886 | 0.000713 | 0.006207     |
| 107 | 0.002602 | 0.001138 | 0.000622 | 0.000572     |
| 108 | 0.001204 | 0.000527 | 0.000477 | 0.000477     |
| 109 | 0.000964 | 0.000665 | 0.0005   | 0.000468     |
| 110 | 0.000991 | 0.000491 | 0.000527 | 0.000715     |
| 111 | 0.00108  | 0.00053  | 0.00051  | 0.000525     |
| 112 | 0.001211 | 0.000601 | 0.000536 | 0.000519     |
| 113 | 0.001074 | 0.003317 | 0.007222 | 0.001199     |
| 114 | 0.002181 | 0.001004 | 0.000592 | 0.000588     |
| 115 | 0.001426 | 0.000595 | 0.000549 | 0.000545     |
| 116 | 0.001322 | 0.000701 | 0.000605 | 0.000616     |
| 117 | 0.001252 | 0.000776 | 0.000727 | 0.000602     |
| 118 | 0.001275 | 0.000809 | 0.00061  | 0.00061      |
| 119 | 0.001263 | 0.011726 | 0.001504 | 0.000727     |
| 120 | 0.001364 | 0.000677 | 0.000837 | 0.000668     |
| 121 | 0.001591 | 0.000677 | 0.003836 | 0.001046     |
| 122 | 0.001788 | 0.000698 | 0.000848 | 0.000729     |
| 123 | 0.009992 | 0.00174  | 0.000929 | 0.000743     |
| 124 | 0.001931 | 0.00083  | 0.000731 | 0.000677     |
| 125 | 0.001919 | 0.000719 | 0.000716 | 0.000728     |
|     |          |          |          |              |
| 127 | 0.003034 | 0.002887 | 0.001837 | 0.000778     |
| 128 | 0.001991 | 0.002168 | 0.00074  | 0.000754     |
| 129 | 0.002342 | 0.01176  | 0.010002 | 0.00177      |
| 130 | 0.002407 | 0.001015 | 0.00078  | 0.000999     |
| 131 | 0.002213 | 0.001462 | 0.000817 | 0.000867     |
| 132 | 0.013036 | 0.001036 | 0.000831 | 0.001097     |
| 133 | 0.002284 | 0.001002 | 0.000837 | 0.000823     |
| 134 | 0.002657 | 0.000895 | 0.000868 | 0.00115      |
| 135 | 0.004108 | 0.008438 | 0.001953 | 0.001553     |
| -   |          |          |          | <del>-</del> |

| 136 | 0.002554 | 0.000993 | 0.00091  | 0.000857 |
|-----|----------|----------|----------|----------|
| 137 | 0.002574 | 0.000907 | 0.001068 | 0.000909 |
| 138 | 0.002615 | 0.000953 | 0.000913 | 0.006275 |
| 139 | 0.005424 | 0.000968 | 0.000921 | 0.001164 |
| 140 | 0.002568 | 0.001116 | 0.001111 | 0.001083 |
| 141 | 0.002765 | 0.00099  | 0.001834 | 0.00287  |
| 142 | 0.009572 | 0.013149 | 0.003253 | 0.003035 |
| 143 | 0.006476 | 0.004434 | 0.001304 | 0.001098 |
| 144 | 0.003088 | 0.001284 | 0.001093 | 0.001026 |
| 145 | 0.003054 | 0.001058 | 0.00124  | 0.001562 |
| 146 | 0.009946 | 0.002494 | 0.001103 | 0.001143 |
| 147 | 0.002983 | 0.001409 | 0.001026 | 0.001105 |
| 148 | 0.003142 | 0.001381 | 0.001274 | 0.003411 |
| 149 | 0.008723 | 0.001114 | 0.001137 | 0.001348 |
| 150 | 0.003281 | 0.001286 | 0.001164 | 0.001296 |
| 151 | 0.00338  | 0.001195 | 0.00964  | 0.004644 |
| 152 | 0.003393 | 0.001422 | 0.001359 | 0.001229 |
| 153 | 0.003523 | 0.003579 | 0.007978 | 0.003544 |
| 154 | 0.003699 | 0.010061 | 0.001504 | 0.001227 |
| 155 | 0.011612 | 0.003601 | 0.001356 | 0.003872 |
| 156 | 0.007162 | 0.014961 | 0.001806 | 0.001435 |
| 157 | 0.003721 | 0.001317 | 0.001444 | 0.01183  |
| 158 | 0.005125 | 0.001539 | 0.001399 | 0.001282 |
| 159 | 0.003965 | 0.001486 | 0.001389 | 0.001496 |
| 160 | 0.011671 | 0.001853 | 0.001383 | 0.002475 |
| 161 | 0.004003 | 0.001432 | 0.001534 | 0.001371 |
| 162 | 0.008227 | 0.007069 | 0.002376 | 0.001713 |
| 163 | 0.004487 | 0.002262 | 0.001431 | 0.012138 |
| 164 | 0.012947 | 0.021083 | 0.006165 | 0.003172 |
| 165 | 0.004501 | 0.001544 | 0.00148  | 0.002115 |
| 166 | 0.007116 | 0.009896 | 0.002993 | 0.001759 |
| 167 | 0.004841 | 0.001533 | 0.001697 | 0.001527 |
| 168 | 0.010979 | 0.005636 | 0.00193  | 0.001629 |
| 169 | 0.004676 | 0.001757 | 0.00158  | 0.001964 |
| 170 | 0.014644 | 0.002786 | 0.001635 | 0.001798 |
| 171 | 0.004963 | 0.001627 | 0.002011 | 0.002007 |
| 172 | 0.016608 | 0.001635 | 0.001932 | 0.010444 |
| 173 | 0.017784 | 0.002402 | 0.004947 | 0.003885 |
| 174 | 0.013414 | 0.004517 | 0.002158 | 0.001781 |
| 175 | 0.005588 | 0.00181  | 0.001944 | 0.001843 |
| 176 | 0.016972 | 0.001815 | 0.001855 | 0.001736 |
| 177 | 0.005826 | 0.001813 | 0.004545 | 0.011847 |
| 178 | 0.006041 | 0.001939 | 0.001818 | 0.001987 |
|     |          |          |          |          |

| 0.013162 | 0.005113  | 0.002007  | 0.002069   |
|----------|---|---|--|
| 0.005655 | 0.002097  | 0.001865  | 0.002073   |
| 0.016644 | 0.006667  | 0.002782  | 0.009411   |
| 0.010474 | 0.004062  | 0.002046  | 0.002069   |
| 0.006023 | 0.010984  | 0.00503   | 0.002008   |
| 0.006045 | 0.002087  | 0.002158  | 0.002114   |
| 0.017231 | 0.002171  | 0.002122  | 0.002235   |
| 0.007019 | 0.015686  | 0.002385  | 0.002127   |
|          |   |   |  |
| 0.007536 | 0.022734  | 0.006724  | 0.005364   |
| 0.007462 | 0.002169  | 0.002267  | 0.010208   |
| 0.007928 | 0.002334  | 0.002206  | 0.002385   |
| 0.01588  | 0.004416  | 0.002708  | 0.002572   |
| 0.007139 | 0.002258  | 0.01455   | 0.002732   |
| 0.007169 | 0.0025  | 0.002267  | 0.002424   |
| 0.015202 | 0.002411  | 0.002363  | 0.002467   |
| 0.01767  | 0.0077  | 0.003004  | 0.002428   |
| 0.024818 | 0.002463  | 0.003752  | 0.002979   |
| 0.007455 | 0.01592   | 0.002757  | 0.002703   |
| 0.007537 | 0.013695  | 0.003532  | 0.002988   |
| 0.007636 | 0.002634  | 0.019995  | 0.003206   |
| 0.00784  | 0.013487  | 0.012518  | 0.012559   |
|          | 0.005655 0.016644 0.010474 0.006023 0.006045 0.017231 0.007019  0.007536 0.007462 0.007928 0.01588 0.007139 0.007169 0.015202 0.01767 0.024818 0.007455 0.007537 0.007636 | 0.005655       0.002097         0.016644       0.006667         0.010474       0.004062         0.006023       0.010984         0.002087       0.002171         0.007019       0.015686         0.007536       0.022734         0.007462       0.002169         0.007928       0.002334         0.01588       0.004416         0.007139       0.002258         0.015202       0.002411         0.01767       0.0077         0.024818       0.002463         0.007537       0.013695         0.007636       0.002634 | 0.005655         0.002097         0.001865           0.016644         0.006667         0.002782           0.010474         0.004062         0.002046           0.006023         0.010984         0.00503           0.007031         0.002087         0.002158           0.017231         0.002171         0.002122           0.007019         0.015686         0.002385           0.007462         0.002169         0.002267           0.007928         0.002334         0.002206           0.01588         0.004416         0.002708           0.007139         0.002258         0.01455           0.007169         0.0025         0.002267           0.015202         0.002411         0.002363           0.01767         0.0077         0.003004           0.024818         0.002463         0.003752           0.007537         0.013695         0.003532           0.007636         0.002634         0.019995 |