

1 Probability

Key Points about Probability

- Assuming all events are equally likely,

$$P(\text{event } A) = \frac{\text{Number of outcomes that make event } A \text{ happen}}{\text{total number of outcomes}}$$

- If we have two events A and B,

$$P(A \text{ and } B \text{ happening}) = P(A \text{ happening}) * P(B \text{ happening given } A \text{ has happened})$$

- If an event can happen exactly one of two different ways, then

$$P(\text{Event}) = P(\text{First way it can happen}) + P(\text{Second way it can happen})$$

- When analyzing if at least one success has happened,

$$P(\text{At least one success}) = 1 - P(\text{zero successes})$$

1. Two six-sided dice are thrown at random.

- What is the probability of rolling a sum of 2?
- What is the probability of rolling a sum of 5?
- What is the probability of rolling the exact same number on each of the dice?
- What is the probability of rolling different numbers on each of dice?
- Repeat parts b,c, and d for if we were rolling four dice instead of two.

2. Four fair, two-sided coins are thrown at random.

- What is the probability of getting all heads, and your third throw is a head?
- What is the probability of getting less than 2 heads?

- (c) What is the probability of seeing at least three heads?
- (d) **Challenge:** What is the probability that we get more heads than tails?